

Question 1

$(p|q|-r) \& ((-r|q|p) \rightarrow ((r|q) \& -q \& -p))$

- $(p \vee q \vee \neg r) \wedge ((\neg r \vee q \vee p) \Rightarrow ((r \vee q) \wedge \neg q \wedge \neg p))$
- I $(p \vee q \vee \neg r) \wedge (\neg(\neg r \vee q \vee p) \vee ((r \vee q) \wedge \neg q \wedge \neg p))$
- N $(p \vee q \vee \neg r) \wedge ((r \wedge \neg q \wedge \neg p) \vee ((r \vee q) \wedge \neg q \wedge \neg p))$
- D $(p \vee q \vee \neg r) \wedge (((r \wedge \neg q \wedge \neg p) \vee (r \vee q)) \wedge (((r \wedge \neg q \wedge \neg p) \vee \neg q)) \wedge (((r \wedge \neg q \wedge \neg p) \vee \neg p)))$
- D $(p \vee q \vee \neg r) \wedge (((r \vee r \vee q) \wedge (\neg q \vee r \vee q) \wedge (\neg p \vee r \vee q) \wedge (r \vee \neg q) \wedge (\neg q \vee \neg q) \wedge (\neg p \vee \neg q) \wedge (r \vee \neg p) \wedge (\neg q \vee \neg p) \wedge (\neg p \vee \neg p)))$
- O
- 1 $\{p, q, \neg r\}$
- 2 $\{r, q\}$
- 3 $\{\neg q, r, q\}$
- 4 $\{\neg p, r, q\}$
- 5 $\{r, \neg q\}$
- 6 $\{\neg q\}$
- 7 $\{\neg p, \neg q\}$
- 8 $\{r, \neg p\}$
- 9 $\{\neg q, \neg p\}$
- 10 $\{\neg p\}$

Resolution

- 11 $\{p, q\}$
- 12 $\{p\}$
- 13 $\{\}$

Question 2

$\forall x \forall y (\text{Horse}(x) \wedge \text{Dog}(y) \Rightarrow \text{Faster}(x, y))$

$\exists g (\text{Greyhound}(g) \wedge \forall r (\text{Rabbit}(r) \Rightarrow \text{Faster}(g, r)))$

$\forall x \forall r (\text{Horse}(x) \wedge \text{Rabbit}(r) \Rightarrow \text{Faster}(x, r))$

neg conclusion: $\neg(\forall x \forall r (\text{Horse}(x) \wedge \text{Rabbit}(r) \Rightarrow \text{Faster}(x, r)))$

Now turn them to clausal form and do the resolution steps.

$\forall x \forall y (\text{Horse}(x) \wedge \text{Dog}(y) \Rightarrow \text{Faster}(x, y))$
 I $\forall x \forall y (\neg((\text{Horse}(x) \wedge \text{Dog}(y)) \vee \text{Faster}(x, y)))$
 N $\forall x \forall y (\neg \text{Horse}(x) \vee \neg \text{Dog}(y) \vee \text{Faster}(x, y))$
 E $\neg \text{Horse}(x) \vee \neg \text{Dog}(y) \vee \text{Faster}(x, y)$
 O $\{\neg \text{Horse}(x), \neg \text{Dog}(y), \text{Faster}(x, y)\}$

$\exists g (\text{Greyhound}(g) \wedge \forall r (\text{Rabbit}(r) \Rightarrow \text{Faster}(g, r)))$
 I $\exists g (\text{Greyhound}(g) \wedge \forall r (\neg \text{Rabbit}(r) \vee \text{Faster}(g, r)))$
 E $\exists g (\text{Greyhound}(g) \wedge (\neg \text{Rabbit}(r) \vee \text{Faster}(g, r)))$
 A $\text{Greyhound}(\text{Grey}) \wedge (\neg \text{Rabbit}(r) \vee \text{Faster}(\text{Grey}, r))$
 O $\{\text{Greyhound}(\text{Grey})\}$
 $\{\neg \text{Rabbit}(r), \text{Faster}(\text{Grey}, r)\}$

Conclusion:

$\neg(\forall x \forall r (\text{Horse}(x) \wedge \text{Rabbit}(r) \Rightarrow \text{Faster}(x, r)))$
 I $\neg(\forall x \forall r (\neg((\text{Horse}(x) \wedge \text{Rabbit}(r)) \vee \text{Faster}(x, r))))$
 N $\neg(\forall x \forall r (\neg \text{Horse}(x) \vee \neg \text{Rabbit}(r) \vee \text{Faster}(x, r)))$
 N $\exists x \exists r (\neg \text{Horse}(x) \vee \neg \text{Rabbit}(r) \vee \text{Faster}(x, r))$
 N $\exists x \exists r (\text{Horse}(x) \wedge \text{Rabbit}(r) \wedge \neg \text{Faster}(x, r))$
 A $\text{Horse}(\text{Happy}) \wedge \text{Rabbit}(\text{Rein}) \wedge \neg \text{Faster}(\text{Happy}, \text{Rein})$
 O $\{\text{Horse}(\text{Happy})\}$
 $\{\text{Rabbit}(\text{Rein})\}$
 $\{\neg \text{Faster}(\text{Happy}, \text{Rein})\}$

And the backgroud knowledge:
 $\forall g (\text{Greyghound}(g) \Rightarrow \text{Dog}(g))$

$\forall x \forall y \forall z (\text{Faster}(x, y) \wedge \text{Faster}(y, z) \Rightarrow \text{Faster}(x, z))$

$\forall g (\text{Greyhound}(g) \Rightarrow \text{Dog}(g))$

I $\forall g \neg \text{Greyhound}(g) \vee \text{Dog}(g)$

A $\neg \text{Greyhound}(g) \vee \text{Dog}(g)$

O $\{\neg \text{Greyhound}(g), \text{Dog}(g)\}$

$\forall x \forall y \forall z (\text{Faster}(x, y) \wedge \text{Faster}(y, z) \Rightarrow \text{Faster}(x, z))$

I $x \forall y \forall z (\neg (\text{Faster}(x, y) \wedge \text{Faster}(y, z)) \vee \text{Faster}(x, z))$

N $\forall y \forall z (\neg \text{Faster}(x, y) \vee \neg \text{Faster}(y, z) \vee \text{Faster}(x, z))$

A $\neg \text{Faster}(x, y) \vee \neg \text{Faster}(y, z) \vee \text{Faster}(x, z)$

O $\{\neg \text{Faster}(x, y), \neg \text{Faster}(y, z), \text{Faster}(x, z)\}$

Resolution:

- | | | |
|----|---|--------|
| 1 | $\{\neg \text{Horse}(x_1), \neg \text{Dog}(y_1), \text{Faster}(x_1, y_1)\}$ | |
| 2 | $\{\text{Greyhound}(\text{Grey})\}$ | |
| 3 | $\{\neg \text{Rabbit}(r_1), \text{Faster}(\text{Grey}, r_1)\}$ | |
| 4 | $\{\neg \text{Greyghound}(g_1), \text{Dog}(g_1)\}$ | |
| 5 | $\{\neg \text{Faster}(x_2, y_2), \neg \text{Faster}(y_2, z_1), \text{Faster}(x_2, z_1)\}$ | |
| 6 | $\{\text{Horse}(\text{Happy})\}$ | |
| 7 | $\{\text{Rabbit}(\text{Rein})\}$ | |
| 8 | $\{\neg \text{Faster}(\text{Happy}, \text{Rein})\}$ | |
| 9 | $\{\text{Dog}(\text{Grey})\}$ | 2, 4 |
| 10 | $\{\text{Faster}(\text{Grey}, \text{Rein})\}$ | 3, 7 |
| 11 | $\{\neg \text{Horse}(x_1), \text{Faster}(x_1, \text{Grey})\}$ | 1, 9 |
| 12 | $\{\text{Faster}(\text{Happy}, \text{Grey})\}$ | 6, 11 |
| 13 | $\{\neg \text{Faster}(\text{Grey}, z_1), \text{Faster}(\text{Happy}, z_1)\}$ | 5, 12 |
| 14 | $\{\text{Faster}(\text{Happy}, \text{Rein})\}$ | 10, 13 |
| 15 | $\{\}$ | 8, 14 |

