# Online POMDP Methods

## **Numerical Approximations**

(approximately solve original problem)

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(approximately solve original problem)



## **Numerical Approximations**

(approximately solve original problem)



Offline

**Online** 

Previously

### **Numerical Approximations**

(approximately solve original problem)



Offline

Previously



**Online** 

## Formulation Approximations

(solve a slightly different problem)

## **Numerical Approximations**

(approximately solve original problem)



Offline

Previously



**Online** 

## Formulation Approximations

(solve a slightly different problem)

Last Time

## **Numerical Approximations**

(approximately solve original problem)



Offline

Previously



**Online** 

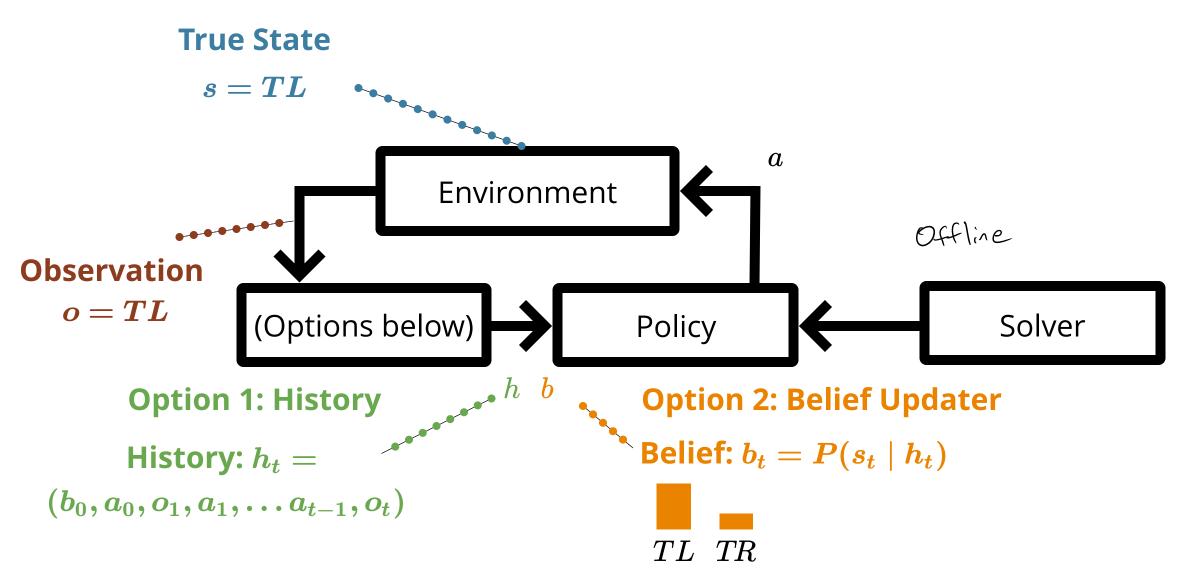
Today!

## Formulation Approximations

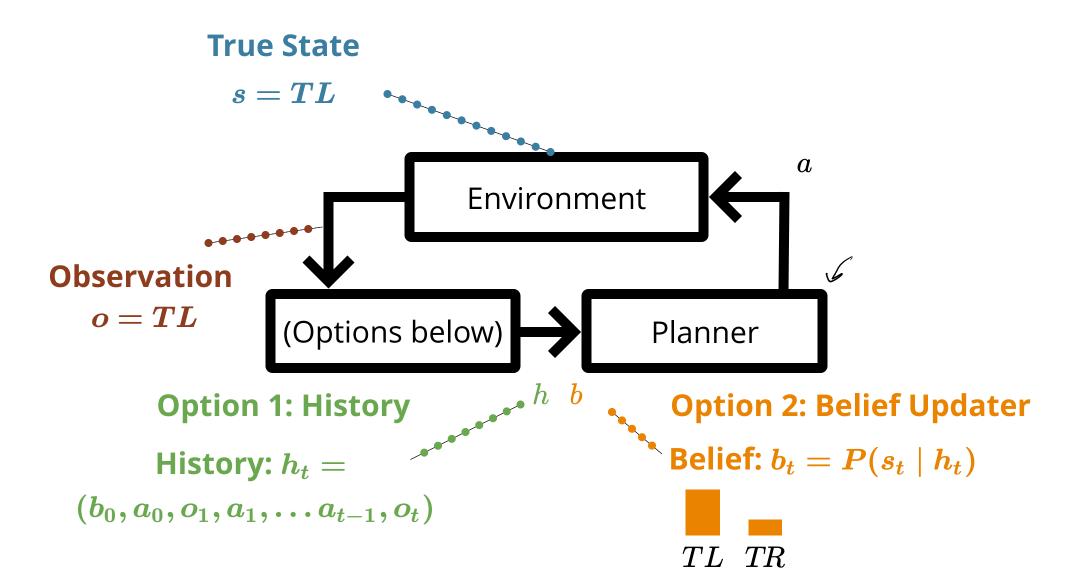
(solve a slightly different problem)

