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CE1007/ CZ1007 DATA STRUCTURES

Lesson 10.4 Recursive Functions - Call by Reference

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The following are the coverage for Recursion:

- What is Recursion?
- Recursive Functions: Examples
- Recursive Functions: Returning Value
- **Recursive Functions: Call by Reference**
- Recursion in Arrays
- How to Design Recursive Functions

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There are 6 main sections to cover for Recursion as shown. This video lesson focuses on the fourth part where we will look into recursive functions using call by reference.

LESSON OBJECTIVES

After this lesson, you should be able to:

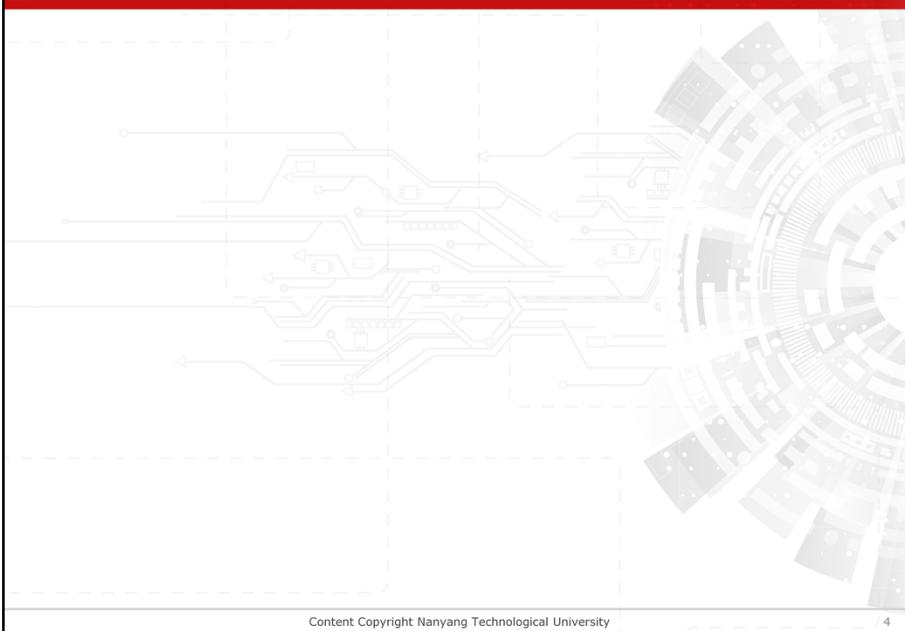
- Apply call by reference in recursive functions

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After this lesson, you should be able to apply call by reference in recursive functions.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE



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Example 6: Recursive Multiplication, Call by Reference

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

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This example works on the same problem as Example 5 covered in previous video lecture.

However, instead of using call by value via returning value, this example will implement the recursive function for integer multiplication via call by reference.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

In the recursive function **multi2()**, it uses call by reference for parameter passing.

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In the recursive function **multi 2()**, it uses call by reference for parameter passing.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

This function differs from the previous Example 5 function **multi()** in that in **multi2()**, the function returns the result through **call by reference** instead of returning the result to the calling function directly through the **return** statement.

From Example 5

```
int multi(int m, int n)  
{  
    if (n == 1)  
        return m;  
    else {  
        return m + multi(m, n-1);  
    }  
}
```

return
the result
through
call by
reference

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This function differs from the previous Example 5 function **multi()** in that in **multi2()**, the function returns the result through **call by reference** instead of returning the result to the calling function directly through the **return** statement.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

Returning the result through **call by reference** is achieved through the use of the pointer parameter **product** of type **int**.



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Returning the result through **call by reference** is achieved through the use of the pointer parameter **product** of type **integer**.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

The other two parameters, **m** and **n**, are specified of type **int** in the function.

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The other two parameters, **m** and **n**, are specified of type **integer** in the function.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

terminating condition

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The terminating condition is when n is equal to 1.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```



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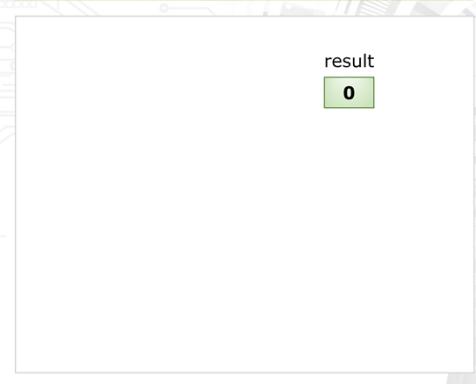
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The recursive condition is when n is greater than 1.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

In the **main()** function, the variable **result** is declared to hold the result of the multiplication operation.



