
CS181P Final Project Proposal #1

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1 Team

The team includes Santi Santichaivekin, Jingyi Liu, Jacob Boerma, Lorraine Zhao, and Princewill Okoroafor. The team name is Go Pika Pika! The team logo is provided below.



2 Project

We will attempt the second project listed on the project ideas:

ML, Search, and Compression. It has been shown that ML is a form of search (we will see this during the course, for example in Montañez (Chapter 3)), and also shown that ML can be viewed as a form of compression (as in minimum description length approaches). Can we show compression is a form of search, search a form of compression, search a form of ML, or compression a form of ML, to make a triangle of two-way equivalences? Or taking a subset of these equivalences, can we apply a set of results from one domain to the other, such as forming no free lunch theorems for compression?

We hypothesize that all the three problems can be phrased as one another. If we prove the three-way equivalency among the three problems, then we can apply different theories from one field to another. Also, this problem is applicable to the real world, where we can solve actual real world problems by directing them as either ML, search, or compression.

3 Initial Plan of Attack

We will start with understanding the concepts of ML, data compression, and search individually, and then trying to prove the “No Free Lunch” theorem for data compression among other theorems of search that might be applied to data compression. We can then look for algorithms for data compression and obtain insights about how it might be framed as a machine learning problem and search.

4 Separation of Work

For now, we will each read the papers and get on the same level of understanding. Once we have a good understanding of ML, compression, and search, we might split up work based on sub-problems that appear. We have divided the readings to different team members, so that one person can focus on one or two readings, and then update the rest of the team members on what he/she learned.

- Jacob will read about No Free Lunch on a high level, and will try to understand the Famine of Forte paper and how we might apply the same concepts to compression schemes.
- Santi will be trying to understand the No Free Lunch Theory and apply it to compression.
- Lorraine will go over her part of the readings and get a better understanding of Machine Learning and Searches, and try to link the two by establishing an equivalent relationship.
- Rose will be reading about data compression algorithms and see how to generalize them as search problems.
- Princewill will also be reading about data compression algorithms and how they can be generalized as search problems.

5 Literature Review

We have found some papers and textbooks that will be useful for our research. We will read the suggested readings for the next few lectures in class, as well as the following papers/articles.

Why ML Works http://www.cs.cmu.edu/~gmontane/montanez_dissertation.pdf [Lorraine]

“Famine of Forte” <https://arxiv.org/pdf/1609.08913.pdf> [Jacob]

“Probabilistic machine learning and artificial intelligence” <https://www.nature.com/articles/nature14541> [Rose]

In his paper “Probabilistic machine learning and artificial intelligence”, Ghahramani provides an overview of the probabilistic approach to machine learning and the state-of-art advances in this field. Specifically, he explores five areas that fall under this framework including probabilistic programming, Bayesian optimization, probabilistic data compression, automatic model discovery, and hierarchical modeling. Under the framework of probabilistic modeling, Ghahramani views machine learning as a process of inferring the most plausible model from a given data set, which is in turn used to improve performance on future predictions. He points out the advantages of using a probabilistic framework by arguing the central role of uncertainty in machine learning models and identifies three sources of uncertainty that are typically present in modeling (452-453). The uncertainties consist of the measurement noise of the data set, the unknown parameters in a given model, and uncertainties about the general structure of the mode. Thus probabilistic modeling comes as a natural remedy for dealing with various sources of uncertainties and identifies the best model in accordance with data. Aside from its ability to represent uncertainties in the model, probabilistic modeling

also brings the advantage of flexibility through the use of Bayesian non-parametric models, which grow in complexity as the data set grows (454). Such flexibility allows machine learning models to capture the regularities of the data and have better performance. Interestingly, he points out that Bayesian nonparametrics is equivalent to a neural network with infinite hidden units. In the section about Bayesian optimization, he formulates the optimization process as a sequential decision problem—a search problem in our words—where you use a probabilistic distribution of the function values and determine the next query by choosing the area with the most uncertainty (and thus the most information gain once the value is reviewed) (456). Here we notice a connection between a specific type of machine learning problems and search is made through the bridge of the probabilistic framework. In the section about data compression, he claims the equivalence of data compression and probabilistic modeling as “two sides of the same coin” and highlights the important role that Bayesian machine-learning models play in the field of data compression (456). The process of optimizing data compression can be viewed as a process of extracting the best model from data, and because of the flexibility provided by Bayesian non-parametric models, some of the best data compression algorithms employs the same idea to achieve better compression rate. Here, a connection is made between machine learning and data compression through the same bridge of probabilistic modeling. Thus from the review of this literature, it is evident that the probabilistic framework can be profound in trying to equate the concepts of machine learning, compression, and search, and is thus an area of interest that we can explore in more details in our project.

“Generalization as Search” <http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.121.5764&rep=rep1&type=pdf> [Lorraine]

“Data Compression Explained” http://mattmahoney.net/dc/dce.html#Section_13 [Rose] [Princewill]

“Minimum Description Length” <https://www.cs.cmu.edu/~aarti/Class/10704/lec13-MDL.pdf> [Princewill]

No Free Lunch For Optimization <https://ti.arc.nasa.gov/m/profile/dhw/papers/78.pdf> [Santi] [Jacob]

The No Free Lunch Theorems for Optimization paper establishes that under an oracle model of search, two algorithms that use the same number of oracle reveals have the same expected performance if all cost functions have the same likelihood of being chosen. Wolpert and Macready proves this by showing that any algorithm reveals the same sequence of cost on average regardless of what has been previously revealed to the algorithm. The formal proof is done by induction using a statistical model, but it could have been done without statistical model too. The paper also goes on to prove the NFL result for time-dependent cost functions and relate the result to other topics such as information theory and geometry. I have not looked into these topics yet as it seems to be more complex.

The search model used in the paper includes simulated annealing and evolutionary algorithm (where each species is independently evaluated). It does not include techniques like branch and bound or coevolutionary algorithm (where species are evaluated against each other). The authors also went on to prove that there is free lunch for coevolutionary algorithms, that is, some algorithm performs objectively better compared to others.

The authors also mention that they had proved a similar result for statistical inference (machine learning) which I have not explored. I think I will need to spend some time to understand the proof for optimization better before delving into the other one.