

Draft Analyzer

1. Modeling

1.1. Defining Items and Objects

Let us define a champion by an ID: each champion has a unique ID between 1 and 170 (since there are currently 170 champions).

Let us define the Victory-Defeat matrix $M \in M_{170}(\mathbb{N})$.

For $(i, j) \in \llbracket 1; 170 \rrbracket^2$, the coefficient $M_{i,j}$ represents the number of victories of champion i over the champion j .

Consequently we can have the number of win $w_i \in \mathbb{N}$ and the number of loose $l_i \in \mathbb{N}$.

$$w_i = \frac{\sum_{k=1}^{170} M_{i,k}}{5}$$
$$l_i = \frac{\sum_{k=1}^{170} M_{k,i}}{5}$$

w_i will be the sum of the line i and l_i will be the sum of the column i . We will explain later why these sums are divided by 5.

1.2. Draft

What is a draft ? A draft is the selection of 5 champions against 5 others champions, all of which are distinct. Mathematically, we can define a draft as a 10-tuple, denoted by D :

$$D = (x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, x_9, x_{10})$$
$$\forall (i, j) \in \llbracket 1, 10 \rrbracket \text{ we have : } x_i \neq x_j$$

The draft is divided into two teams: the “Red” team and the “Blue” team. We can define these teams as two 5 –tuple: R and B :

$$R = (x_1, x_2, x_3, x_4, x_5)$$
$$B = (x_6, x_7, x_8, x_9, x_{10})$$

And finally after a match one of the two team win and the other team loose and we need to update M .

After a match, one team wins and the other loses, and we update the matrix M accordingly. For each victorious champion, we add 1 to each column corresponding to the defeated champions of the opposing team. Since there are 5 champions on each team, this explains why we divide by 5 when calculating the number of wins and losses.

1.3. Probability

Now let's create your model to calculate probability of win of the “Red” or “Blue” with the history of the last match.

First define the “Strength of a champion” called S_i :

$$S_i = \sum_{k=1}^5 \left(\left(\frac{w_{x_k}}{w_{x_k} + l_{x_k}} \right) \frac{1}{3} + \left(\frac{M_{i,k}}{M_{i,k} + M_{k,i}} \right) \frac{2}{3} \right)$$

Lets add details about S_i :

- i is the indice of the champion in draft.

- x_i is the indice of the champion in the opponent team for $i \in \llbracket 1, 5 \rrbracket$.
- $\frac{1}{3}$ and $\frac{2}{3}$ are weights for the general win probability and for the direct matchup.

Now we can define the “Strength of team” for the “Red” and for the “Blue” : S_R and S_B

$$S_t = \sum_{k=1}^5 S_k$$

with $t \in \{R, B\}$

Now lets use the logistic function to have the probability of winning of one side :

$$\mathbb{P}_R = \frac{1}{1 + e^{-(S_R - S_B)}}$$

2. Historical of draft and command in Prolog

initialiser(Matrix).

2.1. KC - TL :

	Victory					Defeat				
Game 1										
TL	Ornn	Maokai	Tristana	Varus	Nautilus	Jayce	Vi	Aurora	Ezreal	Rell
Victory										
Game 2										
KC	Camille	Sejuani	Azir	Miss Fortune	Leona	Ambessa	Skarner	Aurelion Sol	Ashe	Pantheon
Victory										
Game 3										
TL	K'Sante	Nocturne	Taliyah	Lucian	Nami	Gnar	Xin Zhao	Ahri	Zeri	Yuumi
Victory										

Add victory in matrix of the match :

```
add_victory('Ornn','Maokai','Tristana','Varus','Nautilus','Jayce','Vi','Aurora','Ezreal','Rell').
add_victory('Camille','Sejuani','Azir','Miss Fortune','Leona','Ambessa','Skarner','Aurelion Sol','Ashe','Pantheon').
add_victory('K'Sante','Nocturne','Taliyah','Lucian','Nami','Gnar','Xin Zhao','Ahri','Zeri','Yuumi').
```

2.2. TES - HLE

2.2.1. Draft :

	Victory					Defeat				
Game 1										
HLE	Jax	Skarner	Azir	Ezreal	Alistar	Kennen	Vi	Aurora	Miss Fortune	Leona
Victory										
Game 2										
HLE	Aatrox	Nidalee	Akali	Varus	Poppy	Gragas	Nocturne	Orianna	Kalista	Renata Glasc
Victory										

2.2.2. Calcul of winning proba of the drafts

TES-HLE Game 1 :

