

NETFLIX

Restricted Boltzmann Machines

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Outline

Problem

The Model

Learning

Inference

Implementation

Going Further

Problem

Problem: Collaborative Filtering – Movie Ratings

	Star Trek	The Matrix	Van Helsing	Harry Potter	The Hobbit
James T. Kirk	1	1	×	0	×
Trinity	×	1	0	1	1
Anna Valerious	×	×	1	×	0
Severus Snape	0	1	0	1	0
Thorin Oakenshield	1	1	1	×	0

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Goal:

Problem: Collaborative Filtering – Movie Ratings

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Goal:

- ▶ approximately represent a complex probability distribution

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Goal:

- ▶ approximately represent a complex probability distribution
- ▶ learn probability distribution based on given samples

Problem: Collaborative Filtering – Movie Ratings

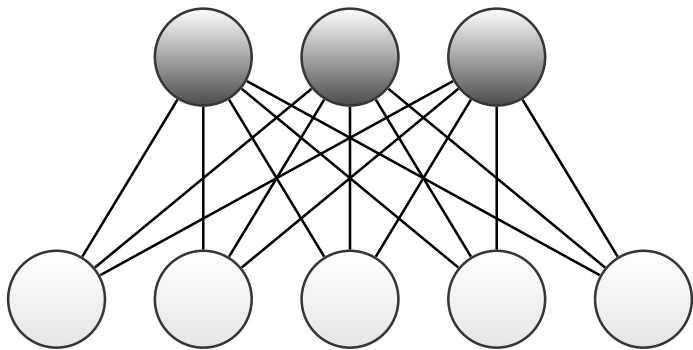
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Goal:

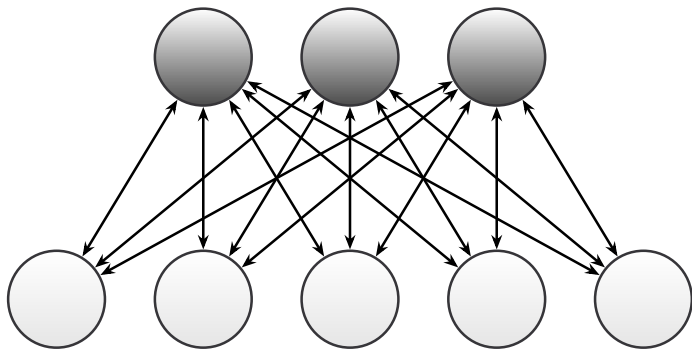
- ▶ approximately represent a complex probability distribution
- ▶ learn probability distribution based on given samples
- ▶ make predictions based on learned parameters

The Model

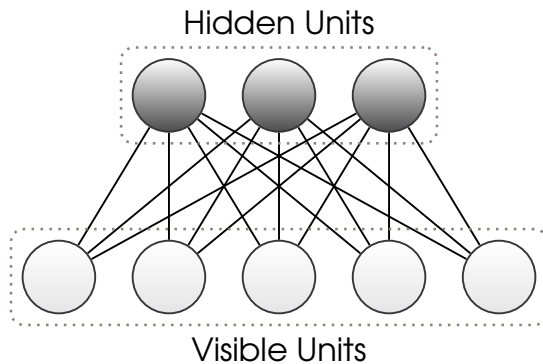
The Model: Idea



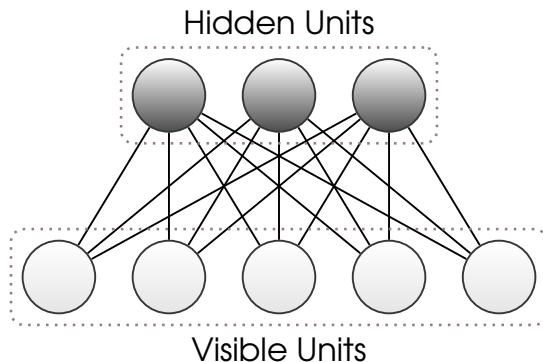
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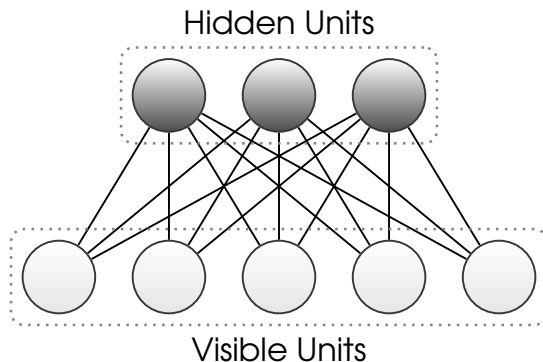


