# Program 1 Report

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# Contents

1	Documentation	2
2	Source code 2.1 EvalXOverMutate.cpp	2
3	Execution output 3.1 Output analysis	
4	Discussions	13
5	Lab Sessions 1 5.1 Execution output	<b>1</b> 4

### 1 Documentation

In this project, we tried to solve Traveling salesman problem (TSP) with genetic algorithm. We are required to implement the core part of the algorithm: evaluation, crossover and mutation. Tsp problem often takes large amount of data and time. And to improve the efficiency, our approach is using OpenMP. My initial attempt is implement a greedy parallelization: parallelize the whole program from evaluate() to populate() with:

```
#pragma omp parallel for
```

however, after trying different things with the program, I realized that populate and mutate does not need to be parallelized. The time spent did increase not have much difference. And select() with parallelization could spend more time than when running multi-thread. Therefore, the only functions I need to parallelize are crossover() and evaluate() which contain much larger loops. I simply added #pragma omp parallel for before the outer for loop inside crossover() and evaluate().

#### 2 Source code

# 2.1 EvalXOverMutate.cpp

```
1
     // Created by yangxiao on 10/8/2018.
2
3
                            // cout
     #include <iostream>
4
                            // ifstream
     #include <fstream>
5
     #include <string.h>
                            // strncpy
6
     #include <stdlib.h>
                            // rand
7
     #include <math.h>
                            // sqrt, pow
8
     #include <time.h>
9
     #include <omp.h>
10
11
     #include <bits/stdc++.h>
     #include "Trip.h"
12
13
     using namespace std;
14
15
16
      float getDis(char a, char b, int coordinates[CITIES][2]);
^{17}
18
      float getDisFromIt(char str[CITIES], float disMax[CITIES][CITIES + 1]);
19
20
     char *getChildB(char childA[CITIES]);
21
22
     int getIndex(char a, char source[CITIES]);
^{23}
24
      int getAscii(char source);
^{25}
26
     const char cit[] = "ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789";
27
28
29
     * Compare tow trip based their fitness, uses as comparator for sorting
30
     * @param t1 trip 1
31
      * @param t2 trip 2
32
     * @return if t1 < t2
33
```

```
35
      bool compareTrip(Trip t1, Trip t2) {
      return (t1.fitness < t2.fitness);</pre>
36
37
38
      /**
39
      * evaluates the distance of each trip and sorts out all the trips
40
      * in the shortest-first order
41
      * @param trip trips to evaluates
42
      * @param coordinates coordinates of all cities
43
      */
44
      void evaluate(Trip trip[CHROMOSOMES], int coordinates[CITIES][2]) {
^{45}
46
      //Parallelization
47
48
      #pragma omp parallel for
      for (int i = 0; i < CHROMOSOMES; ++i) {</pre>
49
      char temp[CITIES];
50
      strncpy(temp, trip[i].itinerary, CITIES);
51
      int indexIn = (temp[0] >= 'A')? temp[0] - 'A': temp[0] - '0' + 26;
52
      double dis = hypot(coordinates[indexIn][0], coordinates[indexIn][1]);
53
      for (int j = 1; j < CITIES; ++j) {
54
      55
      \mathtt{dis} \; +\!\!= \; \mathtt{hypot} \, (\, (\, \mathtt{coordinates} \, [\, \mathtt{indexIn} \, ] \, [\, 0 \, ] \; - \; \mathtt{coordinates} \, [\, \mathtt{index} \, ] \, [\, 0 \, ] \, ) \; ,
56
      (\verb|coordinates|| indexIn | [1] - \verb|coordinates|| index | [1]));
57
      indexIn = index;
58
59
      trip[i].fitness = (float) dis;
60
61
      sort(trip, trip + CHROMOSOMES, compareTrip);
62
63
64
65
      * generates 25,000 off-springs from the parents, calculate distance
66
      * based on their coordinates
      * @param parents
68
      * @param offsprings
69
      * @param coordinates
70
      */
71
      void crossover(Trip parents[TOP_X], Trip offsprings[TOP_X],
72
      int coordinates[CITIES][2]) {
73
74
      #pragma omp parallel for
      for (int i = 0; i < TOP_X; i += 2) {
75
      int selected[100] = \{0\};
76
      char child1[CITIES + 1];
77
      char child2[CITIES + 1];
78
      char *parent1 = parents[i].itinerary;
79
      char *parent2 = parents[i + 1].itinerary;
80
      \mathtt{child1} \hspace{.05cm} [\hspace{.05cm} 0\hspace{.05cm}] \hspace{.1cm} = \hspace{.1cm} \mathtt{parent1} \hspace{.05cm} [\hspace{.05cm} 0\hspace{.05cm}] \hspace{.1cm} ;
