American Computer Science League

Contest #1

INTERMEDIATE DIVISION SOLUTIONS

1.	Computer	Number	Systems
----	----------	--------	----------------

 $23A4B_{16} = 0010\ 0011\ 1010\ 0100\ 1011\ {}_{2} = 100\ 011\ 101\ 001\ 001\ 011\ {}_{2} = 4 \quad 3 \quad 5 \quad 1 \quad 1 \quad 3\ {}_{8}$

1. 435113₈ or 435113

2. Computer Number Systems

 $1_{10} = 1_2$ and $32_{10} = 100000_2$ Number of digits in the binary number:

Number with more 1's than 0's:

1 1 3 4 11

Total is 20.

2. 20

3. Recursive Functions

$$f(20) = f(f(20-2)) + 1 = f(f(18)) + 1 = f(2) + 1 = 1 + 1 = 2$$

$$f(18) = f(f(18-2)) + 1 = f(f(16)) + 1 = f(2) + 1 = 1 + 1 = 2$$

$$f(16) = f(f(16-2)) + 1 = f(f(14)) + 1 = f(2) + 1 = 1 + 1 = 2$$

$$f(14) = f([14/2]) - 1 = f(7) - 1 = 3 - 1 = 2$$

$$f(7) = [7/2] = 3$$

$$f(2) = [2/2] = 1$$

3. 2

4. Recursive Functions

$$f(1) = 2$$
$$f(2) = -2$$

$$f(3) = 2 * f(3-1) + 3 * f(3-2) - 1 = 2 * f(2) + 3 * f(1) - 1$$

= 2 * (-2) + 3 * 2 - 1 = -4 + 6 - 1 = 1

$$f(4) = 2 * f(3) + 3 * f(2) - 1 = 2 * 1 + 3 * (-2) - 1 = 2 - 6 - 1 = -5$$

$$f(5) = 2 * f(4) + 3 * f(3) - 1 = 2 * (-5) + 3 * 1 - 1 = -10 + 3 - 1 = -8$$

$$f(6) = 2 * f(5) + 3 * f(4) - 1 = 2 * (-8) + 3 * (-5) - 1 = -16 - 15 - 1 = -32$$

$$f(7) = 2 * f(6) + 3 * f(5) - 1 = 2 * (-32) + 3 * (-8) - 1 = -64 - 24 - 1 = -89$$

4. -89

American Computer Science League

Contest #1

5. -7

INTERMEDIATE DIVISION SOLUTIONS

5. What Does This Program Do?

a	b	c	d	e	f
10	2	40	5	100	16
10	2	40	10	100	16
10	2	40	10	0	16
10	2	20	10	0	16
10	2	20	10	0	4
10	2	20	10	0	4
10	2	20	10	0	2

$$g = a * b + c + d + e + f * a$$

= 10 * 2 + 20 + 10 + 0 + 2 * 10 = 20 + 20 + 10 + 0 + 20 = 70

$$\begin{split} h &= g \, / \, (c - a) + b * (c \uparrow e + f) \, / \, 3 - b \uparrow a \, / \, f \uparrow 5 \, / \, b \\ &= 70 \, / \, (20 - 10) + 2 * (20 \uparrow 0 + 2) \, / \, 3 - 2 \uparrow 10 \, / \, 2 \uparrow 5 \, / \, 2 \\ &= 70 \, / \, 10 + 2 * (1 + 2) \, / \, 3 - 1024 \, / \, 32 \, / \, 2 \\ &= 7 + 2 * 3 \, / \, 3 - 32 \, / \, 2 \\ &= 7 + 2 - 16 \\ &= -7 \end{split}$$