Question 3

$\forall x(\text{Hummingbird}(x) \Rightarrow \text{Richcolor}(x))$
 $\neg \exists y(\text{Bird}(y) \wedge \text{Large}(y) \wedge \text{LiveonHon}(y))$
 $\forall y(\text{Bird}(y) \wedge \neg \text{LiveonHon}(y) \Rightarrow \neg \text{Richcolor}(y))$
 $\forall x(\text{Hummingbird}(x) \Rightarrow \text{Bird}(x))$ (Background)
 $\forall x(\text{Hummingbird}(x) \Rightarrow \neg \text{Large}(x))$ (Conlusion)

Prover 9:

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1(allx(hummingbird(x)→ richcolor(x)))[assumption].
2(allx → (bird(x)&large(x)&liveonhon(x)))[assumption].
3(allx(bird(x)& → liveonhon(x)→ → richcolor(x)))[assumption].
4(allx(hummingbird(x)→ bird(x)))[assumption].
5(allx(hummingbird(x)→ → large(x)))[goal].
6hummingbird(c1).[deny(5)].
7 → hummingbird(x)|richcolor(x).[clausify(1)].
8 → hummingbird(x)|bird(x).[clausify(4)].
9bird(c1).[resolve(6, a, 8, a)].
10 → bird(x)| → large(x)| → liveonhon(x).[clausify(2)].
11 → bird(x)|liveonhon(x)| → richcolor(x).[clausify(3)].
12 → large(c1)| → liveonhon(c1).[resolve(9, a, 10, a)].
13large(c1).[deny(5)].
14liveonhon(c1)| → richcolor(c1).[resolve(9, a, 11, a)].
15richcolor(c1).[resolve(6, a, 7, a)].
16liveonhon(c1).[resolve(14, b, 15, a)].
17 → liveonhon(c1).[resolve(12, a, 13, a)].
18$F.[resolve(16, a, 17, a)].
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Question 4

mg = My gardener; wl = worth listening to on military subjects;
ar = able to remember the battle of waterloo; old=very old

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∃x(person(x) ∧ mg(x) ∧ wl(x)).
∀y((person(y) ∧ ar(y)) ⇒ old(y)).
∀z((person(z) ∧ wl(z)) ⇒ ar(z)).
∃m(person(x) ∧ mg(m) ∧ old(m)).(conclusion)
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Prover 9:

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1(existsx(person(x)&mg(x)&wl(x)))[assumption].
2(allx(person(x)&ar(x)→ old(x)))[assumption].
3(allx(person(x)&wl(x)→ ar(x)))[assumption].
4(existsm(person(m)&mg(m)&old(m)))[goal].
5→ person(x)|→ ar(x)|old(x).[clausify(2)].
6person(c1).[clausify(1)].
7→ person(x)|→ wl(x)|ar(x).[clausify(3)].
8→ person(x)|→ mg(x)|→ old(x).[deny(4)].
9→ mg(c1)|→ old(c1).[resolve(8, a, 6, a)].
10mg(c1).[clausify(1)].
11→ wl(c1)|ar(c1).[resolve(7, a, 6, a)].
12wl(c1).[clausify(1)].
13ar(c1).[resolve(11, a, 12, a)].
14→ ar(c1)|old(c1).[resolve(5, a, 6, a)].
15old(c1).[resolve(13, a, 14, a)].
16→ old(c1).[resolve(9, a, 10, a)].
17$F.[resolve(15, a, 16, a)].

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Question 5

$$P(P_{13}) = P(P_{22}) = P(P_{31}) = 0.01$$

$$\begin{aligned} P(p_{13}|b_{12}, b_{21}) &= \alpha \sum_{p_{22}} \sum_{p_{31}} (P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, p_{31}) \cdot P(p_{13}) \cdot P(p_{22}) \cdot P(p_{31})) \\ &= \alpha [P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, p_{31}) \cdot P(p_{13}) \cdot P(p_{22}) \cdot P(p_{31}) + \\ &\quad P(b_{12}|p_{13}, \neg p_{22}) \cdot P(b_{21}|\neg p_{22}, p_{31}) \cdot P(p_{13}) \cdot P(\neg p_{22}) \cdot P(p_{31}) + \\ &\quad P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, \neg p_{31}) \cdot P(p_{13}) \cdot P(p_{22}) \cdot P(\neg p_{31}) + \\ &\quad P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|\neg p_{22}, \neg p_{31}) \cdot P(p_{13}) \cdot P(\neg p_{22}) \cdot P(\neg p_{31})] \\ &= \alpha [1 \cdot 1 \cdot 0.01 \cdot 0.01 \cdot 0.01 + 1 \cdot 1 \cdot 0.01 \cdot 0.99 \cdot 0.01 + \\ &\quad 1 \cdot 1 \cdot 0.01 \cdot 0.01 \cdot 0.99 + 0] = \alpha (0.000001 + 0.000099 + 0.000099) \\ &= 0.000199\alpha \end{aligned}$$