81
      selected[child1[0]] = 1;
82
83
      for (int j = 0; j < (CITIES - 1); j++) {
84
      int indexInA = getIndex(child1[j], parent1) + 1;
85
      int indexInB = getIndex(child1[j], parent2) + 1;
86
87
88
      if (indexInA = -1 \mid | indexInB = -1) {
      printf("WHat?\n");
89
90
91
92
      if (indexInA >= CITIES) {
      indexInA = 0;
93
94
      if (indexInB >= CITIES) {
```

```
indexInB = 0;
96
97
98
       float disA = INT_MAX;
99
       float disB = INT_MAX;
100
101
       if (selected[parent1[indexInA]] == 0) {
102
       disA = getDis(child1[j], parent1[indexInA], coordinates);
103
104
       if (selected[parent2[indexInB]] == 0) {
105
       {\tt disB} \, = \, {\tt getDis} \, (\, {\tt child1} \, [\, {\tt j}\, ] \, \, , \, \, \, {\tt parent2} \, [\, {\tt indexInB} \, ] \, \, , \, \, \, {\tt coordinates} \, ) \, ;
106
107
108
       if (disA = INT_MAX \&\& disB = INT_MAX) {
109
110
       int r = rand() \% CITIES;
       int found = 1;
111
       while (found) {
112
       if (selected[parent1[r]] != 1) {
113
       found = 0;
114
       \mathtt{child1} [ \mathtt{j} + \mathtt{1} ] = \mathtt{parent1} [ \mathtt{r} ];
115
116
       r = ((r + 1) >= CITIES) ? 0 : (r + 1);
117
118
       } else {
119
       child1[j + 1] = (disA \ll disB)?
120
       parent1[indexInA] : parent2[indexInB];
121
122
123
       selected[child1[j + 1]] = 1;
124
125
126
127
       strcpy(child2, getChildB(child1));
128
       strncpy(offsprings[i].itinerary, child1, CITIES);
129
       strncpy(offsprings[i + 1].itinerary, child2, CITIES);
130
131
132
133
134
135
       * Improved version, when mutate each city,
136
       * perform mutation if the new one has shorter distance,
137
       * otherwise, do nothing
138
139
       * randomly chooses two distinct cities (or genes)
140
       * in each trip (or chromosome) with a
141
       * given probability, and swaps them
142
       * @param offsprings
143
       * @param disMax
144
145
       146
       for (int i = 0; i < TOP_X; ++i) {
147
       int rate = rand() \% 100;
148
149
       if (rate < MUTATE_RATE) {</pre>
150
       int r1 = rand() \% CITIES;
151
       int r2 = rand() \% CITIES;
       char temp[CITIES + 1];
152
       strncpy(temp, offsprings[i].itinerary, CITIES);
153
       temp[r1] = offsprings[i].itinerary[r2];
154
       temp[r2] = offsprings[i].itinerary[r1];
155
156
       float d1 = getDisFromIt(offsprings[i].itinerary, disMax);
       float d2 = getDisFromIt(temp, disMax);
157
```

```
//check if the new one has shorter distacne
158
159
      if (d1 > d2)  {
160
      strncpy(offsprings[i].itinerary, temp, CITIES);
161
162
163
164
165
166
      * Helper function that calculate distance between two cities
167
168
      float getDis(char a, char b, int coordinates[CITIES][2]) {
169
      int indexA = (a >= 'A') ? a - 'A' : a - '0' + 26;
170
      int indexB = (b >= 'A') ? b - 'A' : b - '0' + 26;
171
172
      float dis = (float) hypot((coordinates[indexA][0] - coordinates[indexB][0]),
      (coordinates[indexA][1] - coordinates[indexB][1]);
173
      return dis;
174
175
176
177
      * Get distacne of the provided route from distance matrix
178
179
      float getDisFromIt(char str[CITIES], float disMax[CITIES][CITIES + 1]) {
180
      int indexIn = (str[0] >= 'A') ? str[0] - 'A' : str[0] - '0' + 26;
181
      double dis = disMax[indexIn][CITIES];
182
      for (int j = 1; j < CITIES; ++j) {
183
      int index = (str[j] >= 'A') ? str[j] - 'A' : str[j] - '0' + 26;
184
185
      dis += disMax[indexIn][index];
186
      indexIn = index;
187
188
189
      return dis;
190
191
192
      * Get the position of the target character
193
      * @param a target character
194
      * @param source source string
195
      * @return index of target char, -1 if not found
196
      */
197
198
      int getIndex(char a, char source[CITIES]) {
      for (int i = 0; i < CITIES; ++i) {
199
      if (a == source[i]) return i;
200
201
      return -1;
202
203
204
205
      * get ascii representation of target char, and map it to its index
206
      * based on ABCDEFGHIJKLMNOPQRSTUVWXYZ0123456789
207
208
      int getAscii(char source) {
209
      return (source >= 'A') ? source - 'A' : source - '0' + 26;
210
211
      }
212
213
      * generate childA's complement
214
215