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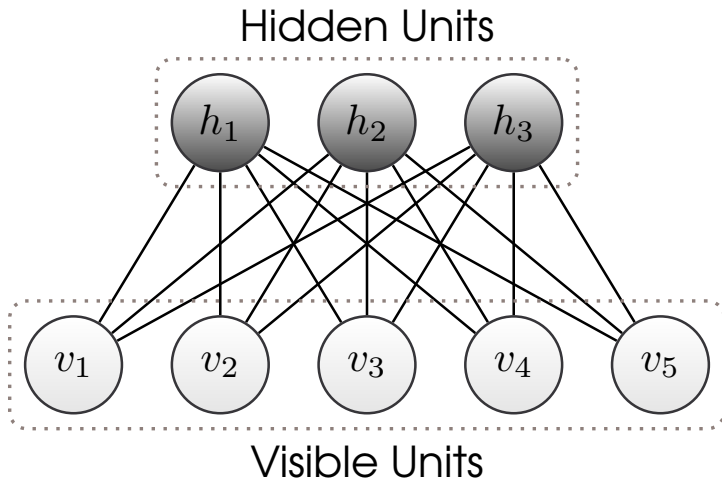
- units are divided into two subsets

The Model: Idea

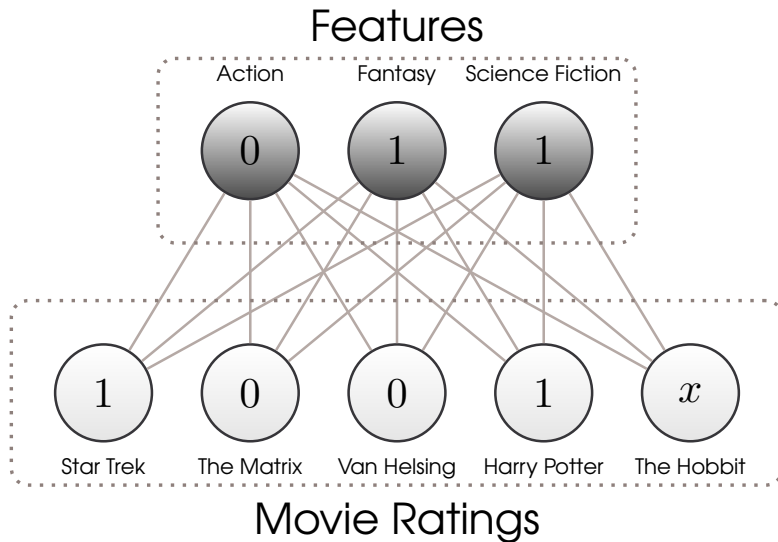


- ▶ units are divided into two subsets
- ▶ only connections between hidden and visible units are allowed

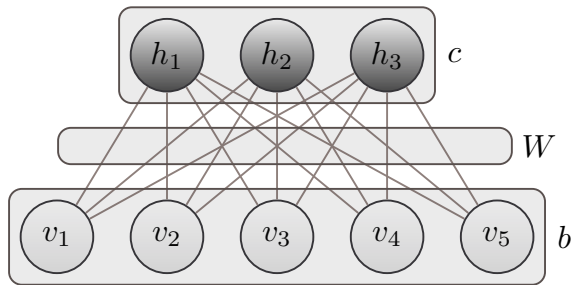
The Model: Idea – Inputs



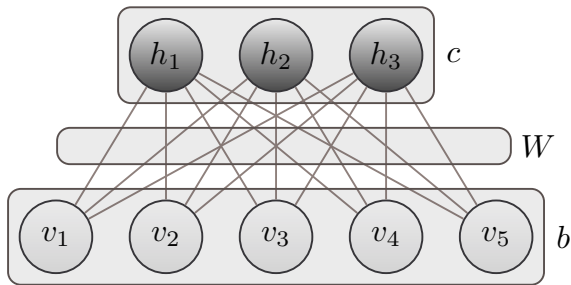
The Model: Idea – Example



The Model: Parameters



The Model: Parameters



$$v \in V := \{0, 1\}^n \quad h \in H := \{0, 1\}^m \quad \vartheta := (W, b, c) \in \mathbb{R}^{(n \times m) + n + m}$$

