



## *Ascent Mission Description*



## *Ascent Mission Analysis*

In general, **ascent** mission is characterized by **events** that occur at specific time **intervals**.

These are usually **related** to operation of various **stages** as well as other **considerations** that impact the **performance**.

In most cases, **events** are time **referenced** in order to **ensure** that each segment performs as **designed**.



## *Ascent Mission Sequence –Delta II*

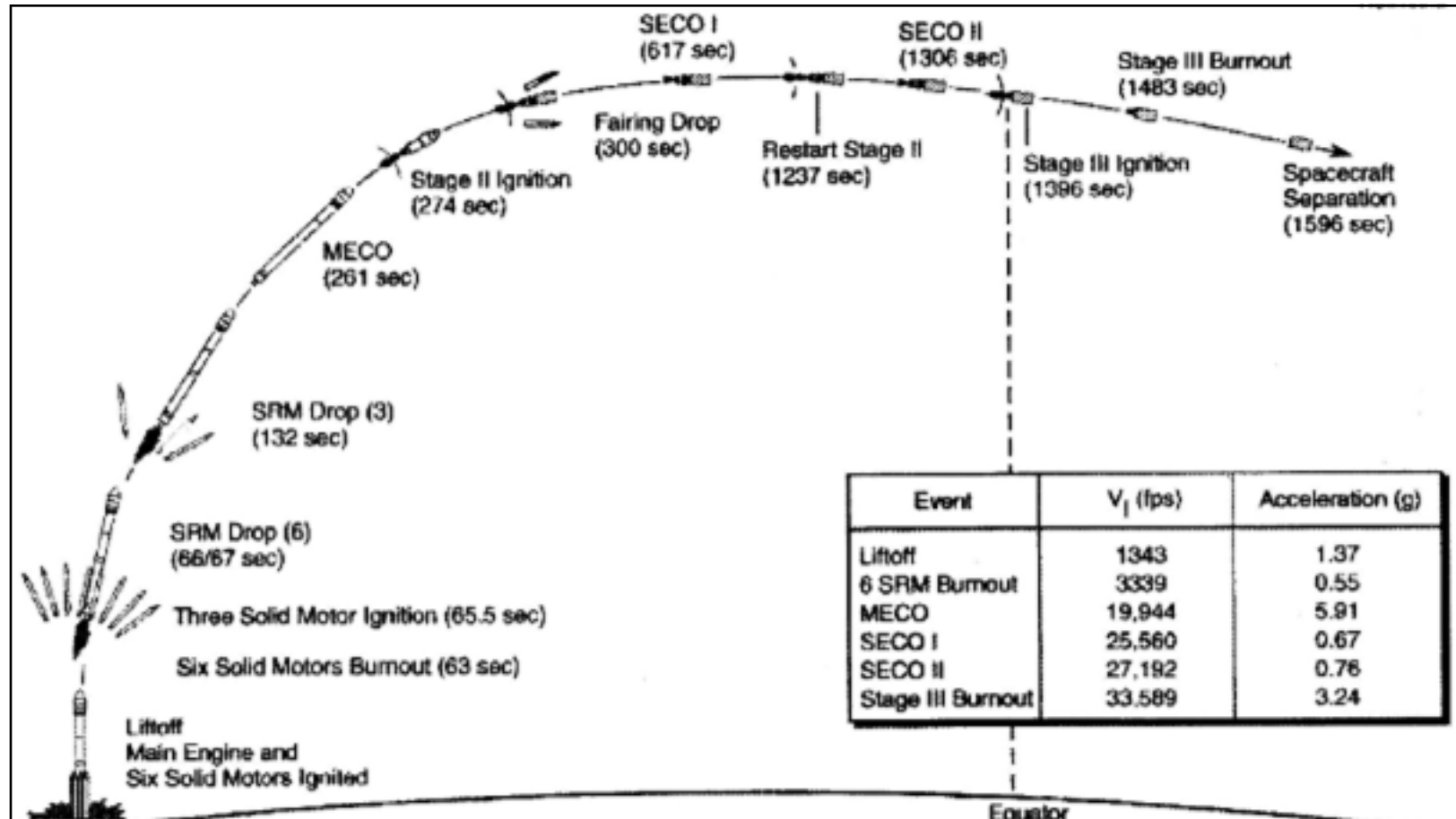


Figure Courtesy Space Vehicle Encyclopaedia



## *Ascent Mission Characteristics*

We note that **events** are not only time **stamped** but also have **trajectory** information e.g. velocity, altitude, inclination etc., **connected** to it.

