

## OVERVIEW

The following are the coverage for Recursion:

- What is Recursion?
- Recursive Functions: Examples
- Recursive Functions: Returning Value
- Recursive Functions: Call by Reference
- **Recursion in Arrays**
- How to Design Recursive Functions

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There are 6 main sections to cover for Recursion as shown. This video lesson focuses on the fifth part where we will look into recursion in arrays.

## LESSON OBJECTIVES

After this lesson, you should be able to:

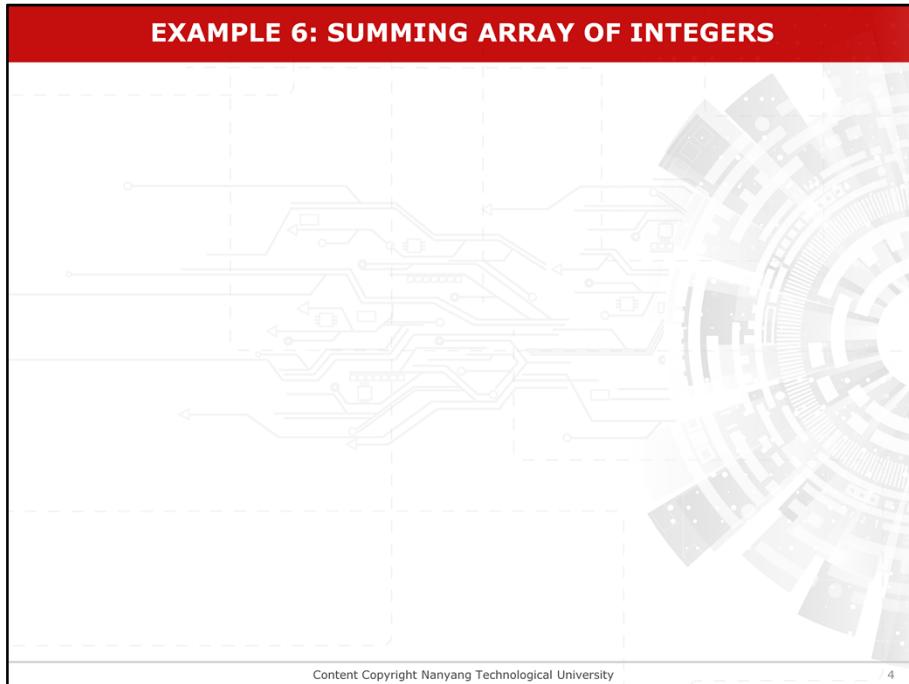
- Apply recursion in array

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After this lesson, you should be able to apply recursion in array.

## EXAMPLE 6: SUMMING ARRAY OF INTEGERS



Example 6: Summing Array of Integers

## EXAMPLE 6: SUMMING ARRAY OF INTEGERS

```
#include <stdio.h>
int sumArray(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;

    sum = sumArray(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
int sumArray(int a[], int size)
{ // iterative version
    int sum = 0;
    for (i = 0; i < size; i++)
        sum = sum + a[i];
    return sum;
}
```

function prototype

calling function

define function

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To implement a function **sum Array()** that computes the sum of all the elements in an array using non-recursive approach is quite straightforward.

A sum Array function can be written.

## EXAMPLE 6: SUMMING ARRAY OF INTEGERS

```
#include <stdio.h>
int sumArray(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;

    sum = sumArray(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
int sumArray(int a[], int size)
{ // iterative version
    int sum = 0;
    for (i = 0; i < size; i++)
        sum = sum + a[i];
    return sum;
}
```

[0]	[1]	[2]	[3]
a	1	2	3

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The array is defined as shown.