      char *getChildB(char childA[CITIES]) {
216
217
      char *childB = (char *) malloc(sizeof(char) * CITIES);
      for (int i = 0; i < CITIES; ++i) {
218
      childB[i] = cit[(CITIES - getAscii(childA[i]) - 1)];
219
```

```
220
221
      return childB;
222
      }
223
224
      /**
225
      * Improved version with distance matrix, avoid calculating distance
226
      * generates 25,000 off-springs from the parents,
227
      * calculate distance based on their coordinates
228
      * @param parents
229
      * @param offsprings
230
      * @param disMax
231
232
      */
      void crossoverB(Trip parents[TOP\_X], Trip offsprings[TOP\_X], float disMax[ \leftrightarrow
233
          CITIES | [CITIES + 1]) {
      #pragma omp parallel for default(none) shared(parents, disMax, offsprings)
234
      for (int i = 0; i < TOP_X; i += 2) {
235
      int selected[100] = \{0\};
236
      char child1[CITIES + 1];
237
      char child2[CITIES + 1];
238
      char *parent1 = parents[i].itinerary;
      char *parent2 = parents[i + 1].itinerary;
240
      child1[0] = parent1[0];
241
      selected[child1[0]] = 1;
242
243
      for (int j = 0; j < (CITIES - 1); j++) {
244
       int indexInA = getIndex(child1[j], parent1) + 1;
245
246
      int indexInB = getIndex(child1[j], parent2) + 1;
247
      if (indexInA = -1 \mid | indexInB = -1) {
248
      printf("WHat?\n");
249
250
251
       if (indexInA >= CITIES) {
252
      indexInA = 0;
253
254
      if (indexInB >= CITIES) {
255
      indexInB = 0;
256
257
258
259
       float disA = INT_MAX;
       float disB = INT_MAX;
260
261
       if (selected[parent1[indexInA]] == 0) {
262
       int indA = getAscii(child1[j]);
263
      int indB = getAscii(parent1[indexInA]);
264
      disA = disMax[indA][indB];
265
266
      if (selected[parent2[indexInB]] == 0) {
267
      int indA = getAscii(child1[j]);
268
      int indB = getAscii(parent2[indexInB]);
269
      disB = disMax[indA][indB];
270
271
      }
272
273
       if (disA = INT_MAX \&\& disB = INT_MAX) {
274
      int r = rand() % CITIES;
      int found = 0;
275
       while (!found) {
276
       if (selected[parent1[r]] != 1) {
277
      found = 1;
278
279
      child1[j + 1] = parent1[r];
280
```

```
r = ((r + 1) >= CITIES) ? 0 : (r + 1);
281
282
283
      } else {
      child1[j + 1] = (disA <= disB) ? parent1[indexInA] : parent2[indexInB];</pre>
284
285
286
      selected[child1[j + 1]] = 1;
287
288
289
      strcpy(child2, getChildB(child1));
290
      strncpy(offsprings[i].itinerary, child1, CITIES);
291
      strncpy(offsprings[i + 1].itinerary, child2, CITIES);
292
293
294
295
296
      * randomly chooses two distinct cities (or genes)
297
      * in each trip (or chromosome) with a
298
      * given probability, and swaps them
299
      * @param offsprings
300
301
      void mutate(Trip offsprings[TOP_X]) {
302
      for (int i = 0; i < TOP_X; ++i) {
303
      int rate = rand() % 100;
304
      if (rate < MUTATE_RATE) {</pre>
305
      int r1 = rand() \% CITIES;
306
      int r2 = rand() \% CITIES;
307
308
      char x1 = offsprings[i].itinerary[r1];
      char x2 = offsprings[i].itinerary[r2];
309
      offsprings[i].itinerary[r1] = x2;
310
      offsprings[i].itinerary[r2] = x1;
311
312
313
      }
314
315
316
317
      * Improved verison, uses distance matrix to avoid calculating distance
318
      * Evaluates the distance of each trip and sorts out all the
319
      * trips in the shortest-first order
320
      * @param trip trips to evaluates
      * @param disMax maxtrix that contain all the distance
322
      * @param first if it's first generation
323
      */
324
      void evaluateB(Trip trip[CHROMOSOMES],
325
      float disMax[CITIES][CITIES + 1], bool first) {
326
      int start = 0;
      if (!first) {
328
      start = TOP_X;
329
330
331
      #pragma omp parallel for default(none) firstprivate(start) shared(trip, \leftarrow
332
          disMax)
333
      for (int i = start; i < CHROMOSOMES; ++i) {</pre>
334
      char temp[CITIES];
335
      strncpy(temp, trip[i].itinerary, CITIES);
      int indexIn = (temp[0] >= 'A')? temp[0] - 'A': temp[0] - '0' + 26;
336
      double dis = disMax[indexIn][CITIES];
337
      for (int j = 1; j < CITIES; ++j) {
338
      int index = (temp[j] >= 'A')? temp[j] - 'A': temp[j] - '0' + 26;
339
      dis += disMax[indexIn][index];
340
341
```

