

## FA $\Leftrightarrow$ RG $\Leftrightarrow$ RE

### I) FA $\Leftrightarrow$ RG

1. Given the regular grammar  $G = (\{S, A\}, \{a, b\}, P, S)$

$$P : S \rightarrow \varepsilon \mid aA$$

$$A \rightarrow aA \mid bA \mid a \mid b,$$

build the equivalent FA.

Sol.:

$$M = (Q, \Sigma, \delta, q_0, F)$$

$$Q = \{S, A, K\}$$

$$\Sigma = \{a, b\}$$

$$q_0 = S$$

$$F = \{K, S\}$$

$$\delta(S, a) = \{A\}$$

$$\delta(A, a) = \{A, K\}$$

$$\delta(A, b) = \{A, K\}$$

2. Given the following FA  $M = (Q, \Sigma, \delta, q_0, F)$

$$Q = \{p, q, r\}, q_0 = p, F = \{p, r\}, \Sigma = \{0, 1\}$$

$\delta$	0	1
$p$	$q$	$p$
$q$	$r$	$p$
$r$	$r$	$r$

build the equivalent right linear grammar.

Sol.:

$$G = (N, \Sigma, P, S)$$

$$N = \{p, q, r\}$$

$$\Sigma = \{0, 1\}$$

$$S = p$$

$$P : p \rightarrow 0q \mid 1p \mid 1 \mid \varepsilon$$

$$q \rightarrow 0r \mid 0 \mid 1p \mid 1$$

$$r \rightarrow 0r \mid 0 \mid 1r \mid 1$$

## II) RG $\Leftrightarrow$ RE

3. Give the RG corresponding to the following RE  $0(0+1)^*1$ .

$$0: G_1 = (\{S_1\}, \{0, 1\}, \{S_1 \rightarrow 0\}, S_1)$$

$$1: G_2 = (\{S_2\}, \{0, 1\}, \{S_2 \rightarrow 1\}, S_2)$$

$$0+1 \quad G_3 = (\{S_1, S_2, S_3\}, \{0, 1\}, \{S_1 \rightarrow 0, S_2 \rightarrow 1, S_3 \rightarrow 0 \mid 1\}, S_3)$$

$$G'_3 = (\{S_3\}, \{0, 1\}, \{S_3 \rightarrow 0 \mid 1\}, S_3)$$

$$(0+1)^* \quad G_4 = (\{S_3\}, \{0, 1\}, \{S_3 \rightarrow 0 \mid 1 \mid \epsilon \mid 0S_3 \mid 1S_3\}, S_3)$$

$$G'_4 = (\{S_3\}, \{0, 1\}, \{S_3 \rightarrow 0S_3 \mid 1S_3 \mid \epsilon\}, S_3) \quad \text{! not regular}$$

$$0(0+1)^* \quad G_5 = (\{S_1, S_3\}, \{0, 1\}, \{S_3 \rightarrow 0S_3 \mid 1S_3 \mid \epsilon, S_1 \rightarrow 0S_3\}, S_1) \quad \text{! not regular}$$

$$0(0+1)^*1 \quad G_6 = (\{S_1, S_2, S_3\}, \{0, 1\}, \{S_2 \rightarrow 1, S_1 \rightarrow 0S_3, S_3 \rightarrow 0S_3 \mid 1S_3, S_3 \rightarrow S_2\}, S_1)$$

$G_6$  not regular

$$\text{Sol.: } G'_6 = (\{S_1, S_3\}, \{0, 1\}, \{S_1 \rightarrow 0S_3, S_3 \rightarrow 0S_3 \mid 1S_3 \mid 1\}, S_1)$$

4. Give the RE corresponding to the following grammar

$$G = (\{S, A, B\}, \{a, b\}, P, S)$$

$$P: S \rightarrow aA$$

$$A \rightarrow aA \mid bB \mid b$$

$$B \rightarrow bB \mid b$$

Sol.: **///???**

$$S = aA$$

$$A = aA + bB + b$$

$$B = bB + b$$

We know that rule 1

$$X = aX + b$$

$$X = a^*b$$

$$B = b^*b \text{ by rule 1}$$

$$B = b^+$$

$$A = aA + B$$

$$A = aA + b^+$$

$$A = a^*b^+ \text{ by rule 1}$$

$$S = aa^*b^+ = a^+ b^+$$

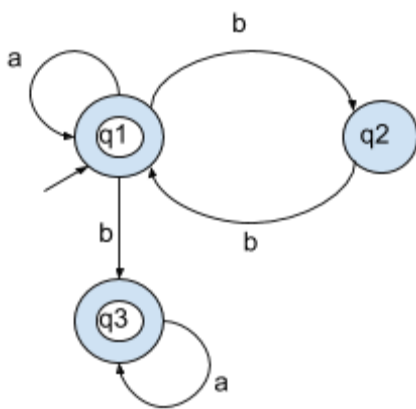
$$\Rightarrow S = a^+b^+$$

### III) FA $\Leftrightarrow$ RE

5. Give the FA corresponding to the following RE  $01(1+0)^*1^*$ .

**Sol:** on pdf board attached to MSTEams Seminar7 meet

6. Give the regular expression corresponding to the FA below.



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$$q1 = \text{epsilon} + q1 a + q2 b$$

$$q2 = q1 b$$

$$q3 = q1 b + q3 a$$

$$X = Xa + b \Rightarrow \text{sol: } X = ba^*$$

$$q_3 = q_1 b a^*$$

$$q_1 = \epsilon + q_1 a + q_1 b b = \epsilon + q_1 (a + b b) \Rightarrow q_1 = (a + b b)^*$$

$$\text{Regular expression: } q_1 + q_3 = (a + b b)^* + (a + b b)^* b a^* = (a + b b)^* (\epsilon + b a^*)$$