# DSA - Seminar 6

# 1. Map - reprezentation on a hash table - collision resolution with coalesced chaining

- Assume:
  - We memorize only the keys
  - o The keys are integer numbers

## For ex:

- 5, 18, 16, 15, 13, 31, 26
- HT:
  - o m = 13
  - Hash function defined with the division method

Ī	K	5	18	16	15	13	31	26
	h(k)	5	5	3	2	0	5	0

	0	1	2	3	4	5	6	7	8	9	10	11	12
t	18	13	15	16	31	5	26						
next	<del>-1</del> 1	<del>-1</del> 4	-1	-1	<del>-1</del> 6	<del>-1</del> 0	-1	-1	-1	-1	-1	-1	-1

firstFree = 0.1467

- firstFree is considered to be the first empty position from left to right (empty positions are no longer linked)
- One "linked list" can contain elements belonging to different collisions: for ex. the list starting at position 5: 5(5) 18(5) 13(0) 31(5) 26(0)

# Reprezentation:

Map:

m: Integer t: TKey[] next:Integer[] firstFree: Integer h: TFunction

```
subalgorithm init (map):
      @ initialize the hash function
       @ initialize the value of m
      for i \leftarrow 0, m-1 execute
             map.t[i] \leftarrow -1
             map.next[i] \leftarrow -1
      end-for
      map.firstFree \leftarrow 0
end-subalgorithm
Complexity: \Theta(m)
Function search(map, k):
// for simplicity we return the position where the key was found, or -1
// in case of a real map, you return the value associated to the key
       i \leftarrow map.h(k)
      while (i \neq -1 and map.t[i] \neq k) execute
             i ← map.next[i]
      end-while
      if i = -1 then
             search \leftarrow -1
             search ← i
end-function
Complexity: \Theta (m) in worst case, but on average \Theta(1)
subalgorithm insert (map, k) is:
//for simplicity we just add the key (we do not check if it exists already)
       i \leftarrow map.h(k)
      if map.t[i] = -1 then
             map.t[i] \leftarrow k
             map.next[i] \leftarrow -1
      else
             if map.firstFree = map.m then
                    @resize and rehash
             end-if
             current ← i
             while map.next[current] ≠ -1 execute
                    current \( \text{map.next[current]} \)
             end-while
             map.t[map.firstFree] ← k
             map.next[map.firstFree] \leftarrow -1
             map.next[current] \( \text{map.firstFree} \)
             changeFirstFree(map)
       end-if
end-subalgorithm
Complexity: \Theta (m) in worst case, but on average \Theta(1)
subalgorithm changeFirstFree(map) is:
      map.firstFree ← map.firstFree + 1
      while map.firstFree < map.m and map.t[map.firstFree] ≠-1 execute</pre>
             map.firstFree \( \) map.firstFree + 1
      end-while
end-subalgorithm
Complexity: O(m)
```

#### Remove: remove key 5

- **Problem:** we might lose links to other elements
- Cannot just do a remove like in case of a linked list on array, because not every element can be at any position in the table. No element can be "before" (considering the links) the position to which it hashes. For example, we cannot move 26 to replace 5 (because 26 hashes to 0, and a search starting from position 0 does not go through position 5).

	0	1	2	3	4	5	6	7	8	9	10	11	12
T	<del>18</del> 13	13	15	16	31	<del>5</del> 18	26						
Nex	t <del>1</del> 4	41	-1	-1	6	0	-1	-1	-1	-1	-1	-1	-1

firstFree: 7

### Steps:

- 1. We cannot just set t[5] = -1 and next[5] = -1 because we lose the link to 18 (and a search for 18 or 31 will not find these elements)
- 2. Search for elements (following the links) that hash to the position from which I am removing an elements (position 5 in our example)
  - a. If no element is found, we remove the element as we remove an element from a singly linked list on array.
  - b. If an element is found, it is moved to the position where we delete from, and the process of removal is repeated with the position from which we moved the element.
- Remove key 5, which is at position 5
- Search for the first key that hashes to position 5 => 18
- Move 18 to position 5
- Now we want to remove key 18, which is at position 0
- Search for the first key that hashes to position 0 => 13
- Move 13 on position 0
- Now we want to remove key 13, which is at position 1
- Search for the first key that hashes to position 1 => no such key
- Remove key 13, modifying the links

```
subalgorithm remove(map, k) is
    i \leftarrow map.h(k)
    j \leftarrow -1 {previous of i, when we want to remove node from pos i, we need
its previous node}
    {parse the table to check if i has any previous element}
    idx \leftarrow 0
    while (idx < map.m and j = -1) execute
         if map.next[idx] = i then
             j \leftarrow idx
         else
             idx \leftarrow idx + 1
         end-if
    end-while
    {find the key to be removed. Set its previous as well}
    while i \neq -1 and map.t[i] \neq k execute
         j ← i
```

```
i ← map.next[i]
    end-while
    if i = -1 then
         @key does not exist
         {find another key that hashes to i}
         over ← false {becomes true when nothing hashes to i}
         repeat
             p ← map.next[i] {first position to be checked}
             pp \leftarrow i \{previous of p\}
             while p \neq -1 and map.h(map.t[p]) \neq i execute
                  pp ← p
                 p \leftarrow map.next[p]
             end-while
             if p = -1 then
                  over ← true
             else
                 map.t[i] \leftarrow map.t[p]
                  j ← pp
                  i ← p
             end-if
         until over
         {remove key from position i}
         if j \neq -1 then
             map.next[j] \( \text{map.next[i]} \)
         end-if
         map.t[i] \leftarrow -1
         map.next[i] \leftarrow -1
         if map.firstFree > i then
             map.firstFree ← i
         end-if
    end-if
end-subalgorithm
```