

CE/CZ1005 Digital Logic Tutorial 4

Combinational Logic

1. Given the following truth table, determine:
 - a. The canonical sum-of-minterms expression
 - b. The minimum cost sum-of-products (SOP) expression from (a) using algebraic manipulation.
 - c. The canonical product-of-maxterms expression
 - d. The minimum cost product-of-sums (POS) expression from (c) using algebraic manipulation.
 - e. The NAND gate only implementation of the minimum cost SOP expression.
 - f. The NOR gate only implementation of the minimum cost POS expression.
 - g. That the two expressions in (b) and (d) are identical using algebraic manipulation.

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1

Karnaugh maps

2. Simplify the following expressions using Karnaugh map:

(a) $X = AB'D' + A'BC'D + A'BCD + A'B'D'$

(b) $Y = (P+Q'+R+S')(P+Q'+R'+S')(P'+Q'+R+S')(P'+Q'+R'+S')$

3. Simplify the Boolean function F together with the don't care condition d, using the K-map method. Give your answer in SOP.

$$F(A, B, C, D) = \sum m (0, 5, 6, 8, 14)$$

$$d(A, B, C, D) = \sum m (2, 7, 15)$$

4. Repeat Question 3. Give your answer in POS.

Answers

1.
 - a. $F_{\text{SOP}} = A'B'C + A'BC + AB'C' + ABC' + ABC$
 - b. $F = AB + A'C + AC'$
 - c. $F_{\text{POS}} = (A+B+C).(A+B'+C).(A'+B+C')$
 - d. $F = (A+C).(A'+B+C')$
 - e. $F = ((AB)'. (A'C)'. (AC')')'$
 - f. $F = ((A+C)' + (A'+B+C')')'$

2.
 - (a) $X = B'D' + A'BD$
 - (b) $Y = Q' + S'$

3.
 - (a) $F = BC + A'BD + B'C'D'$
 - (b) $F = (A'+D')(B+D')(B+C')(B'+C+D)$