Last Time

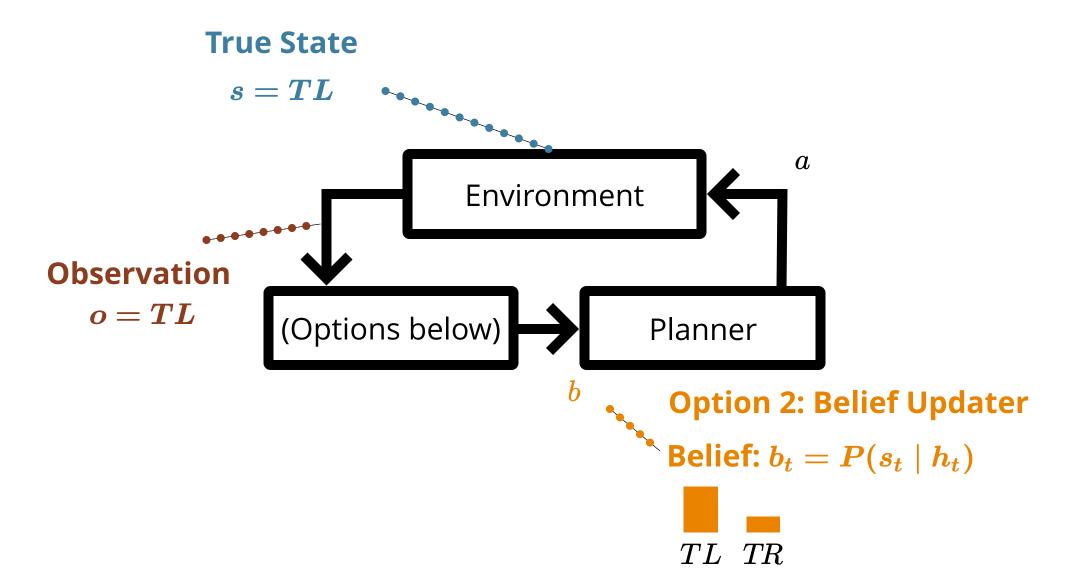
### POMDP Sense-Plan-Act Loop



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# Monte Carlo Tree Search (MCTS/UCT)

