


H, MAS 17D  
 ch 15  
 → ch 13, 14 first  
 mutually exclusive  
 ch 14 B2  
 1. Text  
 2. any notes  
 Game: toss fair coin once  
 $u = \text{"get H"}$   
 $v = \text{"get T"}$

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Game: toss 2 coins

Dime  
nickel

$U =$  dime shows H

$V =$  nickel shows H

$U, V$  mut. excl  $\begin{cases} \text{yes} \\ \text{no} \end{cases}$

because  $U$  and  $V$

$E = \text{get 2 H} = \{HH\}$   
 $F = \text{get 1 H} = \{HT, TH\}$   
 $E, F$  mut excl:

$$P(HH) = P\left(\begin{matrix} D \\ N \end{matrix} \begin{matrix} H \\ H \end{matrix}\right) = \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$$

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$$P(E \text{ or } F) = ?$$

$$= P(E) \oplus P(F)$$

only valid when  $E, F$  are mutually excl.

$$= \frac{1}{4} + P(HT \text{ or } TH)$$

$$P(HT) \oplus P(TH)$$

$$= \frac{1}{4} + \frac{1}{4} + \frac{1}{4}$$

$$= \frac{3}{4}$$

{HT} {TH} mutually excl? ✓

ch 15 A 3, 4, 5

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Ch 15 comments  
formula p. 259

$$7! = 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1$$

~~$P = \frac{1}{2}$~~   
 $P = \frac{3}{5}$



Game:  
Draw 1 ticket  
Repeat!  
n times

focus  $\rightarrow$  Count of W

$$P(\text{get exactly } \underline{k} \text{ W in } n \text{ draws})$$

$$= \frac{n!}{k!(n-k)!} p^k (1-p)^{n-k}$$

$n, k, p$   
 $p = P(\text{get W on 1 draw})$

$$\frac{n!}{k!(n-k)!}$$

= # of ways to write,  
a string of W's & L's,  
n letters long  
with exactly k W's

$$n = 10$$

$$k = 7$$

W W W W W W W L L L

How many words  
using all 10?

$$\frac{10!}{7!3!} = 120$$

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Ch 15 A

$$3. \quad \boxed{RGGGG} \quad n=4$$

$$(a) \quad P(\text{no } R) \\ = P(GGGG)$$

$$\text{mult} = \frac{5}{6} \cdot \frac{5}{6} \cdot \frac{5}{6} \cdot \frac{5}{6} = \left(\frac{5}{6}\right)^4$$

$$\rightarrow (b) \quad P(\text{exactly } 1 R)$$

$$\begin{aligned} &\rightarrow P(RGGG \text{ OR } GRGG \text{ OR } GGGR \text{ OR } GGGR) \\ &= P(\underline{RGGG}) + P(\underline{GRGG}) + P(\underline{GGGR}) + P(\underline{GGGR}) \\ &= \frac{1}{6} \left(\frac{5}{6}\right)^3 + \frac{1}{6} \left(\frac{5}{6}\right)^3 + \frac{1}{6} \left(\frac{5}{6}\right)^3 + \frac{1}{6} \left(\frac{5}{6}\right)^3 \end{aligned}$$

$$= \textcircled{4} \left(\frac{1}{6}\right)^1 \left(\frac{5}{6}\right)^3$$

$$n = 4$$

$$k = 1$$

$$P(R) = \frac{1}{6}$$

$$= \frac{4!}{1!(3!)} \left(\frac{1}{6}\right)^1 \left(1 - \frac{1}{6}\right)^{4-1}$$

use formula

$$p^k$$

$$(1-p)^{n-k}$$

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3c.  $P(\text{exactly } 2 \text{ R in } 4 \text{ draws})$

$$= \frac{4!}{2! 2!} \left(\frac{1}{6}\right)^2 \left(\frac{5}{6}\right)^2 \times 259$$

$\rightarrow n = 4$   
 $\rightarrow k = 2$   
 $\rightarrow p = \frac{1}{6}$

$\left[ \text{R G G G G G} \right]$

$p = P(\text{R on } 1 \text{ draw}) = \frac{1}{6}$

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R G G G G G

$n = 20$  draws

$P(\text{get exactly 10 R in 20 draws}) = ?$

$\frac{20!}{10! \cdot 10!} = \# \text{ ways to make strings}$   
of 10 R's  
& 10 G's

$= 184,756$

$n = 20$   $P = \frac{1}{6}$   
 $k = 10$

$\rightarrow = \frac{20!}{10! \cdot 10!} \left(\frac{1}{6}\right)^{10} \left(\frac{5}{6}\right)^{10}$

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A4

$$P = \frac{1}{6}$$

$$n = 4$$

$$(a) P(\text{no A's}) =$$

$$= P(\text{NNNN}) \leftarrow$$

$$\underline{\underline{k=0}}$$

$$= \left(\frac{5}{6}\right)^4 \quad (\text{mult. rule})$$

$$(c) P(2 \text{ A's in 4 rolls})$$

$$= \text{same as } 3(c)$$

$$n = 4$$


$$k = 2$$

$$P = \frac{1}{6}$$

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A5 "4 to 6 inclusive"  
 $\equiv$  "4 or 5 or 6"  
"4 to 6 exclusive"  
 $\equiv$  exactly 5  
"2 to 7 inclusive"  
 $\equiv$  2 or 3 or 4 or 5 or 6 or 7  
"2 to 7 exclusive"  
 $\equiv$  3 or 4 or 5 or 6