#### 2.2 Tsp.cpp

```
1
     #include <iostream> // cout
2
     #include <fstream>
                            // ifstream
     #include <string.h> // strncpy
3
     #include <stdlib.h> // rand
4
5
     #include <math.h>
                            // sqrt, pow
                            // OpenMP
6
     #include <omp.h>
     #include "Timer.h"
7
     #include "Trip.h"
8
9
     using namespace std;
10
11
      void initialize(Trip trip[CHROMOSOMES], int coordinates[CITIES][2]);
12
13
      void select(Trip trip[CHROMOSOMES], Trip parents[TOP_X]);
14
15
      void populate(Trip trip[CHROMOSOMES], Trip offsprings[TOP_X]);
16
17
      void formDisMax(int coordinates[CITIES][2], float disMax[CITIES][CITIES + 1])\leftarrow
18
19
      extern void evaluate(Trip trip[CHROMOSOMES], int coordinates[CITIES][2]);
20
21
      extern void evaluateB(Trip trip[CHROMOSOMES], float disMax[CITIES][CITIES + \leftarrow
22
         1], bool first);
23
     extern void crossover(Trip parents[TOP_X], Trip offsprings[TOP_X], int ←
24
         coordinates [CITIES][2]);
25
      extern void crossoverB(Trip parents[TOP_X], Trip offsprings[TOP_X], float ↔
26
         disMax[CITIES][CITIES +
27
      1]);
      extern void mutate(Trip offsprings[TOP_X]);
^{28}
      extern void mutateB(Trip offsprings[TOP_X], float disMax[CITIES][CITIES + 1])\leftarrow
30
31
32
      * MAIN: usage: Tsp #threads
33
34
      int main(int argc, char *argv[]) {
35
      //Start random seed based on current time value
36
     srand(time(NULL));
37
38
      //static is required on windows machine
39
                                        // all 50000 different trips (or \leftrightarrow
      static Trip trip[CHROMOSOMES];
40
         chromosomes)
     Trip shortest;
                                     // the shortest path so far
41
                                    // (x, y) coordinates of all 36 cities:
      int coordinates[CITIES][2];
42
      int nThreads = 1;
43
      float disMax[CITIES][CITIES + 1];
44
45
      // verify the arguments
46
      if (argc = 2)
47
     nThreads = atoi(argv[1]);
48
49
      cout << "usage: Tsp #threads" << endl;</pre>
50
     if (argc != 1)
51
```

```
return -1; // wrong arguments
52
53
      cout << "# threads = " << nThreads << endl;</pre>
54
55
      // shortest path not yet initialized
56
      shortest.itinerary[CITIES] = 0; // null path
57
                                          // invalid distance
      shortest.fitness = -1.0;
58
59
      // initialize 5000 trips and 36 cities ' coordinates
60
      initialize(trip, coordinates);
61
62
      //from a distance matrix to improve efficiency
63
      formDisMax(coordinates, disMax);
64
65
66
      // start a timer
67
      Timer timer;
      timer.start();
68
69
      // change # of threads
70
      omp_set_num_threads(nThreads);
71
      // find the shortest path in each generation
73
      for (int generation = 0; generation < MAX_GENERATION; generation++) {
74
      // evaluate the distance of all 50000 trips
75
      evaluate(trip, coordinates, generation == 0);
76
77
      // just print out the progress
78
79
      if (generation \% 20 == 0)
      cout << "generation: " << generation << endl;</pre>
80
81
      // whenever a shorter path was found, update the shortest path
82
      if (shortest.fitness < 0 \mid | shortest.fitness > trip[0].fitness) {
83
      strncpy(shortest.itinerary, trip[0].itinerary, CITIES);
84
      shortest.fitness = trip[0].fitness;
85
86
      cout << "generation: " << generation</pre>
87
      << " shortest distance = " << shortest.fitness
88
      << "\t itinerary = " << shortest.itinerary << endl;</pre>
89
90
91
92
      // define TOP_X parents and offsprings.
      // static is required on windows machine
93
      static Trip parents[TOP_X], offsprings[TOP_X];
94
95
      // choose TOP_X parents from trip
