

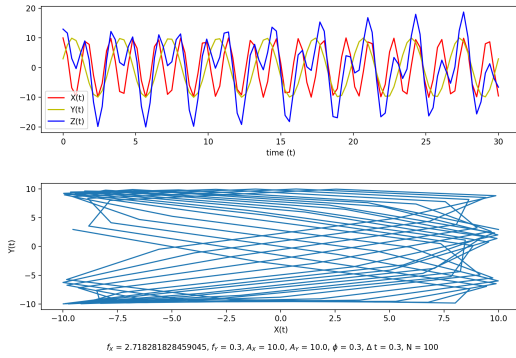
Ph 20: Assignment #1

Maya Fuller

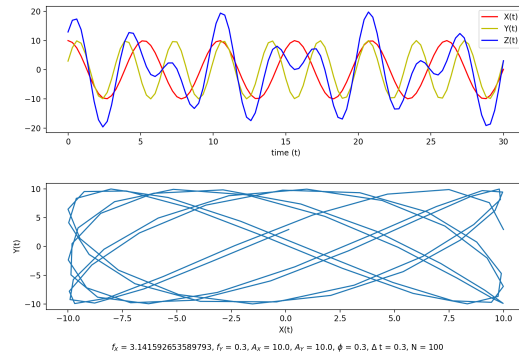
Due: April 9, 2018

Problem 3

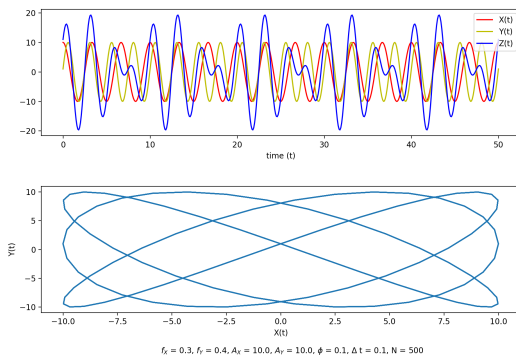
a)



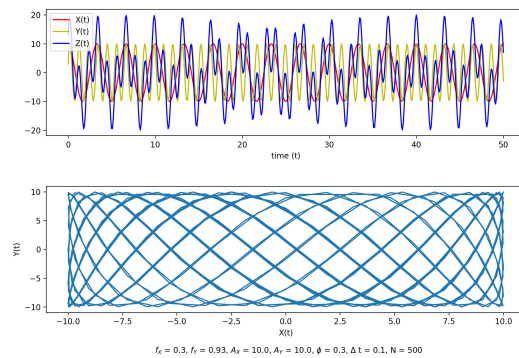
$$(a) \frac{f_x}{f_y} = \frac{e}{0.3}$$



$$(b) \frac{f_x}{f_y} = \frac{\pi}{0.3}$$



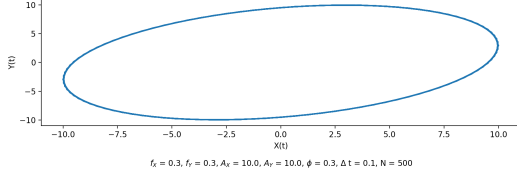
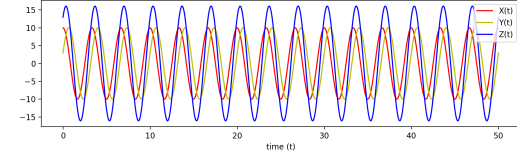
$$(c) \frac{f_x}{f_y} = 0.75$$



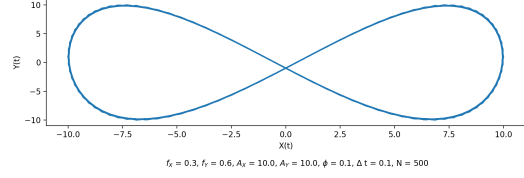
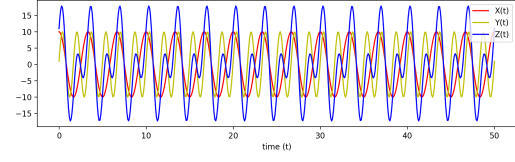
$$(d) \frac{f_x}{f_y} = 0.32$$

Figure 1: $\frac{f_x}{f_y}$ is irrational for (a) and (b) and rational for (c) and (d). (a) and (b) are not closed curves while (c) and (d) are.

