

American Computer Science League

2018-2019

Contest #2

SENIOR DIVISION SOLUTIONS

<p>1. Pre/Post/Infix Notation</p> $ \begin{aligned} &+ / \uparrow 2 \ 4 \# 2 \ 1 * \# 4 \ 5 \uparrow / - * 6 \ 3 \uparrow 2 \ 3 * 5 \ 2 \# 2 \ 2 \\ &= + / (\uparrow 2 \ 4) (\# 2 \ 1) * (\# 4 \ 5) \uparrow / - (* 6 \ 3) (\uparrow 2 \ 3) (* 5 \ 2) (\# 2 \ 2) \\ &= + (/ 16 \ 2) * 5 \uparrow / (- 18 \ 8) 10 \ 2 \\ &= + 8 * 5 \uparrow (/ 10 \ 10) 2 = + 8 * 5 (\uparrow 1 \ 2) \\ &= + 8 (* 5 \ 1) = + 8 \ 5 = 13 \end{aligned} $	<p>1. 13</p>
<p>2. Pre/Post/Infix Notation</p> <p>Prefix: $- + / * A + B C \uparrow B \ 2 / * B C A / + \uparrow A \ 2 \uparrow B \ 2 C$</p> $ \begin{aligned} &= - + / * A (+ B C) (\uparrow B \ 2) / (* B C) A / + (\uparrow A \ 2) (\uparrow B \ 2) C \\ &= - + / (* A (B + C)) (B \uparrow 2) (/ (B * C) A) / (+ (A \uparrow 2) (B \uparrow 2)) C \\ &= - + (/ (A * (B + C)) (B \uparrow 2)) ((B * C) / A) (/ (A \uparrow 2 + B \uparrow 2) C) \\ &= - (+ ((A * (B + C)) / (B \uparrow 2)) ((B * C) / A)) ((A \uparrow 2 + B \uparrow 2) / C) \\ &= - (((A * (B + C)) / (B \uparrow 2)) + ((B * C) / A)) ((A \uparrow 2 + B \uparrow 2) / C) \end{aligned} $ <p>Infix :</p> $ \begin{aligned} &= (((A * (B + C)) / (B \uparrow 2)) + ((B * C) / A)) - ((A \uparrow 2 + B \uparrow 2) / C) \\ &= (((A B C + *) / (B \ 2 \uparrow)) + (B C * A /)) - (A \ 2 \uparrow B \ 2 \uparrow + C /) \\ &= ((A B C + * B \ 2 \uparrow /) + (B C * A /)) - (A \ 2 \uparrow B \ 2 \uparrow + C /) \\ &= (A B C + * B \ 2 \uparrow / B C * A / +) - (A \ 2 \uparrow B \ 2 \uparrow + C /) \end{aligned} $ <p>Postfix: $= A B C + * B \ 2 \uparrow / B C * A / + A \ 2 \uparrow B \ 2 \uparrow + C / -$</p>	<p>2. As shown</p>
<p>3. Bit-String Flicking</p> $ \begin{aligned} &(\text{LSHIFT-2 } 01101) \text{ AND } ((\text{RCIRC-3 } 10010) \text{ OR } 01100) \\ &= 10100 \text{ AND } (01010 \text{ OR } 01100) \\ &= 10100 \text{ AND } 01110 = 00100 \end{aligned} $	<p>3. 00100</p>
<p>4. Bit-String Flicking</p> <p>Let $X = abcde$</p> $ \begin{aligned} \text{LHS} &= (\text{LCIRC-2 } (\text{RSHIFT-1 } (\text{LCIRC-2 } abcde))) \\ &= (\text{LCIRC-2 } (\text{RSHIFT-1 } cdeab)) \\ &= (\text{LCIRC-2 } 0cdea) = dea0c \\ \text{RHS} &= 01001 \text{ OR } (\text{NOT } 10110) = 01001 \text{ OR } 01001 = 01001 \\ \text{LHS} &= \text{RHS} \rightarrow dea0c = 01001 \rightarrow d = 0, e = 1, a = 0, c = 1, b = * \\ \text{Therefore } X &= 0*101 \end{aligned} $	<p>4. 0*101</p>

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5. LISP

5. (2 3)

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(CAR(CDR(CAR(CAR(REVERSE(CDR(CDR
  (CDR '((1 (2 3)) (2 3) 4 (2 3 (1)) 2 3 ((1 (2 3) 4) 1))))))))))
= (CAR(CDR(CAR(CAR(REVERSE(CDR
  (CDR '((2 3) 4 (2 3 (1)) 2 3 ((1 (2 3) 4) 1))))))))))
= (CAR(CDR(CAR(CAR(REVERSE
  (CDR '(4 (2 3 (1)) 2 3 ((1 (2 3) 4) 1))))))))))
= (CAR(CDR(CAR(CAR(REVERSE '((2 3 (1)) 2 3 ((1 (2 3) 4) 1)))))))
= (CAR(CDR(CAR(CAR '((1 (2 3) 4) 1) 3 2 (2 3 (1))))))
= (CAR(CDR(CAR '((1 (2 3) 4) 1)))
= (CAR(CDR '(1 (2 3) 4)))
= (CAR '((2 3) 4))
= (2 3)
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