The Model: Probability Distribution and Energy

$$p[\vartheta]: V \times H \rightarrow [0, 1] \quad p[\vartheta](v, h) := \frac{e^{-E[\vartheta](v, h)}}{Z(\vartheta)}$$

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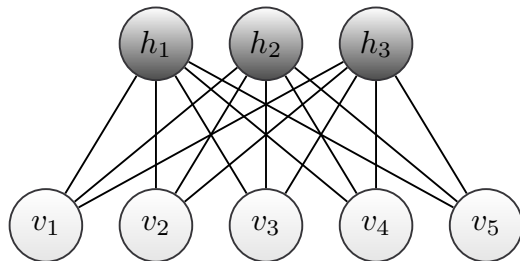
$$E[\vartheta]: V \times H \rightarrow \mathbb{R} \quad E[\vartheta](v, h) := -v^T W h - v^T b - h^T c$$

$$Z(\vartheta) := \sum_{v \in V} \sum_{h \in H} e^{-E[\vartheta](v, h)}$$

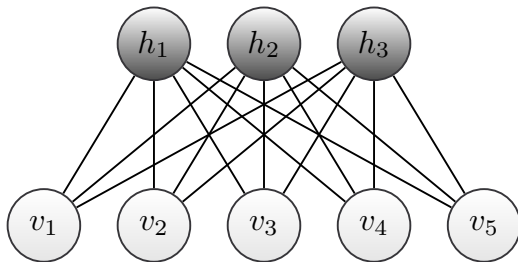
The Model: Probability Distribution for Visible Units

$$p[\vartheta]: V \rightarrow [0, 1] \quad p[\vartheta](v) := \sum_{h \in H} p[\vartheta](v, h)$$

The Model: Posterior Probability



The Model: Posterior Probability



$$p[\vartheta](h|v) = \prod_{j=1}^m p[\vartheta](h_j = 1|v)$$

Learning

Learning: Maximum Likelihood Estimation

$$\mathcal{S} \in V^s \quad \mathcal{L}[\mathcal{S}]: \mathbb{R}^{n \times m + n + m} \rightarrow \mathbb{R} \quad \mathcal{L}[\mathcal{S}](\vartheta) := \frac{1}{s} \sum_{k=1}^s \ln p[\vartheta](\mathcal{S}_k)$$

- ▶ maximize the product of probabilities of given samples
- ▶ equivalent to maximizing log-likelihood function

Learning: Gradient Ascent

$$\nabla_W \mathcal{L}[\mathcal{S}](\vartheta) = \frac{1}{s} \sum_{k=1}^s \mathbb{E}_{\vartheta} \left[\mathcal{V} \mathcal{H}^T \middle| \mathcal{S}_k \right] - \mathbb{E}_{\vartheta} \left[\mathcal{V} \mathcal{H}^T \right]$$

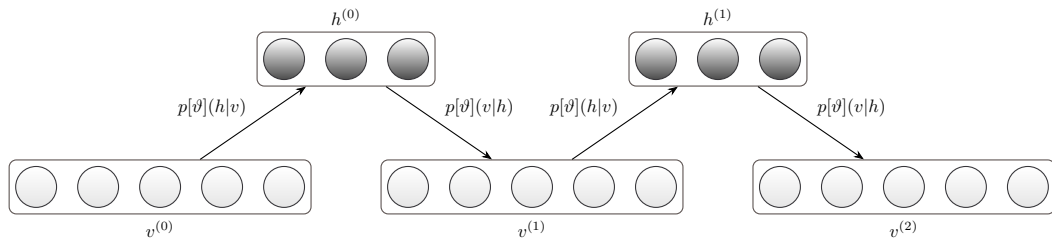
- ▶ use stochastic gradient ascent with minibatches

Learning: Gradient Ascent

$$\nabla_W \mathcal{L}[\mathcal{S}](\vartheta) = \frac{1}{s} \sum_{k=1}^s \mathbb{E}_{\vartheta} \left[\mathcal{V} \mathcal{H}^T \middle| \mathcal{S}_k \right] - \mathbb{E}_{\vartheta} \left[\mathcal{V} \mathcal{H}^T \right]$$