$$\begin{aligned} P(\neg p_{13}|b_{12}, b_{21}) &= \alpha \sum_{p_{22}} \sum_{p_{31}} (P(b_{12}|\neg p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, p_{31}) \cdot P(\neg p_{13}) \cdot P(p_{22}) \cdot P(p_{31})) \\ &= \alpha [P(b_{12}|\neg p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, p_{31}) \cdot P(\neg p_{13}) \cdot P(p_{22}) \cdot P(p_{31}) + \\ &\quad P(b_{12}|\neg p_{13}, \neg p_{22}) \cdot P(b_{21}|\neg p_{22}, p_{31}) \cdot P(\neg p_{13}) \cdot P(\neg p_{22}) \cdot P(p_{31}) + \\ &\quad P(b_{12}|\neg p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, \neg p_{31}) \cdot P(\neg p_{13}) \cdot P(p_{22}) \cdot P(\neg p_{31}) + \\ &\quad P(b_{12}|\neg p_{13}, p_{22}) \cdot P(b_{21}|\neg p_{22}, \neg p_{31}) \cdot P(\neg p_{13}) \cdot P(\neg p_{22}) \cdot P(\neg p_{31})] \\ &= \alpha [1 \cdot 1 \cdot 0.99 \cdot 0.01 \cdot 0.01 + 0 + 1 \cdot 1 \cdot 0.99 \cdot 0.01 \cdot 0.99 + 0] \\ &= \alpha (0.000099 + 0.009801) = 0.0099\alpha \end{aligned}$$

$$\alpha = 1/(0.000199 + 0.0099) = 99.02$$

$$P(p_{13}|b_{12}, b_{21}) = 0.0197$$

$$P(\neg p_{13}|b_{12}, b_{21}) = 0.9803$$

$$\begin{aligned} P(p_{31}|b_{12}, b_{21}) &= \alpha \sum_{p_{13}} \sum_{p_{22}} (P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, p_{31}) \cdot P(p_{13}) \cdot P(p_{22}) \cdot P(p_{31})) \\ &= 0.0197 \end{aligned}$$

$$\begin{aligned} P(\neg p_{31}|b_{12}, b_{21}) &= \alpha \sum_{p_{13}} \sum_{p_{22}} (P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, \neg p_{31}) \cdot P(p_{13}) \cdot P(p_{22}) \cdot P(\neg p_{31})) \\ &= 0.9803 \end{aligned}$$

$$\begin{aligned}
P(p_{22}|b_{12}, b_{21}) &= \alpha \sum_{p_{13}} \sum_{p_{31}} (P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, p_{31}) \cdot P(p_{13}) \cdot P(p_{22}) \cdot P(p_{31})) \\
&= \alpha [P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, p_{31}) \cdot P(p_{13}) \cdot P(p_{22}) \cdot P(p_{31}) + \\
&\quad P(b_{12}|\neg p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, p_{31}) \cdot P(\neg p_{13}) \cdot P(p_{22}) \cdot P(p_{31}) + \\
&\quad P(b_{12}|p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, \neg p_{31}) \cdot P(p_{13}) \cdot P(p_{22}) \cdot P(\neg p_{31}) + \\
&\quad P(b_{12}|\neg p_{13}, p_{22}) \cdot P(b_{21}|p_{22}, \neg p_{31}) \cdot P(\neg p_{13}) \cdot P(p_{22}) \cdot P(\neg p_{31})] \\
&= \alpha(1 \cdot 1 \cdot 0.01 \cdot 0.01 \cdot 0.01 + 1 \cdot 1 \cdot 0.01 \cdot 0.01 \cdot 0.99 \\
&\quad + 1 \cdot 1 \cdot 0.01 \cdot 0.01 \cdot 0.99 + 1 \cdot 1 \cdot 0.99 \cdot 0.01 \cdot 0.99) \\
&= 0.01\alpha
\end{aligned}$$

