

ACM ICPC 2017 - Kharagpur Regional

Presentation of solutions

1. Uniform Strings	Easy
2. Spam Classification using Neural Net	Easy
3. Generating a Permutation	Easy-medium
4. Taxi Making Sharp Turns	Easy-medium
5. Number Game	Medium
6. Non Overlapping Segments	Medium
7. Spanning Tree	Medium
8. SAD Queries	Medium
9. Chef and XOR Queries	Med-Hard
10. Science Fair	Hard
11. Black Discs	Hard

Problem 1

Uniform Strings

Accepted: 67

First solved by: **kgeccoders_1**
Kalyani Government Engineering College

00:03:29

Author: Praveen Dhinwa

Problem 2

Spam Classification Using Neural Net

Accepted: 67

First solved by: **Tesla**
International Institute of Information Technology, Hyderabad

00:13:05

Author: Praveen Dhinwa

P2 - Spam Classification Using Neural Net

- Calculate everything modulo 2
- $(Y_{i+1} = W_i * Y_i + B_i) \bmod 2$
- Only depends whether Y_0 is even or odd
- Count number of even and odd numbers in $[\min X, \max X]$

Problem 3

Generating a Permutation

Accepted: at least 44

First solved by: **ground floor**
Indian Institute of Technology Madras

01:01:30

Author: Archit Karandikar

P3 - Generating a Permutation

Minimum and maximum possible values of $f(P)$?

Minimum: 1, 2, 3, , , n

Maximum: 1, n, 2, (n - 1), ...

Let's take the permutation $P = 1, 2, 3, \dots, n$

If we swap n and (n - 1), we get:

$P' = 1, 2, 3, \dots, \mathbf{n}, \mathbf{n - 1}.$

Note that $f(P') = f(P) + 1$

P3 - Generating a Permutation

Now, swap **n** with **(n - 2)**.

We get $f(P'') = f(P') + 1$.

Key observation:

If you move **n** from the last position to the first position, you can see the **f** values increase by 1 for every move.

For each number, you can determine their positions uniquely.

Complexity: $O(N)$

Problem 4

Taxi Making Sharp Turns

Accepted: at least 7

First solved by: **De_Dana_Dan**
National Institute of Technology Silchar
02:07:49

Author: Praveen Dhinwa and Arjun Arul

P4 - Taxi Making Sharp Turns

- Check if there are any sharp turns - $O(N)$
- If you find a sharp turn at point i , then one of $i-1$, i or $i+1$ have to be changed.
- 50^2 options for each of them
- $O(N)$ to check for each possibility

Problem 5

Number Game

Accepted: at least 10

First solved by: **NDTM**
Indian Institute of Technology Guwahati

01:36:00

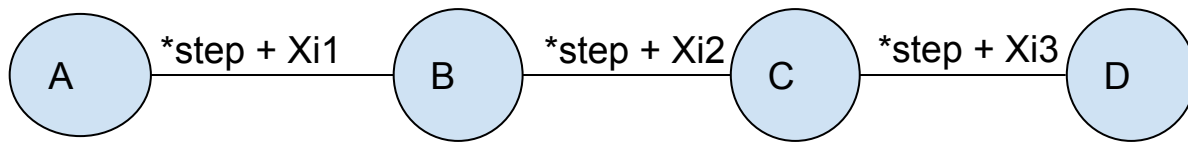
Author: Balajiganapathi

P5 - Number Game

- X_i = The number A with i^{th} digit removed
- Consider k concatenation of some X_i s
- $X_{i_1} X_{i_2} \dots X_{i_k}$
- $X_{i_1} * 10^{k(N-1)} + X_{i_2} * 10^{(k-1)(N-1)} + \dots + X_{i_k} = 0 \bmod M$
- $X_{i_1} * \text{step}^k + X_{i_2} * \text{step}^{(k-1)} + \dots + X_{i_k} = 0 \bmod M$

P5 - Number Game

- $X_{i_1} \cdot \text{step}^k + X_{i_2} \cdot \text{step}^{(k-1)} + \dots + X_{i_k} = 0 \bmod M$
- $((X_{i_1} \cdot \text{step} + X_{i_2}) \cdot \text{step} + X_{i_3}) \cdot \text{step} + X_{i_4} \dots = 0$