## EXAMPLE 6: SUMMING ARRAY OF INTEGERS

```
#include <stdio.h>
int sumArray(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;

    sum = sumArray(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
int sumArray(int a[], int size)
{ // iterative version
    int sum = 0;
    for (i = 0; i < size; i++)
        sum = sum + a[i];
    return sum;
}
```

[0]	[1]	[2]	[3]
a	1	2	3

Non-recursive function using for loop

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A **for** loop can be used to traverse individual elements of array and add them up

## EXAMPLE 6: SUMMING ARRAY OF INTEGERS

```
#include <stdio.h>
int sumArray(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;

    sum = sumArray(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
int sumArray(int a[], int size)
{ // iterative version
    int sum = 0;
    for (i = 0; i < size; i++)
        sum = sum + a[i];
    return sum;
}
```

[0] [1] [2] [3]  
a [1] [2] [3] [4]

returns the result to the calling function

Output

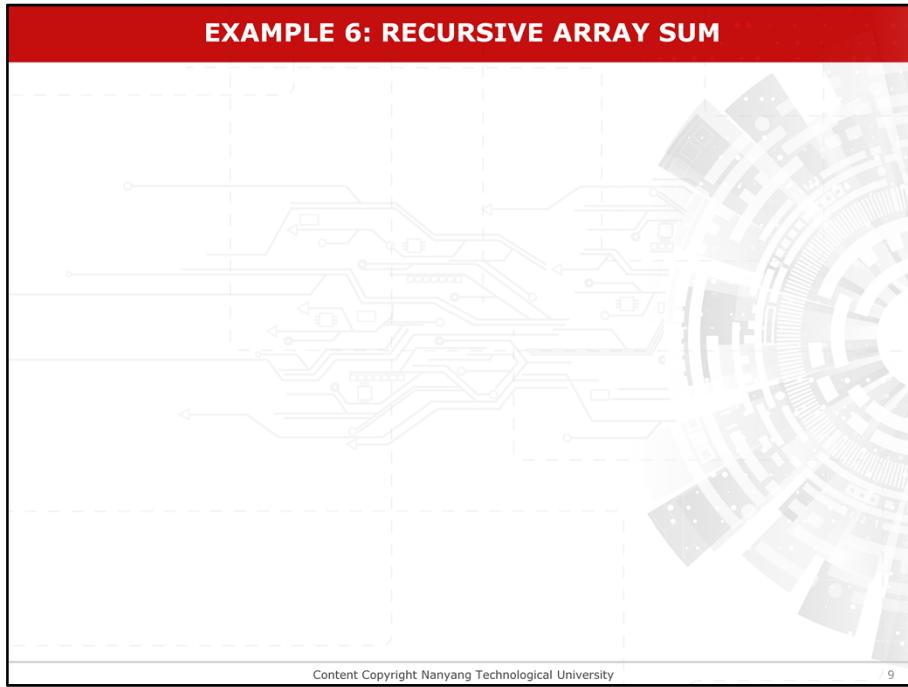
Sum = 10

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and returns the result to the calling function.

## EXAMPLE 6: RECURSIVE ARRAY SUM



We have just seen how to use a non-recursive approach by using for loop to sum an array of integers.

We can also use a recursive approach to give the result of the summation. We will see how to apply recursion on the same example.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
#include <stdio.h>
int recursiveSum(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;
    sum = recursiveSum(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
int recursiveSum(int a[ ], int size)
{ // recursive version
    if (size == 1) /* terminating condition*/
        return a[0];
    else           /* recursive condition*/
        return a[size-1] + recursiveSum(a, size-1);
}
```

[0] [1] [2] [3]  
a [1] [2] [3] [4]

Recursive approach

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This is the code using recursive approach.

To implement the function that recursively computes the sum of elements in arrays is more challenging.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
#include <stdio.h>
int recursiveSum(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;
    sum = recursiveSum(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
int recursiveSum(int a[], int size)
{ // recursive version
    if (size == 1) /* terminating condition*/
        return a[0];
    else           /* recursive condition*/
        return a[size-1] + recursiveSum(a, size-1);
}
```

[0] [1] [2] [3]  
a [1] [2] [3] [4]

