

Corporate default prediction

Statistics for Data science - AEM University of Brescia

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Research questions

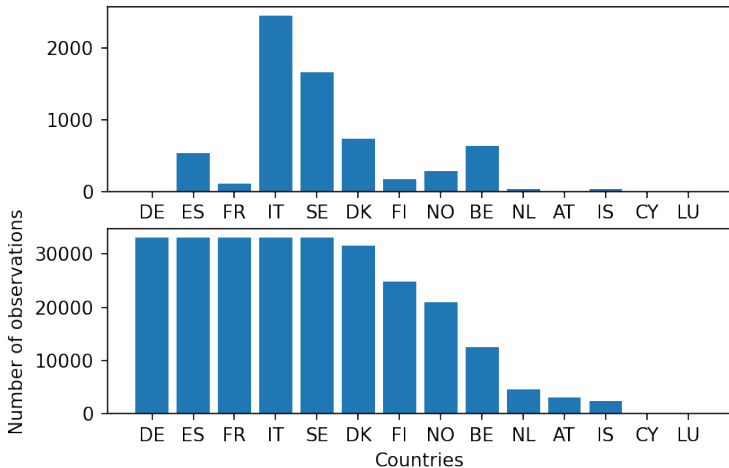
- What are the consequences of applying different resampling methods?
Is the more complex the better?
- What's the most efficient way to make a model of a corporate probability of default?

Overview of data: Basic information

- Data is sourced from Orbis - Private company database
- Geographical location of companies are developed countries in Europe
- in period 2018-2020
- observations were filtered with following criteria:
 - Active, bankrupt or dissolved at time t
 - With known value of some financial ratios at time $t - 1$
 - Standardised legal form: Private and public limited company
 - Entity type: corporate
 - Higher than 5 number of employees at time $t - 1$

Overview of data

Number of active (lower plot) and inactive (upper) companies



Data preprocessing

- Variables with more than 25% not available values were dropped
- Categorical variables were one-hot-encoded
- NAs were imputed with the median of a given variable
- Preprocessed dataset was split into training (80%) and testing dataset

For feature engineering, additional 20 new variables were introduced from initial 30, briefly:

- For some financial data like revenue, net profit, a relative change from previous year was introduced
- Most of the original variables were a standard positions from financial statement, thus financial ratios were introduced with some basic arithmetic operations.

Resampling methods

Corporate default data is known to have a huge class imbalance problem.

In order to address the problem and investigate their modeling consequences, I further apply 3 resampling methods to the training dataset:

- Oversampling
- Undersampling
- Synthetic Minority Over-sampling Technique (SMOTE) [N. Chawla, et. al, 2002] + Undersampling

Further modeling workflow is done for datasets resampled with each of the methods above, in order to compare them.

Applied models (1/3): Penalized logistic regression

$$\min_{w,c} \frac{1-\rho}{2} \beta^T \beta + \rho \|\beta\|_1 + C \sum_{i=1}^n \ln e^{-y_i(X_i^T \beta + c)} + 1$$

Where:

- ρ parameter regulating preference for l-2 or l-1 regularization
- C parameters regulating preference to regularization

Both of the parameters above were tuned with a grid search over cross validated results.

Applied models (2/3): XGBoost - Gradient boosted decision trees

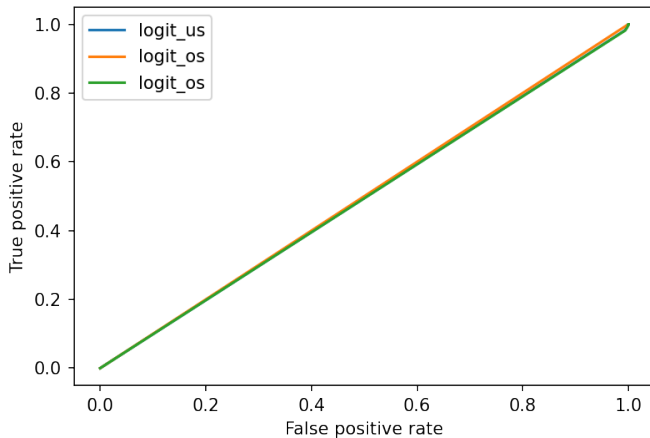
- A workhorse ML model, based on an ensemble of decision trees [T. Chen, C. Guestrin, 2016].
- Trained with a gradient boosting algorithm based on Friedman et al. 2000
- The model is trained in a sequential way, each training round consists of function estimated from previous round and a newly trained one.
- The objective function both tries to minimize log-loss and a regularization term, which penalizes number of leaves and a l-2 norm of leaf score
- all in all, a complex model....
- In herein project, the hyperparameters were tuned with random search.

Applied models (3/3): Multilayer perceptron

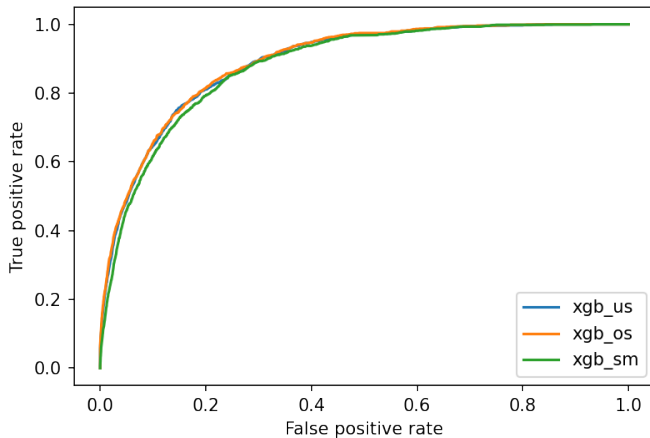
- Basic "vanilla" model of artificial neural networks
- Estimates weights of "neurons" iteratively with backpropagation
- Just like the previous model, can generalize non-linear patterns and has a regularization in a objective function

For this project, the hyperparameters were tuned with a random search.

