CS 61A Fall 2014

Structure and Interpretation of Computer Programs

MIDTERM 1

INSTRUCTIONS

- You have 2 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written $8.5" \times 11"$ crib sheet of your own creation and the official 61A midterm 1 study guide attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a brief explanation.

Last name	
First name	
SID	
Login	
TA & section time	
Name of the person to your left	
Name of the person to your right	
All the work on this exam is my own. (please sign)	

For staff use only

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Q. 1	Q. 2	Q. 3	Q. 4	Total	
/12	/14	/8	/6	/40	

1. (12 points) World Cup

(a) (10 pt) For each of the expressions in the tables below, write the output displayed by the interactive Python interpreter when the expression is evaluated. The output may have multiple lines.

Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error.

Reminder: the interactive interpreter displays the value of a successfully evaluated expression, unless it is None.

The first three rows have been provided as examples.

Assume that you have started Python 3 and executed the following statements:

```
def square(x):
    return x * x

def argentina(n):
    print(n)
    if n > 0:
        return lambda k: k(n+1)
    else:
        return 1 / n

def germany(n):
    if n > 1:
        print('hallo')
    if argentina(n-2) >= 0:
        print('bye')
    return argentina(n+2)
```

Expression	Interactive Output
5*5	> 25
print(5)	1 h Pane
1/0	Error
<pre>print(1, print(2))</pre>	0 Emr
argentina(0)	

Expression	Interactive Output		
argentina(1)(square)			
germany(1)(square)	halh		
germany(2)(germany)	oprov.		

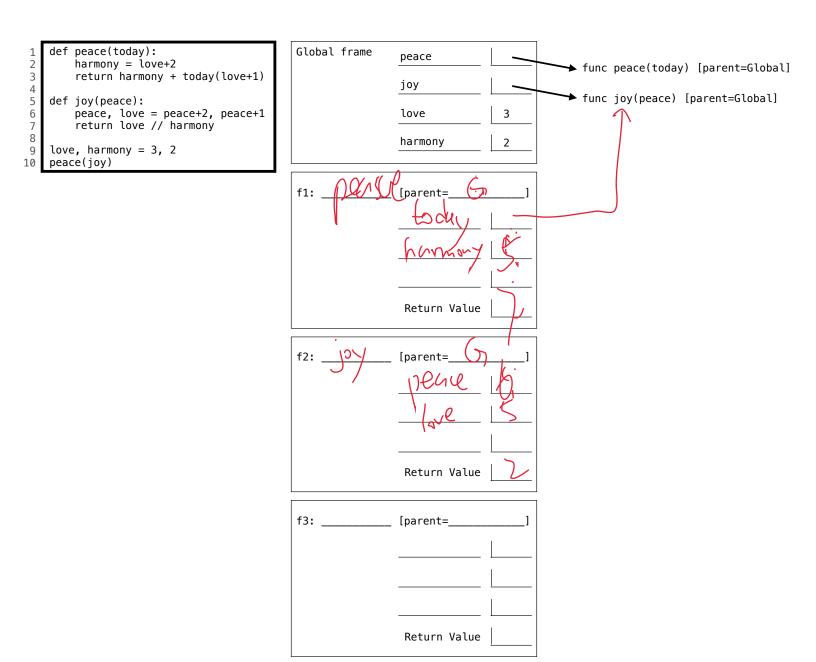
(b) (2 pt) Fill in the blank with an expression so that the whole expression below evaluates to a number. *Hint*: The expression abs > 0 causes a TypeError.

```
(lambda t: argentina(t)(germany)(square))(_____)
```

2. (14 points) Envy, Iron, Mint

- (a) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

 A complete answer will:
 - Add all missing names, labels, and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.



