

Exploratory Data Analysis and Model Building to Predict NBA Points

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```
# Load necessary libraries
library(readxl)

# Load the dataset
df <- read_excel("Dataset1.xlsx")

## Warning: Expecting numeric in 02370 / R2370C15: got '-'

# View the first few rows of the dataset
head(df)

## # A tibble: 6 x 24
##   Team `Match Up` `Game Date` `W/L` MIN PTS FGM FGA `FG%` `3PM` `3PA`
##   <chr> <chr>      <chr>      <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 GSW GSW vs. PHX 10/24/2023 L    240 104 36 101 35.6 10 43
## 2 PHX PHX @ GSW 10/24/2023 W    240 108 42 95 44.2 11 33
## 3 LAL LAL @ DEN 10/24/2023 L    240 107 41 90 45.6 10 29
## 4 DEN DEN vs. LAL 10/24/2023 W    240 119 48 91 52.7 14 34
## 5 MEM MEM vs. NOP 10/25/2023 L    240 104 38 91 41.8 12 43
## 6 IND IND vs. WAS 10/25/2023 W    240 143 56 107 52.3 20 43
## # i 13 more variables: `3P%` <dbl>, FTM <dbl>, FTA <dbl>, `FT%` <dbl>,
## # OREB <dbl>, DREB <dbl>, REB <dbl>, AST <dbl>, STL <dbl>, BLK <dbl>,
## # TOV <dbl>, PF <dbl>, `+/-` <dbl>

# Summarize the dataset to understand basic statistics and data structure
summary(df)

##      Team      Match Up      Game Date      W/L
## Length:2460 Length:2460 Length:2460 Length:2460
## Class :character Class :character Class :character Class :character
## Mode :character Mode :character Mode :character Mode :character
##
##
##
##      MIN      PTS      FGM      FGA
## Min. :240.0 Min. : 73.0 Min. :26.00 Min. : 67.0
## 1st Qu.:240.0 1st Qu.:105.0 1st Qu.:38.00 1st Qu.: 84.0
## Median :240.0 Median :114.0 Median :42.00 Median : 89.0
## Mean :241.4 Mean :114.2 Mean :42.17 Mean : 88.9
## 3rd Qu.:240.0 3rd Qu.:123.0 3rd Qu.:46.00 3rd Qu.: 93.0
## Max. :290.0 Max. :157.0 Max. :65.00 Max. :119.0
##
```

```
##          FG%           3PM           3PA           3P%           FTM
## Min.      :27.70   Min.      : 2.00   Min.      :12.0   Min.      : 6.90   Min.      : 0.00
## 1st Qu.:43.80   1st Qu.:10.00   1st Qu.:30.0   1st Qu.:31.00   1st Qu.:13.00
## Median :47.50   Median :13.00   Median :35.0   Median :36.55   Median :17.00
## Mean      :47.52   Mean      :12.84   Mean      :35.1   Mean      :36.49   Mean      :17.03
## 3rd Qu.:51.20   3rd Qu.:15.00   3rd Qu.:39.0   3rd Qu.:41.70   3rd Qu.:21.00
## Max.      :67.10   Max.      :27.00   Max.      :63.0   Max.      :64.50   Max.      :44.00
##
##          FTA           FT%           OREB           DREB
## Min.      : 0.00   Min.      : 33.30   Min.      : 0.00   Min.      :16.00
## 1st Qu.:17.00   1st Qu.: 72.00   1st Qu.: 8.00   1st Qu.:29.00
## Median :21.00   Median : 78.90   Median :10.00   Median :33.00
## Mean      :21.72   Mean      : 78.33   Mean      :10.55   Mean      :32.99
## 3rd Qu.:26.00   3rd Qu.: 85.20   3rd Qu.:13.00   3rd Qu.:36.00
## Max.      :52.00   Max.      :100.00   Max.      :28.00   Max.      :55.00
##
##          NA's      :1
##          REB          AST          STL          BLK
## Min.      :25.00   Min.      :11.00   Min.      : 0.000   Min.      : 0.000
## 1st Qu.:39.00   1st Qu.:23.00   1st Qu.: 6.000   1st Qu.: 3.000
## Median :43.00   Median :27.00   Median : 7.000   Median : 5.000
## Mean      :43.54   Mean      :26.67   Mean      : 7.474   Mean      : 5.142
## 3rd Qu.:48.00   3rd Qu.:30.00   3rd Qu.: 9.000   3rd Qu.: 7.000
## Max.      :74.00   Max.      :50.00   Max.      :20.000   Max.      :17.000
##
##          TOV          PF          +/-
## Min.      : 3.0   Min.      : 4.00   Min.      : -62
## 1st Qu.:11.0   1st Qu.:16.00   1st Qu.: -10
## Median :14.0   Median :19.00   Median : 0
## Mean      :13.6   Mean      :18.73   Mean      : 0
## 3rd Qu.:16.0   3rd Qu.:21.00   3rd Qu.: 10
## Max.      :29.0   Max.      :34.00   Max.      : 62
##
```