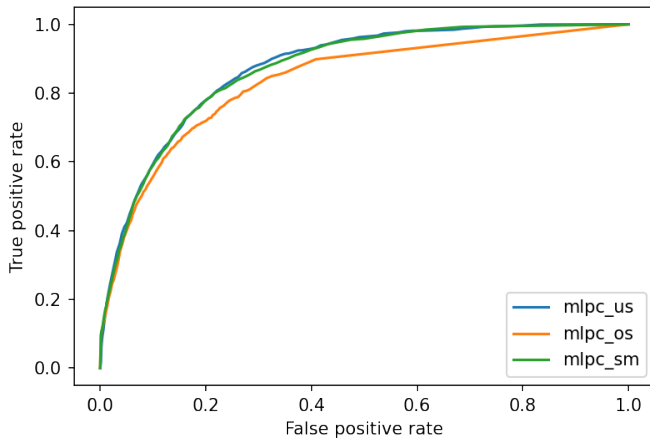
model fitness comparison - ROC



model fitness comparison - ROC

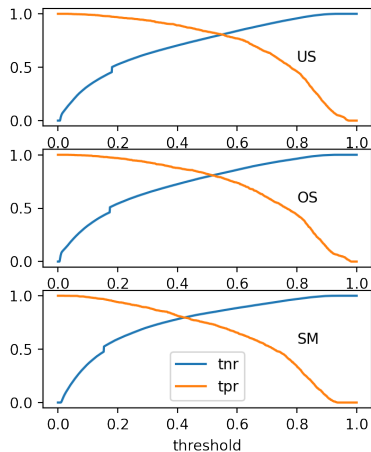


model fitness comparison - ROC

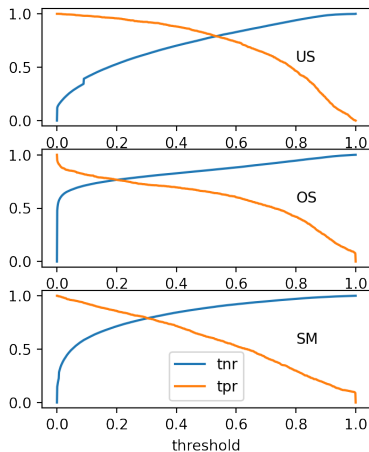


TPR, TNR vs. threshold

XGBoost TNR - TPR plot



MLP Classifier TNR - TPR plot



Metrics with optimal thresholds

- Optimal threshold w.r.t balanced accuracy
- note, it's in-sample optimal (best case scenario)

| | logit_os | logit_us | logit_sm | xgb_us | xgb_os | xgb_sm | mlpc_us | mlpc_os | mlpc_sm |
|---------------------|----------|----------|----------|--------|--------|--------|---------|---------|---------|
| thresholds | 49.9 % | 49.0 % | 48.9 % | 55.4 % | 48.3 % | 36.5 % | 44.3 % | 18.1 % | 28.6 % |
| tpr | 100.0 % | 100.0 % | 100.0 % | 80.5 % | 83.4 % | 85.1 % | 86.0 % | 77.7 % | 80.6 % |
| tnr | 0.1 % | 0.1 % | 0.1 % | 80.9 % | 78.5 % | 75.7 % | 73.1 % | 75.8 % | 77.9 % |
| balanced_acc | 50.0 % | 50.0 % | 50.0 % | 80.7 % | 81.0 % | 80.4 % | 79.6 % | 76.7 % | 79.2 % |

Base case metrics comparison

- Metrics calculated with 50% threshold (base case)

| | logit_os | logit_us | logit_sm | xgb_us | xgb_os | xgb_sm | mlpc_us | mlpc_os | mlpc_sm |
|--------------------------|----------|----------|----------|--------|--------|--------|---------|---------|---------|
| balanced accuracy | 59.0 % | 52.7 % | 56.4 % | 80.3 % | 80.8 % | 79.2 % | 79.3 % | 75.5 % | 75.2 % |
| TPR | 31.4 % | 8.1 % | 21.2 % | 83.3 % | 82.1 % | 74.5 % | 81.6 % | 65.6 % | 61.8 % |
| TNR | 86.6 % | 97.4 % | 91.5 % | 77.3 % | 79.6 % | 83.8 % | 76.9 % | 85.4 % | 88.6 % |
| FPR | 13.4 % | 2.6 % | 8.5 % | 22.7 % | 20.4 % | 16.2 % | 23.1 % | 14.6 % | 11.4 % |
| FNR | 68.6 % | 91.9 % | 78.8 % | 16.7 % | 17.9 % | 25.5 % | 18.4 % | 34.4 % | 38.2 % |

References

- N. V. Chawla, et. al, SMOTE: Synthetic Minority Over-sampling Technique, Journal of Artificial Intelligence Research 16, 2002
- T. Chen, C. Guestrin, XGBoost: A Scalable Tree Boosting System, 2016
- J. Friedman, T. Hastie, and R. Tibshirani. Additive logistic regression: a statistical view of boosting. Annals of Statistics