



American Computer Science League

2019-2020

Contest #2

SENIOR DIVISION SOLUTIONS

1. Prefix/Infix/Postfix Notation

$$\begin{aligned}
 \text{Prefix: } & * a + a \uparrow + \uparrow a 2 * 4 \uparrow b 2 / 1 2 \\
 & = * a + a \uparrow + (\uparrow a 2) * 4 (\uparrow b 2) (/ 1 2) \\
 & = * a + a \uparrow + (a \uparrow 2) (4 * (b \uparrow 2) (1/2)) \\
 & = * a + a \uparrow ((a \uparrow 2) + (4 * (b \uparrow 2)) (1/2)) \\
 & = * a + a (((a \uparrow 2) + (4 * (b \uparrow 2)) \uparrow (1/2))) \\
 & = * a (a + (((a \uparrow 2) + (4 * (b \uparrow 2)) \uparrow (1/2)))) \\
 & = (a * (a + (((a \uparrow 2) + (4 * (b \uparrow 2)) \uparrow (1/2))))))
 \end{aligned}$$

$$\begin{aligned}
 \text{Infix: } & a * (a + (a \uparrow 2 + 4 * b \uparrow 2) \uparrow (1/2)) \\
 & = a * (a + ((a \uparrow 2) + 4 * (b \uparrow 2)) \uparrow (1/2)) \\
 & = a * (a + ((a \uparrow 2) + (4 * (b \uparrow 2)) \uparrow (1/2))) \\
 & = a * (a + (a \uparrow 2 \uparrow 4 b \uparrow 2 \uparrow * + 1/2 \uparrow)) \\
 & = a * (a a \uparrow 2 \uparrow 4 b \uparrow 2 \uparrow * + 1/2 \uparrow +) \\
 & = a a a \uparrow 2 \uparrow 4 b \uparrow 2 \uparrow * + 1/2 \uparrow + *
 \end{aligned}$$

$$\text{Postfix: } a a a \uparrow 2 \uparrow 4 b \uparrow 2 \uparrow * + 1/2 \uparrow + *$$

This is the formula for the surface area of a square pyramid with a base of length a and height of b.

1. As shown

2. Prefix/Infix/Postfix Notation

$$\begin{aligned}
 & - \# / + 7 5 2 - 6 * 4 1 \uparrow 4 2 @ - 6 3 + 5 2 \uparrow 2 3 \\
 & = - \# / (+ 7 5) 2 - 6 (* 4 1) (\uparrow 4 2) @ (- 6 3) (+ 5 2) (\uparrow 2 3) \\
 & = - \# (/ 12 2) (- 6 4) 16 (@ 3 7 8) \\
 & = - (\# 6 2 16) 9 \\
 & = (- 64 9) = 55
 \end{aligned}$$

2. 55

3. Bit-String Flicking

$$\begin{aligned}
 & (\text{LCIRC-2 } 01101) \text{ OR } (\text{NOT } 10110) \text{ AND } (\text{RSHIFT-1 } (\text{RCIRC-2 } 10110)) \\
 & = 10101 \text{ OR } 01001 \text{ AND } (\text{RSHIFT-1 } 10101) \\
 & = 10101 \text{ OR } 01001 \text{ AND } 01010 \\
 & = 10101 \text{ OR } 01000 = 11101
 \end{aligned}$$

3. 11101



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4. Bit-String Flicking

Let $X = abcde$

$LHS = (LSHIFT -1\ 10111) \text{ OR } (LCIRC -2\ (RSHIFT -1\ abcde))$
 $\qquad\qquad\qquad AND\ RCIRC -3\ (NOT\ 01101)$

$= 01110 \text{ OR } (LCIRC -2\ 0abcd) \text{ AND } (RCIRC -3\ 10010)$

$= 01110 \text{ OR } bcd0a \text{ AND } 01010$

$= 01110 \text{ OR } 0c000$

$= 01110$

$LHS = RHS = 01110$

Therefore $a = *, b = *, c = *, d = *, e = *$

4. *****

5. LISP

$(CAR\ (CDR\ (CAR\ (REVERSE\ (CDR\ '((a\ (b\ c))\ c\ d\ (e\ (d\ a\ (c\ b\ (e))))))))))$

$= (CAR\ (CDR\ (CAR\ (REVERSE\ ' (c\ d\ (e\ (d\ a\ (c\ b\ (e))))))))$

$= (CAR\ (CDR\ (CAR\ ' ((e\ (d\ a\ (c\ b\ (e)))d\ c))))$

$= (CAR\ (CDR\ ' (e\ (d\ a\ (c\ b\ (e)))))$

$= (CAR\ ' ((d\ a\ (c\ b\ (e))))$

$= (d\ a\ (c\ b\ (e)))$

5. (d a (c b (e)))