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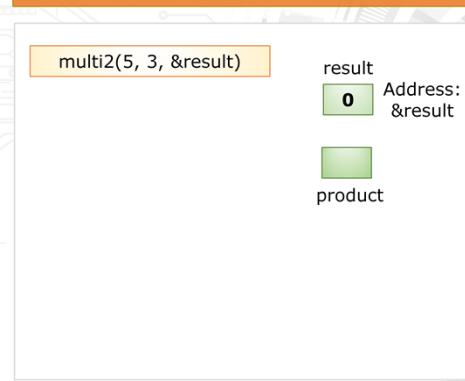
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In the **main()** function, the variable **result** is declared to hold the result of the multiplication operation.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

When it calls the function **multi2()**, it passes the address of the variable **result** via call by reference:
multi2(5, 3, &result);
In the function **multi2()**, it declares a pointer parameter **product** of **integer** type.



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When it calls the function **multi2()**, it passes the address of the variable **result** via call by reference:

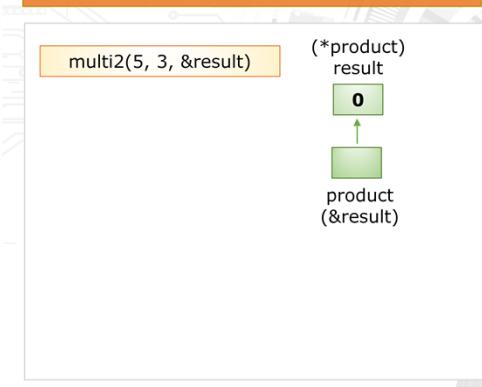
multi2(5, 3, ampersand result);

In the function **multi2()**, it declares a pointer parameter **product** of **integer** type.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

By passing in the address of the variable **result** to **product**, the result will be processed and updated in the memory location of the variable **result**.



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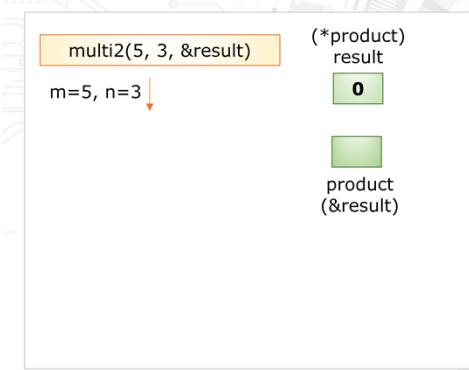
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By passing in the address of the variable **result** to **product**, the result will be processed and updated in the memory location of the variable **result**.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

When the function **multi2(5, 3, &result)** is called from the **main()** function, the code under the recursive condition is executed as **n** is not equal to 1.



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When the function **multi 2 (5, 3, ampersand result)** is called from the **main()** function, the code under the recursive condition is executed as **n** is not equal to 1.

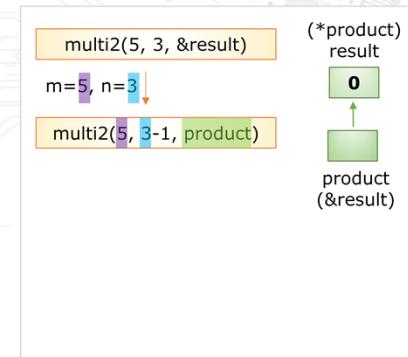
EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

The statement

multi2(m, n - 1, product);

will be executed



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The statement

multi 2 (m, n minus 1, product);

will be executed

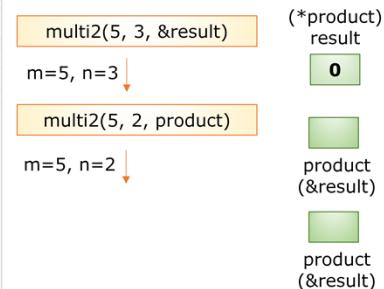
EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

The statement

multi2(m, n - 1, product);

will be executed and call the function
multi2(5, 2, product) with n reduced to 2.



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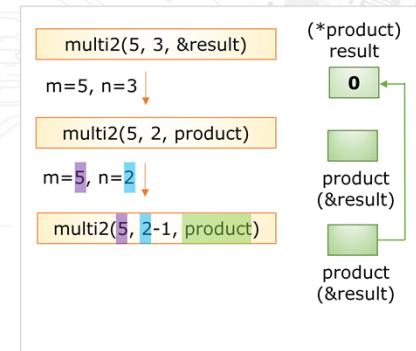
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and call the function **multi 2 (5, 2, product)** with **n** reduced to 2.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

This will in turn execute the function call
multi2(5, 1, product).



