

Pair Approach

Number of splits $\leftarrow 2$

Number of Reducers $\leftarrow 1$

Mapper Input	Mapper 0	Mapper 1
record 1	15 91 80 12 19 80 18	19 15 80 18 19 18
record 2	17 15 80 18 19 18	18 15 18 18 82 18
Mapper output	Mapper 0	Mapper 1
	$((15, 91), 1)$ $((15, *), 1)$ $((15, 80), 1)$ $((15, 12), 1)$ $((15, 19), 1)$ $((15, 80), 1)$ $((15, 18), 1)$ $((91, 80), 1)$ $((91, *), 1)$ $((91, 12), 1)$ $((91, 19), 1)$ $((91, 80), 1)$ $((91, 18), 1)$ $((80, 12), 1)$ $((80, *), 1)$ $((80, 19), 1)$ $((12, 19), 1)$ $((12, *), 1)$ $((12, 80), 1)$ $((12, 18), 1)$ $((19, 80), 1)$ $((19, *), 1)$ $((19, 18), 1)$ $((18, 18), 1)$ $((18, *), 1)$	$((19, 15), 1)$ $((19, *), 1)$ $((19, 80), 1)$ $((19, 18), 1)$ $((15, 80), 1)$ $((15, *), 1)$ $((15, 18), 1)$ $((15, 19), 1)$ $((15, 18), 1)$ $((80, 18), 1)$ $((80, *), 1)$ $((80, 19), 1)$ $((80, 18), 1)$ $((18, 19), 1)$ $((18, *), 1)$ $((19, 18), 1)$ $((19, *), 1)$

(2)

 $((17, 15), 1)$ $((17, *), 1)$ $((17, 80), 1)$ $((17, 18), 1)$ $((17, 19), 1)$ $((17, 18), 1)$ $((15, 80), 1)$ $((15, *), 1)$ $((15, 18), 1)$ $((15, 19), 1)$ $((15, 18), 1)$ $((80, 18), 1)$ $((80, *), 1)$ $((80, 19), 1)$ $((80, 18), 1)$ $((18, 19), 1)$ $((18, *), 1)$ $((19, 18), 1)$ $((19, *), 1)$ $((18, 15), 1)$ $((18, *), 1)$ $((15, 18), 1)$ $((15, *), 1)$ $((15, 18), 1)$ $((15, 88), 1)$ $((15, 18), 1)$ $((18, 88), 1)$ $((18, *), 1)$ $((88, 18), 1)$ $((88, *), 1)$

12, 15, 17

18, 19,

80, 88, 91

- Reducer Input -

// Shuffle sort then

 $((12, *), [1, 1, 1])$ // 3 $((12, 18), [1])$ $((12, 19), [1])$ $((12, 80), [1])$ $((15, *), [1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1])$ // 18 $((15, 12), [1])$ $((15, 12), [1, 1, 1, 1, 1, 1, 1, 1])$ // 8 $((15, 19), [1, 1, 1])$ $((15, 80), [1, 1, 1, 1])$ $((15, 88), [1])$ $((15, 91), [1])$

Reducer input cut'd output

→ ((17,*), [1,1,1,1,1]) //5

((17,15), [1])

((17,18), [1,1])

((17,19), [1])

((17,80), [1])

→ ((18,*), [1,1,1,1])

((18,15), [1])

((18,19), [1,1])

((18,88), [1])

→ ((19,*), [1,1,1,1,1,1,1]) //7

((19,15), [1])

((19,18), [1,1,1,1])

((19,80), [1,1])

→ ((80,*), [1,1,1,1,1,1,1,1,1]) //9

((80,12), [1])

((80,18), [1,1,1,1,1]) //5

((80,19), [1,1,1])

→ ((88,*), [1])

((88,18), [1])

→ ((91,*), [1,1,1,1,1]) //5

((91,12), [1])

((91,18), [1])

((91,19), [1])

((91,80), [1,1])

Reducer output (one Reducer)

→ ((12, 18), 1/3)

((12, 19), 1/3)

((12, 80), 1/3)

→ ((15, 12), 1/18)

((15, 18), 8/18)

((15, 19), 3/18)

((15, 80), 4/18)

((15, 88), 1/18)

((15, 91), 1/18)

→ ((17, 15), 1/5)

((17, 18), 2/5)

((17, 19), 1/5)

((17, 80), 1/5)

→ ((18, 15), 1/4)

((18, 19), 2/4)

((18, 88), 1/4)

→ ((19, 15), 1/7)

((19, 18), 4/7)

((19, 80), 2/7)

→ ((80, 12), 1/9)

((80, 18), 5/9)

((80, 19), 3/9)

→ ((88, 18), 1)

