

Databases

Lecture 9

Indexes. Trees

Indexes

Indexes

- problems
 - what does a data entry contain?
 - how are the entries of an index organized?

Indexes - Data Entries

- let k^* be a data entry in an index; the data entry:
 - alternative 1
 - is an actual data record with search key value = k
 - alternative 2
 - is a pair $\langle k, \text{rid} \rangle$ (rid – id of a data record with search key value = k)
 - alternative 3
 - is a pair $\langle k, \text{rid_list} \rangle$ (rid_list – list of ids of data records with search key value = k)

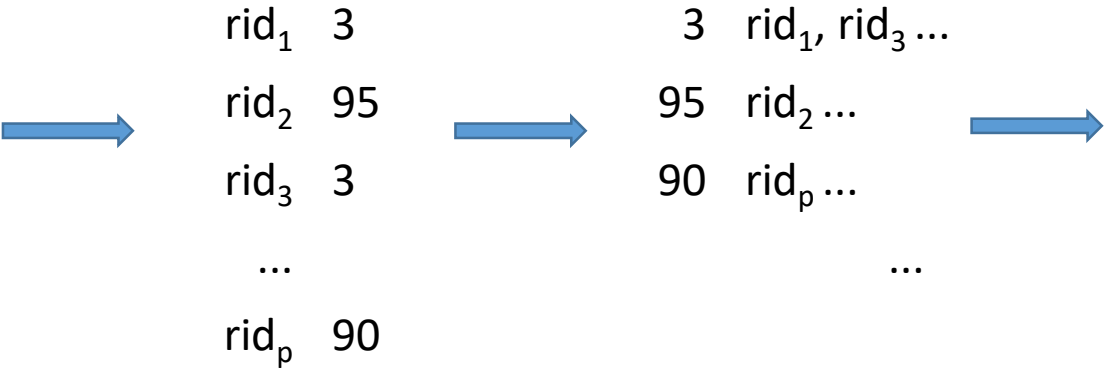
Indexes - Data Entries

- a1
 - the file of data records needn't be stored in addition to the index
 - the index is seen as a special file organization
 - at most 1 index / collection of records should use alternative a1 (to avoid redundancy)
- a2, a3
 - data entries point to corresponding data records
 - in general, the size of an entry is much smaller than the size of a data record
 - a3 is more compact than a2, but can contain variable-length records
 - can be used by several indexes on a collection of records
 - independent of the file organization

Creating an index - example

	Name	Score	Age
rid ₁	Popescu	3	44
rid ₂	Ionescu	95	80
rid ₃	Vladescu	3	45
...		...	
rid _p	Xulescu	90	14

search key



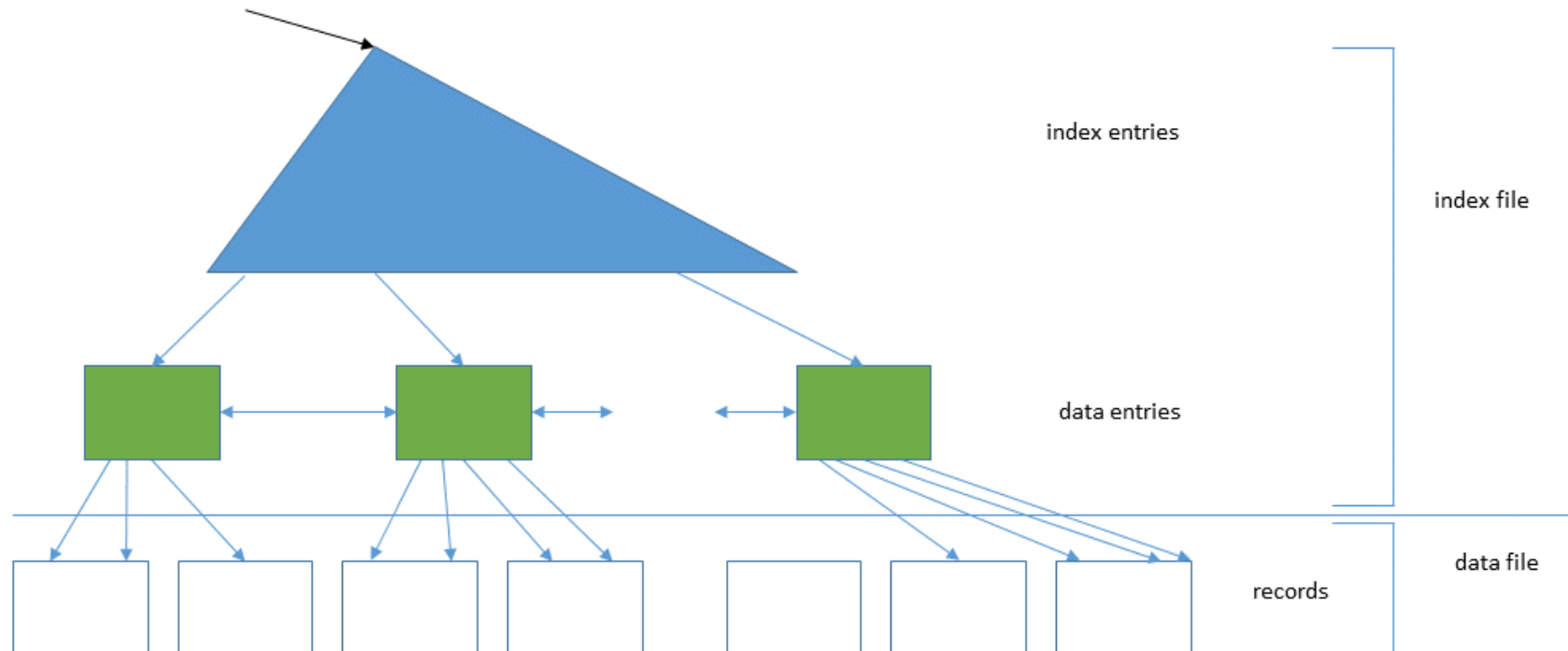
data entry

...	
3	rid ₁ , rid ₃ ...
90	rid _p ...
95	rid ₂ ...
...	

index file

Indexes - Properties

- clustered vs. unclustered
 - clustered index
 - the order of the data records is close to / the same as the order of the data entries
 - index entries guide the search for data entries