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#5


$n=10$   
 $k=5$   
 $p=\frac{1}{2}$

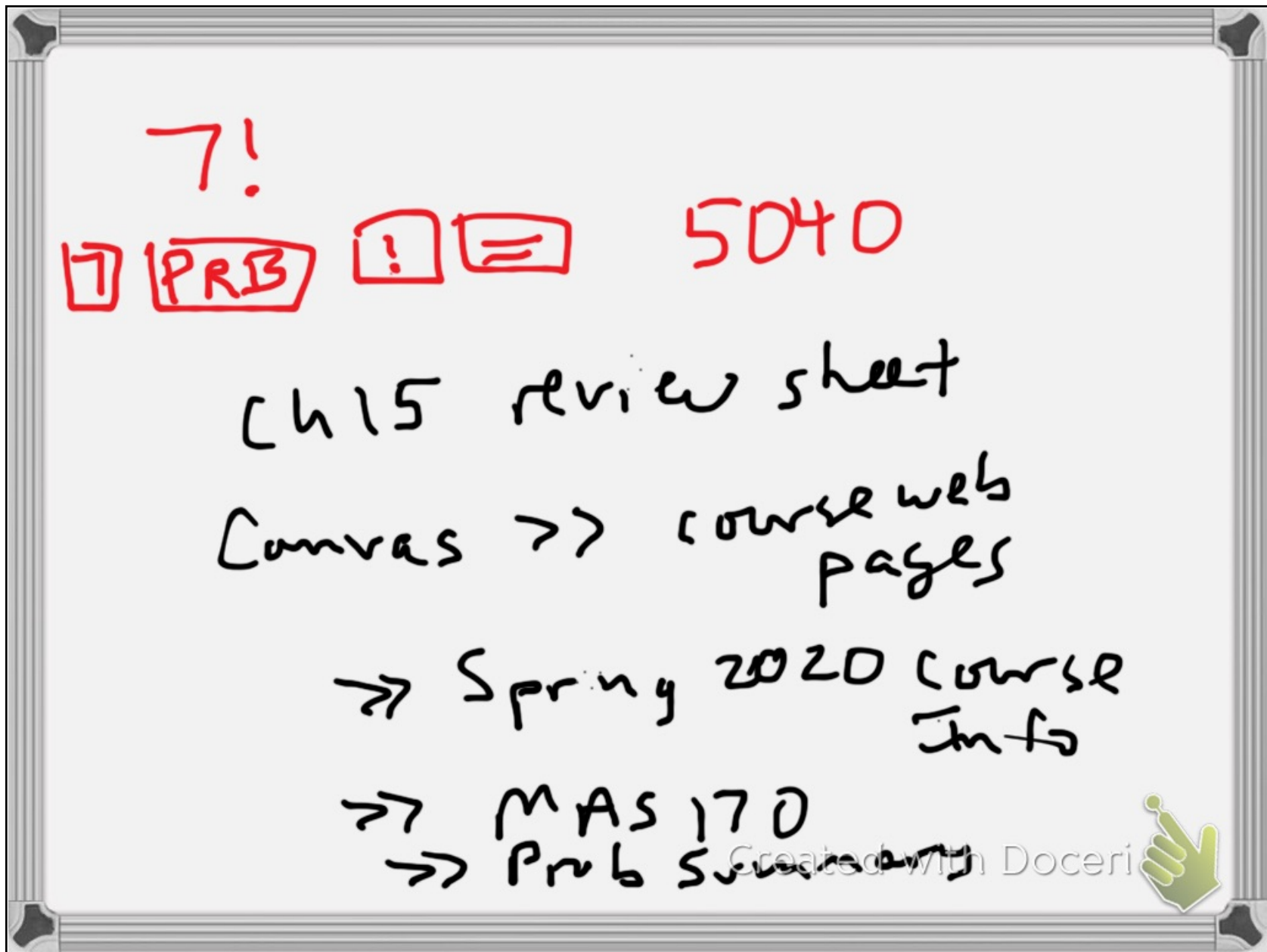
$$P(\text{exactly } 5 \text{ H in } 10 \text{ tosses})$$

$$= \frac{10!}{5!5!} \underbrace{\left(\frac{1}{2}\right)^5 \left(\frac{1}{2}\right)^5}_{\left(\frac{1}{2}\right)^{10}} = \frac{252}{1024}$$

$\rightarrow P(4 \text{ or } 5 \text{ or } 6 \text{ H in } 10 \text{ tosses})$

$$= \frac{10!}{4!6!} \left(\frac{1}{2}\right)^{10} + \frac{10!}{5!5!} \left(\frac{1}{2}\right)^{10} + \frac{10!}{6!4!} \left(\frac{1}{2}\right)^{10}$$

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Ch15 Review Ex p261

→ Special Review Ex p263  
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