

Systemic Risk and Financial Connectedness: Empirical Evidence

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Theoretical background

- "Robust-yet-fragile" property of financial system can serve at the same time as shock-absorbers and shock-amplifiers to the financial sector (Haldane 2009).
- This makes the system robust, when the magnitude of shock is relatively small, but fragile, when the shock is large.
- A seminal paper by Acemoglu, Ozdaglar, and Tahbaz-Salehi 2015a, provides a formal model, in which an extent of financial contagion exhibits a form of regime transition.
 - When the shocks are small, the damages are dissipated through large number of financial institutions.
 - When the shock is above some threshold, the properties of the system changes markedly. The damages are amplified through the network.

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- The aim is to provide (and quantify) empirical evidence for the regime-dependent effect of connectedness on financial stability, i.e.:
 - Stable markets regime: Higher connectedness \rightarrow less volatility
 - High shock regime: Higher connectedness \rightarrow more volatility
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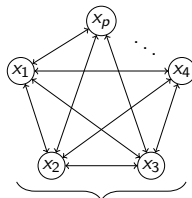
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(Financial) network estimation from time series

$$\underbrace{\begin{pmatrix} x_{11} & x_{12} & \dots & x_{1n} \\ x_{21} & x_{22} & \dots & x_{2n} \\ x_{31} & x_{32} & \dots & x_{3n} \\ \vdots & \vdots & \ddots & \vdots \\ x_{T1} & x_{T2} & \dots & x_{Tn} \end{pmatrix}}_{\text{Time series matrix } \mathbf{X} \text{ of size } T \times n.} \xrightarrow{f: \mathbb{R}^{T \times n} \rightarrow \mathbb{R}^{n \times n}} \underbrace{\begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \dots & a_{nn} \end{pmatrix}}_{\text{Adjacency matrix } \mathbf{A} \times n.}$$

||



Graph representation of matrix \mathbf{A} .

Connectedness measures - denoted γ_t

- 1 Average correlation: $\frac{\sum_{i \neq j}^N \sum_{j \neq i}^N \rho_{i,j}(R)}{N^2 - N}$, with $\rho(\cdot)$ being the Ledoit-Wolf estimator of the covariance matrix (Ledoit and Wolf 2003).
- 2 $\frac{\sum_i^k \lambda_i}{\sum_i^N \lambda_i}$, with λ being an eigenvalue of the covariance matrix.
- 3 (Granger 1969) - based measure of connectedness:
 - For each of stock pair estimate:
$$r_{i,t+1} = \beta_0 + \beta_1 r_{m,t} + \beta_2 r_{j,t} + \sum_k^5 \beta_{c+2k} x_{c,t} + \epsilon_t$$
 - The "causality" matrix is set as: $G_{i,j} = \begin{cases} 1 & \text{if } \beta_2 \text{ is significant} \\ 0 & \text{otherwise} \end{cases} \quad \forall i \neq j$
 - As with before we calculate average connectedness: $\frac{\sum_{i \neq j}^N \sum_{j \neq i}^N G_{i,j}}{N \times (N-1)}$
 - Last two measures are as described in Billio et al. 2012

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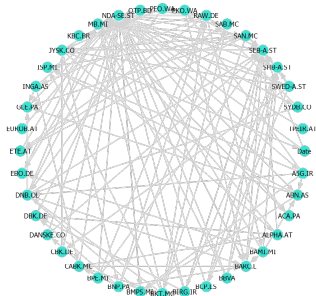
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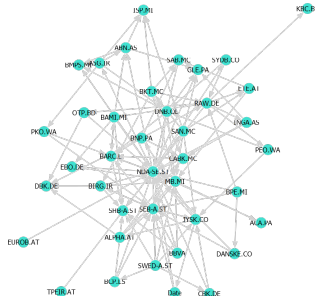
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Example of estimated network



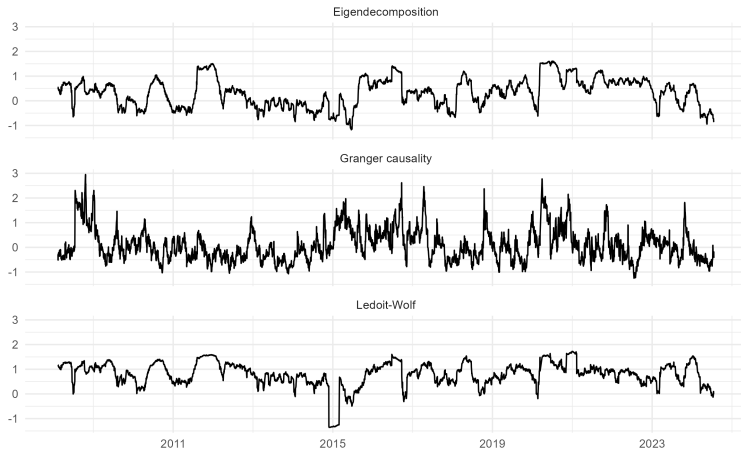
(a) Circle representation of graph



(b) Representation of graph with random position

Connectedness measures results

Figure: Standardized time series of connectedness measures for US market and a rolling window of 63 trading days (quarter)