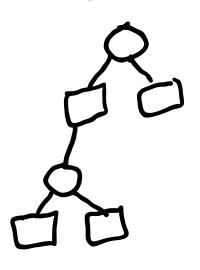
Search



$$Q(s,a) + c\sqrt{rac{\log N(s)}{N(s,a)}}$$

low N(s,a)/N(s) = high bonus start with  $c=2(ar{V}-V)$ 

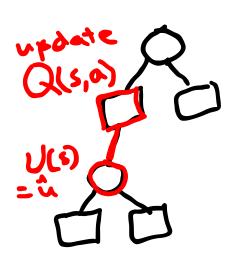
Expansion



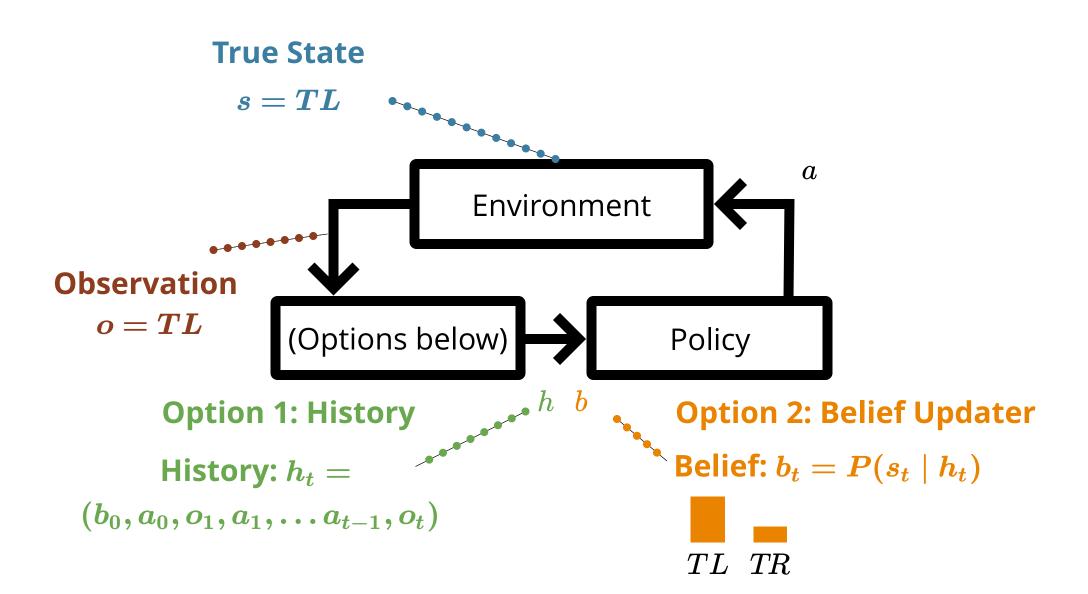
Rollout



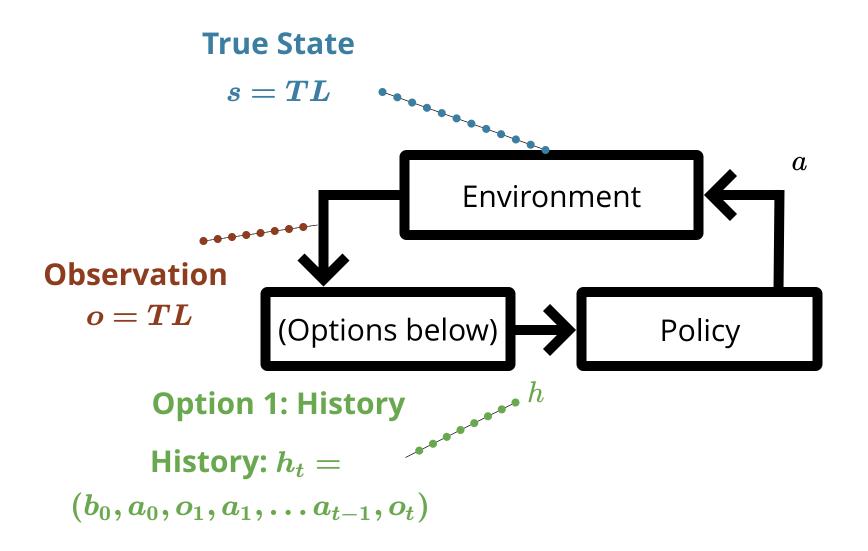
Backup



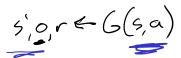
## How should we adapt MCTS for POMDPs?