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The function **recursive Sum()** has two parameters: **a** is an array and **size** is the size of the array to be processed.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
#include <stdio.h>
int recursiveSum(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;
    sum = recursiveSum(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
int recursiveSum(int a[ ], int size)
{ // recursive version
    if (size == 1) /* terminating condition*/
        return a[0];
    else           /* recursive condition*/
        return a[size-1] + recursiveSum(a, size-1);
}
```

[0] [1] [2] [3]  
a [1] [2] [3] [4]

recursive function

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In the function **recursive Sum()**, it computes the sum of all the elements in the array by recursively processes the array and reduces the size of the array by one element each time until the terminating condition is reached. In which case, the array will contain only one element.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
#include <stdio.h>
int recursiveSum(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;
    sum = recursiveSum(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
int recursiveSum(int a[ ], int size)
{ // recursive version
    if (size == 1) /* terminating condition*/
        return a[0];
    else           /* recursive condition*/
        return a[size-1] + recursiveSum(a, size-1);
}
```

[0] [1] [2] [3]  
a [1] [2] [3] [4]

recursive function

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We will look into detail the tracing of the recursive function when **recursive Sum (a, 4)** is called from the main() function.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] +
               recursiveSum(a, size-1);
}
```

recursiveSum(a, 4)

[0] [1] [2] [3]  
a 

1	2	3	4
---	---	---	---

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The highlighted code is the recursive function which we will look in detail how **recursive Sum (a, 4)** will be executed.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

recursiveSum(a, 4)  
size=4  
a[4-1] + recursiveSum(a, 4-1)

[0] [1] [2] [3]  
a [1] [2] [3] [4]

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Size is equal to 4 so the code under the recursive condition is executed as **size** is not equal to 1.

The statement

**return array a [size-1] + recursive Sum(a, size-1);**

will be executed

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] +
               recursiveSum(a, size-1);
}
```

recursiveSum(a, 4)

size=4 ↓

a[3] + recursiveSum(a, 3)

[0] [1] [2] [3]  
a 

1	2	3	4
---	---	---	---

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and call the function **recursiveSum(a, 3)**

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] +
               recursiveSum(a, size-1);
}
```

recursiveSum(a, 4)

size=4 ↓

a[3] + recursiveSum(a, 3)

size=3 ↓

a[3-1] + recursiveSum(a, 3-1)

[0] [1] [2] [3]  
a 

1	2	3	4
---	---	---	---

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with **size** reduced to 3.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] +
               recursiveSum(a, size-1);
}
```

recursiveSum(a, 4)

size=4

a[3] + recursiveSum(a, 3)

size=3

a[2] + recursiveSum(a, 2)

[0] [1] [2] [3]  
a 

1	2	3	4
---	---	---	---

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This will in turn execute the function call **recursiveSum(a, 2)**.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] +
               recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
  |  
  1 2 3 4

recursiveSum(a, 4)

size=4 ↓

a[3] + recursiveSum(a, 3)

size=3 ↓

a[2] + recursiveSum(a, 2)

size=2 ↓

a[2-1] + recursiveSum(a, 2-1)

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[no audio]

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] +
               recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
  |  
  1 2 3 4

recursiveSum(a, 4)

size=4 ↓

a[3] + recursiveSum(a, 3)

size=3 ↓

a[2] + recursiveSum(a, 2)

size=2 ↓

a[1] + recursiveSum(a, 1)

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When the function **recursiveSum(a, 1)** is executed,

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] +
               recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
  |  
  1 2 3 4

recursiveSum(a, 4)

size=4 ↓

a[3] + recursiveSum(a, 3)

size=3 ↓

a[2] + recursiveSum(a, 2)

size=2 ↓

a[1] + recursiveSum(a, 1)

size=1 ↓

a[0]

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the code under the terminating condition will be executed.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] +
               recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
1 2 3 4

recursiveSum(a, 4)

size=4 ↓

a[3] + recursiveSum(a, 3)

size=3 ↓

a[2] + recursiveSum(a, 2)

size=2 ↓

a[1] + recursiveSum(a, 1)

size=1 ↓

a[0]

sum = 1

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The value of **a[0]** (that is 1)