```
# Remove rows where FT% is recorded as "-"
df <- df[df$'FT%' != "-", ]

# Convert FT% column to numeric
df$'FT%' <- as.numeric(df$'FT%')

# Summarize the dataset again after cleaning
summary(df)
```

```
##          Team          Match Up          Game Date          W/L
## Length:2460   Length:2460   Length:2460   Length:2460
## Class :character   Class :character   Class :character   Class :character
## Mode  :character   Mode  :character   Mode  :character   Mode  :character
##
##
##
##          MIN          PTS          FGM          FGA
## Min.      :240.0   Min.      : 73.0   Min.      :26.00   Min.      : 67.0
## 1st Qu.:240.0   1st Qu.:105.0   1st Qu.:38.00   1st Qu.: 84.0
## Median :240.0   Median :114.0   Median :42.00   Median : 89.0
## Mean      :241.4   Mean      :114.2   Mean      :42.17   Mean      : 88.9
```

```
## 3rd Qu.:240.0 3rd Qu.:123.0 3rd Qu.:46.00 3rd Qu.: 93.0
## Max. :290.0 Max. :157.0 Max. :65.00 Max. :119.0
## NA's :1 NA's :1 NA's :1 NA's :1
## FG% 3PM 3PA 3P% FTM
## Min. :27.70 Min. : 2.00 Min. :12.0 Min. : 6.9 Min. : 1.00
## 1st Qu.:43.80 1st Qu.:10.00 1st Qu.:30.0 1st Qu.:31.0 1st Qu.:13.00
## Median :47.50 Median :13.00 Median :35.0 Median :36.6 Median :17.00
## Mean :47.52 Mean :12.84 Mean :35.1 Mean :36.5 Mean :17.04
## 3rd Qu.:51.20 3rd Qu.:15.00 3rd Qu.:39.0 3rd Qu.:41.7 3rd Qu.:21.00
## Max. :67.10 Max. :27.00 Max. :63.0 Max. :64.5 Max. :44.00
## NA's :1 NA's :1 NA's :1 NA's :1 NA's :1
## FTA FT% OREB DREB
## Min. : 2.00 Min. : 33.30 Min. : 0.00 Min. :16.00
## 1st Qu.:17.00 1st Qu.: 72.00 1st Qu.: 8.00 1st Qu.:29.00
## Median :21.00 Median : 78.90 Median :10.00 Median :33.00
## Mean :21.73 Mean : 78.33 Mean :10.55 Mean :32.99
## 3rd Qu.:26.00 3rd Qu.: 85.20 3rd Qu.:13.00 3rd Qu.:36.00
## Max. :52.00 Max. :100.00 Max. :28.00 Max. :55.00
## NA's :1 NA's :1 NA's :1 NA's :1
## REB AST STL BLK
## Min. :25.00 Min. :11.00 Min. : 0.000 Min. : 0.000
## 1st Qu.:39.00 1st Qu.:23.00 1st Qu.: 6.000 1st Qu.: 3.000
## Median :43.00 Median :27.00 Median : 7.000 Median : 5.000
## Mean :43.54 Mean :26.67 Mean : 7.473 Mean : 5.142
## 3rd Qu.:48.00 3rd Qu.:30.00 3rd Qu.: 9.000 3rd Qu.: 7.000
## Max. :74.00 Max. :50.00 Max. :20.000 Max. :17.000
## NA's :1 NA's :1 NA's :1 NA's :1
## TOV PF +/-
## Min. : 3.00 Min. : 4.00 Min. : -62.00000
## 1st Qu.:11.00 1st Qu.:16.00 1st Qu.: -10.00000
## Median :14.00 Median :19.00 Median : 1.00000
## Mean :13.61 Mean :18.73 Mean : 0.00529
## 3rd Qu.:16.00 3rd Qu.:21.00 3rd Qu.: 10.00000
## Max. :29.00 Max. :34.00 Max. : 62.00000
## NA's :1 NA's :1 NA's :1
```