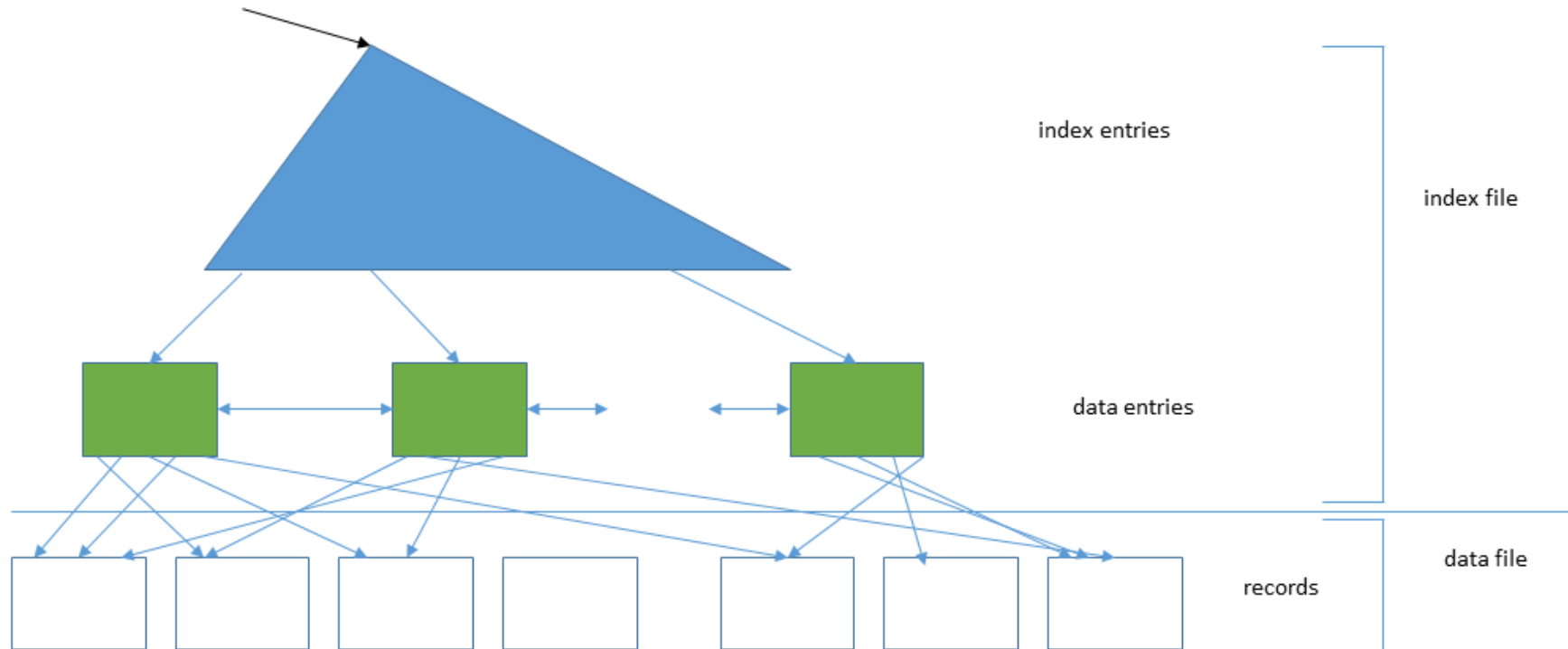


Indexes - Properties

- clustered vs. unclustered
 - $a_1 \rightarrow$ clustered index
 - indexes using a_2 / a_3 are clustered only if the data records are ordered on the search key
 - at most 1 clustered index / data file
 - maintaining a clustered index
 - costly operation

Indexes - Properties

- clustered vs. unclustered
 - unclustered index
 - index that is not clustered



Indexes - Properties

- clustered vs. unclustered
 - unclustered index
 - several unclustered indexes could be built on a file
- range search query
 - unclustered index usage cost
 - each data entry that meets the condition in a query could contain a rid pointing to a distinct page
 - => the number of I/O operations could be equal to the number of data entries that satisfy the query's condition

Indexes - Properties

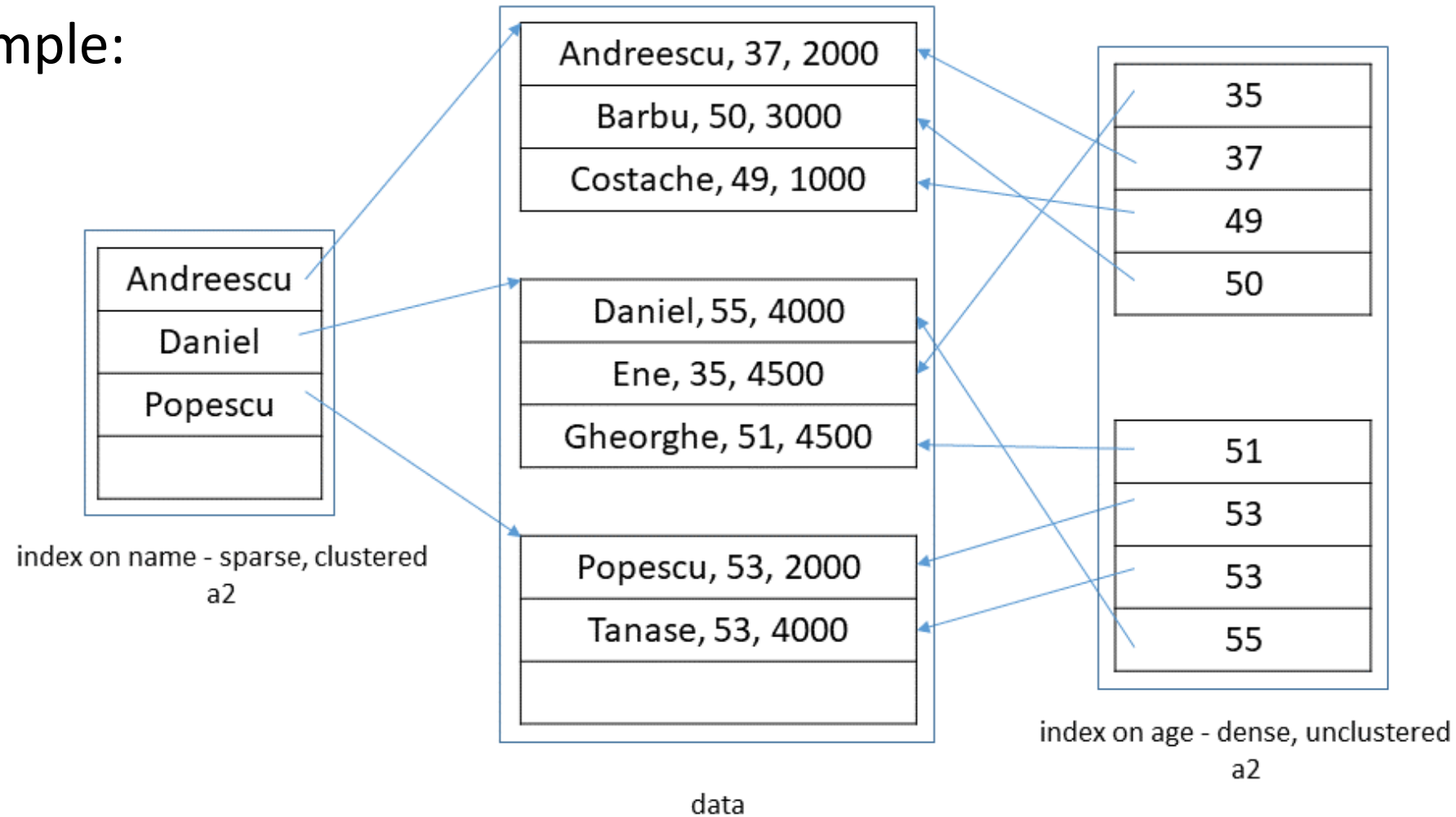
- primary and secondary
 - primary index
 - the search key includes the primary key
 - secondary index
 - index that is not primary
- unique index
 - the search key contains a candidate key
- duplicates
 - data entries with the same search key value
- primary indexes, unique indexes cannot contain duplicates
- secondary indexes can contain duplicates

Indexes - Properties

- sparse vs. dense
- dense index
 - at least one data entry for every search key value that appears in a data record
 - in the presence of duplicates and a2, multiple data entries can have the same search key value
- sparse index
 - one entry for each data page
 - more compact
- a1 => dense index
- sparse index => clustered

