

Institution Building without Commitment + A Theory of Gradual Trade Liberalization and Retrenchment

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Question

- Time inconsistency is a pervasive issue
 - taxation, government debt, consumption-saving problem, monetary policy, ...
- Two Benchmarks:
 - Markov equilibrium
 - Sequential equilibrium/sustainable plan

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 - Outcome determined by fundamentals
 - ... but can be largely improved upon

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- Markov equilibrium:
 - Interesting comparative statics
 - Outcome determined by fundamentals
 - ... but can be largely improved upon
- Sequential equilibrium:
 - Can often attain very good outcomes (folk theorem)
 - Can also attain very bad outcomes (folk theorem again)
 - Relies on self-punishment as a threat

Our View

- Good institutions and social norms do not evolve overnight
- Collaboration across cohorts of decision makers builds slowly
- It probably also erodes slowly
- Look for equilibrium concept that captures this, and addresses shortcomings of Markov & Best Sequential Eq.

Equilibrium Properties

- Compare with Markov equilibrium
 - payoff only depends on state variables, like Markov equilibrium
 - action can depend on history, different from Markov equilibrium
- Compare with sequential equilibrium
 - no self-punishment
 - Refinement I: same continuation value on or off equilibrium path
 - Refinement II: no one wants to deviate and wait for a restart of the game
- New issue with state variables
 - how to induce stationary environment

Quantitative Findings

- Steady state
 - allocation is close to Ramsey outcome, much better than Markov equilibrium
- Transition
 - allocation starts similar to Markov, converges to similar to Ramsey

Related Literature

- Markov equilibrium and GEE
 - Currie and Levine (1993), Bassetto and Sargent (2005), Klein and Ríos-Rull (2003), Klein, Quadrini and Ríos-Rull (2005), Krusell and Ríos-Rull (2008), Krusell, Kuruscu, and Smith (2010), Song, Storesletten and Zilibotti (2012)
- Sustainable plan
 - Stokey (1988), Chari and Kehoe (1990), Abreu, Pearce and Stacchetti (1990), Phelan and Stacchetti (2001)
- Quasi-geometric discounting growth model
 - Strotz (1956), Phelps and Pollak (1968), Laibson (1997), Krusell and Smith (2003), Chatterjee and Eyigungor (2015), Bernheim, Ray, and Yeltekin (2017), Cao and Werning (2017)
- Refinement of subgame perfect equilibrium
 - Farrell and Maskin (1989), Kocherlakota (1996), Prescott and Ríos-Rull (2005), Nozawa (2014), Ales and Sleet (2015)

Plan

- 1 An example: a growth model with quasi-geometric discounting
- 2 General definition and properties
- 3 (In progress: adding uncertainty)
- 4 Application to Foreign Trade

Part I: A Growth Model

The Environment

- Preferences: quasi-geometric discounting

$$\Psi_t = u(c_t) + \delta \sum_{\tau=1}^{\infty} \beta^{\tau} u(c_{t+\tau})$$

- period utility function $u(c) = \log c$
- $\delta = 1$ is the time-consistent case

- Technology

$$f(k_t) = k_t^{\alpha}, \quad k_{t+1} = f(k_t) - c_t.$$

Benchmark I: Markov Perfect Equilibrium

- Take future $g(k)$ as given

$$\max_{k'} u[f(k) - k'] + \delta\beta\Omega(k'; g)$$

cont. value: $\Omega(k; g) = u[f(k) - g(k)] + \beta\Omega[g(k); g]$

- The Generalized Euler Equation (GEE)

$$u_c = \beta u'_c [\delta f'_k + (1 - \delta) g'_k]$$

- The equilibrium features a constant saving rate

$$k' = \frac{\delta\alpha\beta}{1 - \alpha\beta + \delta\alpha\beta} k^\alpha = s^M k^\alpha$$

Benchmark II: Ramsey Allocation with Commitment

- Choose all future allocations at period 0

$$\max_{k_1} u[f(k_0) - k_1] + \delta\beta\Omega(k_1)$$

cont. value: $\Omega(k) = \max_{k'} u[f(k) - k'] + \beta\Omega(k')$

- The sequence of saving rates is given by

$$s_t = \begin{cases} s^M = \frac{\alpha\delta\beta}{1-\alpha\beta+\delta\alpha\beta}, & t = 0 \\ s^R = \alpha\beta, & t > 0 \end{cases}$$