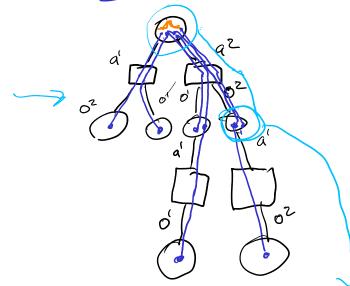


## How should we adapt MCTS for POMDPs?



## **MCTS** on Histories



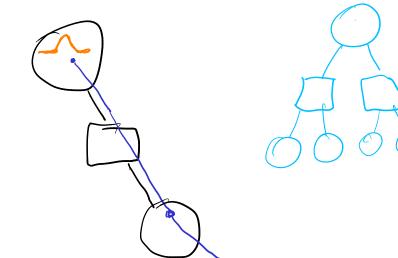


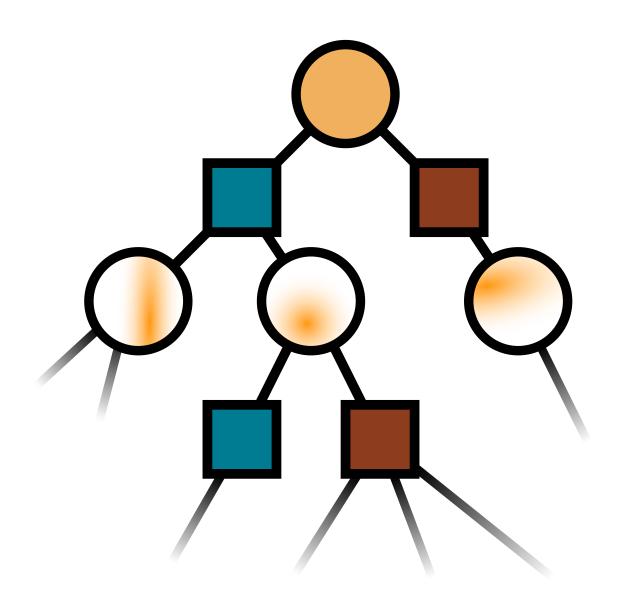


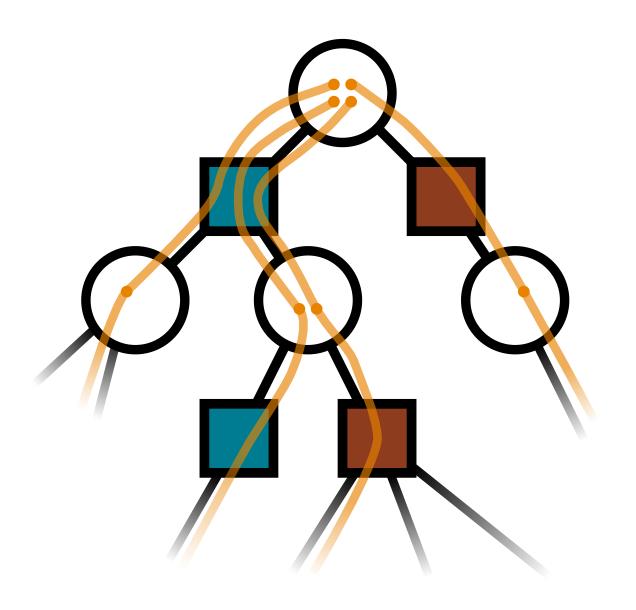
PO-UCT

POME P belief updates

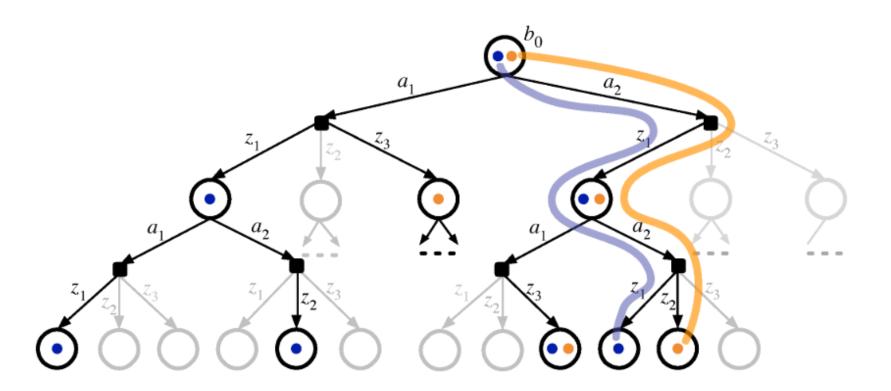
(Partially observable Monte Carlo Planning)