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
1 2 3 4

recursiveSum(a, 4)

size=4 ↓

a[3] + recursiveSum(a, 3)

size=3 ↓

a[2] + recursiveSum(a, 2)

size=2 ↓

a[1] + recursiveSum(a, 1)

size=1 ↓

a[0] sum = 1

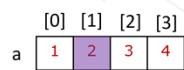
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will be returned to the calling function.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```



recursiveSum(a, 4)

size=4

a[3] + recursiveSum(a, 3)

size=3

a[2] + recursiveSum(a, 2)

size=2

a[1] + recursiveSum(a, 1)

size=1

sum = 2 + 1

a[0]

sum = 1

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The previous calling function will receive the value 1 and add the returned value to **a[1]**

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
  | 1 2 3 4

recursiveSum(a, 4)

size=4 ↓

a[3] + recursiveSum(a, 3)

size=3 ↓

a[2] + recursiveSum(a, 2)

size=2 ↓

a[1] + recursiveSum(a, 1)

sum = 3

size=1 ↓

a[0]

sum = 1

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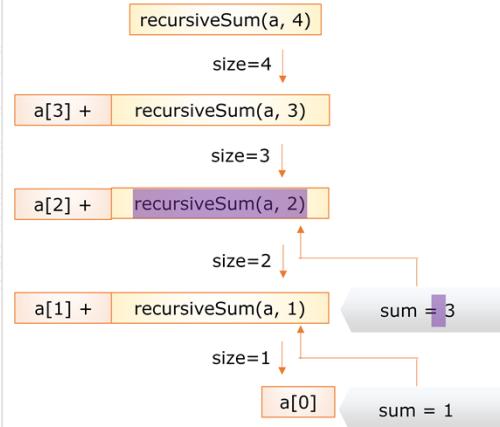
25

[no audio]

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
1 2 3 4



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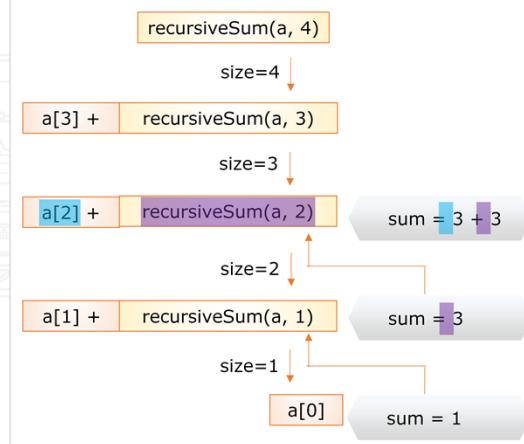
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The sum of 3 is then returned to the previous calling function.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
1 2 3 4



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The function will add the returned value of 3 to `a[2]`.

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
[1] [2] [3] [4]

recursiveSum(a, 4)

size=4

a[3] + recursiveSum(a, 3)

size=3

a[2] + recursiveSum(a, 2)

sum = 6

size=2

a[1] + recursiveSum(a, 1)

sum = 3

size=1

a[0]

sum = 1

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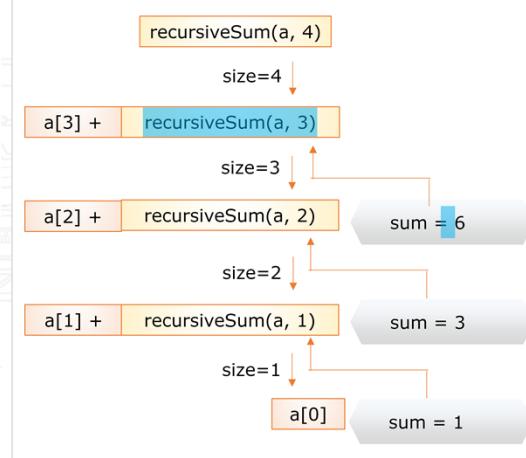
28