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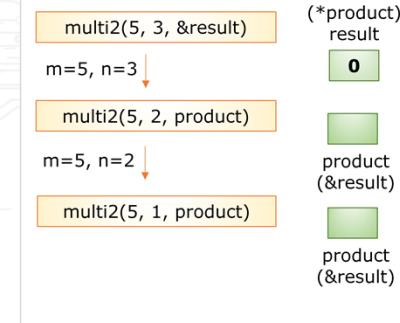
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This will in turn execute the function call **multi 2 (5, 1, product).**

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

This will in turn execute the function call
`multi2(5, 1, product).`



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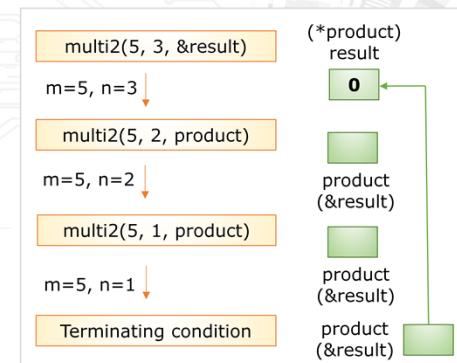
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EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

When the function **multi2(5, 1, product)** is executed, the code under the terminating condition will be executed.



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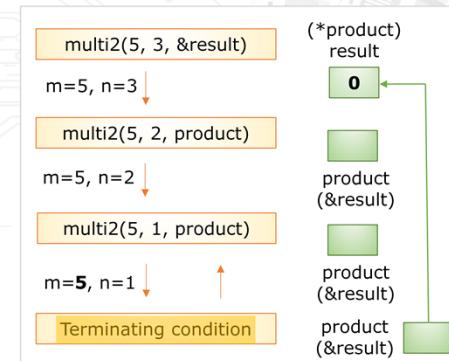
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When the function **multi2(5, 1, product)** is executed, the code under the terminating condition will be executed.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

The value 5 will be stored in result via *product



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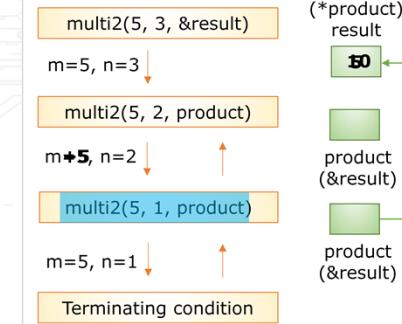
The value 5 will be stored in result via asterisk product

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result
is passed via pointer */
#include <stdio.h>
void multi2(int m, int n, int *product);
int main()
{
    int result=0;
    multi2(5, 3, &result);
    printf("5 * 3 = %d\n", result);
    return 0;
}
void multi2(int m, int n, int *product)
{
    if (n == 1)
        *product = m;
    else {
        multi2(m, n-1, product);
        *product = *product + m;
    }
}
```

multi2() will store the updated result via *product as:

$$*product = *product + m;$$



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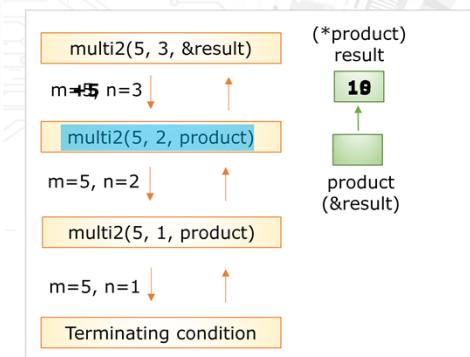
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Multi 2() will store the updated result via **asterisk product** as:
asterisk product = asterisk product + m;

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

That is, after each function call, the result will be updated directly via the memory location of the variable **result** in the **main()** function.



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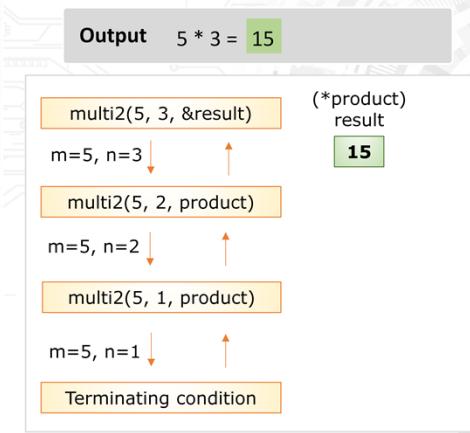
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That is, after each function call, the result will be updated directly via the memory location of the variable **result** in the **main()** function.

EXAMPLE 6: RECURSIVE MULTIPLICATION – CALL BY REFERENCE

```
/* Using pass by reference and result  
is passed via pointer */  
#include <stdio.h>  
void multi2(int m, int n, int *product);  
int main()  
{  
    int result=0;  
    multi2(5, 3, &result);  
    printf("5 * 3 = %d\n", result);  
    return 0;  
}  
void multi2(int m, int n, int *product)  
{  
    if (n == 1)  
        *product = m;  
    else {  
        multi2(m, n-1, product);  
        *product = *product + m;  
    }  
}
```

The final result 15 will then be printed on the screen.



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The final result 15 will then be printed on the screen.

SUMMARY

After this lesson, you should be able to:

- Apply call by reference in recursive functions

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In summary, after viewing this video lesson, you should be able to apply call by reference in recursive functions.