

American Computer Science League

2020-2021 • Contest 3: Solutions • Senior Division

1. Boolean Algebra

$$\begin{aligned} A\overline{B} + \overline{B}\overline{C} + \overline{A}C &= A\overline{B} + (\overline{B} + \overline{C}) + \overline{A}C \\ &= \overline{B}(A + 1) + \overline{C} + \overline{A}C \\ &= \overline{B} + \overline{C} + \overline{A}C \end{aligned}$$

To be FALSE, each term must be 0.

$$\overline{B} = 0 \Rightarrow B = 1 \text{ and } \overline{C} = 0 \Rightarrow C = 1$$

$$\overline{A}C = 0, C = 1 \Rightarrow \overline{A} = 0 \Rightarrow A = 1$$

Therefore (1, 1, 1) makes it FALSE.

1. (1, 1, 1) (A)

2. Boolean Algebra

$$\begin{aligned} \overline{A}\overline{\overline{A}\overline{B}}\overline{B}\overline{C} + \overline{C} &= (\overline{A} + \overline{\overline{A}\overline{B}})(\overline{B} + \overline{C}) + \overline{C} \\ &= \overline{A}\overline{B} + \overline{A}\overline{C} + A\overline{B}B + AB\overline{C} + \overline{C} \\ &= \overline{A}\overline{B} + (\overline{A}\overline{C} + AB\overline{C} + \overline{C}) \\ &= \overline{A}\overline{B} + \overline{C} \end{aligned}$$

To be TRUE, at least one term is TRUE.

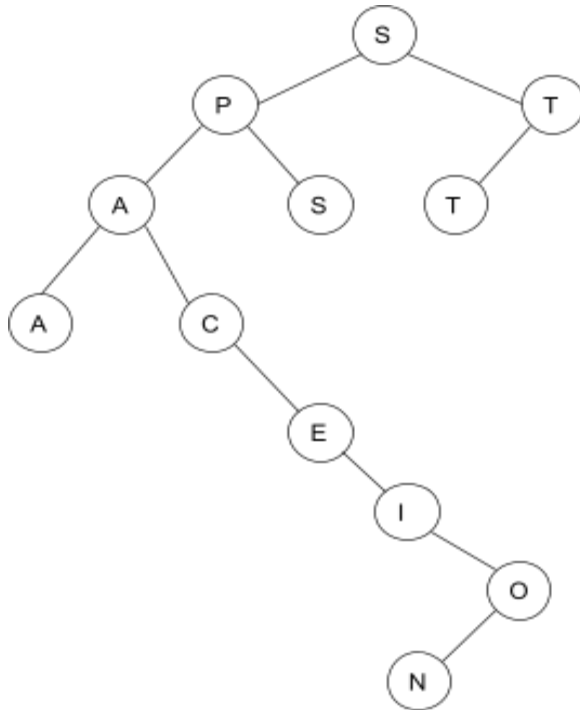
If $\overline{C} = 1$, then $C = 0$, $A = *$, $B = *$ \Rightarrow 4 triples

If $\overline{C} = 0$, then $C = 1$, $\overline{A}\overline{B} = 1 \Rightarrow \overline{A} = 1, \overline{B} = 1$
 $\Rightarrow A = 0, B = 0 \Rightarrow$ 1 triple

2. 5 (D)

3. Data Structures

The binary search tree for SPACESTATION is:



The internal path length is:

$$\begin{aligned} &2*1 + 3*2 + 2*3 + 1*4 + 1*5 + 1*6 + 1*7 \\ &= 2 + 6 + 6 + 4 + 5 + 6 + 7 \\ &= 36 \end{aligned}$$

3. 36 (C)

4. Data Structures

The stack is constructed using LIFO and the additional rule as follows:

A, AT, AT~~F~~, A, A~~A~~, AC, ACK, AC, A, AO. AOF, AOFT, AOF,
AOFH, AOFHE, AOFHEE, AOFHEM, AOFHEMP, AOFHEM,
AOFHE, AOFHEI, AOFHEIR, AOFHEI, AOFHE, AOFHEE,
AOFH, AOF

The next item popped would be an F.

4. F (B)

5. FSA's & Regular Expressions

The regular expression is: `[^dkp]*[aeiou][a-el-t]?(s|es|er)`

Choices A, D, E and G cannot be accepted based on the following:

- A. dahlias - string cannot start with d
- B. roses - valid
- C. lilies - valid
- D. aster - s and t cannot both come from `[a-el-t]?`
- E. azaleas - valid
- F. irises - valid
- G. clover - v is not in `[a-el-t]?`
- H. lilacs - valid
- I. violets - valid

5. A, D, G (E)