```
# Fit an initial multiple linear regression (MLR) model
# Exclude non-numeric predictors and highly collinear variables
model <- lm(PTS ~. -Team -`Match Up` -`Game Date` -`W/L` -FGM -FGA -`3PM` -`3PA` -FTM -FTA, data = df)

# View the model summary
summary(model)
```

```
##
## Call:
## lm(formula = PTS ~ . - Team - `Match Up` - `Game Date` - `W/L` -
## FGM - FGA - `3PM` - `3PA` - FTM - FTA, data = df)
##
## Residuals:
## Min 1Q Median 3Q Max
## -22.5561 -3.7035 -0.1289 3.5637 20.7164
##
## Coefficients: (1 not defined because of singularities)
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) -94.46062 4.80467 -19.660 <2e-16 ***
```

```
## MIN          0.33000    0.01853   17.810   <2e-16 ***
## `FG%`        1.58155    0.03527   44.843   <2e-16 ***
## `3P%`        0.31297    0.01739   17.997   <2e-16 ***
## `FT%`        0.19252    0.01131   17.021   <2e-16 ***
## OREB         0.93540    0.03372   27.741   <2e-16 ***
## DREB         0.28687    0.03004    9.550   <2e-16 ***
## REB          NA        NA        NA        NA
## AST          0.32214    0.02802   11.498   <2e-16 ***
## STL          0.37875    0.04581    8.269   <2e-16 ***
## BLK          0.07163    0.04462    1.605    0.1085
## TOV         -0.85829    0.03281  -26.162   <2e-16 ***
## PF           0.42271    0.02759   15.324   <2e-16 ***
## `+/-`       -0.03311    0.01345   -2.461    0.0139 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.555 on 2446 degrees of freedom
## (1 observation deleted due to missingness)
## Multiple R-squared:  0.8137, Adjusted R-squared:  0.8128
## F-statistic: 890.3 on 12 and 2446 DF,  p-value: < 2.2e-16
```

```
# Perform ANOVA to assess predictor significance
anova(model)
```

```
## Analysis of Variance Table
##
## Response: PTS
##          Df Sum Sq Mean Sq  F value    Pr(>F)
## MIN          1  13717   13717  444.4378 < 2.2e-16 ***
## `FG%`        1 230920  230920 7482.0038 < 2.2e-16 ***
## `3P%`        1  11476   11476  371.8181 < 2.2e-16 ***
## `FT%`        1   6884    6884  223.0521 < 2.2e-16 ***
## OREB          1  28336  28336  918.1075 < 2.2e-16 ***
## DREB          1   1318    1318  42.6903 7.776e-11 ***
## AST          1   7282    7282  235.9283 < 2.2e-16 ***
## STL          1   1280    1280  41.4608 1.443e-10 ***
## BLK          1     4      4    0.1145  0.73508
## TOV          1  21132  21132  684.6928 < 2.2e-16 ***
## PF           1   7212    7212  233.6741 < 2.2e-16 ***
## `+/-`        1    187    187    6.0542  0.01394 *
## Residuals 2446  75492     31
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
# Remove statistically insignificant predictors to create a reduced model
reduced_model <- update(model, ~. -BLK -REB)
```