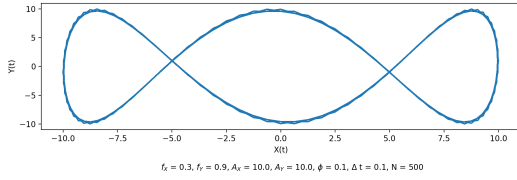
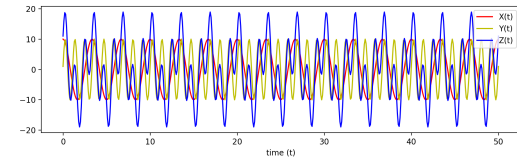
b)



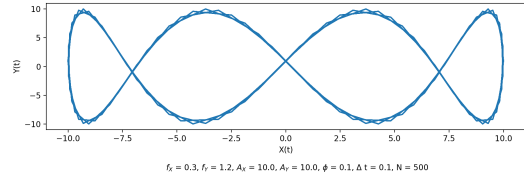
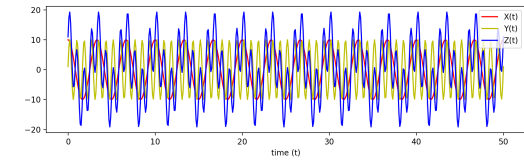
(a) $\frac{f_x}{f_Y} = 1$



(b) $\frac{f_x}{f_Y} = \frac{1}{2}$



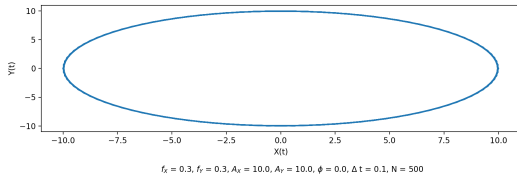
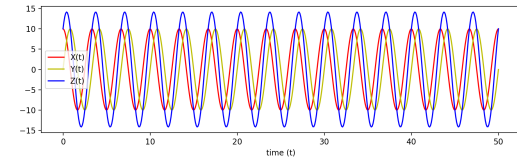
(c) $\frac{f_x}{f_Y} = \frac{1}{3}$



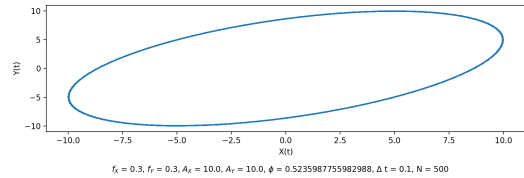
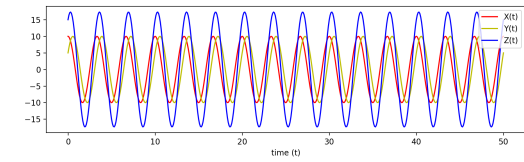
(d) $\frac{f_x}{f_Y} = \frac{1}{4}$

Figure 2: $\frac{f_x}{f_Y}$ determines the number of intersections of the $X(t)$ vs $Y(t)$ curve. When $\frac{1}{f_x/f_Y}$ is a natural number, $\frac{1}{f_x/f_Y}$ is the number of sections the curve is divided into.

c)