- Steady state capital in Markov equilibrium is lower than Ramsey

$$s^M < s^R$$

Elements of Organization Equilibrium: Action Space

- Use saving rate as player t 's action; equilibrium outcome is a sequence of saving rates $\{s_0, s_1, s_2, \dots\}$
- Note $s \in [0, 1]$ always feasible, no matter what k is
- Given an initial capital k_0 , the proposal induces a sequence of capital

$$k_1 = s_0 k_0^\alpha$$

$$k_2 = s_1 k_1^\alpha = k_0^{\alpha^2} s_1 s_0^\alpha$$

$$\vdots$$

$$k_t = k_0^{\alpha^t} \prod_{j=0}^{t-1} s_j^{\alpha^{t-j-1}}$$

Value Function and Separability

- The lifetime utility for player t is

$$\begin{aligned}
 & \underbrace{U(k_t, s_t, s_{t+1}, \dots)}_{\text{total payoff}} \\
 &= \log[(1 - s_t)k_t^\alpha] + \delta \sum_{j=1}^{\infty} \beta^j \log [(1 - s_{t+j})k_{t+j}^\alpha] \\
 &= \frac{\alpha(1 - \alpha\beta + \delta\alpha\beta)}{1 - \alpha\beta} \log k_t + \log(1 - s_t) \\
 & \quad + \delta \sum_{j=1}^{\infty} \beta^j \log \left[(1 - s_{t+j}) \prod_{\tau=0}^{j-1} s_{t+\tau}^{\alpha^{j-\tau}} \right] \\
 &\equiv \underbrace{\phi \log k_t}_{\text{Contribution of the state}} + \underbrace{V(s_t, s_{t+1}, \dots)}_{\text{action payoff}}
 \end{aligned}$$

Organizational Equilibrium

Proposition

A sequence $\{\bar{s}_t\}_{t=0}^{\infty}$ that satisfies the following properties is an organizational equilibrium:

① *No-restarting:*

$$V(\bar{s}_t, \bar{s}_{t+1}, \bar{s}_{t+2}, \dots) = \bar{V} \quad \forall t \geq 0;$$

② *Optimality: No other sequence satisfying no-restarting achieves a higher constant value;*

③ *No-delay:*

$$V(\bar{s}_0, \bar{s}_1, \bar{s}_2, \dots) \geq \max_s V(s, \bar{s}_0, \bar{s}_1, \dots).$$

- It is a proposition, not a definition, because we will define OE in terms of a game
- Proposition has some assumptions, satisfied in our example

Where Do these Properties Come From?

- No-restarting:
 - akin to symmetry in Kocherlakota
 - From renegotiation proofness
 - If equilibrium is too generous to player 0, player 1 wants to forget the past.
- Optimality: no waste
- No-delay: who should start this game?
 - Comes from any ambiguity to the answer.
 - Many revolutions talk about “forgetting the past”
 - “This time’s different”
 - Time 0 could be any time, and player 0 should not have an incentive to wait it out

Is the Ramsey Outcome an Organizational Equilibrium?

- Imagine the initial agent with k_0 proposes $\{s^M, s^R, s^R, \dots\}$, which implies

$$k_1 = s^M k_0^\alpha$$

- By following the proposal, the next agent's payoff is

$$U(k_1, s^R, s^R, s^R, \dots) = \phi \log k_1 + V(s^R, s^R, s^R, \dots)$$

- By copying the proposal, the next agent's payoff is

$$\begin{aligned} U(k_1, s^M, s^R, s^R, \dots) &= \phi \log k_1 + V(s^M, s^R, s^R, \dots) \\ &> \phi \log k_1 + V(s^R, s^R, s^R, \dots) \end{aligned}$$

- Copying is better than following, Ramsey outcome cannot be implemented (no-restarting fails)

Can a Constant Saving Rate be Implemented?

- Consider $\{s, s, s \dots\}$
- By following the proposal, the payoff for agent in period t is