$$\begin{aligned}
P(\neg p_{22}|b_{12}, b_{21}) &= \alpha \sum_{p_{13}} \sum_{p_{31}} (P(b_{12}|p_{13}, \neg p_{22}) \cdot P(b_{21}|\neg p_{22}, p_{31}) \cdot P(p_{13}) \cdot P(\neg p_{22}) \cdot P(p_{31})) \\
&= \alpha [P(b_{12}|p_{13}, \neg p_{22}) \cdot P(b_{21}|\neg p_{22}, p_{31}) \cdot P(p_{13}) \cdot P(\neg p_{22}) \cdot P(p_{31}) + \\
&\quad P(b_{12}|\neg p_{13}, \neg p_{22}) \cdot P(b_{21}|\neg p_{22}, p_{31}) \cdot P(\neg p_{13}) \cdot P(\neg p_{22}) \cdot P(p_{31}) + \\
&\quad P(b_{12}|p_{13}, \neg p_{22}) \cdot P(b_{21}|\neg p_{22}, \neg p_{31}) \cdot P(p_{13}) \cdot P(\neg p_{22}) \cdot P(\neg p_{31}) + \\
&\quad P(b_{12}|\neg p_{13}, \neg p_{22}) \cdot P(b_{21}|\neg p_{22}, \neg p_{31}) \cdot P(\neg p_{13}) \cdot P(\neg p_{22}) \cdot P(\neg p_{31})] \\
&= \alpha(1 \cdot 1 \cdot 0.01 \cdot 0.99 \cdot 0.01 + 0 + 0 + 0) = 0.000099\alpha
\end{aligned}$$

$$\alpha = 1/(0.01 + 0.000099) = 99.02$$

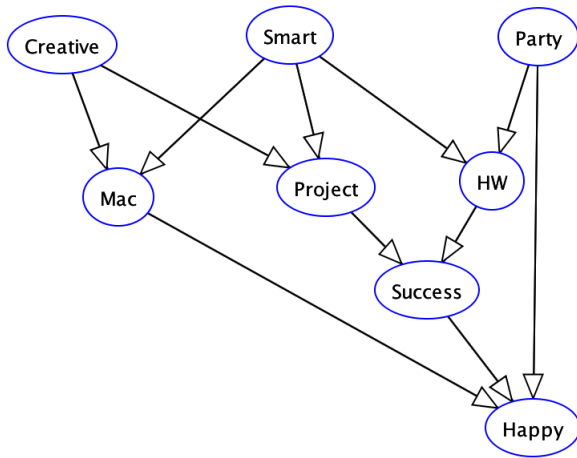
$$P(p_{22}|b_{12}, b_{21}) = 0.9902$$

$$P(\neg p_{22}|b_{12}, b_{21}) = 0.0098$$

Going to [2,2] is almost certain death. So, a probabilistic agent will never choose to go to [2,2]. On the other hand, to a logical agent, squares [1,3], [2,2], [3,1] look the same. So, the logical agent would choose either one with equal chance (1/3). By doing that, the agent will die with a chance of about 1/3.

Question 6

1



2

Party	Smart	P(HW Party, Smart)			Smart	Creative	P(Mac Smart, Creative)			Success	Mac	Party	P(Happy Success, Mac, Party)		
T	T	1722	2145	0.8027972	T	T	1685	2457	0.68579569	T	T	T	921	960	0.959375
T	F	81	866	0.0935335	T	F	441	1067	0.41330834	T	T	F	271	757	0.3579921
F	T	1239	1379	0.8984772	F	T	933	1040	0.89711538	T	F	T	456	632	0.721519
F	F	186	610	0.304918	F	F	53	436	0.12155963	F	T	T	449	912	0.4923246
										T	F	F	135	440	0.3068182
										F	T	F	99	483	0.2049689
										F	F	T	213	507	0.4201183
										F	F	F	29	309	0.0938511
Smart	Creative	P(Project Smart, Creative)			HW	Project	P(Success HW, Project)			F	F	F			
T	T	2224	2457	0.9051689	T	T	2394	2670	0.89662921						
T	F	847	1067	0.7938144	T	F	171	558	0.30645161	Party			P(Party)		
F	T	419	1040	0.4028846	F	T	179	866	0.20669746	T	3011	5000	0.6022		
F	F	46	436	0.1055046	F	F	45	906	0.04966887	Smart			P(Smart)		
										T	3524	5000	0.7048		
										Creative			P(Creative)		
										T	3497	5000	0.6994		

