Two JavaFX rectangles with constructor arguments  $(X_1, Y_1, W_1, H_1)$  and  $(X_2, Y_2, W_2, H_2)$  are given. Two points  $(A_1, B_1)$  and  $(A_2, B_2)$  are chosen, one for each rectangle. If both the rectangles rotate as much as  $\theta$ , the new coordinates are

$$X_{1}^{\text{rot}} = X_{1} + \frac{W_{1}}{2} + \left(A_{1} - X_{1} - \frac{W_{1}}{2}\right) \cos \theta - \left(B_{1} - Y_{1} - \frac{H_{1}}{2}\right) \sin \theta,$$

$$Y_{1}^{\text{rot}} = Y_{1} + \frac{H_{1}}{2} + \left(A_{1} - X_{1} - \frac{W_{1}}{2}\right) \sin \theta + \left(B_{1} - Y_{1} - \frac{H_{1}}{2}\right) \cos \theta,$$

$$(1)$$

and

$$X_2^{\text{rot}} = X_2 + \frac{W_2}{2} + \left(A_2 - X_2 - \frac{W_2}{2}\right) \cos \theta - \left(B_2 - Y_2 - \frac{H_2}{2}\right) \sin \theta,$$

$$Y_2^{\text{rot}} = Y_2 + \frac{H_2}{2} + \left(A_2 - X_2 - \frac{W_2}{2}\right) \sin \theta + \left(B_2 - Y_2 - \frac{H_2}{2}\right) \cos \theta.$$
(2)

We enforce  $X_1^{\rm rot}=X_2^{\rm rot}$  and  $Y_1^{\rm rot}=Y_2^{\rm rot}$ . We know that  $A_i-X_i-\frac{W_i}{2}=a_i\frac{W_i}{2}$  and  $B_i-Y_i-\frac{H_i}{2}=b_i\frac{H_i}{2}$ . These values are given in the following table for the eight corner points. Hence,

$$X_{2} + \frac{W_{2}}{2} + \frac{a_{2}W_{2}}{2}\cos\theta - \frac{b_{2}H_{2}}{2}\sin\theta = X_{1} + \frac{W_{1}}{2} + \frac{a_{1}W_{1}}{2}\cos\theta - \frac{b_{1}H_{1}}{2}\sin\theta$$

$$Y_{2} + \frac{H_{2}}{2} + \frac{a_{2}W_{2}}{2}\sin\theta + \frac{b_{2}H_{2}}{2}\cos\theta = Y_{1} + \frac{H_{1}}{2} + \frac{a_{1}W_{1}}{2}\sin\theta + \frac{b_{1}H_{1}}{2}\cos\theta$$
(3)

or

$$X_{2} = X_{1} + \frac{W_{1} - W_{2}}{2} + \frac{a_{1}W_{1} - a_{2}W_{2}}{2}\cos\theta - \frac{b_{1}H_{1} - b_{2}H_{2}}{2}\sin\theta$$

$$Y_{2} = Y_{1} + \frac{H_{1} - H_{2}}{2} + \frac{a_{1}W_{1} - a_{2}W_{2}}{2}\sin\theta + \frac{b_{1}H_{1} - b_{2}H_{2}}{2}\cos\theta.$$

$$(4)$$

index	$a_1$	$b_1$
0	-1	-1
1	-1	0
2	-1	1
3	0	1
4	1	1
5	1	0
6	1	-1
7	0	-1

We can assume that  $a_1=a_2=a$  and  $b_1=b_2=b$ . Hence, by defining  $H_1-H_2=\delta_{\rm H}$  and  $W_1-W_2=\delta_{\rm W}$  we have

$$X_2 = X_1 + \frac{\delta_{\mathcal{W}}}{2} (1 + a\cos\theta) - \frac{b\delta_{\mathcal{H}}}{2} \sin\theta,$$
  

$$Y_2 = Y_1 + \frac{a\delta_{\mathcal{W}}}{2} \sin\theta + \frac{\delta_{\mathcal{H}}}{2} (1 + b\cos\theta).$$
(5)

On dynamicDragRectangle:

- 1. onMousePressed
  - (a) On Ctrl button up:
    - i. If pressed mouse on no shape (mouse press location contained by no shape), unselect all shapes and set to drawing dynamicDragRectangle.
    - ii. If pressed mouse on an unselected shape, unselect all and select the highest-layer shape containing the mouse press location.
    - iii. If pressed mouse on a selected shape, do nothing.
- 2. onMouseDragged
  - (a) On Ctrl button up or down:
    - i. I suspect we only need to move the selected objects.

## 0.1 Resizing

The resizing transformation can be generally described as two independent resizing along two perpendicular vectors. WLOG, we can assume these vectors to be  $v_1 = [\cos \theta, \sin \theta]$  and  $v_2 = [-\sin \theta, \cos \theta]$ . They resize, so that the new vectors are  $v_1^{\text{new}} = [s_x \cos \theta, s_x \sin \theta]$  and  $v_2^{\text{new}} = [-s_y \sin \theta, s_y \cos \theta]$ . We wish to find out what happens to the whole space.

Fortunately, such a transformation linear and invertible. This means that we can model whole the transformation process by a matrix. We assume then, that the transformation is a result of three consecutive transformations:

- 1- The plane is rotated as much as  $-\theta$ .
- 2- The plane is scaled as much as  $s_x$  and  $s_y$  along the x- and y- axes, resp.
- 3- The plane is rotated as much as  $\theta$ .

The resizing transformation matrix is then

$$R = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

$$= \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} s_x \cos \theta & s_x \sin \theta \\ -s_y \sin \theta & s_y \cos \theta \end{bmatrix}$$

$$= \begin{bmatrix} s_x \cos^2 \theta + s_y \sin^2 \theta & (s_x - s_y) \sin \theta \cos \theta \\ (s_x - s_y) \sin \theta \cos \theta & s_x \sin^2 \theta + s_y \cos^2 \theta \end{bmatrix}$$
(6)

If a point  $\begin{bmatrix} p_x & p_y \end{bmatrix}^T$  is regarded as a fixed point, a translation is needed as much as

$$(I - R) \begin{bmatrix} p_x \\ p_y \end{bmatrix} = \begin{bmatrix} 1 - s_x \cos^2 \theta - s_y \sin^2 \theta & (s_y - s_x) \sin \theta \cos \theta \\ (s_y - s_x) \sin \theta \cos \theta & 1 - s_x \sin^2 \theta - s_y \cos^2 \theta \end{bmatrix} \begin{bmatrix} p_x \\ p_y \end{bmatrix}$$
(7)