$$U(k_t, s, s, \dots) = \phi \log k_t + V(s, s, \dots)$$

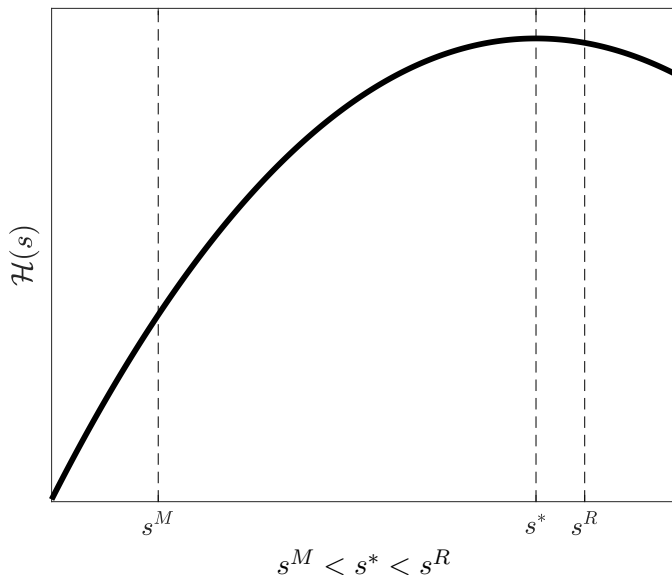
where

$$V(s, s, \dots) \equiv \mathcal{H}(s) = \left(1 + \frac{\beta\delta}{1-\beta}\right) \log(1-s) + \frac{\delta\alpha\beta}{(1-\alpha\beta)(1-\beta)} \log(s)$$

- No-restarting is fine
- Optimality: pick

$$s^* = \operatorname{argmax} \mathcal{H}(s)$$

Optimal Constant Saving Rate



Can $\{s^*, s^*, \dots\}$ be Implemented?

- No-delay fails:
- Player 0 prefers to choose s^M , and wait the next to start $\{s^*, s^*, \dots\}$

$$\begin{aligned}U(k_0, s^M, s^*, s^*, \dots) &= \phi \log k_0 + V(s^M, s^*, s^*, \dots) \\ &> \phi \log k_0 + V(s^*, s^*, s^*, \dots)\end{aligned}$$

- But, something else can be implemented, which converges to s^*

Construct the Organizational Equilibrium

- Look for a sequence of saving rates $\{s_0, s_1, \dots\}$
- Every generation obtains the same \bar{V}

$$V(s_t, s_{t+1}, \dots) = V(s_{t+1}, s_{t+2}, \dots) = \bar{V}$$

which induces the following difference equation

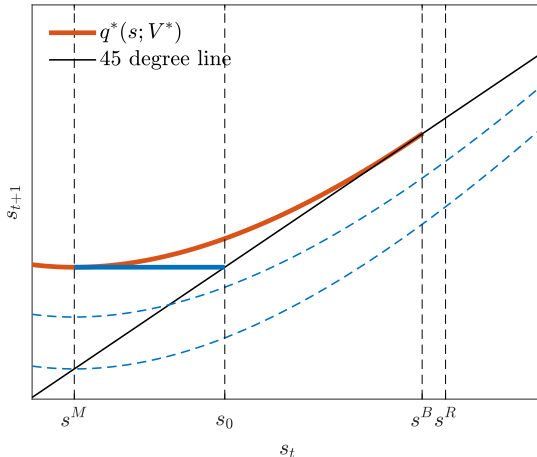
$$\beta(1 - \delta) \log(1 - s_{t+1}) = \frac{\delta\alpha\beta}{1 - \alpha\beta} \log s_t + \log(1 - s_t) - (1 - \beta)\bar{V}$$

- We call this difference equation as the proposal function

$$s_{t+1} = q(s_t; \bar{V})$$

- The maximal \bar{V} and an initial s_0 are needed to determine $\{s_\tau\}_{\tau=0}^\infty$

Determine V^*



- As \bar{V} increases, the proposal function $q(s; \bar{V})$ moves upwards
- The highest $\bar{V} = V^*$ is achieved when $q(s; \bar{V})$ is tangent to the 45 degree line

Determine the Initial Saving Rate s_0

- The first agent should have no incentive to delay the proposal

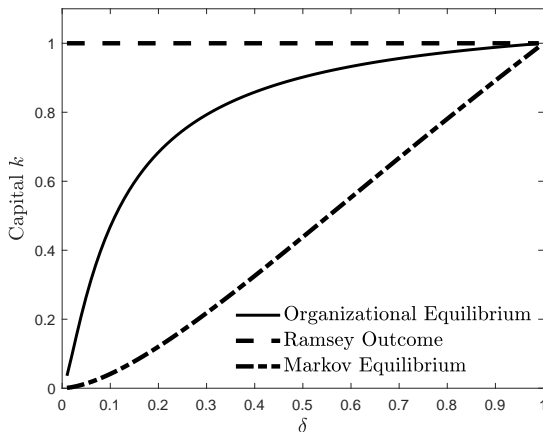
$$\max_s V(s, s_0, s_1, s_2, \dots) = V(s^M, s_0, s_1, s_2, \dots)$$