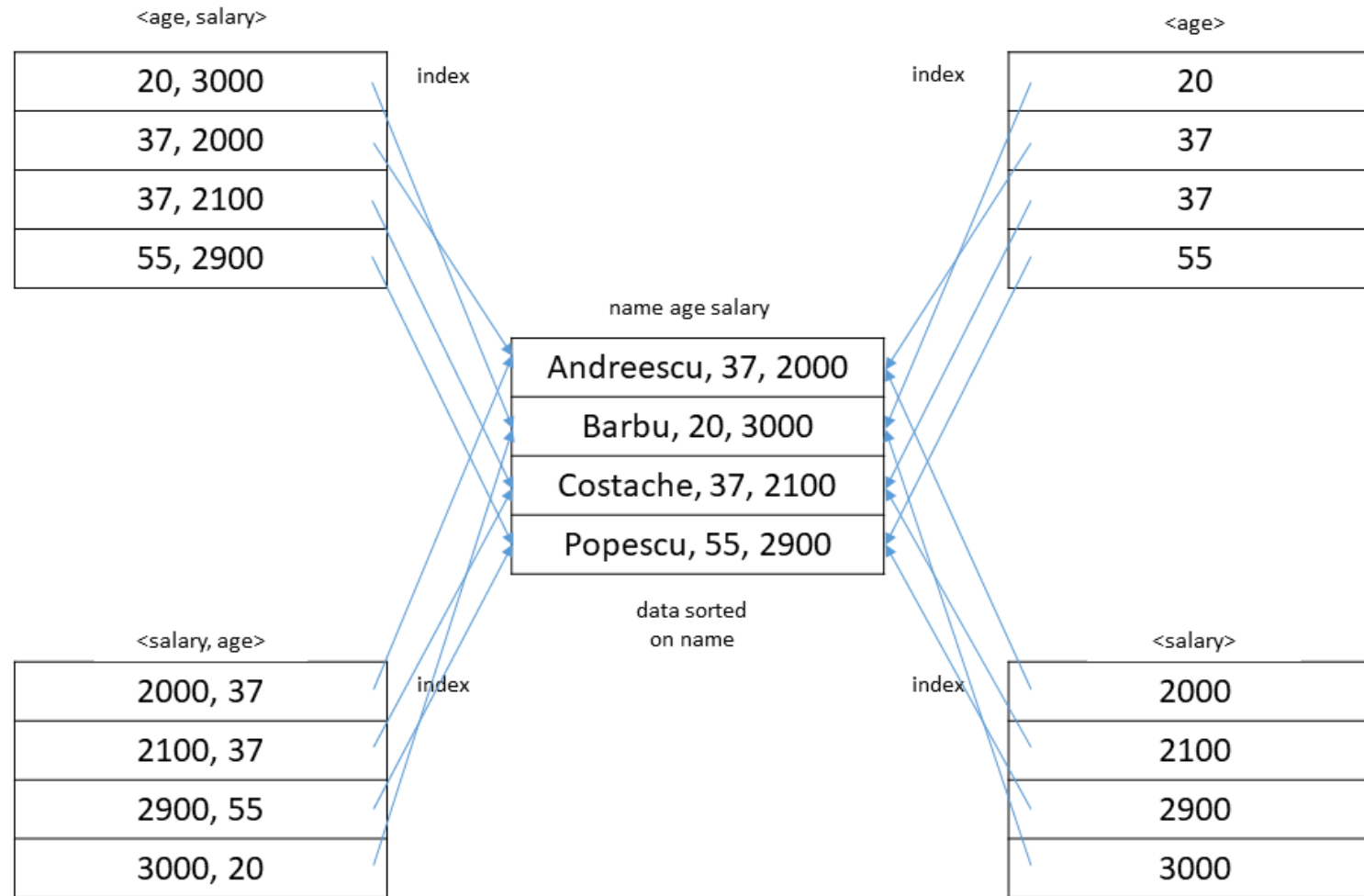
Indexes - Properties

- sparse vs. dense
- example:



Indexes - Properties

- composite (concatenated) search key - search key that contains several fields
 - example:



* example

- the *Professors* relation sorted by age
- a page stores at most 3 records: the 1st tuple is in page 1 slot 1, the second - in page 1 slot 2, etc

prof_id	name	mail	age	impact_factor
4563	Popescu	pu@cs.edu	20	2.5
4570	Antonescu	au@cs.edu	25	3
4500	Ionescu	iu@by.edu	30	3.5
4555	Tanasescu	tu@cs.edu	65	3.1
4450	Tanasescu	tu@mc.edu	65	4

- dense index on *age* with a1 – the entire file
- dense index on *age* with a2 – data entries (20, <1, 1>), (25, <1, 2>), (30, <1, 3>), (65, <2, 1>), (65, <2, 2>)*

*recall that a record can be identified by <page id, slot number>

* example

prof_id	name	mail	age	impact_factor
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4555	Tanasescu	tu@cs.edu	65	3.1
4450	Tanasescu	tu@mc.edu	65	4

- dense index on *age* with a3 – entries (20, <1, 1>), (25, <1, 2>), (30, <1, 3>), (65, <2, 1>, <2, 2>)
- sparse index on *age* with a1 – cannot be built (by definition)
- sparse index on *age* with a2 – (20, <1, 1>), (65, <2, 1>)
- sparse index on *age* with a3 – (20, <1, 1>), (65, <2, 1>, <2, 2>)

* example

prof_id	name	mail	age	impact_factor
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- dense index on *impact_factor* with a2 – (2.5, <1, 1>), (3, <1, 2>), (3.1, <2, 1>), (3.5, <1, 3>), (4, <2, 2>)
- dense index on *impact_factor* with a3 – (2.5, <1, 1>), (3, <1, 2>), (3.1, <2, 1>), (3.5, <1, 3>), (4, <2, 2>)
- sparse index on *impact_factor* with a1 – cannot be built (by definition)
- sparse index on *impact_factor* with a2 or a3 – the values in the search key are not ordered

Data Collection Stored in a Binary Tree

- binary search algorithm on ordered collections
 - very fast; reduced search time (+)
 - maintaining the records' sort order - costly (especially for dynamic collections with many INSERT, UPDATE, DELETE operations) (-)
- solution
 - store the collection using a *binary tree*
 - record - stored in a node
 - node with key value v
 - left subtree
 - records with key values $< v$
 - right subtree
 - records with key values $> v$

- memory structure for a binary tree node
 - record's values stored in K, INF

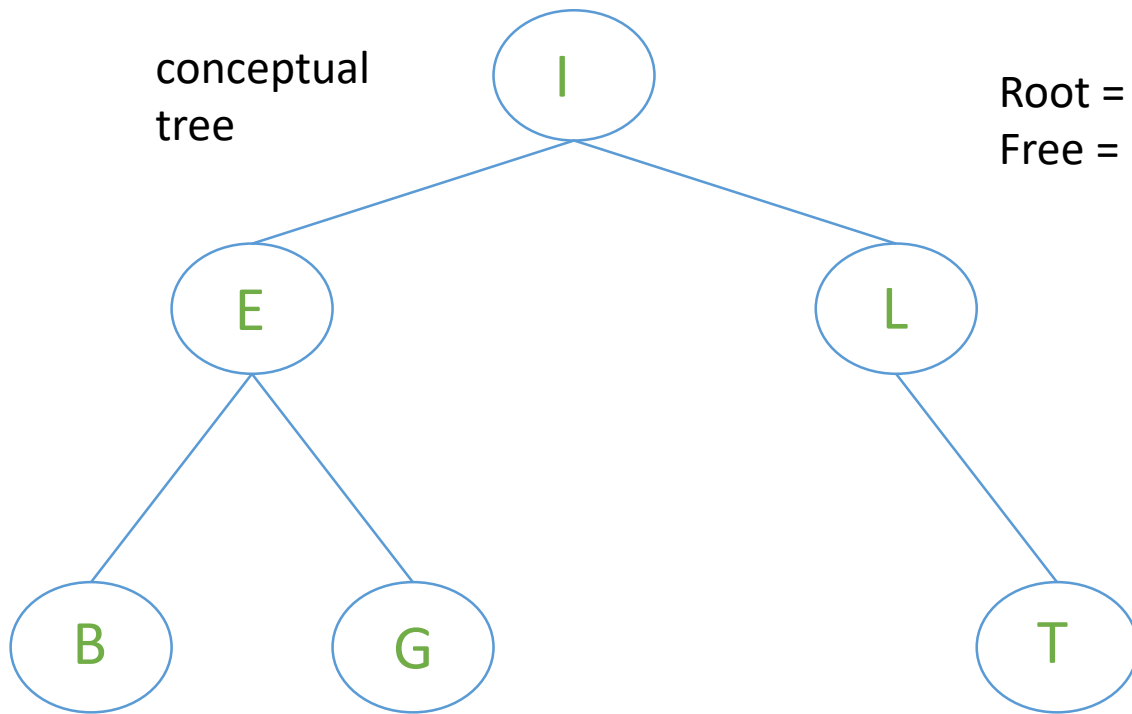
r



- memory structure for a binary tree file
 - collection of nodes
 - pointer to the root
 - list of empty nodes
 - linked by PointerL