((91, 12), 1/5)

((91, 18), 1/5)

((91, 19), 1/5)

((91, 80), 2/5)

Stripe Approach

Mapper Input	Mapper 0	Mapper 1																																																																																						
record 1	15 91 80 12 19 80 18	19 15 80 18 19 18																																																																																						
record 2	17 15 80 18 19 18	18 15 18 18 88 18																																																																																						
Mapper output	Mapper 0	Mapper 1																																																																																						
→	<div>(15, <table><tr><td>91</td><td>80</td><td>12</td><td>19</td><td>18</td></tr><tr><td>1</td><td>2</td><td>1</td><td>1</td><td>1</td></tr></table>)</div> <div>(91, <table><tr><td>80</td><td>12</td><td>19</td><td>18</td></tr><tr><td>2</td><td>1</td><td>1</td><td>1</td></tr></table>)</div> <div>(80, <table><tr><td>12</td><td>19</td></tr><tr><td>1</td><td>1</td></tr></table>)</div> <div>(12, <table><tr><td>19</td><td>80</td><td>18</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>)</div> <div>(19, <table><tr><td>80</td><td>18</td></tr><tr><td>1</td><td>1</td></tr></table>)</div> <div>(80, <table><tr><td>18</td></tr><tr><td>1</td></tr></table>)</div> <div>(17, <table><tr><td>15</td><td>80</td><td>18</td><td>19</td></tr><tr><td>1</td><td>1</td><td>2</td><td>1</td></tr></table>)</div> <div>(15, <table><tr><td>80</td><td>18</td><td>19</td></tr><tr><td>1</td><td>2</td><td>1</td></tr></table>)</div> <div>(80, <table><tr><td>18</td><td>19</td></tr><tr><td>2</td><td>1</td></tr></table>)</div> <div>(18, <table><tr><td>19</td></tr><tr><td>1</td></tr></table>)</div> <div>(19, <table><tr><td>18</td></tr><tr><td>1</td></tr></table>)</div>	91	80	12	19	18	1	2	1	1	1	80	12	19	18	2	1	1	1	12	19	1	1	19	80	18	1	1	1	80	18	1	1	18	1	15	80	18	19	1	1	2	1	80	18	19	1	2	1	18	19	2	1	19	1	18	1	<div>(19, <table><tr><td>15</td><td>80</td><td>18</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>)</div> <div>(15, <table><tr><td>80</td><td>18</td><td>19</td></tr><tr><td>1</td><td>2</td><td>1</td></tr></table>)</div> <div>(80, <table><tr><td>18</td><td>19</td></tr><tr><td>2</td><td>1</td></tr></table>)</div> <div>(18, <table><tr><td>19</td></tr><tr><td>1</td></tr></table>)</div> <div>(19, <table><tr><td>18</td></tr><tr><td>1</td></tr></table>)</div> <div>(18, <table><tr><td>15</td></tr><tr><td>1</td></tr></table>)</div> <div>(15, <table><tr><td>18</td><td>88</td></tr><tr><td>3</td><td>1</td></tr></table>)</div> <div>(18, <table><tr><td>88</td></tr><tr><td>1</td></tr></table>)</div> <div>(88, <table><tr><td>18</td></tr><tr><td>1</td></tr></table>)</div>	15	80	18	1	1	1	80	18	19	1	2	1	18	19	2	1	19	1	18	1	15	1	18	88	3	1	88	1	18	1
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Reducer Input

(12, [

19	80	18
1	1	1

])

(15, [

91	80	12	19	18
1	2	1	1	1

 ,

80	18	19
1	2	1

 ,

80	18	19
1	2	1

 ,

18	88
3	1

])

(17, [

15	80	18	19
1	1	2	1

])

Reducer Input Cont'd

(18, [¹⁹

1

, ¹⁹

1

, ¹⁵

1

, ⁸⁸

1

])

(19, [^{80 18}

1	1
---	---

, ¹⁸

1

, ^{15 80 18}

1	1	1
---	---	---

, ¹⁸

1

])

(80, [^{12 19}

1	1
---	---

, ¹⁸

1

, ^{18 19}

2	1
---	---

, ^{18 19}

2	1
---	---

])

(88, [¹⁸

1

])

(91, [^{80 12 19 18}

2	1	1	1
---	---	---	---

])

Reducer output

Sum		12	15	17	18	19	88	91
3	12				1/3	1/3	1/3	
18	15	1/18			8/18	3/18	4/18	1/18
5	17		1/5		2/5	1/5	1/5	
4	18		1/4			2/4	1/4	
7	19		1/7		4/7		2/7	
9	80	1/9	5/9		3/9			
1	88				1			
5	91	1/5			1/5	1/5	2/5	