- s_0 has to be such that

$$V^* = V(s_0, s_1, s_2, \dots) \geq V(s^M, s_0, s_1, s_2, \dots)$$

- We select $s_0 = q^*(s^M)$, which yields the highest welfare for period $t + 1$

Comparison: Steady State



- Organizational equilibrium is much better than the Markov equilibrium

Part II: Organizational Equilibrium for Weakly Separable Economies

General Definition: Game of Perfect Information

An infinite sequence of decision makers is called to act

- state $k \in K$
- action $a \in A$
- state evolves $k_{t+1} = F(k_t, a_t)$
- Player t preferences: $U(k_t, a_t, a_{t+1}, a_{t+2}, \dots)$

Separability Assumption

Assumption

- 1 *At any point in time t , the set A is independent of the state k_t*
- 2 *U is weakly separable in k and in $\{a_s\}_{s=0}^{\infty}$*

$$U(k, a_0, a_1, a_2, \dots) \equiv v(k, V(a_0, a_1, a_2, \dots)).$$

and such that v is strictly increasing in its second argument.

- 3 *Technical stuff: A is compact, convex, V is continuous and quasiconcave...*

On the Choice of Actions

- Weak separability and state independence of A depend on the specification of the action set
- Example: hyperbolic discounting. If the choice is c , feasible actions depend on k
- So, sometimes a problem may look nonseparable, but may become separable by rescaling actions appropriately

Requirements

Look for Subgame-Perfect Equilibria that satisfy:

- ① State Independence: the strategy followed by any player is independent of the state k
- ② No-restarting and optimality: Equilibria are symmetric, that is, the action payoff is independent of the past. Best among symmetric eq.
- ③ No Delay: Restarting the strategy profile from period 0 is a sufficient deterrent against any deviation:

$$\bar{V} = V(a_{0,\sigma}, a_{1,\sigma}, a_{2,\sigma}, \dots) \geq V(a, a_{0,\sigma}, a_{1,\sigma}, a_{2,\sigma}, \dots).$$

Definition

An Organizational Equilibrium is the outcome of any subgame perfect equilibrium that satisfies the requirements above.

Existence Results

- An optimally symmetric state-independent equilibrium exists
- If

$$V(a_0, a_1, a_2, \dots) \equiv \tilde{V}(a_0, \hat{V}(a_1, a_2, \dots)),$$

then an optimally symmetric state-independent equilibrium that satisfies no delay exists.

Organizational Equilibrium (OE) vs. Subgame-Perfect Equilibrium

- ① OE is the equilibrium path of a sub-game perfect equilibrium
- ② It can be implemented through various strategies. Examples:
 - restart from the beginning when someone deviates
 - use difference equation to make each player indifferent between deviating and following the equilibrium strategy (over a range)

Properties

- A **sequence** of actions satisfying no-restarting, optimality and no-delay is an organizational equilibrium
- Assume that continuation utility is recursive:

$$\widehat{V}(a_1, a_2, \dots) = W(a_1, \widehat{V}(a_2, a_3, \dots))$$

Then:

- OE admits a recursive structure

$$v_{t+1} = g(v_t)$$

- Equilibrium converges to the best constant allocation
($\max V(a, a, a, \dots)$)
- Convergence is not immediate (except in degenerate cases)

Alternative Game

- Record keeping not immediately possible: players do not observe past actions
- Becomes **possible** at random time \hat{t} (not known)
- From time \hat{t} on, player t chooses a_t and ρ_t :
 - $\rho_t = H$: **H**ide history from the past. Future players do not observe past actions.
 - $\rho_t = S$: **S**tart record keeping. Future players only observe a_t .
 - $\rho_t = C$: **C**ontinue record keeping. Future players only observe history from last restart

Equivalence: Justifying No-Delay

Proposition

If

$$U(k, a_0, a_1, a_2, \dots) \equiv \bar{v}(k)V(a_0, a_1, a_2, \dots) + \bar{\bar{v}}(k).$$

a state-independent sequential equilibrium which is optimally symmetric from \hat{t} on satisfies no-delay

Intuition: can always pretend that \hat{t} has not happened yet.