- **$A \cdot \text{step} + X_i = B \bmod M$ for some i**
- Then add a directed edge from A to B
 $0 < A, B < M$

P5 - Number Game

- Atmost M distinct X_i
- For A in $[0..M)$:
 - For x in distinct(X_i)
 - $B = (A * \text{step} + x) \bmod M$
- Find all the nodes from where 0 is reachable
- $O(M^2)$ per test

Problem 6

Non Overlapping Segments

Accepted: at least 2

First solved by: **LongTimeNoC**
Indian Institute of Technology Kanpur

01:29:08

Author: Archit Karandikar

P6 - Non Overlapping Segments

Let **$dp(i, j)$** denote the

- ***maximum number of extra segments that can still be accommodated***
- if we fix **j** segments in the first **i** segments with **i^{th}** segment fixed)

P6 - Non Overlapping Segments

Time Complexity: $O(N^3)$

$$\mathbf{dp[i][j] = \min(dp[k][j-1] + \text{distance}(i \text{ to } k)/R)}$$

If $\mathbf{dp[i][j] > N-j}$ then we can fix j segments. Find max such j.

Problem 7

Spanning Tree

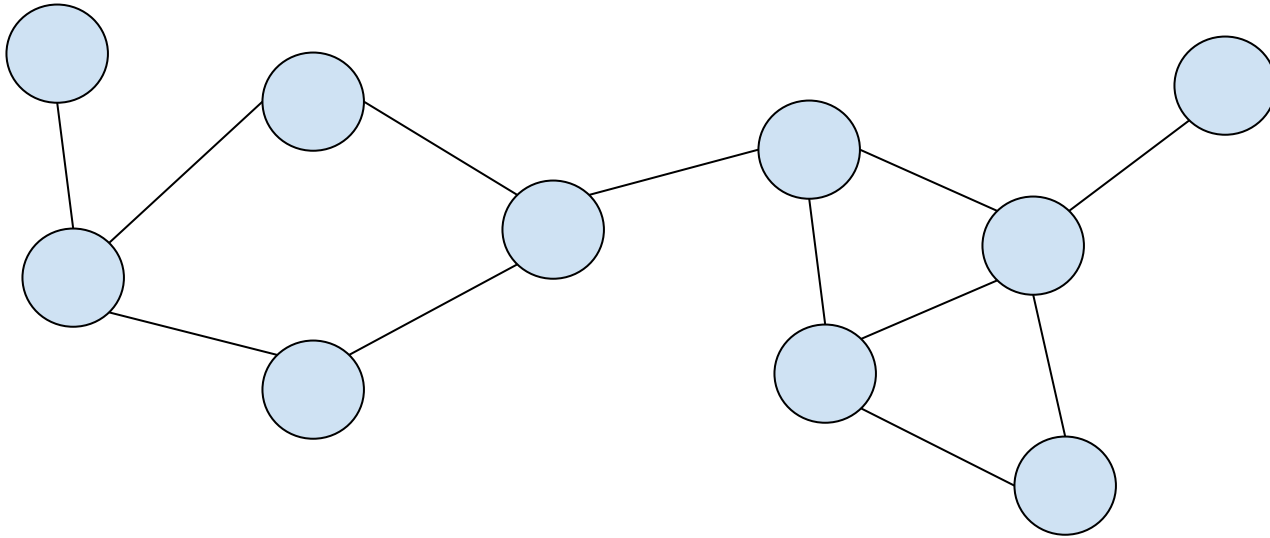
Accepted: at least 4

First solved by: **DU_Inception**
University of Dhaka

01:56:08

Author: Sidhant Bansal

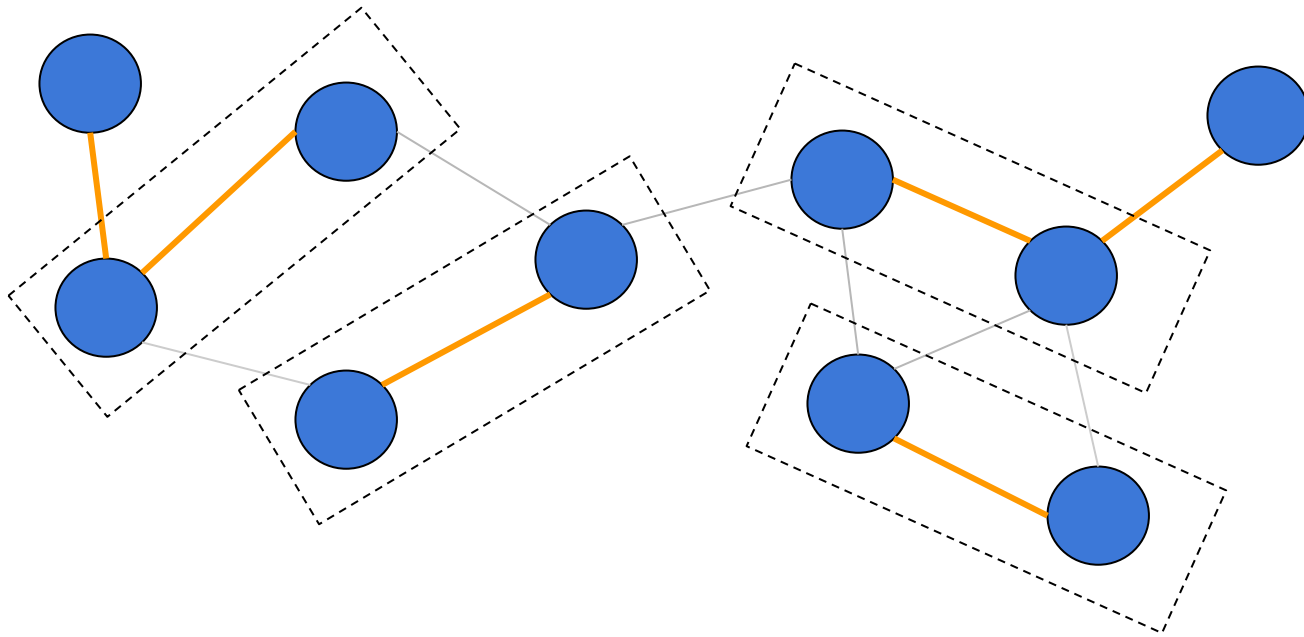
P7 - Spanning Tree



1. Let's find the nearest node for each node.