- (b) (8 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

 A complete answer will:
 - Add all missing names, labels, and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.

def k(g, b): 1 Global frame → func k(g, b) [parent=Global] 2 def n(s, a): return g-p 3 4 5 return b(n(b, p)) 6 g, p = 3, 77 k(p+1, lambda s: g+3) [parent= Return Value [parent= Return Value [parent= Return Value

3. (8 points) Express Yourself

(a) (3 pt) A k-bonacci sequence starts with K-1 zeros and then a one. Each subsequent element is the sum of the previous K elements. The 2-bonacci sequence is the standard Fibonacci sequence. The 3-bonacci and 4-bonacci sequences each start with the following ten elements:

```
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, ...
kbonacci(n, 2): 0, 1, 1, 2, 3, 5, 8, 13, 21, 35, ...
kbonacci(n, 3): 0, 0, 1, 1, 2, 4, 7, 13, 24, 44, ...
kbonacci(n, 4): 0, 0, 0, 1, 1, 2, 4, 8, 15, 29, ...
```

```
Fill in the blanks of the implementation of kbonacci below, a function that takes non-negative integer n and
positive integer k and returns element n of a k-bonacci sequence.
def kbonacci(n, k):
   """Return element N of a K-bonacci sequence.
   >>> kbonacci(3, 4)
   >>> kbonacci(9, 4)
   29
   >>> kbonacci(4, 2)
   >>> kbonacci(8, 2)
   21
   .....
   if n < k - 1:
       return 0
   elif n == k - 1:
       return 1
   else:
       total = 0
       i = _____
       while i < n:
           total = total + ______
           i = i + 1
```

return total

(b) (5 pt) Fill in the blanks of the following functions defined together in the same file. Assume that all arguments to all of these functions are positive integers that do not contain any zero digits. For example, 1001 contains zero digits (not allowed), but 1221 does not (allowed). You may assume that reverse is correct when implementing remove.

```
def combine(left, right):
   """Return all of LEFT's digits followed by all of RIGHT's digits."""
   factor = 1
   while factor <= right:
       factor = factor * 10
   return left * factor + right
def reverse(n):
   """Return the digits of \ensuremath{\mathbb{N}} in reverse.
   >>> reverse(122543)
   345221
   if n < 10:
       return n
   else:
       return combine(______)
def remove(n, digit):
   """Return all digits of N that are not DIGIT, for DIGIT less than 10.
   >>> remove(243132, 3)
   2412
   >>> remove(243132, 2)
   4313
   >>> remove(remove(243132, 1), 2)
   433
   11 11 11
   removed = 0
   while n != 0:
       if _____:
   return reverse (removed)
```

4. (6 points) Lambda at Last

(a) (2 pt) Fill in the blank below with an expression so that the second line evaluates to 2014. You may only use the names two_thousand, two, k, four, and teen and parentheses in your expression (no numbers, operators, etc.).

```
two_thousand = lambda two: lambda k: ______
two_thousand(7)(lambda four: lambda teen: 2000 + four + teen)
```

(b) (4 pt) The if_fn returns a two-argument function that can be used to select among alternatives, similar to an if statement. Fill in the return expression of factorial so that it is defined correctly for non-negative arguments. You may only use the names if_fn, condition, a, b, n, factorial, base, and recursive and parentheses in your expression (no numbers, operators, etc.).

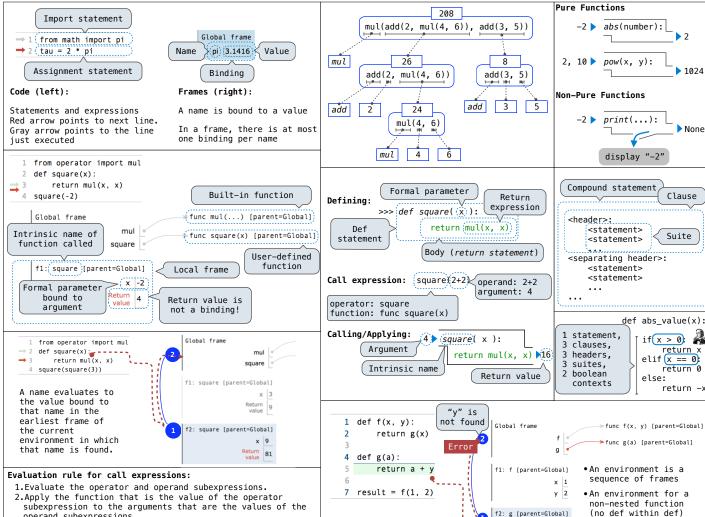
```
def if_fn(condition):
    if condition:
        return lambda a, b: a
    else:
        return lambda a, b: b
def factorial(n):
    """Compute N! for non-negative N. N! = 1 * 2 * 3 * ... * N.
    >>> factorial(3)
    >>> factorial(5)
    120
    >>> factorial(0)
    1
    11 11 11
    def base():
        return 1
    def recursive():
        return n * factorial(n-1)
```

return ______

Scratch Paper

Scratch Paper

Scratch Paper



operand subexpressions.