96
97
      select(trip, parents);
98
      // generates TOP_X offsprings from TOP_X parenets
99
      crossover(parents, offsprings, coordinates);
100
101
      // mutate offsprings
102
      mutateB(offsprings, disMax);
103
      // populate the next generation.
104
105
      populate(trip, offsprings);
106
107
      // stop a timer
108
      cout << "elapsed time = " << timer.lap() << endl;</pre>
109
110
      return 0;
111
      }
112
      * Initializes trip [CHROMOSOMES] with chromosome.txt and coordinates [CITIES -
113
```

```
[2] with cities.txt
114
       * @param trip[CHROMOSOMES]:
                                           50000 different trips
115
       * @param coordinates [CITIES][2]: (x, y) coordinates of 36 different cities: \leftarrow
116
          ABCDEFGHIJKLMNOPQRSTUVWXYZ
      */
117
       void initialize(Trip trip[CHROMOSOMES], int coordinates[CITIES][2]) {
118
       // open two files to read chromosomes (i.e., trips) and cities
119
      ifstream chromosome_file("chromosome.txt");
120
      ifstream cities_file("cities.txt");
121
122
       for (int i = 0; i < CHROMOSOMES; i++) {</pre>
123
       chromosome_file >> trip[i].itinerary;
124
      trip[i].fitness = 0.0;
125
126
      }
127
       for (int i = 0; i < CITIES; i++) {
128
129
       char city;
       cities_file >> city;
130
       int index = (city \Rightarrow 'A') ? city - 'A' : city - '0' + 26;
131
       cities_file >> coordinates[index][0] >> coordinates[index][1];
132
133
134
       chromosome_file.close();
135
       cities_file.close();
136
137
       if (DEBUG) {
138
139
       for (int i = 0; i < CHROMOSOMES; i++)
       cout << trip[i].itinerary << endl;</pre>
140
       for (int i = 0; i < CITIES; i++)
141
      cout \ll coordinates[i][0] \ll "\t" \ll coordinates[i][1] \ll endl;
142
143
144
145
146
       * Select the first TOP_X parents from trip [CHROMOSOMES]
147
148
       * @param trip[CHROMOSOMES]: all trips
149
       * @param parents [TOP_X]:
                                     the firt TOP-X parents
150
       * /
151
      void select(Trip trip[CHROMOSOMES], Trip parents[TOP_X]) {
152
       // just copy TOP_X trips to parents
153
       for (int i = 0; i < TOP_X; i++)
154
      strncpy(parents[i].itinerary, trip[i].itinerary, CITIES + 1);
155
156
157
158
       * Replace the bottom TOP_X trips with the TOP_X offsprings
159
160
      161
       // just copy TOP_X offsprings to the bottom TOP_X trips.
162
       for (int i = 0; i < TOP_X; i++) {
163
       \mathtt{strncpy}(\mathtt{trip}[\mathtt{CHROMOSOMES} - \mathtt{TOP}_\mathtt{X} + \mathtt{i}].\mathtt{itinerary}, \ \mathtt{offsprings}[\mathtt{i}].\mathtt{itinerary}, \ \hookleftarrow
164
          CITIES);
165
       // for debugging
166
       if (DEBUG) {
167
       for (int chrom = 0; chrom < CHROMOSOMES; chrom++)
168
       cout << "chrom[" << chrom << "] = " << trip[chrom].itinerary</pre>
169
      << ", trip distance = " << trip[chrom].fitness << endl;</pre>
170
171
172
```

```
173
174
         * Generate CITIES distances for each city, total CITIES * CITIES distances
175
         * @param coordinates (x, y) coordinates of CITIES different cities
176
         * @param disMax Distance matrix
177
178
         void formDisMax(int coordinates[CITIES][2], float disMax[CITIES][CITIES + 1]) \leftarrow
179
              (int i = 0; i < CITIES; ++i)
180
         for (int j = 0; j < CITIES; ++j)
181
         \mathtt{disMax}\left[\,\mathbf{i}\,\right]\left[\,\mathbf{j}\,\right] \;=\; \mathtt{hypot}\left(\left(\,\mathsf{coordinates}\left[\,\mathbf{i}\,\right]\left[\,\mathbf{0}\,\right]\right. \;-\; \mathsf{coordinates}\left[\,\mathbf{j}\,\right]\left[\,\mathbf{0}\,\right]\right) \;,
182
         (coordinates[i][1] - coordinates[j][1]);
183
184
         disMax[i][CITIES] = hypot(coordinates[i][0], coordinates[i][1]);
185
186
187
```