Query: **A** = {u}, **B** = {all except u}

P7 - Spanning Tree



- We get components of size=2.
- Use DSU to maintain components.

P7 - Spanning Tree

- For the available component, we keep on querying:
{component} vs {all except component}
- After every merge, the size of a component gets **doubled**.

P7 - Spanning Tree

How many times does each node appear in a query?

$O(\log(N))$

Cost incurred by one appearance of a node?

1

$$\text{Total cost} = N * \log(N) < 10^4$$

Problem 8

Chef and XOR Queries

Accepted: at least 4

First solved by: **Plumbus**
IIT Roorkee

01:47:43

Author: Utkarsh Saxena

P8 - Chef and XOR Queries

- Do you need the tree ?
- $X_i = \mathbf{XOR}$ of all edges from **root** to node **i**
- $\mathbf{F(u, v) = XOR}$ of path from **u** to **v** = $\mathbf{X_u} \wedge \mathbf{X_v}$
- **Problem: Given xor values of some pair of numbers. Can you infer xor of some other pairs**

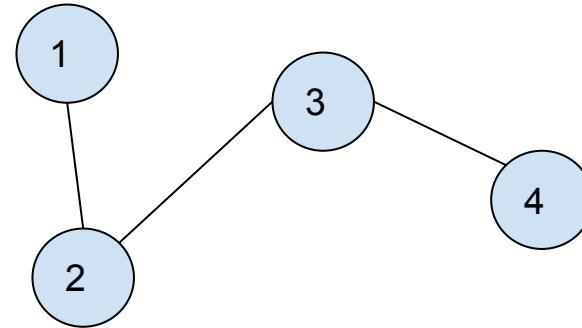
P8 - Chef and XOR Queries

- **Problem: Given xor values of some pair of numbers. Can you infer xor of some other pairs**
- $X1 \wedge X2 = Y12$
 $X2 \wedge X3 = Y23$
 $X3 \wedge X4 = Y34$
- What is
 $X1 \wedge X3?$ $Y12 \wedge Y23$
 $X1 \wedge X4?$ $Y12 \wedge Y23 \wedge Y34$