Introducing uncertainty: Preference shock



$$\begin{aligned}
 & U(k_t, s_t, s_{t+1}, \dots) \\
 &= \frac{\alpha(1 - \alpha\beta + \delta\alpha\beta)}{1 - \alpha\beta} \log k_t + \log(1 - s_t) + \frac{\alpha\beta\delta_t}{1 - \alpha\beta} \log s_t \\
 &+ \delta_t E \sum_{j=1}^{\infty} \beta^j [\log(1 - s_{t+j}) + \frac{\alpha\beta}{1 - \alpha\beta} \log s_{t+j}]
 \end{aligned}$$

- δ_t i.i.d. (for now)
- To make it recursive, define version with $\delta_t = 1$ and take expected value:

$$\begin{aligned}
 & W(s_t, s_{t+1}, \dots) \\
 &= E \log(1 - s_t) + \frac{\alpha\beta}{1 - \alpha\beta} \log s_t + \beta E W(s_{t+1}, s_{t+2}, \dots)
 \end{aligned}$$

Recursive formulation



$$U(k, s, w'; \delta) = v(k) + V(s, \delta) + \beta \delta w'$$



$$w = E[V(s, 1) + \beta w']$$

Key System

- Walk into period with w , solve for $s(\delta), w'(\delta)$:
- Constant **expected** value **before shock is realized**:

$$\bar{V} = E[V(s, \delta) + \beta \delta w']$$

- Promise-keeping

$$w = E[V(s, 1) + \beta w']$$

- Incentive-compatibility (two shocks):

$$V(s(\delta^H), \delta^H) + \beta \delta^H w'(\delta^H) \geq V(s(\delta^L), \delta^H) + \beta \delta^H w'(\delta^L)$$

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- Efficiency: Choose solution that maximizes $Ev(k')$

Key trade-off

- Easier to induce high δ agent to save more
- Spreading saving apart costly (concavity of v)

Part III: Trade Policy

Setup

- Two countries, home and foreign
- Two tradeable intermediate goods, 1 and 2
- One final good
- Two units of hands-to-mouth households per country, each unit has one unit of labor usable in one of the sectors (labor immobile across sectors and countries)
- A group of capitalists making saving decisions

Technology

- Home country in sector i

$$A_i K_t^{1-\alpha} l_{it}^{1-\alpha} k_{it}^{\alpha}$$

- $A_1 > A_2$
- Foreign: symmetric (A_1 TFP of intermediate 2)
- Final good (can be consumed or invested as capital):

$$y_t = [0.5^{1-\rho} m_{1t}^{\rho} + 0.5^{1-\rho} m_{2t}^{\rho}]^{\frac{\rho-1}{\rho}}$$

Government Policy

- A tariff τ_t on imports
- Study cooperative solution across the two countries

Preferences

- Workers:

$$\sum_{t=0}^{\infty} \beta^t \log c_{it}$$

- Capitalists:

$$\sum_{t=0}^{\infty} \beta^t \frac{c_{it}^{1-\sigma}}{1-\sigma},$$

$$\sigma < 1$$

- Government:

$$U_t \equiv ((1 - \theta) \log c_{1t} + \theta \log c_{2t}) + \beta E_t U_{t+1}$$

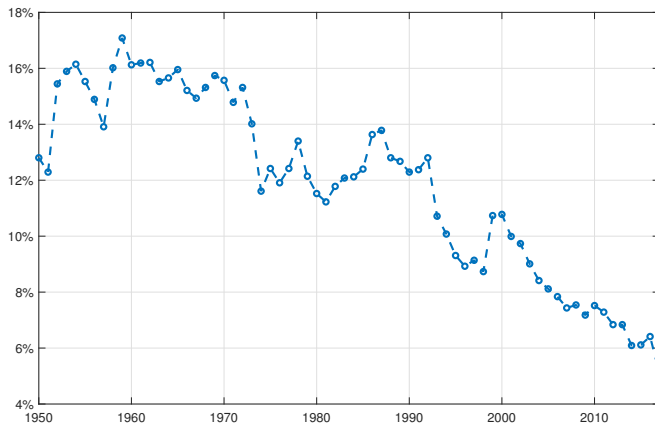
Policy game: details

Competitive equilibrium: details

Time Inconsistency

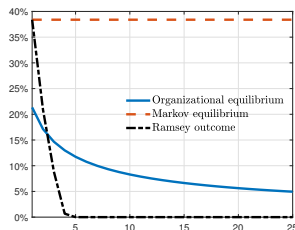
- A tariff protects the wages of sector-2 workers in the home country (and sector-1 workers in the foreign country)
- A tariff discourages saving, hurts everybody in the long run