* Example

- Root - pointer to the root
- Free - pointer to the head of the empty nodes list



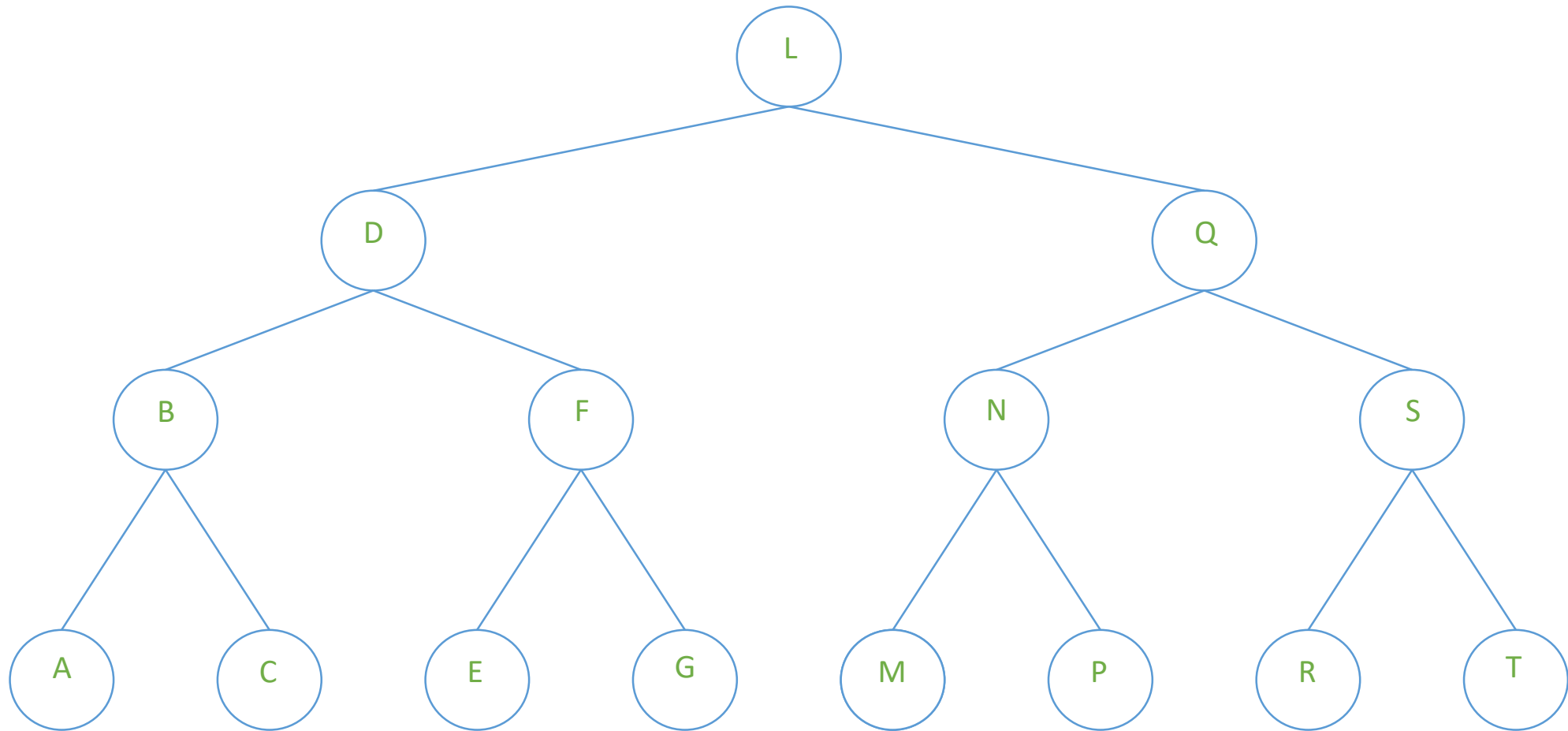
Root = 1
Free = 3

1	2	4	I	INF _I
2	8	7	E	INF _E
3	-6	NULL		
4	NULL	5	L	INF _L
5	NULL	NULL	T	INF _T
6	-9	NULL		
7	NULL	NULL	G	INF _G
8	NULL	NULL	B	INF _B
9	NULL	NULL		

- operations in a binary tree (BT)
 - searching for a record with key value K_0
 - inserting a record
 - removing a record
 - traversal - partial (between 2 values) / total

* Example - binary tree (only key values are shown)

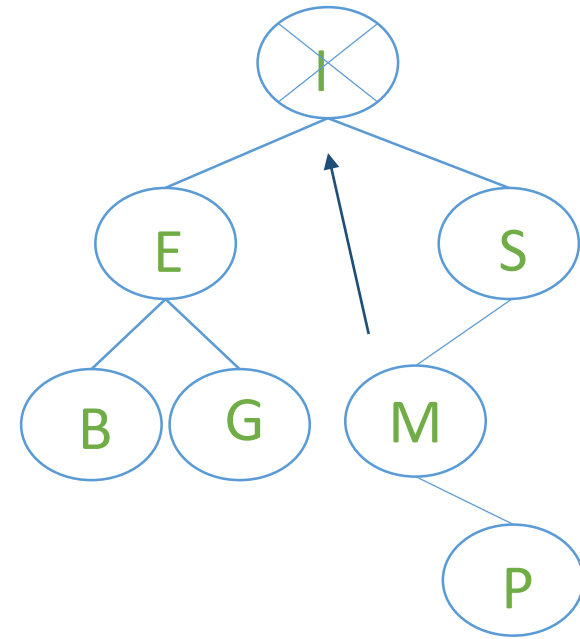
- key values: {L, D, B, Q, N, F, S, R, T, M, E, G, P, A, C}



- searching for a record
 - search starts at the root, follows PointerL / PointerR - based on a comparison result, a subtree is not considered anymore
 - how many comparisons to find record with key value M in the previous tree?
 - analysis, e.g.:
 - collection of English texts; tuples: (L, 50k), (D, 100k), etc
 - analyzing the most common letters in English; how many times does a letter appear in the collection?

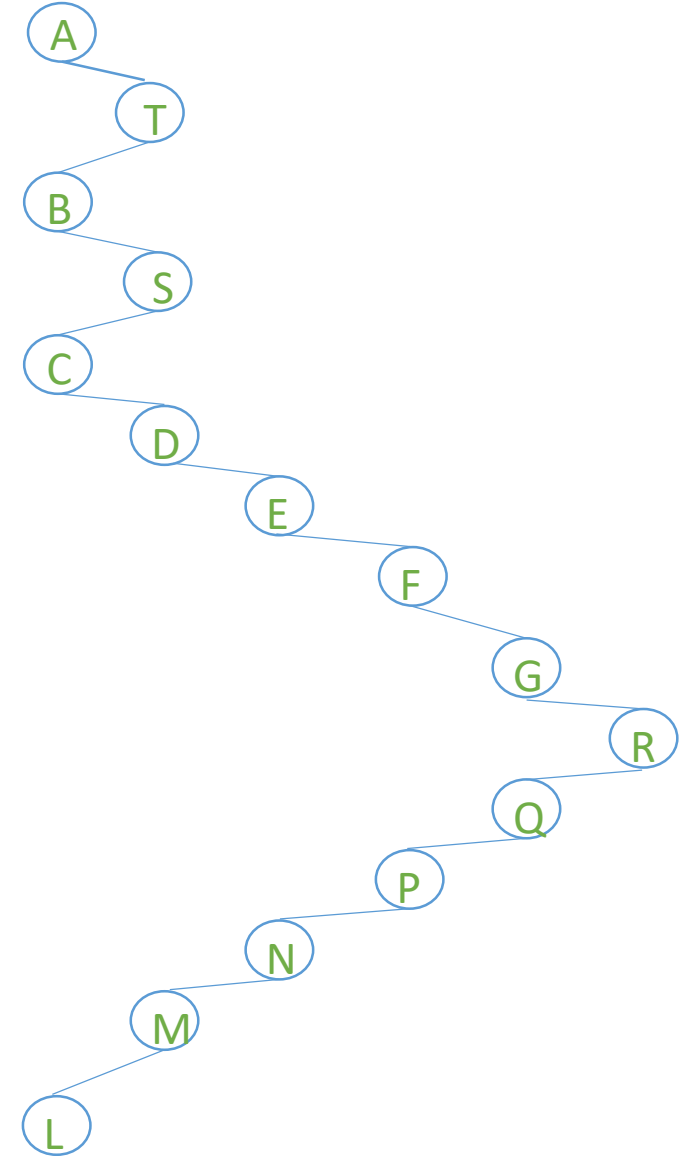
- inserting a record
 - detect the position of the record
 - store the record in a free node
 - link the node to its parent