```
# View the reduced model summary
summary(reduced_model)
```

```
##
## Call:
## lm(formula = PTS ~ MIN + `FG%` + `3P%` + `FT%` + OREB + DREB +
##     AST + STL + TOV + PF + `+/-`, data = df)
##
## Residuals:
```

```

##      Min      1Q   Median      3Q      Max
## -22.4054  -3.6856  -0.0981   3.5382  21.1849
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -94.51114    4.80612  -19.665 < 2e-16 ***
## MIN          0.33182    0.01850   17.936 < 2e-16 ***
## `FG%`        1.57999    0.03527   44.801 < 2e-16 ***
## `3P%`        0.31181    0.01738   17.940 < 2e-16 ***
## `FT%`        0.19253    0.01131   17.016 < 2e-16 ***
## OREB         0.93425    0.03372   27.704 < 2e-16 ***
## DREB         0.28922    0.03001    9.637 < 2e-16 ***
## AST          0.32327    0.02802   11.538 < 2e-16 ***
## STL          0.37675    0.04580    8.225 3.12e-16 ***
## TOV         -0.85404    0.03271  -26.109 < 2e-16 ***
## PF           0.42039    0.02756   15.256 < 2e-16 ***
## `+/-`       -0.03056    0.01337   -2.287 0.0223 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.557 on 2447 degrees of freedom
## (1 observation deleted due to missingness)
## Multiple R-squared:  0.8135, Adjusted R-squared:  0.8127
## F-statistic: 970.4 on 11 and 2447 DF,  p-value: < 2.2e-16

# Load the 'car' package for calculating Variance Inflation Factor (VIF)
library(car)

## Loading required package: carData

# Calculate VIF values to check for multicollinearity (threshold: VIF > 5 indicates concern)
vif(reduced_model)

##      MIN      `FG%`      `3P%`      `FT%`      OREB      DREB      AST      STL
## 1.099206 2.991048 1.673378 1.050744 1.319250 2.097086 1.626274 1.329328
##      TOV      PF      `+/-`
## 1.237588 1.037889 3.543332

# Perform stepwise regression (backward elimination based on AIC)
stepwise_model <- step(reduced_model, direction = "backward")

