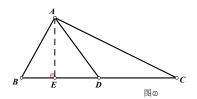
$$(1)AB^2 + AC^2 = 2(AD^2 + CD^2)$$

(2)

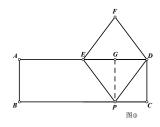


成立

思路:作 $AE \perp BC$ 交BC 于E

可得: $AC^2 = AE^2 + CE^2 = AE^2 + (DC + DE)^2$ $AB^2 = AE^2 + BE^2 = AE^2 + (DC - DE)^2$ 化简 $AB^2 + AC^2$ 即可得证

(3)



作EG = DG,连接PG由(2)同理可得: $PE^2 + PD^2 = 2(PG^2 + DG^2)$ 求出DG,PG的最小值后再使用勾股定理即可求解