- removing a record
 - search for the record
 - 3 cases
 - it doesn't have children
 - the parent's pointer := NULL
 - it has 1 child
 - the child is attached to the parent
 - it has 2 children
 - it's replaced with the closest value (e.g., in-order successor)
 - the node is added to the empty nodes list



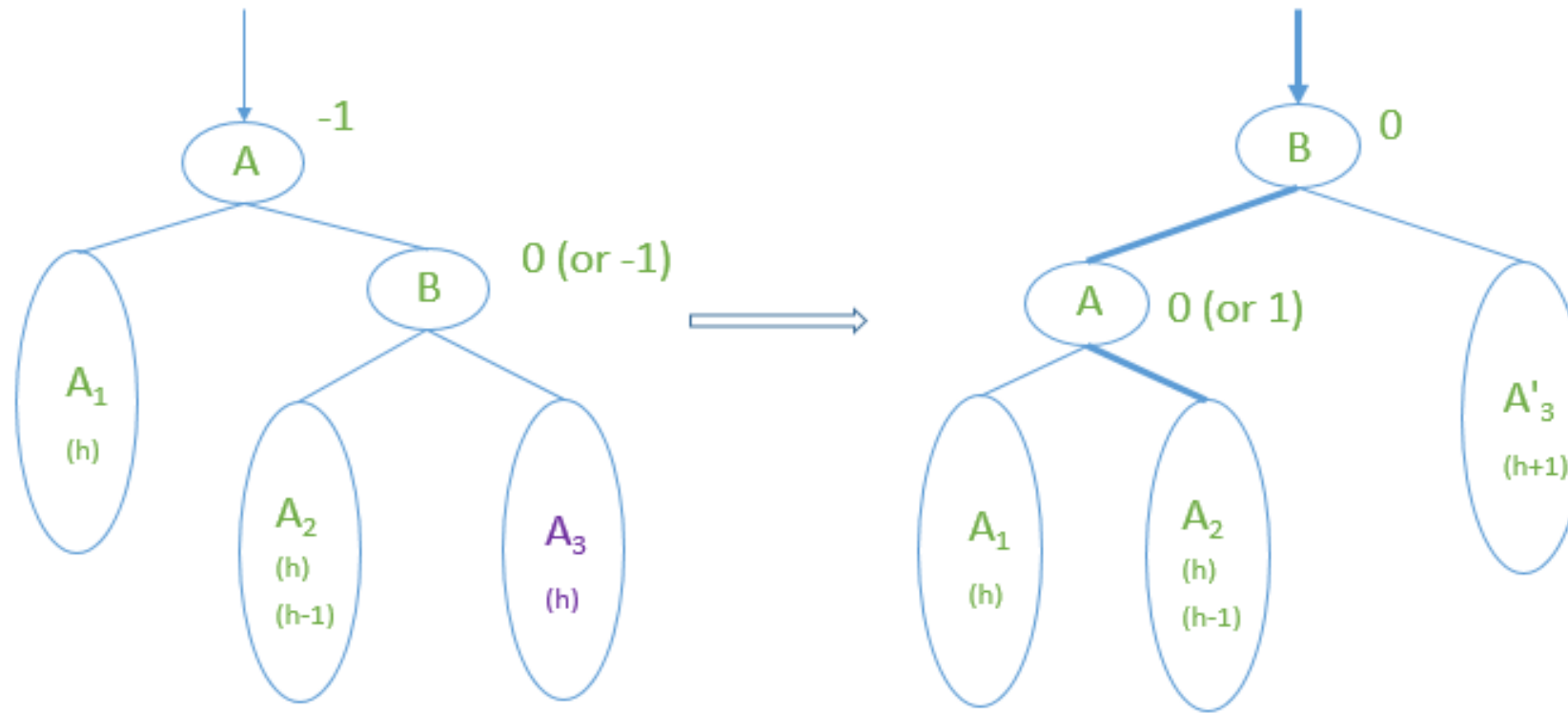
* Example

- key values {L, D, B, Q, N, F, S, R, T, M, E, G, P, A, C} are now provided in a different order: {A, T, B, S, C, D, E, F, G, R, Q, P, N, M, L}
- the tree on the right is obtained
- how many comparisons to find record with key value M?
- *degenerate tree*
 - sequential search
- the shape of the tree, and hence the search time, depends on the order in which data is added to the collection
- minimum search time - an *optimal tree*, i.e., one in which terminals are stored on at most 2 consecutive levels



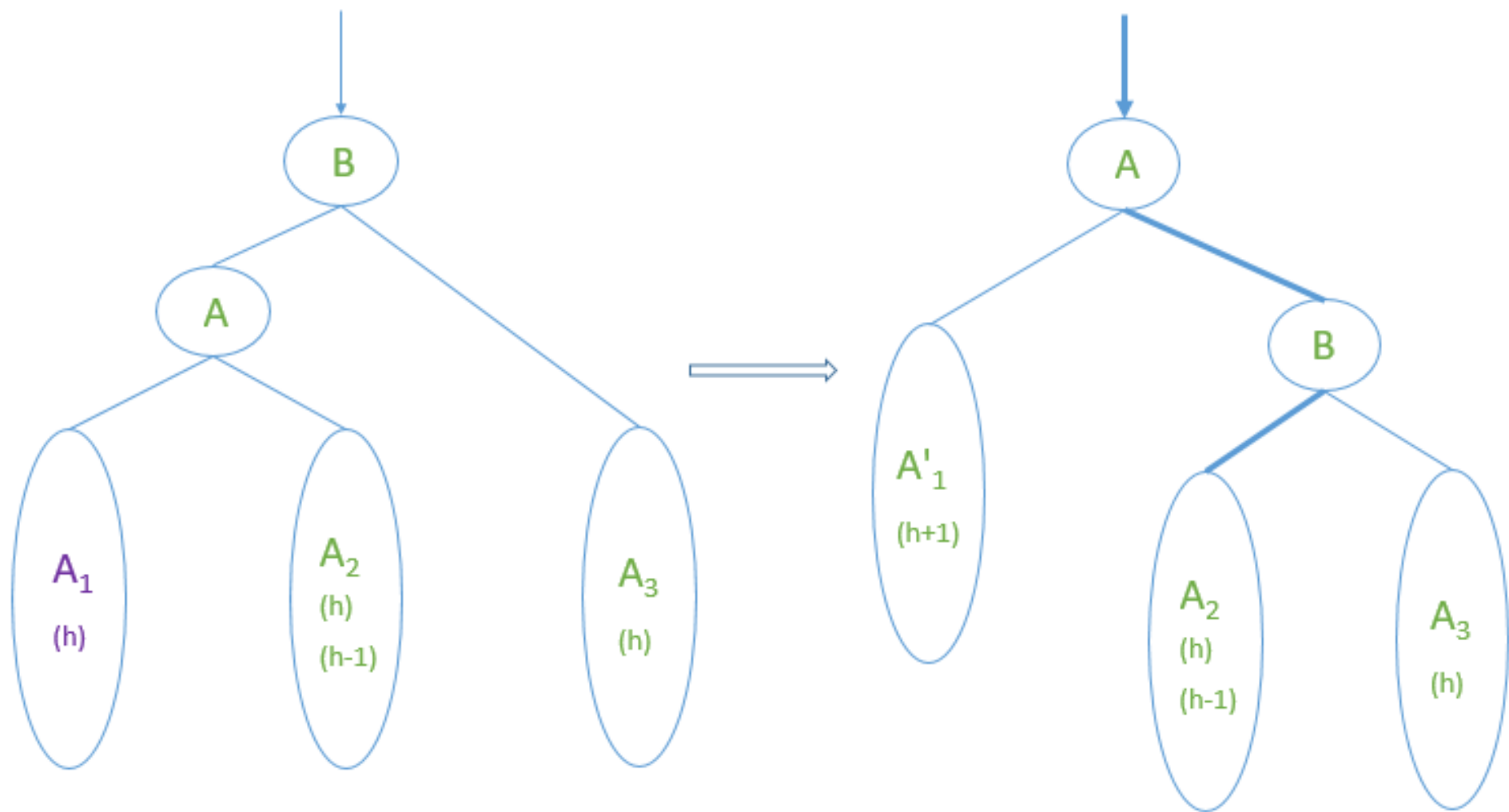
- definitions
 - *height* of the tree
 - length of longest path from root to terminals
 - a binary tree is *balanced* if, for every node N, the difference between the heights of N's subtrees is 0, 1 or -1
- obs. operations on a balanced tree can unbalance it; the tree can be rebalanced through a small number of changes
- a value is added to the A_3 tree on the next page (v1), causing its height to change (it increases by 1)
 - the subtrees' heights are shown between parentheses; for nodes A and B, the difference between the heights of their subtrees is also shown
 - after the insertion, the tree becomes unbalanced
 - the right-hand side of the figure shows a transformation that rebalances the tree with the root in A