## Start:  AIC=8446.87
## PTS ~ MIN + `FG%` + `3P%` + `FT%` + OREB + DREB + AST + STL +
##      TOV + PF + `+/-`
##
##      Df Sum of Sq      RSS      AIC
## <none>                75571 8446.9
## - `+/-`    1         161  75733 8450.1
## - STL      1        2089  77661 8511.9
## - DREB     1        2868  78439 8536.5
## - AST      1        4112  79683 8575.1
## - PF       1        7188  82759 8668.3
## - `FT%`    1       8942  84513 8719.9
## - MIN      1       9935  85507 8748.6
## - `3P%`    1       9939  85511 8748.7
## - TOV      1      21053  96624 9049.2

```

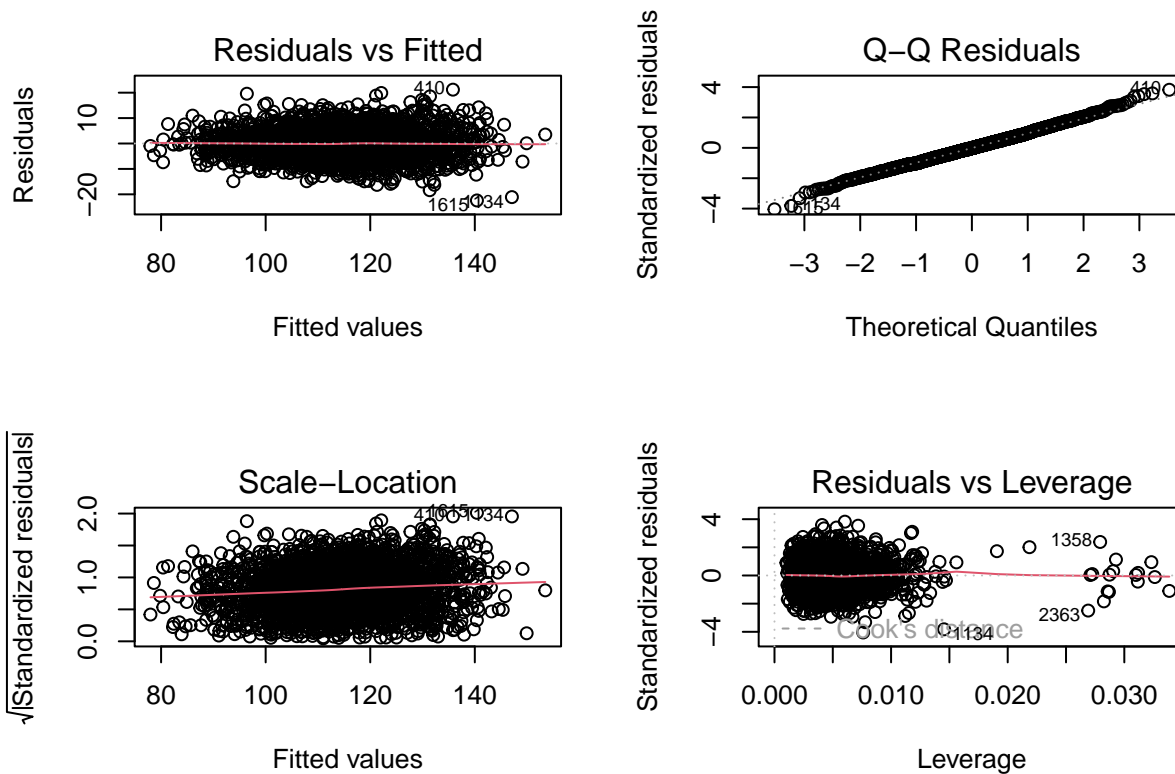
```
## - OREB    1      23704  99275 9115.7
## - `FG%`   1      61988 137559 9917.8

# View the stepwise selected model summary
summary(stepwise_model)

##
## Call:
## lm(formula = PTS ~ MIN + `FG%` + `3P%` + `FT%` + OREB + DREB +
##     AST + STL + TOV + PF + `+/-`, data = df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -22.4054  -3.6856  -0.0981   3.5382  21.1849
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -94.51114     4.80612  -19.665 < 2e-16 ***
## MIN           0.33182     0.01850   17.936 < 2e-16 ***
## `FG%`        1.57999     0.03527   44.801 < 2e-16 ***
## `3P%`        0.31181     0.01738   17.940 < 2e-16 ***
## `FT%`        0.19253     0.01131   17.016 < 2e-16 ***
## OREB          0.93425     0.03372   27.704 < 2e-16 ***
## DREB          0.28922     0.03001    9.637 < 2e-16 ***
## AST           0.32327     0.02802   11.538 < 2e-16 ***
## STL           0.37675     0.04580    8.225 3.12e-16 ***
## TOV          -0.85404     0.03271  -26.109 < 2e-16 ***
## PF            0.42039     0.02756   15.256 < 2e-16 ***
## `+/-`       -0.03056     0.01337   -2.287  0.0223 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.557 on 2447 degrees of freedom
## (1 observation deleted due to missingness)
## Multiple R-squared:  0.8135, Adjusted R-squared:  0.8127
## F-statistic: 970.4 on 11 and 2447 DF, p-value: < 2.2e-16