P8 - Chef and XOR Queries

- **Problem: Given xor values of some pair of numbers. Can you infer xor of some other pairs**

- $X1 \wedge X2 = Y12$
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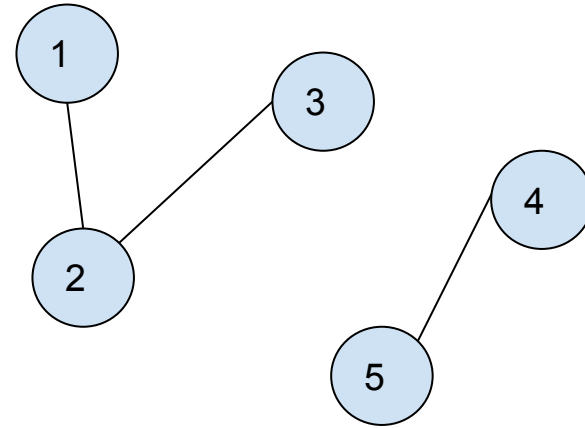


- What is
 $X1 \wedge X3?$ $Y12 \wedge Y23$
 $X1 \wedge X4?$ $Y12 \wedge Y23 \wedge Y34$

P8 - Chef and XOR Queries

- **Problem: Given xor values of some pair of numbers. Can you infer xor of some other pairs**

- $X1 \oplus X2 = Y12$
 $X2 \oplus X3 = Y23$
 $X4 \oplus X5 = Y45$



- What is
 $X1 \oplus X3?$ $Y12 \oplus Y23$
 $X1 \oplus X4?$?? ??? **You can't say**

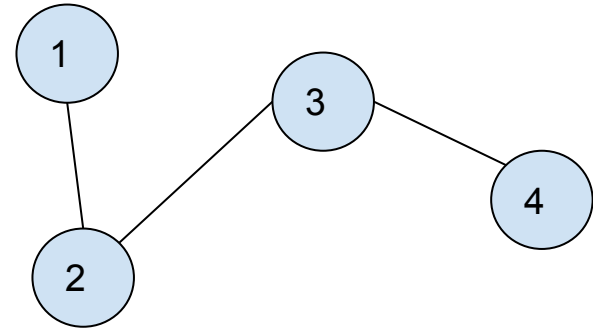
P8 - Chef and XOR Queries

- **Problem: Given xor values of some pair of numbers. Can you infer xor of some other pairs**
- When you have information of $X_u \oplus X_v$: add an edge from **u** to **v**
- You can tell answer $X_i \oplus X_j$ if and only if there is a path from **i** to **j** in this graph.
- Maintain all connected components.
- You can answer queries belonging to the same component.

P8 - Chef and XOR Queries

- **Problem:** Given xor values of some pair of numbers in same **connected component**. Can you infer xor of some other pairs.

- $X1 \oplus X2 = Y12$
 $X2 \oplus X3 = Y23$
 $X3 \oplus X4 = Y34$
- What if we assume $X1 = 0$.
- $X2 = Y12$
 $X3 = X2 \oplus Y12$
 $X4 = X3 \oplus Y34$
- Consistent with the given information



P8 - Chef and XOR Queries

- **Problem:** Given xor values of some pair of numbers in same **connected component**. Can you infer xor of some other pairs.
- Fix value of one node in every component(say root of dsu)
- Let X_i denote the assumed value of i^{th} node in its component.
- Query **a, b:** $X_a \oplus X_b$ iff a and b in the same component.