v1

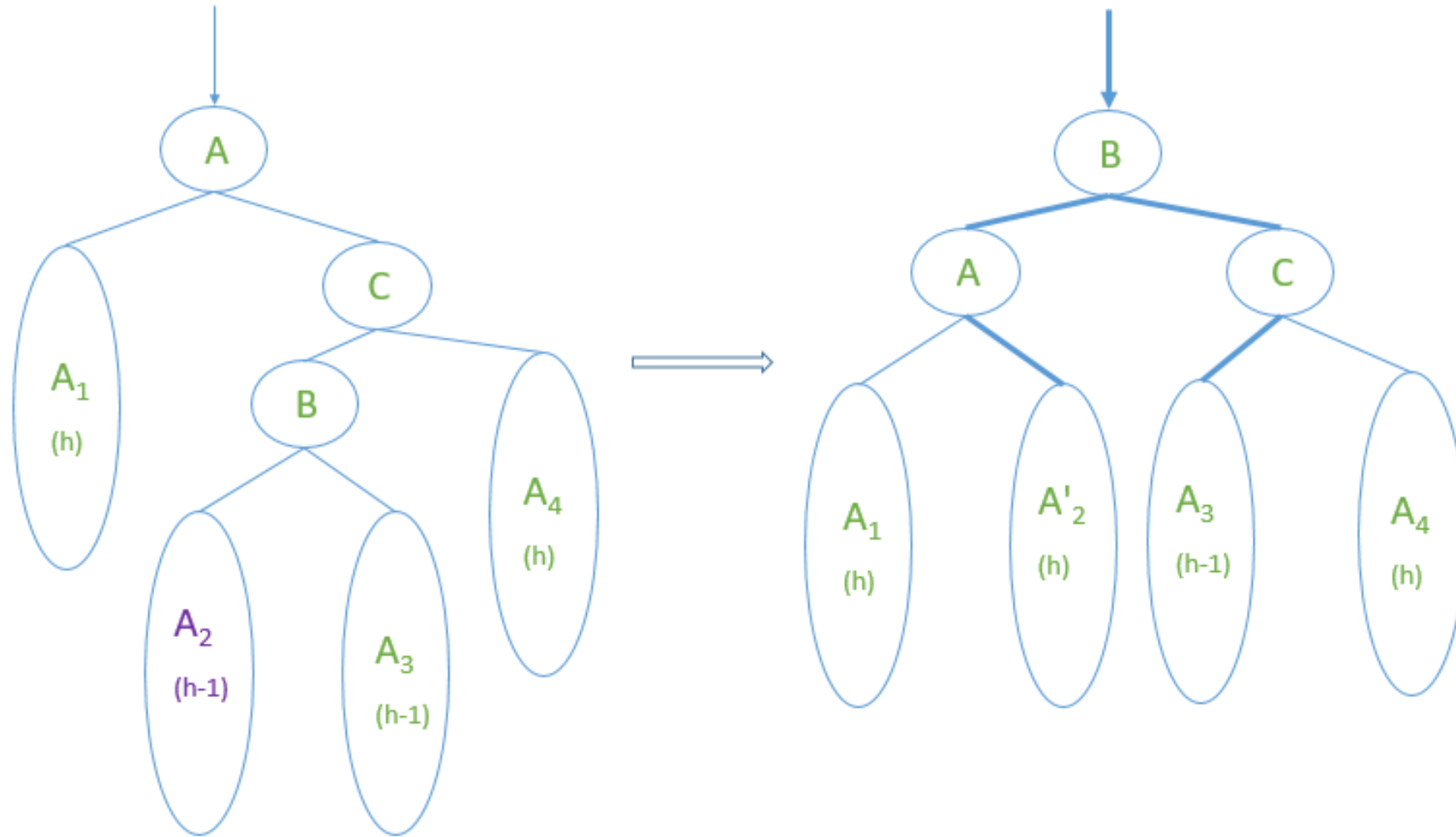


- some assignments are necessary for this rebalancing in the memory area that stores the tree (PointerR for A, PointerL for B, pointer referring to A will refer to B)
- [Kn76] enumerates all 6 rebalancing transformations