# Set up 2x2 plotting space for diagnostic plots
par(mfrow = c(2,2))

# Generate the four diagnostic plots for the reduced model
plot(reduced_model, which = 1) # Residuals vs Fitted
plot(reduced_model, which = 2) # Normal Q-Q plot
plot(reduced_model, which = 3) # Scale-Location plot
plot(reduced_model, which = 5) # Residuals vs Leverage
```



```
# Load 'lmtest' package for additional model testing
library(lmtest)
```

```
## Loading required package: zoo
```

```
##
```

```
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':
```

```
##
```

```
##      as.Date, as.Date.numeric
```

```
# Perform Breusch-Pagan (BP) test to check for heteroscedasticity
bptest(reduced_model)
```

```
##
```

```
## studentized Breusch-Pagan test
```

```
##
```

```
## data: reduced_model
```

```
## BP = 79.923, df = 11, p-value = 1.527e-12
```

```
# Transform the response variable to address heteroscedasticity detected by BP test
df$PTS_transformed <- df$PTS^2
```

```
# Prepare the dataset by removing unnecessary columns
```

```
df_reduced1 <- df[, !(names(df) %in% c("PTS", "Team", "Match Up", "Game Date", "W/L", "FGM", "FGA", "3PT"))]
```

```
# Fit a model using the transformed response
```

```
model_transformed <- lm(PTS_transformed ~., data = df_reduced1)
```

```
# View the transformed model summary
```

```
summary(model_transformed)
```

```
##
## Call:
## lm(formula = PTS_transformed ~ ., data = df_reduced1)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5235.0  -893.2   -30.2    784.9   6501.2
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -35101.538    1143.265  -30.703 < 2e-16 ***
## MIN           78.299      4.401   17.792 < 2e-16 ***
## `FG%`        358.683      8.389   42.756 < 2e-16 ***
## `3P%`         71.660      4.135   17.332 < 2e-16 ***
## `FT%`         44.363      2.691   16.483 < 2e-16 ***
## OREB          212.329      8.022   26.469 < 2e-16 ***
## DREB           65.996      7.139    9.244 < 2e-16 ***
## AST           77.107      6.665   11.570 < 2e-16 ***
## STL           85.099     10.895    7.811 8.38e-15 ***
## TOV          -193.327      7.781  -24.846 < 2e-16 ***
## PF            95.952      6.555   14.638 < 2e-16 ***
## `+/-`        -7.000      3.179   -2.202  0.0278 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1322 on 2447 degrees of freedom
## (1 observation deleted due to missingness)
## Multiple R-squared:  0.8015, Adjusted R-squared:  0.8006
## F-statistic: 898.4 on 11 and 2447 DF, p-value: < 2.2e-16
```

```
# Perform BP test again on the transformed model
```

```
bptest(model_transformed)
```

```
##
## studentized Breusch-Pagan test
##
## data: model_transformed
## BP = 169.59, df = 11, p-value < 2.2e-16
```

```
# Define weights based on the fitted values to apply Weighted Least Squares (WLS)
weights <- 1 / fitted(model_transformed)^2 # Assign lower weights to large residuals
weights <- weights[1:nrow(df_reduced1)] # Match the number of rows
```

```
# Fit a WLS model
```

```
wls_model <- lm(PTS_transformed ~ ., data = df_reduced1, weights = weights)
```

```
# View the WSL model
```

```
summary(wls_model)
```

```
##
## Call:
## lm(formula = PTS_transformed ~ ., data = df_reduced1, weights = weights)
##
## Weighted Residuals:
##      Min       1Q   Median       3Q      Max
```