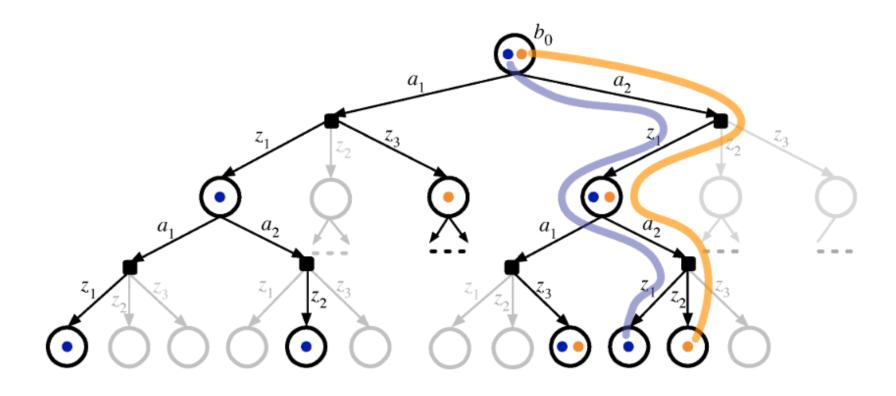




## **DESPOT**

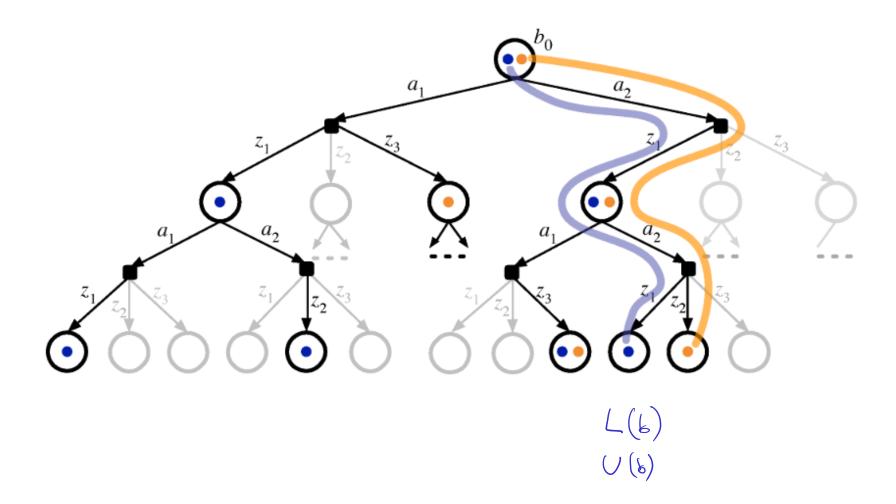


## **DESPOT**



DeterminizedScenarios

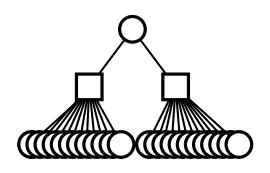
## **DESPOT**



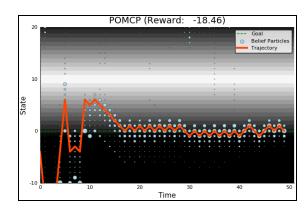
- DeterminizedScenarios
- Guided by Lower and Upper Bounds

Similar to FSSS

#### **POMCP**

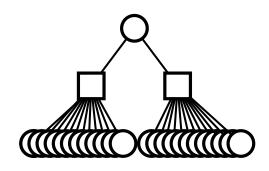


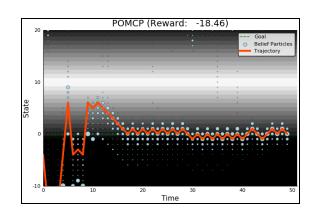




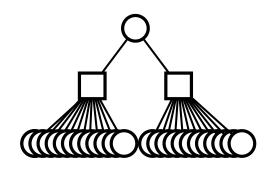
#### **POMCP**

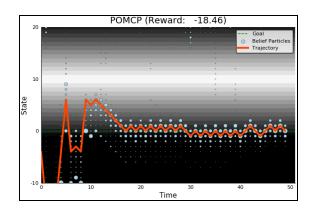
#### **POMCPOW**



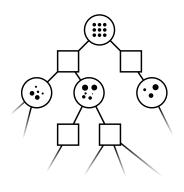


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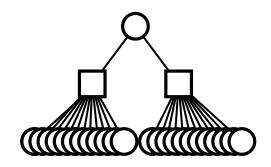


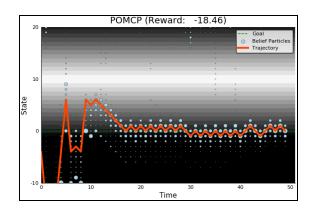


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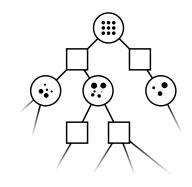