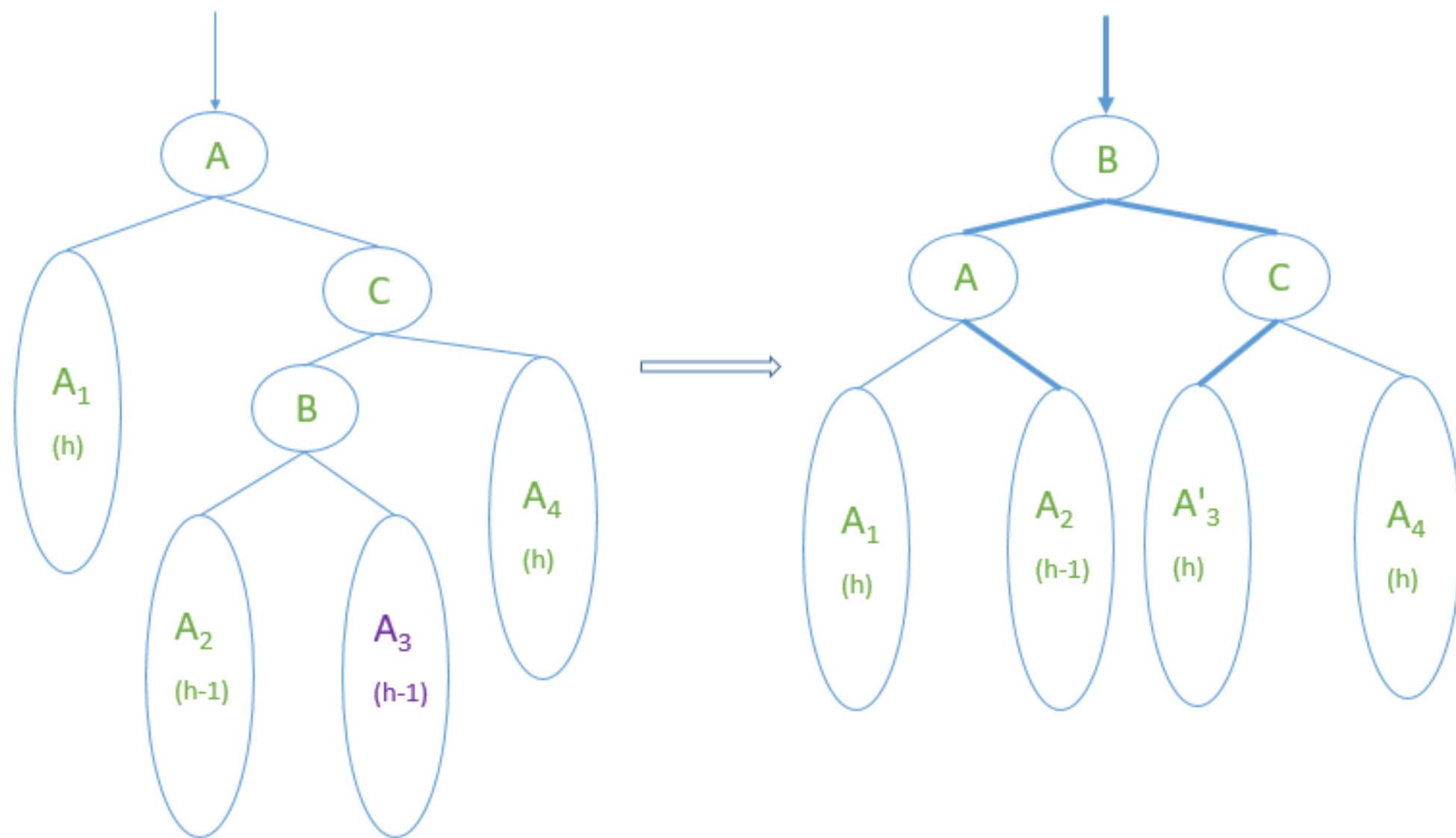
v2



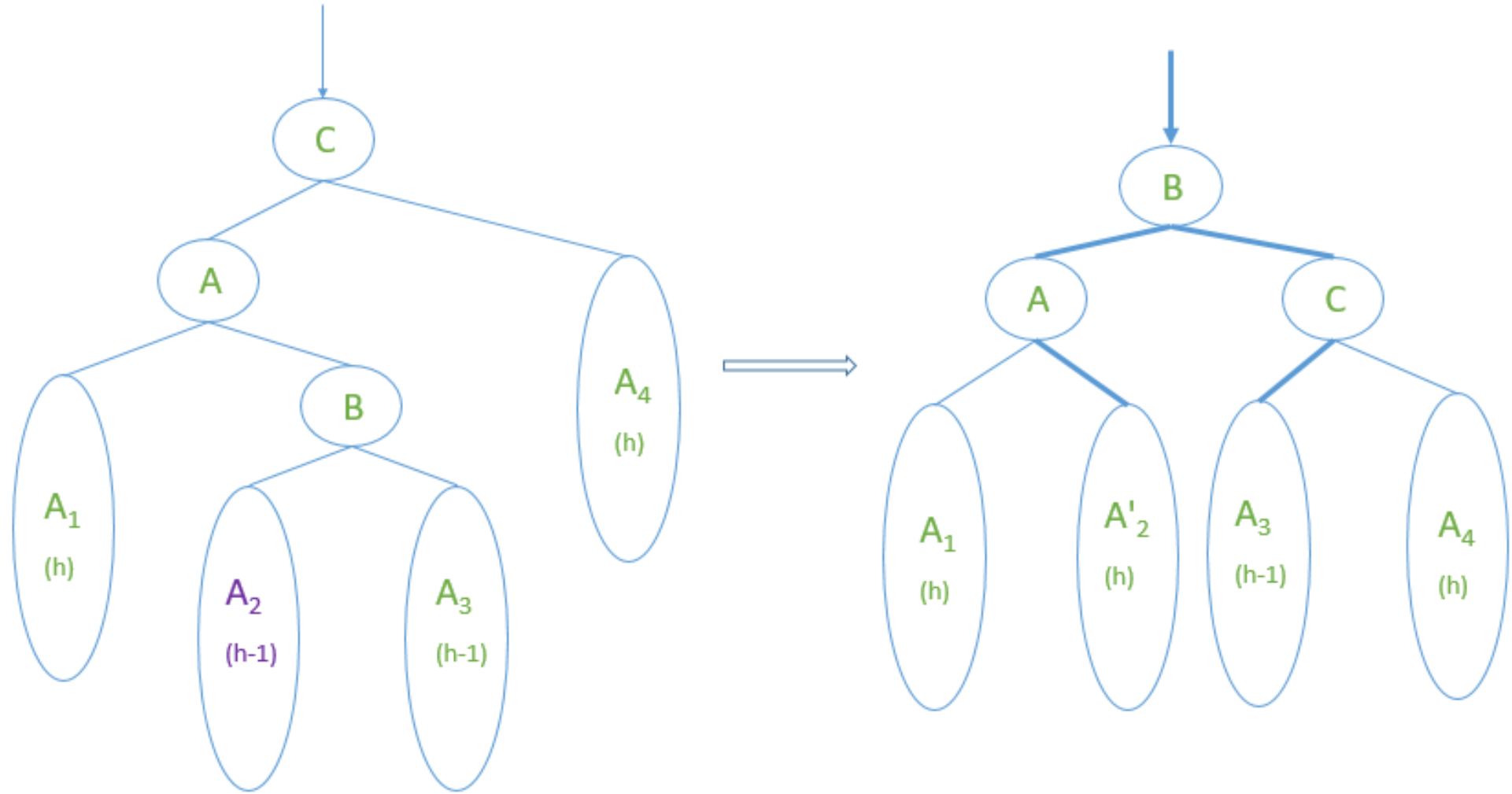
v3



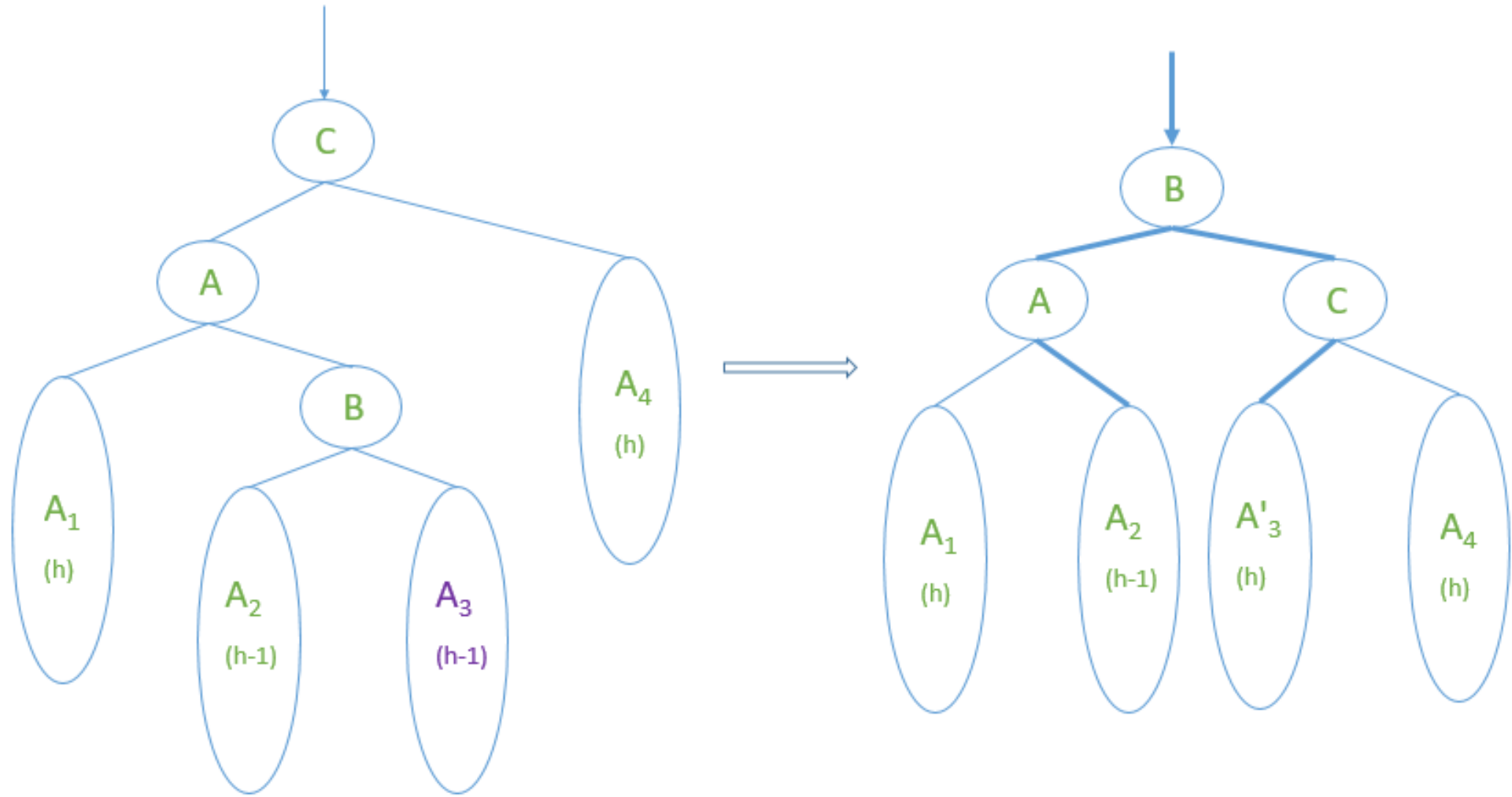
v4



v5



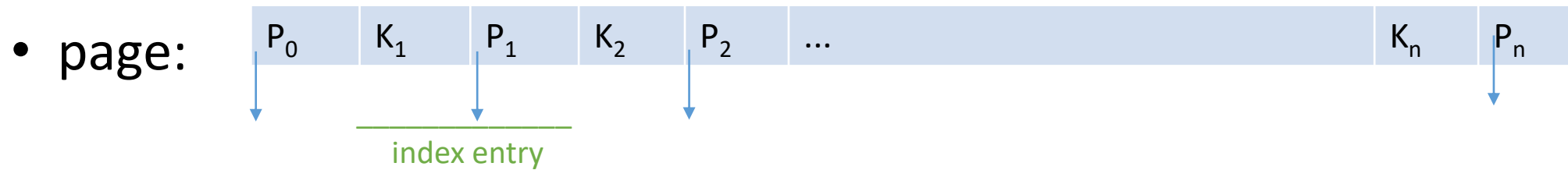
v6



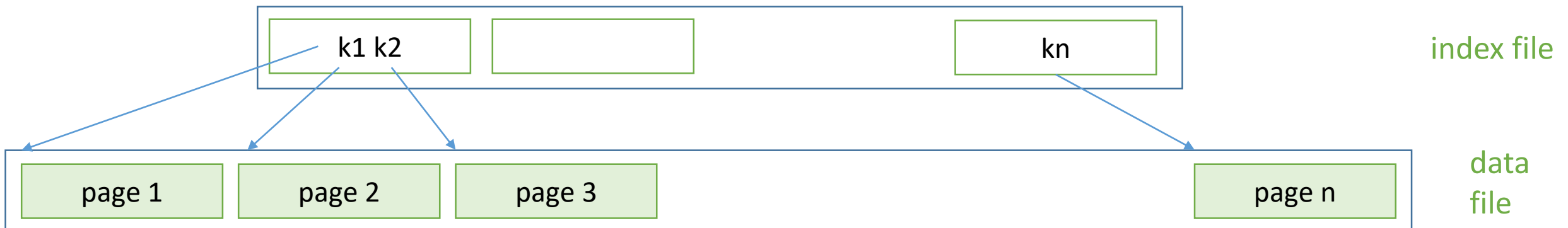
Indexed Sequential Access Method (ISAM)

* Example. Q: Find all phones with *rating* > 9 - range selection query

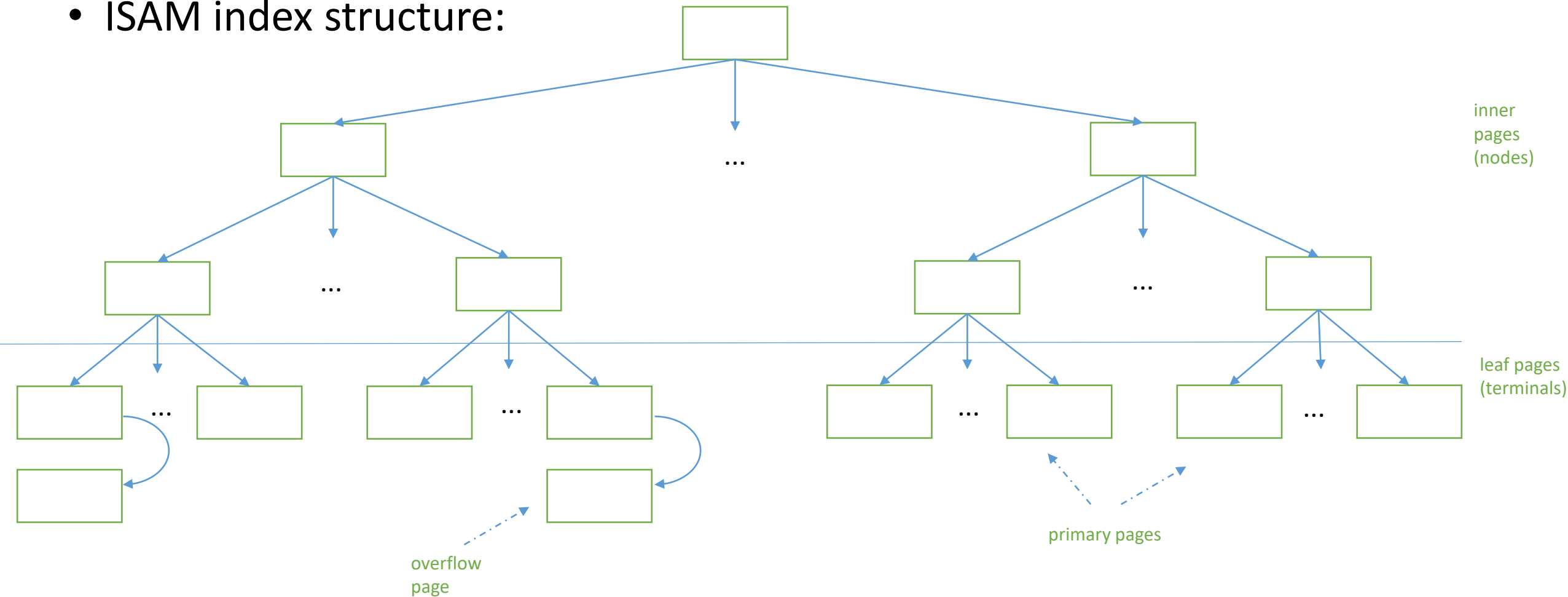
- data stored in sorted file - identify 1st phone using binary search; scan file to get the rest of the phones
- large file => potentially expensive binary search
- create another file - one record / page in the data file
- records of the form <1st key on the page, pointer to the page>, sorted on the key (*rating* in the example)



- one-level index file:



- size of index file - much smaller than size of data file => faster binary search
- to further reduce the cost of binary search, index files are repeatedly created on top of previously created ones, until one such file fits on a single page
- ISAM index structure:



- file creation
 - allocate leaf pages - sequentially allocated, sorted on the key
 - allocate inner pages
 - inserts that exceed a page's capacity – allocate overflow pages
- search
 - starts at the root
 - comparisons with the key to find the leaf page
 - cost – disk I/O
 - $\log_f n$, where n – number of primary leaf pages, f – number of children / index page (*fan-out*)
 - binary search cost: $\log_2 n$
 - one-level index cost: $\log_2(n/f)$

data pages

index pages

overflow pages

References

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- [Si10] SILBERSCHATZ, A., KORTH, H., SUDARSHAN, S., Database System Concepts, McGraw-Hill, 2010
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