3

$$\begin{aligned}
& P(\text{happy}|\text{party}, \text{smart}, \neg\text{creative}) \\
&= \alpha \sum_{\text{mac}} \sum_{\text{project}} \sum_{\text{hw}} \sum_{\text{success}} [P(\text{happy}, \text{mac}, \text{success}, \text{hw}, \text{project}, \text{party}, \text{smart}, \neg\text{creative})] \\
&= \alpha \sum_{\text{mac}} \sum_{\text{project}} \sum_{\text{hw}} \sum_{\text{success}} [P(\text{happy}|\text{mac}, \text{success}, \text{party}) \cdot P(\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success}|\text{project}, \text{hw}) \cdot P(\text{hw}|\text{party}, \text{smart}) \cdot P(\text{project}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\text{party}) \cdot P(\text{smart}) \cdot P(\neg\text{creative})] \\
&= \alpha P(\text{party}) \cdot P(\text{smart}) \cdot P(\neg\text{creative}) \cdot \sum_{\text{project}} P(\text{project}|\neg\text{creative}, \text{smart}) \\
&\quad \sum_{\text{mac}} \sum_{\text{hw}} \sum_{\text{success}} P(\text{happy}|\text{mac}, \text{success}, \text{party}) \cdot P(\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success}|\text{project}, \text{hw}) \cdot P(\text{hw}|\text{party}, \text{smart}) \\
&= \alpha P(\text{party}) \cdot P(\text{smart}) \cdot P(\neg\text{creative}) \cdot \sum_{\text{project}} P(\text{project}|\neg\text{creative}, \text{smart}) \\
&\quad [P(\text{happy}|\text{mac}, \text{success}, \text{party}) \cdot P(\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success}|\text{project}, \text{hw}) \cdot P(\text{hw}|\text{party}, \text{smart}) + \\
&\quad P(\text{happy}|\neg\text{mac}, \text{success}, \text{party}) \cdot P(\neg\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success}|\text{project}, \text{hw}) \cdot P(\text{hw}|\text{party}, \text{smart}) + \\
&\quad P(\text{happy}|\text{mac}, \text{success}, \text{party}) \cdot P(\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success}|\text{project}, \neg\text{hw}) \cdot P(\neg\text{hw}|\text{party}, \text{smart}) + \\
&\quad P(\text{happy}|\text{mac}, \neg\text{success}, \text{party}) \cdot P(\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\neg\text{success}|\text{project}, \text{hw}) \cdot P(\text{hw}|\text{party}, \text{smart}) + \\
&\quad P(\text{happy}|\neg\text{mac}, \neg\text{success}, \text{party}) \cdot P(\neg\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\neg\text{success}|\text{project}, \text{hw}) \cdot P(\text{hw}|\text{party}, \text{smart}) + \\
&\quad P(\text{happy}|\neg\text{mac}, \text{success}, \text{party}) \cdot P(\neg\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success}|\text{project}, \neg\text{hw}) \cdot P(\neg\text{hw}|\text{party}, \text{smart}) + \\
&\quad P(\text{happy}|\text{mac}, \neg\text{success}, \text{party}) \cdot P(\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\neg\text{success}|\text{project}, \neg\text{hw}) \cdot P(\neg\text{hw}|\text{party}, \text{smart}) + \\
&\quad P(\text{happy}|\neg\text{mac}, \neg\text{success}, \text{party}) \cdot P(\neg\text{mac}|\neg\text{creative}, \text{smart}) \cdot \\
&\quad P(\neg\text{success}|\text{project}, \neg\text{hw}) \cdot P(\neg\text{hw}|\text{party}, \text{smart})] \\
&= 0.692
\end{aligned}$$