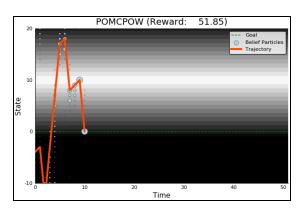
#### **POMCP**





#### **POMCPOW**





 $\mathbf{M_P}$  = Particle belief MDP approximation of POMDP  $\mathbf{P}$ 

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For any  $\epsilon > 0$  and  $\delta > 0$ , if C (number of particles) is high enough,

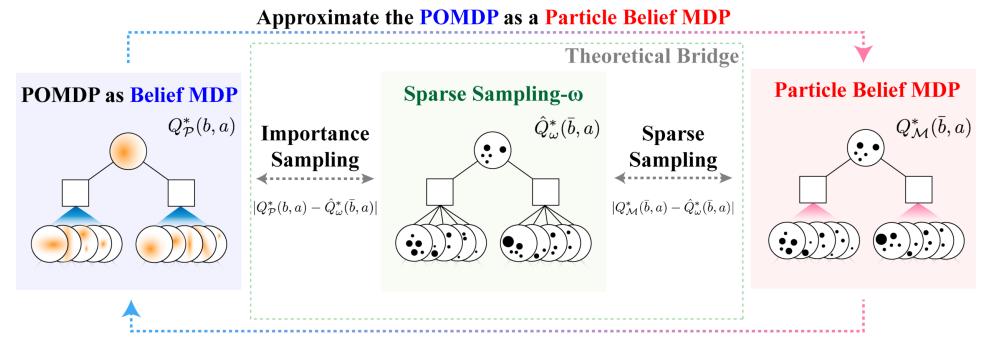
 $\mathbf{M_P}$  = Particle belief MDP approximation of POMDP  $\mathbf{P}$ 

For any  $\epsilon > 0$  and  $\delta > 0$ , if C (number of particles) is high enough,

$$|Q_{\mathbf{P}}^*(b,a) - Q_{\mathbf{M}_{\mathbf{P}}}^*(\overline{b},a)| \leq \epsilon \quad ext{w.p. } 1 - \delta$$

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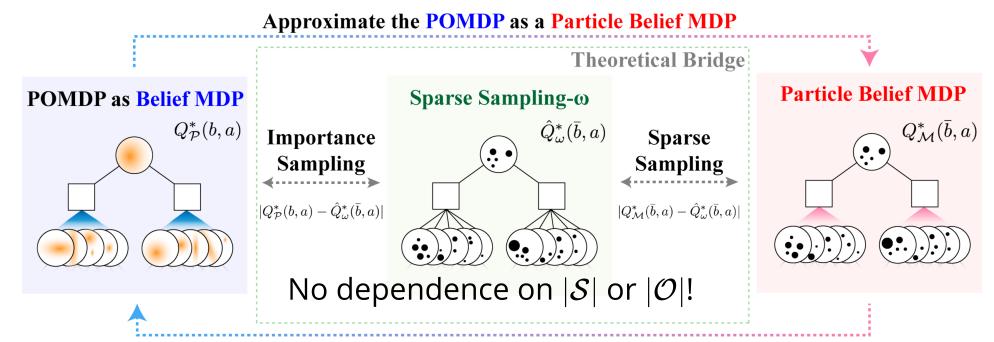


Solve the Particle Belief MDP to make a decision in the POMDP

 $\mathbf{M_P}$  = Particle belief MDP approximation of POMDP  $\mathbf{P}$ 

For any  $\epsilon > 0$  and  $\delta > 0$ , if C (number of particles) is high enough,

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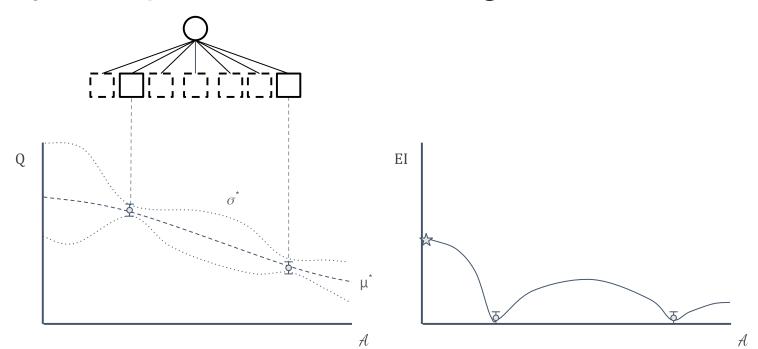
Solve the Particle Belief MDP to make a decision in the POMDP