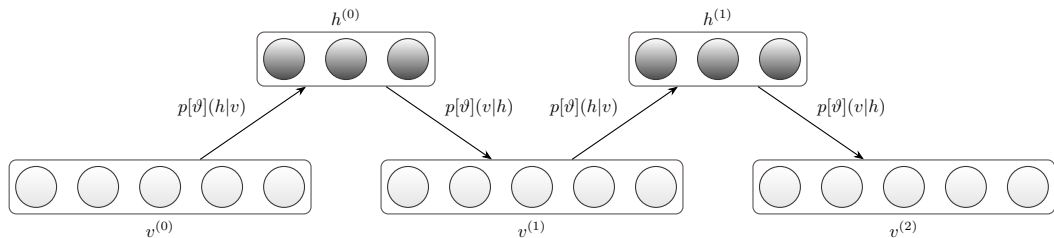
- ▶ use stochastic gradient ascent with minibatches
- ▶ evaluating the gradient introduces problems

Learning: Gibbs Sampling



► to estimate $\mathbb{E}_{\vartheta} [\mathcal{V}\mathcal{H}^T]$ perform Gibbs sampling

Learning: Gibbs Sampling



- ▶ to estimate $\mathbb{E}_{\vartheta} [\mathcal{V}\mathcal{H}^T]$ perform Gibbs sampling
- ▶ slow because it has to reach equilibrium

Learning: Contrastive Divergence

- ▶ abort Gibbs Sampling after $v^{(k)}$ and $h^{(k)}$ are computed

Learning: Contrastive Divergence

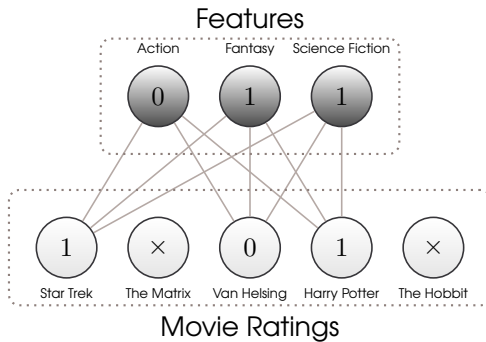
- ▶ abort Gibbs Sampling after $v^{(k)}$ and $h^{(k)}$ are computed
- ▶ approximate the expectation value

Learning: Contrastive Divergence

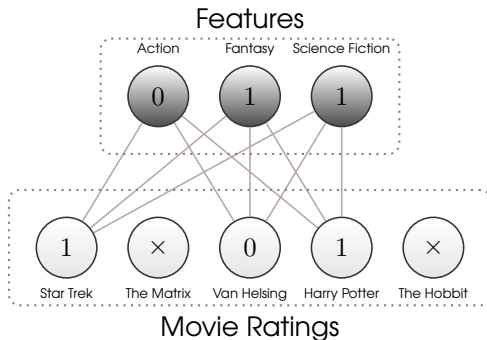
- ▶ abort Gibbs Sampling after $v^{(k)}$ and $h^{(k)}$ are computed
- ▶ approximate the expectation value