$$\begin{aligned}
& P(\neg \text{happy} | \text{party}, \text{smart}, \neg \text{creative}) \\
&= \alpha \sum_{\text{mac}} \sum_{\text{project}} \sum_{\text{hw}} \sum_{\text{success}} [P(\neg \text{happy}, \text{mac}, \text{success}, \text{hw}, \text{project}, \text{party}, \text{smart}, \neg \text{creative})] \\
&= \alpha \sum_{\text{mac}} \sum_{\text{project}} \sum_{\text{hw}} \sum_{\text{success}} [P(\neg \text{happy} | \text{mac}, \text{success}, \text{party}) \cdot P(\text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success} | \text{project}, \text{hw}) \cdot P(\text{hw} | \text{party}, \text{smart}) \cdot P(\text{project} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\text{party}) \cdot P(\text{smart}) \cdot P(\neg \text{creative})] \\
&= \alpha P(\text{party}) \cdot P(\text{smart}) \cdot P(\neg \text{creative}) \cdot \sum_{\text{project}} \cdot P(\text{project} | \neg \text{creative}, \text{smart}) \\
&\quad \sum_{\text{mac}} \sum_{\text{hw}} \sum_{\text{success}} P(\neg \text{happy} | \text{mac}, \text{success}, \text{party}) \cdot P(\text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success} | \text{project}, \text{hw}) \cdot P(\text{hw} | \text{party}, \text{smart}) \\
&= \alpha P(\text{party}) \cdot P(\text{smart}) \cdot P(\neg \text{creative}) \cdot \sum_{\text{project}} \cdot P(\text{project} | \neg \text{creative}, \text{smart}) \\
&\quad [P(\neg \text{happy} | \text{mac}, \text{success}, \text{party}) \cdot P(\text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success} | \text{project}, \text{hw}) \cdot P(\text{hw} | \text{party}, \text{smart}) + \\
&\quad P(\neg \text{happy} | \neg \text{mac}, \text{success}, \text{party}) \cdot P(\neg \text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success} | \text{project}, \text{hw}) \cdot P(\text{hw} | \text{party}, \text{smart}) + \\
&\quad P(\neg \text{happy} | \text{mac}, \text{success}, \text{party}) \cdot P(\text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success} | \text{project}, \neg \text{hw}) \cdot P(\neg \text{hw} | \text{party}, \text{smart}) + \\
&\quad P(\neg \text{happy} | \text{mac}, \neg \text{success}, \text{party}) \cdot P(\text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\neg \text{success} | \text{project}, \text{hw}) \cdot P(\text{hw} | \text{party}, \text{smart}) + \\
&\quad P(\neg \text{happy} | \neg \text{mac}, \neg \text{success}, \text{party}) \cdot P(\neg \text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\neg \text{success} | \text{project}, \text{hw}) \cdot P(\text{hw} | \text{party}, \text{smart}) + \\
&\quad P(\neg \text{happy} | \neg \text{mac}, \text{success}, \text{party}) \cdot P(\neg \text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\text{success} | \text{project}, \neg \text{hw}) \cdot P(\neg \text{hw} | \text{party}, \text{smart}) + \\
&\quad P(\neg \text{happy} | \text{mac}, \neg \text{success}, \text{party}) \cdot P(\text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\neg \text{success} | \text{project}, \neg \text{hw}) \cdot P(\neg \text{hw} | \text{party}, \text{smart}) + \\
&\quad P(\neg \text{happy} | \neg \text{mac}, \neg \text{success}, \text{party}) \cdot P(\neg \text{mac} | \neg \text{creative}, \text{smart}) \cdot \\
&\quad P(\neg \text{success} | \text{project}, \neg \text{hw}) \cdot P(\neg \text{hw} | \text{party}, \text{smart})] \\
&= 0.308
\end{aligned}$$

4

$$P(\text{happy}|\text{smart}, \text{creative}) = 0.58156$$

5

$$P(\text{happy}|\neg \text{party}, \text{hw}, \text{project}) = 0.32045$$

6

$$P(\text{happy}|\text{mac}) = 0.56272$$

7

$$P(\text{party}|\text{smart}) = 0.6022$$

8

$$P(\text{party}|\text{smart}, \text{happy}) = 0.79265$$