## 3 Execution output

## 3.1 Output analysis

- 1. The shortest trip in my program is equal to 447.638
- 2. The performance improvement with four threads in my program is equal to 50548672 / 23005048 = 2.2 times

#### 3.2 Output

```
# threads = 1
generation: 0
generation: 0 shortest distance = 1265.72 itinerary = V1SPMBQAN26G4J37DX8OTF95ZUH0EYRLCWKI
generation: 1 shortest distance = 1031.81 itinerary = I61YHO9F48KGATL7UJR3BQ20ENXVSCZWP5MD
generation:\ 2\ shortest\ distance = 979.47\ itinerary = KFL94NT86OJAGX7RD3IU2W5PBS10EZHYVCMQ
generation: 3 \text{ shortest distance} = 882.109 \text{ itinerary} = V1O6XG84K9AFLPDBM3Q7NTIUZJE02HYCSW5R
generation: 4 \text{ shortest distance} = 724.804 \text{ itinerary} = V1YHEJUZ02CSW5MBQDR794X6IONTK8FALG3P
generation: 5 shortest distance = 627.852 itinerary = V1YHEZ02CSW5MPBQDR3JU7ALGF4NT89KX6IO
generation: 7 shortest distance = 626.585 itinerary = V1IO6JE02WCS5HZYFAL7R3DBQMPUKX4NT8G9
generation: 8 shortest distance = 603.274 itinerary = V1YHEUZJWSC205MPQ3RDB7LAF9KGX48TN6OI
generation: 10 shortest distance = 556.14 itinerary = V1YZHUE0MSWC5DBQR37LA9KFGXNT48IO6J2P
generation:\ 11\ shortest\ distance = 542.062\ itinerary = V1YZHUE0MPBQR37LA9KFGXNT48IO6J2SWC5D
generation: 13 \text{ shortest distance} = 477.948 \text{ itinerary} = V1YZHUE02WSC5MPBQDR37LA9KFGXNT48IO6J
generation: 16 shortest distance = 474.401 itinerary = V1YZHUE02WSC5MPBQDR37LAFK9GXNT48IO6J
generation: 18 shortest distance = 467.935 itinerary = V1YZHUE0J6OI84NTGXKF9AL7R3DBQPMSWC52
generation: 19 \text{ shortest distance} = 467.25 \text{ itinerary} = V1YZH5CWSMPQBDR37LAF9KGXNT48IO6J0E2U
generation: 20
generation:\ 20\ shortest\ distance = 464.471\ itinerary = V1YZHUE20J6OI84NTGX9FKAL7R3DBQPMWSC5
generation: 24 shortest distance = 461.723 itinerary = V1YZHUE025CWSMPQBDR37LA9KFGXNT48IO6J
generation: 30 \ shortest \ distance = 459.941 \ itinerary = V1YZHUE20J6OI84NTGX9FKAL7R3DBQPMSWC5
generation: 33 \ shortest \ distance = 459.436 \ itinerary = V1YZH5CWSMPQBDR37LAF9KGXNT48IO6JUE20
generation: 35 \ shortest \ distance = 458.176 \ itinerary = V1YZHUE025CWSMPQBDR37LAFK9GXNT48IO6J
generation: 37 \, shortest \, distance = 457.536 \, itinerary = V1YZH5CWSMPQBDR37LAF9KGXNT48IO6J02EU
generation: 40
generation: \ 43 \ shortest \ distance = 456.303 \ itinerary = V1YZHUE20J6OI84NTGX9KFAL7R3DBQPMSWC5
generation: 44 shortest distance = 452.975 itinerary = V1YZHUE025CWSMPQBDR37LAF9KGXNT48IO6J
generation: 54 \text{ shortest distance} = 449.658 \text{ itinerary} = V1YZHUE025CWSMPQBD3R7LAF9KGXNT48IO6J
generation: 60
generation: \ 61 \ shortest \ distance = 449.552 \ itinerary = V1YZHUE20J6OI84NTXGK9FAL7R3DBQPMSWC5
```

```
generation: 71 \, shortest \, distance = 447.638 \, itinerary = V1YZHUE20J6OI84TNXGK9FAL7R3DBQPMSWC5