$$\mathbb{E}_{\vartheta} [\mathcal{V}\mathcal{H}^T] \approx v^{(k)} h^{(k)T}$$

Learning: Example

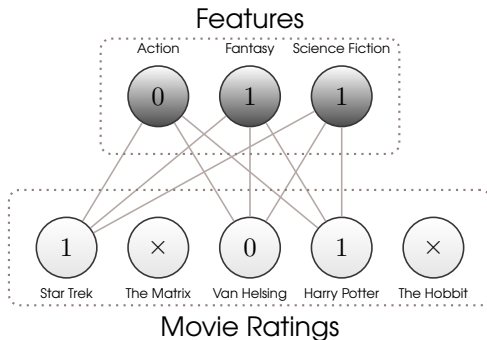


Learning: Example



- ▶ one RBM for every user with connections for rated movies

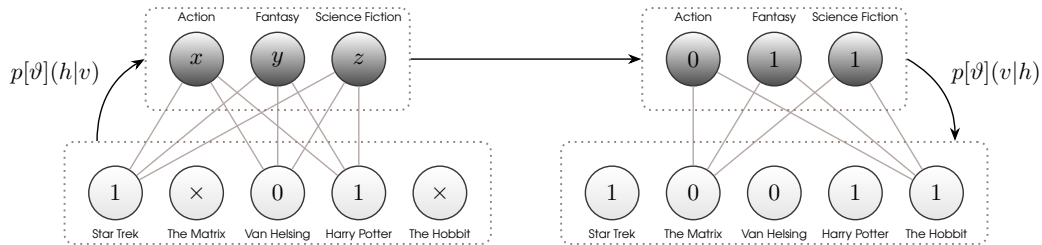
Learning: Example



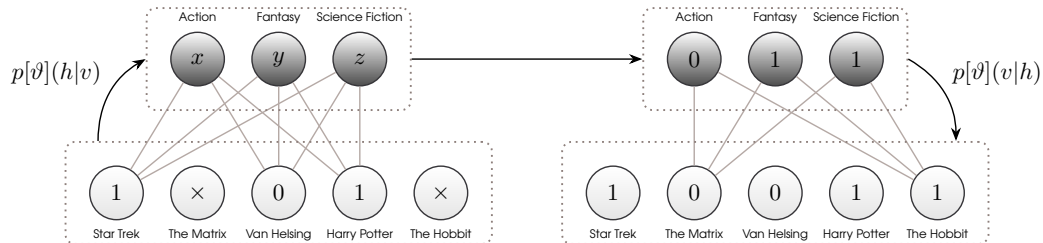
- ▶ one RBM for every user with connections for rated movies
- ▶ weights and biases of all RBM are tied together

Inference

Inference: Example

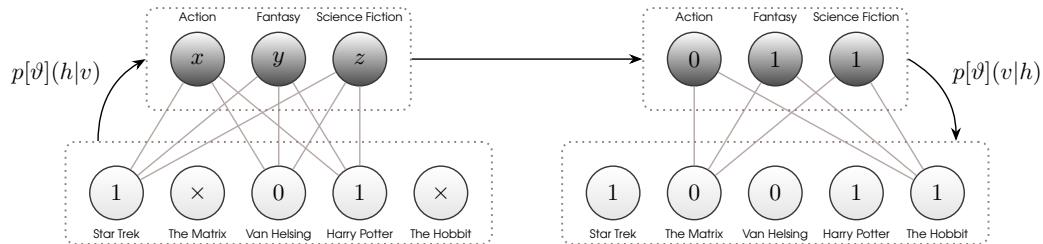


Inference: Example



- compute hidden values only for rated movies

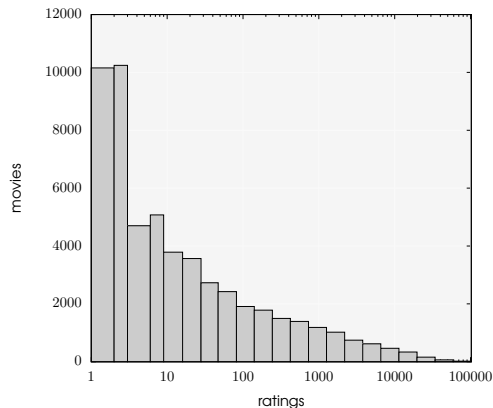
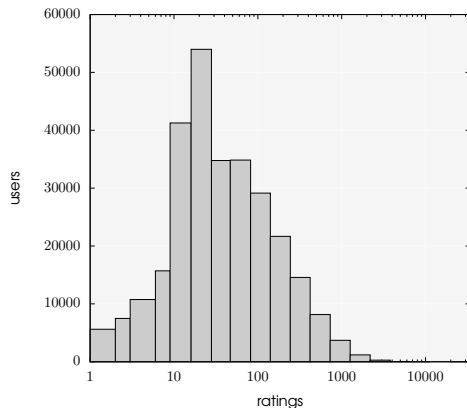
Inference: Example



- ▶ compute hidden values only for rated movies
- ▶ compute visible values of unrated movies based on hidden values

Implementation

Implementation: MovieLens Dataset by GroupLens



Implementation: Rating Database

	Star Trek	The Matrix	Van Helsing	Harry Potter	The Hobbit
James T. Kirk	1	1	×	0	×
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- ▶ implement as sparse matrix in CSR format
- ▶ entries should be floating point

Implementation: Training and Testing

- ▶ same users in training and testing dataset
- ▶ divide ratings of users into training and testing dataset
- ▶ learn biases and weights for every user only for rated movies

Going Further

Going Further: Tweak the Learning

- ▶ Contrastive Divergence Variants
- ▶ Momentum
- ▶ Weight Decay
- ▶ Different types of units

Going Further: Applications

- ▶ language modeling and document retrieval
- ▶ classification
- ▶ reducing dimensionality of data

References

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