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Jax','Skarner','Azir','Ezreal','Alistar','Kennen'
Fortune','Leona',Matrix,P).
-> Matrix = [[0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0,
0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0|...], [0|...],
```

```
[...|...|...],
-> P = 0.47834688488309984.
```

This model give probability of 0.47 at the first five champ entered in data.

In the final result the 5 first champ win this game We can say the model guess wrong the issue of the match.

TES - HLE Game 2 :

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Gragas','Nocturne','Orianna','Kalista','Renata
Glasc','Aatrox','Nidalee','Akali','Varus','Poppy',Matrix,P).
-> Matrix = [[0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0,
0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0, 0|...], [0, 0|...], [0|...],
[...|...|...],
-> P = 0.5.
```

This model give probability of 0.5 at the first five champ entered in data.

In the final result the 5 first champ win this game.

2.2.3. Add Victory in Matrix

```
add_victory('Jax','Skarner','Azir','Ezreal','Alistar','Kennen','Vi','Aurora','Miss
Fortune','Leona').
add_victory('Aatrox','Nidalee','Akali','Varus','Poppy','Gragas','Nocturne','Orianna','Kalista','Ren
Glasc').
```

2.3. KC - CFO

2.3.1. Draft

	Victory					Defeat				
Game 1 CFO Victory	Rumble	Skarner	Viktor	Ezreal	Leona	Ambessa	Vi	Aurora	Kai'Sa	Rakan
Game 2 CFO Victory	Sion	Sejuani	Taliyah	Miss Fortune	Rell	Jayce	Brand	Yone	Varus	Nautilus

2.3.2. Calculus of the winning probability of the drafts

KC - CFO Game 1 :

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Ambessa','Vi','Aurora','Kai\'Sa','Rakan','Rumble'
-> Matrix = [[0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0,
0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0, 0|...], [0, 0|...], [0|...],
[...|...|...],
-> P = 0.4419298941260467.
```

This model give probability of 0.44 at the first five champ entered in data.

In the final result the 5 last champ win this game. We can say the model give a good reponse because he give a proba of 56% to win at the last five champ.

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Jayce','Brand','Yone','Varus','Nautilus','Sion','Sejuani','Taliyah','Miss
Fortune','Rell',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0|...], [0, 0,
0, 0, 0|...], [0, 0, 0, 0|...], [0, 0, 0|...], [0, 0|...], [0|...], [...|...|...], P = 0.5133301737382324.
```

2.3.3. Add victory in matrix

```
add_victory('Rumble','Skarner','Viktor','Ezreal','Leona','Ambessa','Vi','Aurora','Kai\'Sa','Rakan')
add_victory('Sion','Sejuani','Taliyah','Miss Fortune','Rell','Jayce','Brand','Yone','Varus','Nautilus').
```

2.4. TES - TL

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Rumble','Vi','Aurora','Ashe','Braum','Galio','Xin Zhao','Tristana','Ezreal','Rakan',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], P = 0.46892897678537176.
```

```
add_victory('Rumble','Vi','Aurora','Ashe','Braum','Galio','Xin Zhao','Tristana','Ezreal','Rakan').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('K'Sante','Maokai','Hwei','Kalista','Nautilus','Aatrox','Pantheon','Sylas',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], P = 0.49222284950490025.
```

```
add_victory('Aatrox','Pantheon','Sylas','Varus','Neeko','K'Sante','Maokai','Hwei','Kalista','Nautilus').
```

2.5. HLE - CFO

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Rumble','Vi','Yone','Ashe','Rakan','Karma','Wukong','Azir','Ezreal','Alistar',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], P = 0.4553966612109141.
```

```
add_victory('Rumble','Vi','Yone','Ashe','Rakan','Karma','Wukong','Azir','Ezreal','Alistar').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Vladimir','Nidalee','Zed','Miss Fortune','Rell','Gragas','Kindred','Taliyah','Corki','Leona',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], P = 0.51499550161941.
```

```
add_victory('Vladimir','Nidalee','Zed','Miss Fortune','Rell','Gragas','Kindred','Taliyah','Corki','Leona').
```

2.6. TES - KC

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Ambessa','Viego','Aurora','Kalista','Renata Glasc','Jayce','Skarner','Taliyah','Ashe','Karma',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], P = 0.46588641397664204.
```

```
add_victory('Jayce','Skarner','Taliyah','Ashe','Karma','Ambessa','Viego','Aurora','Kalista','Renata Glasc').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Gnar','Karthus','Corki','Varus','Rell','Aatrox','Ivern','Yone','Ezreal','Leona',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], P = 0.5036110483266414.
```