generation: 80
generation: 100
generation: 120
generation: 140
elapsed time = 50548672
# threads = 4
generation: 0
generation: 0 \text{ shortest distance} = 1265.72 \text{ itinerary} = V1SPMBQAN26G4J37DX8OTF95ZUH0EYRLCWKI
generation:\ 1\ shortest\ distance = 1043.94\ itinerary = I61YHO9F48KGATL7UJR3BQ2P5SCZW0ENXVMD
generation: 2 \text{ shortest distance} = 871.976 \text{ itinerary} = \text{VU25BSCWMPQDR37JZHT8IONX9AF46K0EY1GL}
generation: 3 shortest distance = 825.757 itinerary = V8TNKA9FXGIO1HZYUE5C6RL73DMBQPSW2J04
generation: 4 \text{ shortest distance} = 805.385 \text{ itinerary} = 1 \text{VKF9X7AGTJ} 6 \text{OI4N83RL0SWC25BPMQDEUHYZ}
generation: 5 shortest distance = 716.93 itinerary = 8TN4X9KGAF6OIJ02EHYZU1VSCWM5BDL7R3QP
generation: 7 \text{ shortest distance} = 652.966 \text{ itinerary} = 1V6OI9KFAL7J0WC5SMPBQ3RDHZYUE284GXNT}
generation: 8 shortest distance = 635.406 itinerary = V1YIO6NTXK948GR3DBPMS5CW02ZHUEJ7LFAQ
generation:\ 9\ shortest\ distance = 583.042\ itinerary = V1YZUH5CSWMPBQD3R7AF9KTNX4GOI68L2E0J
generation:\ 10\ shortest\ distance = 564.252\ itinerary = V1YHUZ5CWSMPQBDR37LJOI4NT89FKXGA6E02
generation:\ 11\ shortest\ distance = 558.654\ itinerary = UHZY1VO6I8KGXNT49FAL7R3QBPMSWC520EJD
generation:\ 12\ shortest\ distance = 545.421\ itinerary = V1YZHUE20J6OI9FK84NTGXAL73RDBQSWCMP5
generation:\ 13\ shortest\ distance = 536.668\ itinerary = V1YZHUE20J6OI4N8T9XGKFAL73R5CWSMPQBD
generation: 14 \text{ shortest distance} = 520.507 \text{ itinerary} = V1YZHU5CWSE0J6OI84NTXG9KFAL7R3DBPM2Q}
generation: 15 \text{ shortest distance} = 496.876 \text{ itinerary} = V1YZHUE0J6OI84NTXGK9FLA7R325CWSMPBDQ}
generation:\ 16\ shortest\ distance = 496.376\ itinerary = V1YZHUE02WSC5MPQBD3R7LAGXKF984NTJ6OI
generation:\ 17\ shortest\ distance = 484.545\ itinerary = V1YZHUE02J6OI84NT9FKXGAL7R3QBDPMSWC5
generation:\ 18\ shortest\ distance = 469.679\ itinerary = V1YZHUE025CWSMPQBDR37LAFKGXNT849IO6J
generation: 20
generation:\ 22\ shortest\ distance = 467.855\ itinerary = V1YZHUE02J6OI84NT9FKXGAL7R3DBQPMSWC5
generation: 24 shortest distance = 460.906 itinerary = V1YZHUE20J6OI84NT9FKXGAL7R3DBQPMSWC5
generation: 29 \text{ shortest distance} = 460.657 \text{ itinerary} = V1YZHUE02J6OI84NTXGKF9AL7R3DBQPMSWC5
generation: 36 \text{ shortest distance} = 453.709 \text{ itinerary} = V1YZHUE20J6OI84NTXGKF9AL7R3DBQPMSWC5
generation: 40
generation: 43 \ shortest \ distance = 449.552 \ itinerary = V1YZHUE20J6OI84NTXGK9FAL7R3DBQPMSWC5
generation: 60
generation: 60 \text{ shortest distance} = 447.638 \text{ itinerary} = V1YZHUE20J6OI84TNXGK9FAL7R3DBQPMSWC5
generation: 80
generation: 100
generation: 120
generation: 140
elapsed time = 23005048
```