Applying user-defined functions:

- 1.Create a new local frame with the same parent as the function that was applied.
- 2. Bind the arguments to the function's formal parameter names in that frame.
- 3.Execute the body of the function in the environment beginning at that frame.

Execution rule for def statements:

- 1.Create a new function value with the specified name, formal parameters, and function body.
 2.Its parent is the first frame of the current environment.
- 3.Bind the name of the function to the function value in the first frame of the current environment.

Execution rule for assignment statements:

1.Evaluate the expression(s) on the right of the equal sign. 2.Simultaneously bind the names on the left to those values, in the first frame of the current environment.

Execution rule for conditional statements:

Each clause is considered in order.

1.Evaluate the header's expression.

2.If it is a true value, execute the suite, then skip the remaining clauses in the statement.

Evaluation rule for or expressions:

- 1.Evaluate the subexpression <left>
- 2.If the result is a true value v, then the expression evaluates to v.
- 3.Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for and expressions:

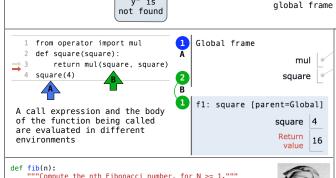
- 1.Evaluate the subexpression <left>.
- 2.If the result is a false value v, then the expression evaluates to v.
- 3.0 therwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for not expressions:

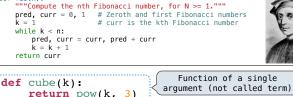
1.Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

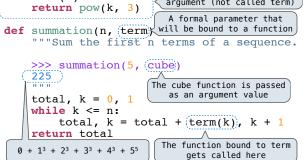
Execution rule for while statements:

- 1. Evaluate the header's expression.
- If it is a true value, execute the (whole) suite, then return to step 1.



is







pow(x, y):

display "-2"

1024

None

Clause

Suite

def abs_value(x):

else:

consists of one local

frame, followed by the

if(x > 0: 🚜

return x elif (x == 0):

return 0

return -x

Nested def function bo Higher-o Nested ef statements: Functions
bodies are bound to name Lue function s a functi es in the takes a function a return value within e local other frame as