[no audio]

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
1 2 3 4



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the sum of 6 is then returned to the previous calling function

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
[1] [2] [3] [4]

recursiveSum(a, 4)

size=4

sum = 4 + 6

a[3] + recursiveSum(a, 3)

size=3

sum = 6

a[2] + recursiveSum(a, 2)

size=2

sum = 3

a[1] + recursiveSum(a, 1)

size=1

sum = 1

a[0]

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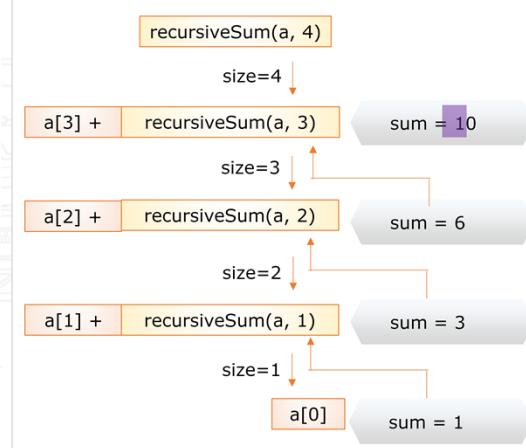
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The function will add the returned value of 6 to a[3]

## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
[1] [2] [3] [4]



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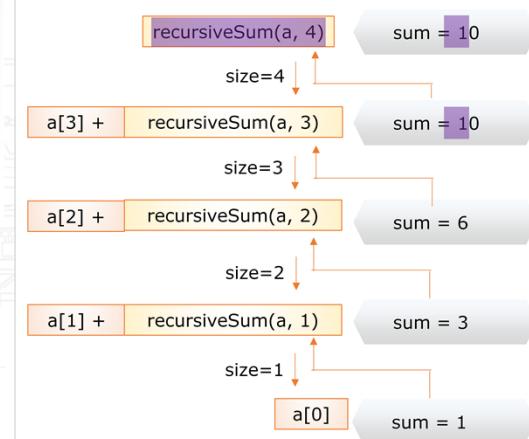
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## EXAMPLE 6: RECURSIVE ARRAY SUM

```
int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size-1] + recursiveSum(a, size-1);
}
```

a [0] [1] [2] [3]  
1 2 3 4



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The sum of 10 will be returned to the calling function `main()`

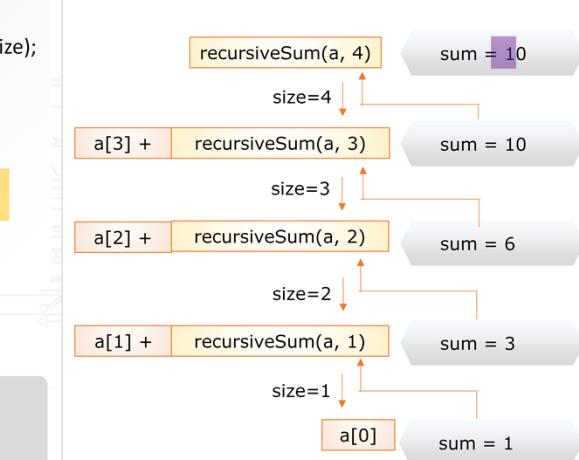
## EXAMPLE 6: RECURSIVE ARRAY SUM

```
#include <stdio.h>
int recursiveSum(int a[], int size);
int main()
{
    int a[10] = {1, 2, 3, 4};
    int sum;
    sum = recursiveSum(a, 4);
    printf("Sum = %d", sum);
    return 0;
}
```

a [0] [1] [2] [3]  
1 2 3 4

Output

Sum = 10



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In the **main()** function, the returned value of 10 will then be printed to the screen.

## SUMMARY

After this lesson, you should be able to:

- Apply recursion in array

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In summary, after viewing this video lesson, you should be able to apply recursion in array.