## **DESPOT-** $\alpha$

# **Continuous Action Spaces**

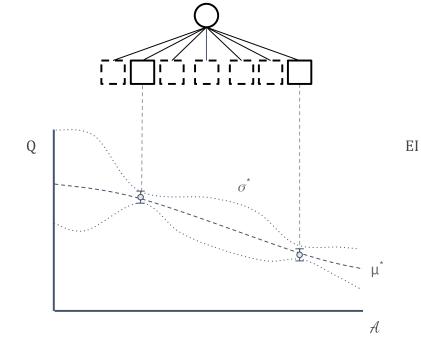
# Continuous Action Spaces BOMCP

#### **Bayesian Optimized Action Branching**



# Continuous Action Spaces BOMCP

#### **Bayesian Optimized Action Branching**



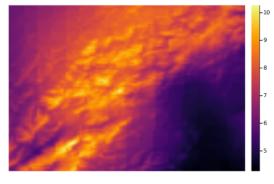
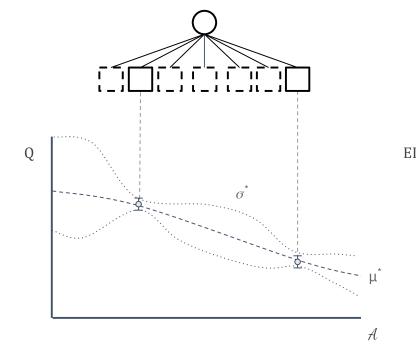


Figure 2: Wind Map. Figure shows wind map for Altamont Pass, CA at  $100\mathrm{m}$  altitude. The colors represent the average annual wind speed in m/s.

# Continuous Action Spaces BOMCP

#### **Bayesian Optimized Action Branching**



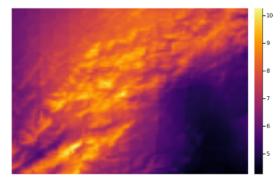
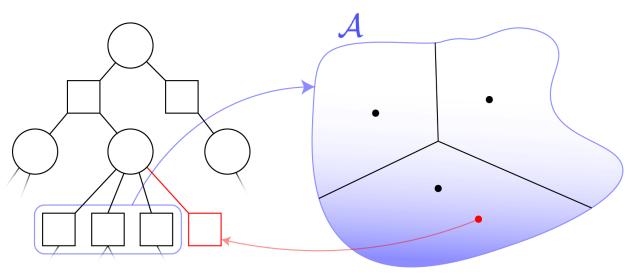


Figure 2: Wind Map. Figure shows wind map for Altamont Pass, CA at 100m altitude. The colors represent the average annual wind speed in m/s.

Algorithm	Queries	Score	Time (seconds)
POMCPOW	10	$15708 \pm 229$	$2.25 \pm 0.07$
	25	$16234 \pm 217$	$4.80 \pm 0.07$
	50	$16374 \pm 212$	$6.27 \pm 0.08$
	100	$16018 \pm 262$	$11.98 \pm 0.07$
	200	$15787 \pm 233$	$20.67 \pm 0.09$
ВОМСР	10	$18095 \pm 183$	$2.55 \pm 0.08$
	25	$18154 \pm 158$	$5.21 \pm 0.07$
	50	$18015 \pm 163$	$6.71 \pm 0.06$
	100	$18225 \pm 119$	$13.39 \pm 0.07$
	200	$18113 \pm 157$	$25.14 \pm 0.08$
Expert	_	$8130 \pm 51$	_

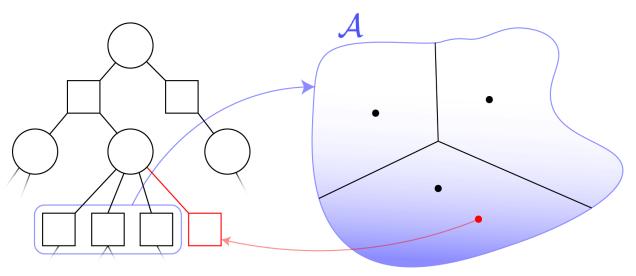
## **Voronoi Progressive Widening**



Online Tree Search Planner

Voronoi Progressive Widening

## Voronoi Progressive Widening



Online Tree Search Planner

Voronoi Progressive Widening