#### 4 Discussions

In addition, I tried to improve the whole efficiency by replacing calculating distance with a cached matrix that contains all the 36 \* 36 distance. This implementation decrease significant amount of time spent, although this made the program program with single thread runs faster than that with multi-thread. This also explained why select() with multi-thread could be slower than that with single thread. Starting a multi-thread could require some time to analysis the for-loop and distribute the tasks. Therefore, it is best to use multi-thread when the loop is large and require large computational power.

To improve the performance of current program, just use the implementation I mentioned above to shorten the time required to calculate the distance. However, this only works with the current data set, it could be less efficient with larger data sets.

### 5 Lab Sessions 1

Lab 1 we parallelize two programs that compute Pi using Monte Carlo methods and Integration. As the result shown, multi-thread decrease significant amount of time that required to finish the program. However, if the number of iterations is too small, the performance would decrease.

#### 5.1 Execution output

```
pi_integral_omp
Enter the number of iterations used to estimate pi: 1000000000
Enter the number of threads: 1
elapsed time for pi = 10850791
\# of trials = 1000000000, estimate of pi is 3.1415926535899708, Error is 0.000000000001776
Enter the number of iterations used to estimate pi: 1000000000
Enter the number of threads: 4
elapsed time for pi = 2831500
\# of trials = 1000000000, estimate of pi is 3.1415926535898211, Error is 0.0000000000000280
pi_monte_omp
Enter the number of iterations used to estimate pi: 1000000000
Enter the number of threads: 1
elapsed time for pi = 44118944
\# of trials = 1000000000, estimate of pi is 3.1416131730000001, Error is 0.0000205194102070
Enter the number of iterations used to estimate pi: 1000000000
Enter the number of threads: 4
elapsed time for pi = 14253004
\# of trials = 1000000000, estimate of pi is 3.1415967750000000, Error is 0.0000041214102069
```