Modeling the regime-dependent effect of connectedness

Mean specification of the model:

$$r_{b,t} = \beta_0 + \underbrace{\sum_{i=1}^k \beta_i r_{b,t-i}}_{\text{Banking index}} + \underbrace{\sum_{j=0}^p \beta_{k+j} r_{m,t-j}}_{\text{Broad market index}} + \epsilon_t$$

The Markov-switching ARCH specification is:

$$\sqrt{\epsilon_t^2} = \alpha_{0,S_t} + \underbrace{\alpha_{1,S_t} \gamma_{t-1}}_{\text{connectedness}} + \underbrace{\sum_{i=1}^p \alpha_{i+1} \sqrt{\epsilon_{t-i}^2}}_{\text{lag controls}} + \vartheta_t$$

$$\vartheta \sim \mathcal{N}(0, \eta)$$

With regime changes according to Markov process:

$$P(S_t = i | S_{t-1} = j) = \begin{bmatrix} \pi_1 & 1 - \pi_2 \\ 1 - \pi_1 & \pi_2 \end{bmatrix}$$

Estimation results

US banking sector and 252 trading days (year) rolling window

Connectedness measure		Regime 1		Regime 2	
		Estimate	S.E.	Estimate	S.E.
Ledoit-Wolf	α_0	0.37*	0.013	1.342*	0.037
	α_1	0.014	0.006	0.226*	0.026
	η	0.319	0.007	0.888	0.009
	$\pi_{i,i}$	80.64%		57.8%	
Eigenvalue-based	α_0	0.378*	0.014	1.337*	0.037
	α_1	0.025	0.007	0.222*	0.028
	η	0.319	0.007	0.89	0.01
	$\pi_{i,i}$	80.3%		57%	
Granger-based	α_0	0.375*	0.013	1.352*	0.036
	α_1	0.019	0.007	0.197*	0.024
	η	0.316	0.007	0.889	0.009
	$\pi_{i,i}$	80.7%		58.84%	
* coefficient with 5% statistical significance					

EU banking sector and 63 trading days (year) rolling window

Connectedness measure		Regime 1		Regime 2	
		Estimate	S.E.	Estimate	S.E.
Ledoit-Wolf	α_0	0.441*	0.019	1.82*	0.05
	α_1	0.019*	0.01	0.302*	0.036
	η	0.401	0.009	1.209	0.011
	$\pi_{i,i}$	73.4%		48.16%	
Eigenvalue-based	α_0	0.434*	0.017	1.829*	0.048
	α_1	-0.013*	0.008	0.303*	0.043
	η	0.49	0.008	1.22	0.11
	$\pi_{i,i}$	74.8%		60.8%	
Granger-based	α_0	0.445*	0.018	1.824*	0.05
	α_1	0.018	0.001	0.276*	0.033
	η	0.401	0.009	1.215	0.011
	$\pi_{i,i}$	74.56%		50.76%	
* coefficient with 5% statistical significance					

- Are there confounders in the bank specific characteristics?
- To check this I use quarterly financial statement data:
 - Data is sourced from Orbis database.
 - Substantial reduction of used data due to lower frequency of reports and their availability.
 - N banks: $51 \rightarrow 30$. T observations $6240 \rightarrow 260$.
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Robustness check - results

Results for EU banks with a rolling window of 52 weeks

Granger-based		Regime 1		Regime 2	
		Estimate	S.E.	Estimate	S.E.
Correlation-based	α_0	1.524*	0.19*	5.031*	0.53
	α_1	0.129	0.093	1.175*	0.434
	η	1.013	0.045	2.872	0.086
	$\pi_{i,i}$	80.36%		51.8%	
* coefficient with 5% statistical significance					

Concluding remarks

- The theory is confirmed to some degree - the connectedness effect is indeed regime dependent.
- The effect is asymmetric - the connectedness is more important in the high shock regime. Consistent with *financial network externality* (Acemoglu, Ozdaglar, and Tahbaz-Salehi 2015b)

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Thank you!

- Contact: m.dadej@unibs.it
- Working paper and replication code may be found at my github:
github.com/m-dadej/robust_fragile

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