

# Computational Graph for Multi-layer Perceptron (MLP)

definitions:

input:  $x \in \mathbb{R}^n$ ;  $y \in \mathbb{R}^m$

our MLP:  $f(x; W)$  weight matrix parameterizing our MLP

loss function:  $L(f(x, W), y)$

$\sigma(\cdot)$ : activation function, e.g., tanh, sigmoid

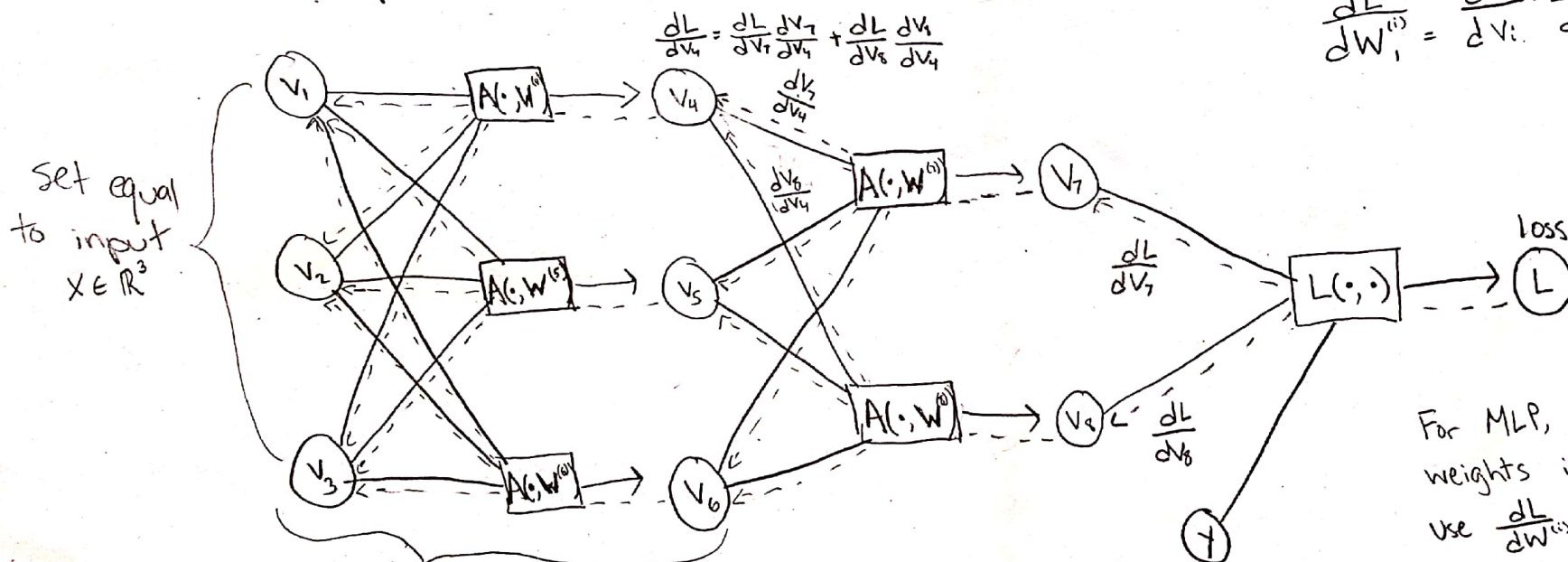
\* For simplicity, we consider  $A(x, W) = \sigma(x^T W)$  as a primitive

How to calculate  $\frac{dL}{dW^{(i)}}$ ?

$$v_i = A(\cdot, W^{(i)}) = \sigma(x^T W^{(i)}) = \sigma(x_1 W_1^{(i)} + \dots + x_n W_n^{(i)})$$

$$\frac{dL}{dW^{(i)}} = \frac{dL}{dv_i} \cdot \frac{dv_i}{dW^{(i)}} = \frac{dL}{dv_i} \sigma'(x^T W^{(i)}) x^{(i)}$$

\* here we use  $x = \langle v_{\text{prev}} \rangle$ , the set of nodes coming into  $v_i$



For MLP, we optimize over  $W$ , all weights in our MLP. We can then use  $\frac{dL}{dW^{(i)}}$  in e.g., gradient descent updates

$$W^{(i)} \leftarrow W^{(i)} - \underset{\substack{\uparrow \\ \text{learning rate}}}{\alpha} \frac{dL}{dW^{(i)}}$$