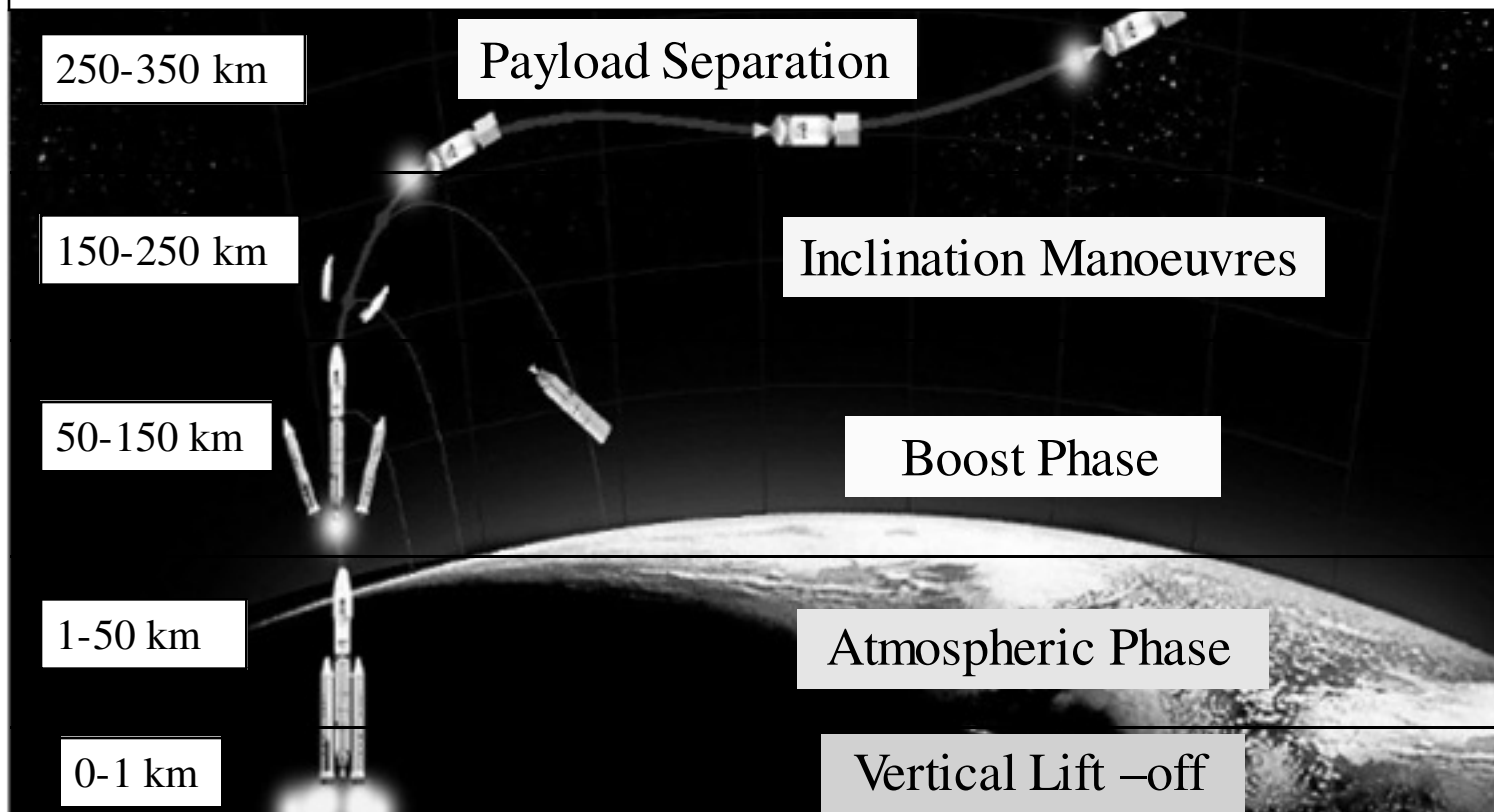
Further, as events **denote** changes in **force** system, these have a **mechanics** related implication, as well.