```

## -0.41863 -0.06806 -0.00294 0.06112 0.45344
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept) -33029.361    1225.895  -26.943 < 2e-16 ***
## MIN          73.465       4.852   15.141 < 2e-16 ***
## `FG%`       346.014       7.624   45.387 < 2e-16 ***
## `3P%`       72.178       3.823   18.880 < 2e-16 ***
## `FT%`       41.439       2.455   16.878 < 2e-16 ***
## OREB        199.262       7.288   27.340 < 2e-16 ***
## DREB         68.483       6.428   10.653 < 2e-16 ***
## AST         75.986       6.371   11.928 < 2e-16 ***
## STL         90.022      10.000    9.003 < 2e-16 ***
## TOV        -185.496       6.972  -26.607 < 2e-16 ***
## PF          86.895       6.017   14.441 < 2e-16 ***
## `+/-`      -10.171       2.829   -3.596 0.00033 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09873 on 2446 degrees of freedom
## (2 observations deleted due to missingness)
## Multiple R-squared:  0.827, Adjusted R-squared:  0.8262
## F-statistic: 1063 on 11 and 2446 DF, p-value: < 2.2e-16
# Perform BP test on the WSL model to confirm improvement
bptest(wls_model)

##
## studentized Breusch-Pagan test
##
## data:  wls_model
## BP = 3.4603e-06, df = 11, p-value = 1
# Perform stepwise regression again on the WLS model
stepwise_model <- step(wls_model, direction = "both")

## Start:  AIC=-11370.22
## PTS_transformed ~ MIN + `FG%` + `3P%` + `FT%` + OREB + DREB +
##           AST + STL + TOV + PF + `+/-`
##
##           Df Sum of Sq    RSS    AIC
## <none>                 23.844 -11370.2
## - `+/-`    1      0.1260 23.970 -11359.3
## - STL      1      0.7901 24.634 -11292.1
## - DREB     1      1.1064 24.951 -11260.7
## - AST      1      1.3869 25.231 -11233.3
## - PF       1      2.0329 25.877 -11171.1
## - MIN      1      2.2346 26.079 -11152.0
## - `FT%`    1      2.7768 26.621 -11101.4
## - `3P%`    1      3.4747 27.319 -11037.8
## - TOV      1      6.9013 30.745 -10747.4
## - OREB     1      7.2867 31.131 -10716.8
## - `FG%`    1     20.0808 43.925  -9870.5
# View the final selected WSL model summary
summary(stepwise_model)

```

```
##
## Call:
## lm(formula = PTS_transformed ~ MIN + `FG%` + `3P%` + `FT%` +
##      OREB + DREB + AST + STL + TOV + PF + `+/-`, data = df_reduced1,
##      weights = weights)
##
## Weighted Residuals:
##      Min        1Q      Median        3Q        Max
## -0.41863 -0.06806 -0.00294  0.06112  0.45344
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -33029.361   1225.895  -26.943 < 2e-16 ***
## MIN           73.465     4.852   15.141 < 2e-16 ***
## `FG%`        346.014     7.624   45.387 < 2e-16 ***
## `3P%`         72.178     3.823   18.880 < 2e-16 ***
## `FT%`         41.439     2.455   16.878 < 2e-16 ***
## OREB          199.262     7.288   27.340 < 2e-16 ***
## DREB           68.483     6.428   10.653 < 2e-16 ***
## AST           75.986     6.371   11.928 < 2e-16 ***
## STL           90.022    10.000    9.003 < 2e-16 ***
## TOV          -185.496     6.972  -26.607 < 2e-16 ***
## PF            86.895     6.017   14.441 < 2e-16 ***
## `+/-`        -10.171     2.829   -3.596  0.00033 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09873 on 2446 degrees of freedom
## (2 observations deleted due to missingness)
## Multiple R-squared:  0.827, Adjusted R-squared:  0.8262
## F-statistic: 1063 on 11 and 2446 DF, p-value: < 2.2e-16

# Set up 2x2 plotting space again for final WSL diagnostic plots
par(mfrow = c(2,2))

# Generate diagnostic plots for the final WSL model
plot(wls_model, which = 1) # Residuals vs Fitted
plot(wls_model, which = 2) # Normal Q-Q plot
plot(wls_model, which = 3) # Scale-Location plot
plot(wls_model, which = 5) # Residuals vs Leverage
```