```
add_victory('Aatrox','Ivern','Yone','Ezreal','Leona','Gnar','Karthus','Corki','Varus','Rell').
```

2.7. CFO - TL

```
load_matrix('matrix.txt',Matrix),win_proba_draft('K'Sante','Xin Zhao','Azir','Ezreal','Alistar','Gwen','Vi','Taliyah','Kai'Sa','Rakan',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], P = 0.4830620392311757.
```

```
add_victory('K'Sante','Xin Zhao','Azir','Ezreal','Alistar','Gwen','Vi','Taliyah','Kai'Sa','Rakan').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Jax','Sejuani','Corki','Ziggs','Poppy','Gangplank','Maokai','Yone','Tristana',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0, 0, 0|...], P = 0.5122197884189273.
```

```
add_victory('Gangplank','Maokai','Yone','Tristana','Leona','Jax','Sejuani','Corki','Ziggs','Poppy').
```

2.8. KC - HLE

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Rumble','Xin Zhao','Taliyah','Ezreal','Leona','Aurora','Vi','Sylas','Varus','Poppy',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0|...], [0|...], [...|...]|...], P = 0.5647338377718968.
```

```
add_victory('Aurora','Vi','Sylas','Varus','Poppy','Rumble','Xin Zhao','Taliyah','Ezreal','Leona').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Ambessa','Ivern','Azir','Jhin','Alistar','Gnar','Maokai','Corki','Ashe','Renata Glasc',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0|...], [0|...], [...|...]|...], P = 0.5271953567276605.
```

```
add_victory('Ambessa','Ivern','Azir','Jhin','Alistar','Gnar','Maokai','Corki','Ashe','Renata Glasc').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Vladimir','Wukong','Jayce','Kai'Sa','Rell','Sion','Sejuani','Ryze','Draven',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0, 0|...], [0, 0|...], [0|...], [...|...]|...], P = 0.4628463872345206.
```

```
add_victory('Vladimir','Wukong','Jayce','Kai'Sa','Rell','Sion','Sejuani','Ryze','Draven','Rakan').
```

2.9. CFO - TES

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Jayce','Sejuani','Taliyah','Ezreal','Alistar','K'Sante','Nidalee','Yone','Jhin',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0, 0|...], [0, 0|...], [0|...], [...|...]|...], P = 0.4652676676122881.
```

```
add_victory('Jayce','Sejuani','Taliyah','Ezreal','Alistar','K'Sante','Nidalee','Yone','Jhin','Leona').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Rumble','Xin Zhao','Sylas','Corki','Poppy','Sion','Skarner','Azir','Caitlyn','Nautilus',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0, 0|...], [0, 0|...], [0|...], [...|...]|...], P = 0.5049998333399998.
```

```
add_victory('Sion','Skarner','Azir','Caitlyn','Nautilus','Rumble','Xin Zhao','Sylas','Corki','Poppy').
```

2.10. HLE - TL

```
load_matrix('matrix.txt',Matrix),win_proba_draft('K'Sante','Pantheon','Ziggs','Kalista','Renata Glasc','Kayle','Vi','Ryze','Draven','Pyke',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0|...], [0|...], [...|...]|...], P = 0.5020833212770899.
```

```
add_victory('Kayle','Vi','Ryze','Draven','Pyke','K'Sante','Pantheon','Ziggs','Kalista','Renata Glasc').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Renekton','Maokai','Cassiopeia','Varus','Rakan','Quinn','Zyra','Tristana',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0, 0|...], [0, 0|...], [0|...], [...|...]|...], P = 0.48611468225399523.
```

```
add_victory('Renekton','Maokai','Cassiopeia','Varus','Rakan','Quinn','Zyra','Tristana','Jhin','Rell').
```

```
load_matrix('matrix.txt',Matrix),win_proba_draft('Ambessa','Skarner','Kassadin','Sivir','Braum','Jax','Ivern','Viktor','Ezreal',Matrix,P). Matrix = [[0, 0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0, 0|...], [0, 0, 0, 0, 0|...], [0, 0, 0, 0|...], [0, 0, 0|...], [0, 0|...], [0|...], [...|...]|...], P = 0.4775151752081999.
```

```
add_victory('Ambessa','Skarner','Kassadin','Sivir','Braum','Jax','Ivern','Viktor','Ezreal','Leona').
```

3. Result and conclusion