(a) $\phi = 0$



(b) $\phi = \frac{\pi}{6}$

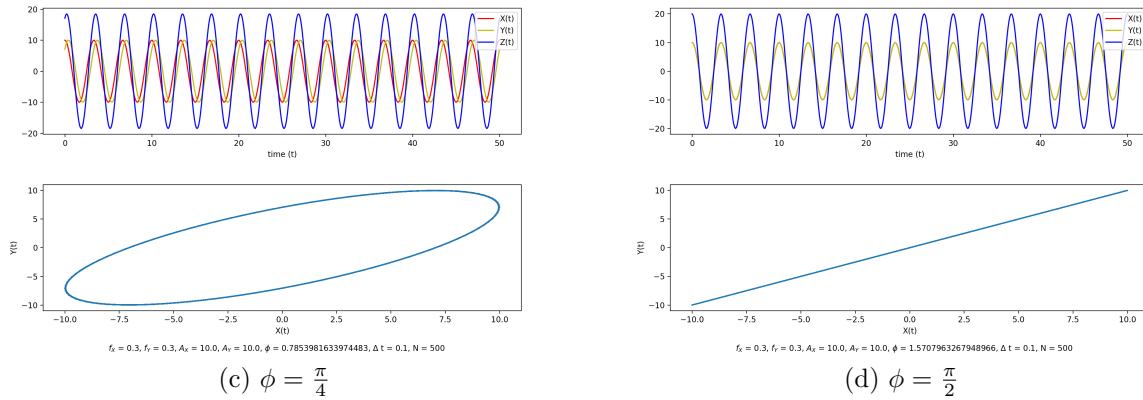


Figure 3: When $f_X = f_Y$, ϕ affects the apparent rotation angle of the figure.

Problem 4

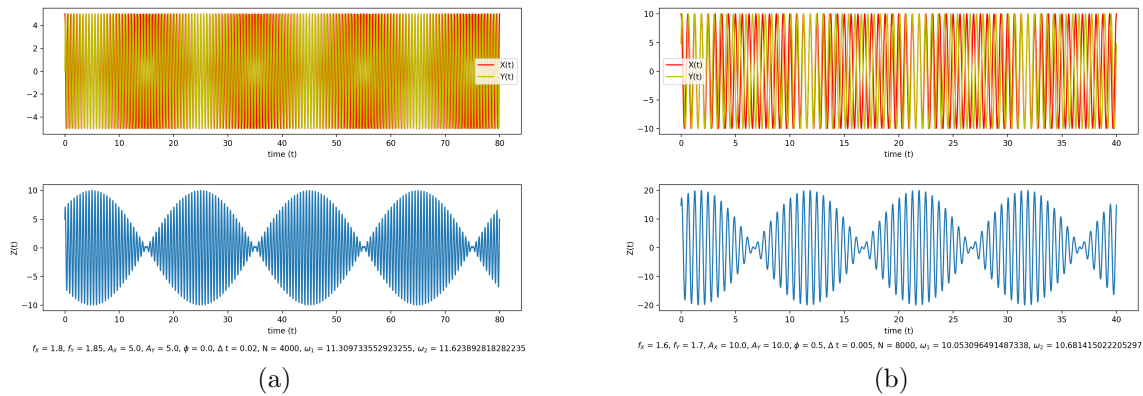


Figure 4: In both (a) and (b), $Z(t)$ displays both the carrier frequency, $\frac{\omega_1 + \omega_2}{2}$, and modulation cycles at frequency $\omega_1 - \omega_2$.

When $\phi = 0$, we can say that $X(t) + Y(t)$ is roughly $2\sin(\frac{\omega_1 + \omega_2}{2})\cos(\frac{\omega_1 - \omega_2}{2})$ by the sine product-sum identity. If $2\cos(\frac{\omega_1 - \omega_2}{2})$ is interpreted as the amplitude, the frequency includes two modulation cycles rather than one. Therefore, the frequency of the modulation cycles are at frequency $\omega_1 - \omega_2$ rather than $\frac{\omega_1 - \omega_2}{2}$.

Problem 5

I've had a decent amount of experience with `numpy` already, but this was a nice refresher. I've had little to no experience with `matplotlib` because the few times I've tried using did not turn out to be very successful. Over the past few years I've exclusively used Mathematica for plotting, although, this assignment has changed my mind about `matplotlib`. I really like how customizable and straightforward plotting is in `matplotlib`, so I plan to use it more often.

The majority of my coding experience is in Python, but I also have experience in C/C++ and Java. I find Python much more user-friendly and universal than C and Java, so I tend to code strictly in Python.