P8 - Chef and XOR Queries

- The information stored inside a component is still consistent if we change $\mathbf{X[i] = X[i] \wedge r}$ for all i in the component.
- $X[u] \wedge X[v]$ does not change if we change
 - $X[u] = X[u] \wedge r$
 - $X[v] = X[v] \wedge r$

P8 - Chef and XOR Queries

- **Deal with new information**
- New information only when xor of two disconnected nodes is given
- Given $F(u, v) = r$ & u and v are disconnected
- Merge component of u and v
- Need to $X[u]$ so that $X[u] \oplus X[v] = r$
Change $X[u]$ to $r \oplus X[v]$
- But what about the initial information in the component of u ???
- Change $X[i] = X[i] \oplus (r \oplus X[v])$ for all i in the component of u .

P8 - Chef and XOR Queries

- **Complexity ?**
- When we merge two components: Size of smaller component atleast doubles.
- $O(N \cdot \log N + Q)$

Problem 9

SAD Queries

Accepted: at least 23

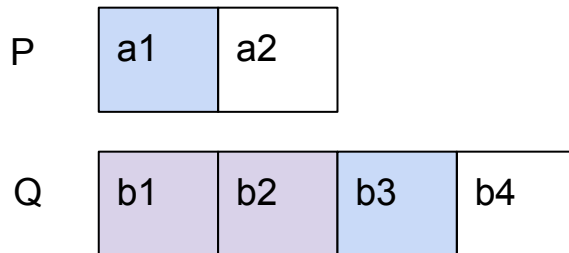
First solved by: **NDTM**
IIT Guwahati

00:53:14

Author: Archit Karandikar

P9 - SAD Queries

- Preprocess:
 - Sort all arrays
 - Maintain prefix sums for each.
- For each $P[i]$, find largest $Q[j]$ less than $P[i]$



- Q is monotonic
 - Binary search to find $Q[j]$.
- Key observation:
 - Always keep P as the smaller array and Q as the larger array.

P9 - SAD Queries

- Contribution to total sum by $P[i]$, $Q[1..j]$?
 - $j * P[i] - \text{prefix_sum_Q}[j]$
- Contribution to total sum by $P[i]$, $Q[j+1..s_Q]$?
 - $\text{suffix_sum_Q}[j+1..s_Q] - ((s_Q - j) * P[i])$
- Time Complexity per query?
 - $O(s_P \log(s_Q))$

But will this not TLE?

P9 - SAD Queries

- Arrays of size $\geq \sqrt{N}$ -> ***heavy***
- Arrays of size $< \sqrt{N}$ -> ***light***

- Key observation:
 - There can be at most $O(\sqrt{N})$ heavy arrays.

- 3 types of queries:
 - Light-Light
 - Light-Heavy
 - Heavy-Heavy

P9 - SAD Queries

- Light-Light
 - Max possible size of P: $O(\sqrt{N})$
 - Max possible size of Q: $O(\sqrt{N})$
 - Worst-case complexity: $O(\sqrt{N}\log(\sqrt{N}))$
- Light-Heavy
 - Max possible size of P: $O(\sqrt{N})$
 - Max possible size of Q: $O(N)$
 - Worst-case complexity: $O(\sqrt{N}\log(N))$
- Heavy-Heavy
 - Max possible size of P: $O(N)$
 - Max possible size of Q: $O(N)$
 - Worst-case complexity: ??

P9 - SAD Queries

- How many times can a heavy array play the role of array P?
 - No. of possible heavy arrays $Q = O(\sqrt{N})$
- Therefore, every element in that heavy array (P) is iterated $O(\sqrt{N})$ times.
- Heavy-Heavy
 - Max possible size of P: $O(N)$
 - Max possible size of Q: $O(N)$
 - Worst-case complexity: $O(N\sqrt{N}\log(N))$
- What if there are 2 heavy arrays of size $N/2$ each?
 - Memoize solution for each query

Problem 10

Science Fair

Submits: 0
Accepted: 0

First solved by: 0

00:00:00

Author: Utkarsh Saxena

P10 - Science Fair

- Modified Travelling Salesman Problem
(***TSP is a prerequisite***)
- $\text{Cost}(\{S1, S2, \dots, Sk\}) = \text{TSP} + [\text{Talk}(S1) * \text{Talk}(S2) * \dots * \text{Talk}(Sk) * \text{Talk}(E1) * \text{Talk}(E2) \dots \bmod 1e9+7]$
- The only catch: The driver picks up every child on its path even if not mentioned(**E1, E2,...**) on the list.
- Cost changes if you visit an unexpected node.