Therefore, it is **possible** to define appropriate **segments** of ascent **mission** that are based on **corresponding** models.



## *Ascent Mission Phases*

A typical **ascent** trajectory is **broken** into broad **phases**, based on **nature** of forces / manoeuvres, as shown **below**.





## *Lift off & Atmospheric Phase*

**Lift –off** is a critical phase, as **toppling** due to gravity is the **major** issue and is modelled simply as  $T > W$ , while ensuring vertical **attitude**.

Once **clear** of launch tower, **boosters** and/or first stage **engines** propel the **vehicle** through dense **atmosphere**.

In this phase, while **gravity** & thrust are the **dominant** forces, aerodynamic **drag** is also quite significant.



## ***Boost Phase & Inclination Manoeuvres***

In **boost** phase, as the **rocket** is out of **atmosphere**, larger velocity **increments** are possible.

Towards the end of **boost** phase, manoeuvres are carried out to **rotate** the velocity **vector** in order to **achieve** the desired terminal **inclination**.

In these phases, **motion** is assumed to be in **vacuum**, though altitude correction to **gravity** may be needed.



## *Ascent Mission – Terminal*

**Terminal** phase is considered the **most** crucial as spacecraft **separates** after acquiring required **velocity** / inclination.

In this **phase**, thrust is very **small** so that the motion is **governed** mainly by the gravitational **force**.

However, **distance** travelled over Earth can be very **large**, needing a suitable **Earth** surface geometric model.





# *Ascent Mission Modelling*



## *Ascent Mission Modelling*

**Modelling** of the ascent mission involves, (1) identifying the applicable **forces**, (2) desired motion **parameters** and (3) the physical **laws**, governing the motion.

As we have seen, **launch** vehicle experiences **forces** due to **propellant** burning, gravity and **atmosphere**.

Similarly, **motion** variables of interest are **position** and velocity vectors of the **centre of mass** (or velocity, altitude and flight path angle).



## *Basic Governing Equation*

In **inertial** frame, equation of **motion** for the centre of **mass** can be written using **Newton's 2<sup>nd</sup>** law as,

$$\frac{d}{dt}\{m\vec{V}\} = \vec{F}; \quad \vec{x} = \int \vec{V} dt$$



## *Basic Governing Equation*

Here, the inertial **velocity** vector is expressed as,

$$\vec{V} = \vec{V}_0 + \vec{V}_b + \vec{\Omega}_0 \times \vec{R}_b; \quad \vec{V}_0 \rightarrow \text{Velocity of Origin}$$
$$\vec{\Omega}_0 \rightarrow \text{Frame Rotational Velocity}$$
$$\vec{R}_b, \vec{V}_b \rightarrow \text{Relative Position, Velocity}$$

In the context of **ascent** missions, launch point is commonly **taken** as origin of a suitable reference **frame**.



## *Choice of Coordinate Axes*

Further, generally **Cartesian** (i.e. X, Y & Z) coordinate **axes** are used to represent forces and motion variables.

However, in cases where **motion** is confined to a **plane**, either polar (**R**,  **$\theta$** ) coordinates or **curvilinear** (s, n) coordinates are also **employed**.



## *Ascent Mission Force Models*

**Ascent** mission starts from **earth's** surface and ends at a **pre-fixed** point where **payload** is released.

Further, **motion** profile is generally highly **curvilinear**.



## *Ascent Mission Force Models*

In addition, launch vehicle **accelerates** through propulsive **forces**, in the presence of **gravity** & aerodynamic **forces**.

Thus, we need **models** for gravity, propulsive and **aerodynamic** forces, to setup the governing **equations**.

It should be **noted** here that, while there are **other** forces e.g. due to magnetic field, solar radiation, **these** are much smaller in **magnitude** and, hence, are generally **ignored** for the ascent mission **modelling**.



## *Summary*

**Ascent** mission, while **composed** of time-sequenced **events**, can be defined in terms of **trajectory** segments based on the **nature** of forces and motion.

**Newton's** law is employed to **formulate** equations in the **coordinate** system that is **located** on the launch **site**.

**Forces** that influence the **ascent** trajectory are propulsive, gravitational and **aerodynamic**.