World Average Tariff

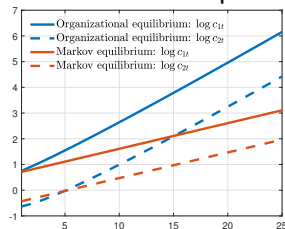


Source: Antras (2020)

Comparing Different Equilibria



Tariff in Various Equilibria



Consumption of Workers in Various Equilibria

Introducing uncertainty (in progress)

- Shock to government preferences:

$$U_t \equiv ((1 - \theta_t) \log c_{1t} + \theta_t \log c_{2t}) + \beta E_t U_{t+1}$$

- Assume i.i.d. for now
- High $\theta_t \implies$ higher tariff
- Gradual return to lower tariffs

Other Applications

- Climate change
- Capital-income taxation

Separable Economies

- Most economies do not satisfy separability condition
- Our strategy: use local approximations
- Linear or second-order approximation
 - satisfies separability
 - choose approximating point so that it's the steady state implied by OE

Conclusion

- New equilibrium concept
- Suitable for positive analysis of gradual policy transition under time inconsistency
- Easy to compute

Organizational Equilibrium in Policy Problems – New Game

- The government in power chooses $a \in A$ first
- Continuum of households choose $s \in S$
- **Aggregate** state: $k' = F(k, a, s)$
- Do not describe individual consequences of deviations

Household Preferences

$$Z(k_t, \{a_j, s_j, s_j^-\}_{j=t}^\infty),$$

- s_j : individual action
- s_j^- : action taken by (almost) all others

Technical Assumptions

- Usual concavity, compactness, continuity etc. etc.
- Weak separability
- Time-consistency of individual preferences

Competitive Equilibrium

A competitive equilibrium from t and state k_t : sequence $\{a_v, s_v\}_{v=t}^{\infty}$, such that

$$Z(k_t, \{a_v, s_v, s_v\}_{v=t}^{\infty}) = \max_{\{\tilde{s}_v\}_{v=t}^{\infty}} Z(k_t, \{a_v, \tilde{s}_v, s_v\}_{v=t}^{\infty}).$$

- Proposition: CE exists given a sequence of policy actions
- Assumption: CE unique given policy actions (can verify in the application)

Government Preferences

$$\Psi^g(k_t, a_t, s_t, a_{t+1}, s_{t+1}, a_{t+2}, s_{t+2}, \dots)$$

- Ψ^g weakly separable in k_t and the rest
- Given a sequence of government actions, get unique CE
- Specify government preferences over sequences of actions as utility of CE associated with actions
- Proceed as before (but may need to check existence and properties case by case)

Back to tariffs

Static Competitive Equilibrium, part 1 (period t , K_t given)

- Fraction of capital allocated to sector 2:

$$\phi_t := \left(1 + \left(\frac{A}{1 + \tau_t} \right)^{\frac{1}{1-\alpha}} \right)^{-1}, \quad \frac{\partial \phi}{\partial \tau_t} > 0$$

- Relative price of intermediates (equilibria with trade):

$$p_{1t}/p_{2t} \equiv p_{1t} = 1/(1 + \tau_t)$$

- Price index:

$$\mathcal{P}_t = \left[0.5 p_{1t}^{\frac{\rho}{\rho-1}} + 0.5 \right]^{\frac{\rho-1}{\rho}}$$

Static Competitive Equilibrium, part 2

- Real wage in the export-led sector:

$$w_{1t} = (1 - \alpha)(1 + \tau_t)^{-1} A(1 - \phi_t)^\alpha K_t / \mathcal{P}_t, \quad \frac{\partial w_{1t}}{\partial \tau_t} < 0$$

- Wage in the import-competing sector:

$$w_{2t} = (1 - \alpha)\phi_t^\alpha K_t / \mathcal{P}_t, \quad \frac{\partial w_{2t}}{\partial \tau_t} > 0$$

- Rental rate of capital:

$$r_t = \alpha \phi_t^{\alpha-1} / \mathcal{P}_t, \quad \frac{\partial r_t}{\partial \tau_t} < 0$$

Within-Period Welfare

- Workers:

$$\log c_{it} = \chi_i(\tau_t) \log K_t$$

- Government:

$$\chi(\tau_t) := [\lambda \chi_1(\tau_t) + (1 - \lambda) \chi_2(\tau_t)] \log K_t$$

[Back to pictures](#)