# Homework Set No. 9

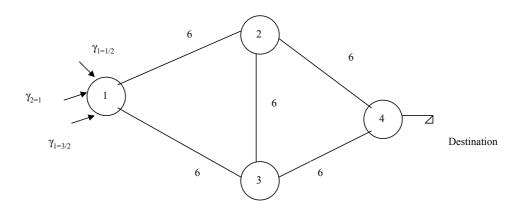
ECE 642 Dr. Bijan Jabbari

### Problems 5.22,5.26,5.27,5.29&5.30 from M.Schwartz's book

### Problem 1.

Consider the packet-switched network shown in figure below. Terminals 1,2 and 3 generate Poisson traffic at the rate of  $\gamma_1 = 1/2$ ,  $\gamma_2 = 1$  and  $\gamma_3 = 3/2$  packets/sec respectively as shown. All packets are  $1/\mu = 1/6$  sec long, on the average, exponentially distributed. All are destined for node 4, as shown. All line capacities are  $\mu = 6$  packets/sec as shown.

- $\bullet$  Find the average time-delay T from node 1 to node 4 if the packets go directly through node 2.
- Repeat a. if the packets follow the path 1-2-3-4.
- Packets are now routed randomly through the network, from node 1 to node 4, with the following routing probabilities:  $q_{13} = 1/3$ ,  $q_{23} = 3/4$ ,  $q_{34} = 1$ . Find the average network-wide delay in this case.



## Problem 2.

Consider the VC shown in figure below. A sliding window mechanism is used to control this VC. Use Buzen's algorithm to find the time-delay throughput characteristic for  $\lambda \gg 2\mu$ . Take N=1,2,3,4,5,6. Compare with the plot of delay vs throughput in case of a sliding window model.  $(M=3,\ldots\infty)$ . Do the results agree with what you expect?



### Problem 3.

Use Buzens algorithm to find the Nortons equivalent of an M-hop virtual circuit. Find u(n) for various values of n and M and show that it is given by the expression  $u(n) = n\mu/(n+M-1)$ . Show as a check that the average number of packets in each queue is n/M.

### Problem 4.

Refer to the Figs.5-41 and 5-42.

- Let N=1. Show that  $P_B=\rho$  and  $\gamma/\mu=\rho(1-\rho)$ . Sketch  $\gamma/\mu$  as a function of  $\rho$
- Let N=5. Sketch  $\gamma/\mu$  versus  $\rho$  and compare with the curve in Fig.5-42
- For any N, show that for  $\rho' = 1$ ,  $\rho = N/(N+1)$ ,  $\gamma/\mu = (N/(N+1))^2$ . Show that for  $\rho' \to \infty$ ,  $\rho \to 1$ ,  $1 P_B \to 1/\rho \to 0$  and  $\gamma/\mu \to (1 P_B) \to 0$ . Show that for  $\rho \ll 1$ ,  $\gamma/\mu = \rho$ . Can you use these values to sketch  $\gamma/\mu$  versus  $\rho$  for any N? Compare with parts a and b above as well with the curve N = 8 in Fig.5-42.

### Problem 5.

Refer to the section on input-buffer limiting. Take  $N=2,\ N_I=1,$  write and use simple computer program to solve for  $P_{B_T}$  and  $P_{B_I}$  interactively. Use this to find the average throughput  $\gamma_1=\lambda_1(1-P_{B_I})$  as a function of load  $\lambda_I$  for serveral values of  $\lambda_I$ . Take n=2, compare with the results of the previous problem. One possible procedure: Initialize with  $P_{B_T}=P_{B_I}=0$ . Keep repeating until, at iteration  $K+1,\ \sqrt{(P_{B_T}^{K+1}-P_{B_T}^K)^2+(P_{B_T}^{K+1}-P_{B_I}^K)^2}<\epsilon$  (a stopping constant). You can try any other initial values and stopping threshold.