

Assignment MH

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1 Greedy algorithm

```
S ← {}
for each e in E do incompatibles[e] ← ∑b∈E I[e][b]
for h in 1 ≤ h ≤ 72 do
    demandh = ct
    while demandh > 0 do
        Seth ← {}
        for each e in E do
            if (< e, h > ∉ S and ∑b∈S I[e][b] = 0 and ( h mod= 1 or
                (< e, h - 1 > ∉ S and < e, h - 2 > ∉ S)))
                then Seth ← Seth ∪ e
            if |Seth| = 0 then return INFEASIBLE
        ebest ← argmin {q(< e, h > | e ∈ Seth)}
        S ← S ∪ < ebest, h >
        demandh ← demandh - 60/pt
return S
```

Greedy Function :

$$q < e, h > = \min \begin{cases} 0 & \text{if } e \in S \\ incompatibles[e] + 1 & \text{if } e \notin S \end{cases}$$

The greedy function selects the minimum cost for using each available employee (note that an employee is available if the hours constraints are satisfied, he is not already assigned at that hour and there is no incompatible employee assigned). The greedy function returns a 0 if the employee was already assigned before to the solution before, this is the best case so we don't have to add another employee. In the second case the greedy function returns the number of incompatibilities plus one (to avoid conflicts with 0), this is because its better to assign an employee with lower number of incompatibilities for the immediate future.

2 GRASP

```

S ← {}
for each  $e$  in  $E$  do incompatibles[e] ←  $\sum_{b \in E} I[e][b]$ 
for  $h$  in  $1 \leq h \leq 72$  do
    demand $h$  =  $c_t$ 
    while demand $h$  > 0 do
        Set $h$  ← {}
        for each  $e$  in  $E$  do
            if ( $\langle e, h \rangle \notin S$  and  $\sum_{b \in S} I[e][b] = 0$  and ( $h \bmod 1 = 1$  or
                ( $\langle e, h-1 \rangle \notin S$  and  $\langle e, h-2 \rangle \notin S$ )))
            then Set $h$  ← Set $h$   $\cup$   $e$ 
            if |Set $h$ | = 0 then return INFEASIBLE
         $e_{min} \leftarrow \text{argmin} \{q(\langle e, h \rangle) \mid e \in \text{Set}_h\}$ 
         $e_{max} \leftarrow \text{argmax} \{q(\langle e, h \rangle) \mid e \in \text{Set}_h\}$ 
         $RCL_{min} \leftarrow \{q(\langle e, h \rangle) \leq e_{min} + \alpha(e_{max} - e_{min}) \mid e \in \text{Set}_h\}$ 
         $e_{random} \leftarrow \text{random } e \in RCL_{min}$ 
         $S \leftarrow S \cup \langle e_{random}, h \rangle$ 
        demand $h$  ← demand $h$  - 60/pt
return S

```

Greedy Function :

$$q(\langle e, h \rangle) = \min \begin{cases} 0 & \text{if } e \in S \\ \text{incompatibles}[e] + 1 & \text{if } e \notin S \end{cases}$$

2.1 GRASP RCL construction

For the hour 4, c_t is 60, so we need at least 5 employees. From the full set of available employees, 11 and 15 are discarded, as they don't satisfy the hours constraint. The value of $q(\cdot)$ for the previous assigned employees is 0, as they are already part of the solution 5, 6, 16, 18, and for the rest of employees the value will be the number of incompatibilities of each one (incompatibles[e]).

So the e_{min} and e_{max} will be 0 and 5 respectively (4 is the maximum number of incompatibilities). RCL is computed as following:

$$RCL_{min} \quad q(\langle e, h \rangle) \leq 0 + 0.3(5 - 0) \mid e \in \text{Set}_h$$

And employees with a $q(\cdot) \leq 1.5$ will be selected:
 $RCL_{min} \quad q(\langle e, h \rangle) = 5, 6, 16, 18, 22, 25, 27, 29$

Where $q(\cdot)(5, 6, 16, 18) = 0$ and $q(\cdot)(22, 25, 27, 29) = 1$

3 Local Search

```
Given a solution  $S$ 
Sort  $e \in S$  by decreasing amount of work
for  $h$  in  $1 \leq h \leq 72$  do
    for each  $e'$  in  $S_h$  do
        for each  $e$  in  $S$  do
             $S' \leftarrow S \setminus \langle e', h \rangle \cup \langle e, h \rangle$ 
            if  $S'$  is not UNFEASIBLE and  $f(S') < f(S)$ 
            then
                 $S \leftarrow S'$ 
return  $S$ 
```

This local search algorithm uses a best improvement strategy, as it tries to get the optimal assignment for each employee, instead of using only the first assignment that improves the solution. Also, it uses a reassignment neighborhood, because it focus on moving one employee to hours, instead of doing exchanges between employees in different hours. The algorithm sorts the employees by amount of work, so the employees with less work will be selected first, then a hour is selected so the algorithm starts moving employees from the available pool to that hour, substituting the assigned employees until it finds a better solution.