an

```
square = lambda x: x * x
 square = \left| \frac{x,y}{x} \right| = \left| \frac{x+y}{x} \right| Evaluates to a function.
                                      No "return" keyword!
                                                                                   • Both create a function with the same domain, range, and behavior.
           A function
                with formal parameters x and y
                                                                                   • Both functions have as their parent the environment in which they
                      that returns the value of "\times \times y,"
                   Must be a single expression
def make_adder(n): A function that returns a function
        'Return a function that takes one argument k and returns k + n.
     >>> add_three = make_adder(3) 
                                            The name add three is
                                             bound to a function
     7
                               A local
    def adder(k):
                            def statement
         return k +(n)
     return adder
                            Can refer to names in
                            the enclosing function
• Every user-defined function has
  a parent frame
 • The parent of a function is the
  frame in which it was defined
                                                 A function's signature
 • Every local frame has a parent
                                                 has all the information
  frame
                                                 to create a local frame
 • The parent of a frame is the
  parent of the function called
                                  3
                                      Global frame
                                                                   func make adder(n) [parent=Global]
                                                make_adder
   1 def make_adder(n):
                                                                  func adder(k) [parent=f1]
                                                  add_three
     def adder(k):
return k + n
 Nested
                                      f1: make_adder [parent=G]
         return adder
  def
   6 add_three = make_adder(3)
                                                     adder
   7 add_three(4)
                                                     Return
                                       f2: adder [parent=f1]
 def curry2(f):
       ""Returns a function g such that g(x)(y) returns f(x, y)."""
     def g(x):
         def h(y):
                                Currying: Transforming a multi-argument
function into a single-argument,
             return f(x, y)
         return h
                                 higher-order function.
     return q
 Anatomy of a recursive function:
 • The def statement header is similar to other functions
• Conditional statements check for base cases

    Base cases are evaluated without recursive calls

 • Recursive cases are evaluated with recursive calls
 def sum_digits(n):
  """Return the sum of the digits of positive integer n.""" if \frac{n}{l} < 10 \colon
       return n
   else:
       all_but_last, last = n // 10, n % 10
       return sum_digits(all_but_last) + last
                           Global frame
    def cascade(n):
                                                      >> func cascade(n) [parent=Global]
       if n < 10:
                                         cascade e
          print(n)
        else:
                           f1: cascade [parent=Global] \circ Each cascade frame is from a different call
           print(n)
                                          n 123
           cascade(n//10)
                                                    to cascade.
           print(n)
                           f2: cascade [parent=Global]
                                                  • Until the Return value
                                         n 12
                                                   appears, that call has not completed.
  9 cascade(123)
                                       Return
value None
Program output:
Any statement can
                                                    appear before or after
1 12
                                                    the recursive call.
                                       Return
value None
                                               n: 0, 1, 2, 3, 4, 5, 6, 7, 8,
           def inverse_cascade(n):
1
                                          fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,
                grow(n)
12
                print(n)
                                         def fib(n):
    if n == 0:
                shrink(n)
123
                                             if n == 0:
return 0
elif n == 1:
           def f_then_g(f, g, n):
1234
                if n:
                                                  return 1
123
                     f(n)
                                             else:
return fib(n-2) + fib(n-1)
                     q(n)
12
           grow = lambda n: f_then_g(grow, print, n//10)
1
           shrink = lambda n: f_then_g(print, shrink, n//10)
```

```
· Both bind that function to the name square.
• Only the def statement gives the function an intrinsic name.
When a function is defined:

    Create a function value: func <name>(<formal parameters>)

2. Its parent is the current frame.
         f1: make_adder
                               func adder(k) [parent=f1]
3. Bind <name> to the function value in the current frame
   (which is the first frame of the current environment).
When a function is called:
1. Add a local frame, titled with the <name> of the function being
    called.
    Copy the parent of the function to the local frame: [parent=<label>]

    Bind the <formal parameters> to the arguments in the local frame.
    Execute the body of the function in the environment that starts with

    the local frame.
                    def fact(n):
                         if n == 0:
                             return 1
                  4
                         else:
                             return n * fact(n-1)
                  7 fact(3)
                                                → func fact(n) [parent=Global]
                Global frame
                                  fact
                f1: fact [parent=Global]
                                   n 3
                f2: fact [parent=Global]
                                   n 2
                f3: fact [parent=Global]
                                   n 1
                f4: fact [parent=Global]
                                   n 0
                                Return 1
            Is fact implemented correctly?
                  Verify the base case.
                  Treat fact as a functional abstraction!
            2.
            3.
                  Assume that fact(n-1) is correct.
                  Verify that fact(n) is correct.
                  assuming that fact(n-1) correct.

    Recursive decomposition:

                                 def count_partitions(n, m):
 finding simpler instances of
                                     if n == 0:
 a problem.
                                         return 1
E.g., count_partitions(6, 4)
                                      elif n < 0:
Explore two possibilities:Use at least one 4
                                          return 0
                                     elif m == 0:
  Don't use any 4
                                         return 0
Solve two simpler problems:count_partitions(2, 4)
                                     else:
                                     with_m = count_partitions(n-m, m)
  count_partitions(6, 3)
                                         without_m = count_partitions(n, m-1)
• Tree recursion often involves
                                          return with_m + without_m
 exploring different choices.
from operator import floordiv, mod
def divide_exact(n, d):
     """Return the quotient and remainder of dividing N by D.
    \Rightarrow \neq (q, r = divide\_exact(2012, 10)) \leq Multiple assignment
    >>> 'q
                                                to two names
    201
    >>> r
    000
                                            Multiple return values,
                                              separated by commas
    return floordiv(n, d), mod(n, d) <
```

def square(x):

return x * x

VS