P10 - Science Fair

- $Sp[i][j]$ = shortest path between i^{th} student and j^{th} student.
- Calculate TSP dp on this matrix.
- $Dp[\text{mask}]$ = Shortest path covering all students with bits ON in mask
- Cost of a trip(mask) = $Dp[\text{mask}] + \text{talkativeness}[\text{mask}]$

P10 - Science Fair

- $Sp[i][j]$ = shortest path between i^{th} student and j^{th} student.
- Calculate TSP dp on this matrix.
- $Dp[\text{mask}]$ = Shortest path covering all students with bits ON in mask
- Cost of a trip(mask) = $Dp[\text{mask}] + \text{talkativeness}[\text{mask}]$

Wrong

P10 - Science Fair: Avoid unwanted student

- $Sp[i][j]$ = shortest path between i^{th} student and j^{th} student THAT DOES CONTAIN ANY OTHER STUDENT.
- $Dp[mask][i]$ = Shortest path to cover only those students mentioned in mask and end the trip at i^{th} student.
- $dp[mask|2^a][a] = \min(dp[mask][b] + sp[b][a], dp[mask|2^b][a])$
over all b in mask
- Can't solve this using **TSP DP**. Contains cycle dependency.
- Solve it using **Dijkstra**

P10 - Science Fair: How to deal unwanted students

- $\text{cost}[\text{mask}] = \text{dp}[\text{mask}] + \text{talk}[\text{mask}]$
- **Given a mask of student: The driver**
 - Might want to cover more students to reduce cost
 - Might be forced to cover some other student
 - He might end up covering an optimal mask ***opt(mask)*** for this mask
- **Mask is always a subset of $\text{opt}(\text{mask})$**

P10 - Science Fair: How to deal unwanted students

- $\text{cost}[\text{mask}] = \text{dp}[\text{mask}] + \text{talk}[\text{mask}]$
- **Mask is always a subset of $\text{opt}(\text{mask})$**
- Random observation: $\text{opt}(\text{opt}(\text{mask})) = \text{opt}(\text{mask})$
- Assume $\text{omask} = \text{opt}(\text{mask})$
Given omask as the list to driver:
 - Will not cover any unwanted student.
 - $\text{cost_trip}(\text{omask}) = \text{cost}[\text{omask}] = \text{dp}[\text{omask}] + \text{talk}[\text{omask}]$
- $\text{cost_trip}(\text{mask}) = \min(\text{cost_trip}(\text{mask2}))$ where *mask* is a subset of *mask2*

P10 - Science Fair: How to deal unwanted students

- $\text{cost}[\text{mask}] = \text{dp}[\text{mask}] + \text{talk}[\text{mask}]$
- **Mask is always a subset of $\text{opt}(\text{mask})$**
- Random observation: $\text{opt}(\text{opt}(\text{mask})) = \text{opt}(\text{mask})$
- Assume $\text{omask} = \text{opt}(\text{mask})$
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- $\text{cost_trip}(\text{mask}) = \min(\text{cost_trip}(\text{mask2}))$ where *mask is a subset of mask2*

S O S D P

Problem 11

Black Discs

Submits: 0

Accepted: at least 0

Author: Triveni Mahatha

P11 - Black Discs

- Idea: Monte-carlo search
 - Select a bounding box (B)
 - Generate N random points within the box
 - Check how many points lie within the curve who's area is to be estimated. Let's say K of the points lie within the curve.
 - The estimated area is: $(K/N) * \text{area}(B)$

P11 - Black Discs

- High-level approach
 - Maintain a set of arcs - the max value of y for each x
 - For each query circle
 - Iterate over arcs
 - Add area of intersection of query circle and arc to total area
- How to uniformly generate points within a circle of radius R ?
 - Let's define $\text{uniform}(L, R)$ as a function that gives a random real number in $[L..R]$ with uniform probability
 - Generate θ - $\text{uniform}(0, 360)$
 - Generate $r = R * \text{sqrt}(\text{uniform}(0, 1))$

Thanks!