

# A Spatial AR System for Wide-area Axis-aligned Metric Augmentation of Planar Scenes

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## Abstract

Augmented reality (AR) promises to enable use cases in industrial settings that include the embedding of assembly instructions directly into the scene, potentially reducing or altogether obviating the need for workers to refer to instructions in paper form or on a screen. *Spatial* AR, in turn, is a form of AR whereby the augmentation of the scene is carried out using a projector, with the advantage of rendering the augmentation visible to all onlookers simultaneously without calling for each to wear some form of head-mounted display. In carrying out spatial AR, however, care must be taken to appropriately warp the images to be projected in a manner that they appear free of distortions to the viewer. For planar scene geometry (such as a floor, wall, or table), this can be done in a cumbersome manual process called keystone correction—often using software bundled with the projector—to compute an appropriate corrective image warp.

We propose a spatial AR system for wide-area metric augmentation of planar scene surfaces that produces the effect of keystone correction analytically as a function of the relative geometry of the projector and scene plane, by using a projector equipped with a steerable mirror and a camera facing the scene plane. Our system renders the placement of augmentations in the scene more

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intuitive than manual keystone correction in two ways. First, (i) placement of the desired augmentations is carried out in accordance with the axes of an image of the scene acquired by the camera, thereby making setting those axes as simple as appropriately rotating the camera. Second, (ii) the desired dimensions of the projected augmentations are specified in metric terms, thereby allowing for consistent scaling across all target locations.

*Keywords:* Spatial augmented reality (SAR), computer vision, steerable mirror projector, projector-camera calibration, Industry 4.0

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## 1. Introduction

Augmented reality (AR) [1, 2] promises to enable use cases in industrial settings that include the embedding of assembly instructions directly into the scene [3, 4, 5, 6, 7, 8], potentially reducing or altogether doing away with the  
5 need for workers to refer to instructions in paper form or on a screen. Typically, AR works by embedding the augmentation in an image of the scene acquired from the viewpoint of a single individual, with the resulting augmented image in turn displayed typically using some form of head-mounted display. Reliance on head-mounted displays, however, has two adverse consequences: (i) a head-  
10 mounted display must be worn by each individual wishing to partake in the augmentation, and (ii) such a head-mounted display—in some cases taking the form of a helmet in order to house multiple sensors in support of accurately tracking the viewpoint of the viewer relative to the scene—can be obtrusive. In turn, a form of augmented reality referred to as *spatial* AR[9] is carried out  
15 not by embedding the augmentation in an image of the scene as with a head-mounted display, but by projection to the scene itself, thus eliminating both aforementioned problems. Yet considering a planar surface to be augmented (e.g., a floor, wall, or table), unless the projector faces the surface frontally, the bounds of a projected rectangular image will not appear rectangular, but will  
20 instead be subject to projective distortions. Such distortions can be corrected for by carrying out a cumbersome manual process referred to as keystone correction

to appropriately warp the image to be projected, often using software bundled with the projector.

Our contribution is to propose a wide-area spatial AR system for planar  
25 scenes that produces the effect of keystone correction analytically, free of any  
manual interaction. Most importantly, we do this in a manner placing the axes  
of the augmentation in accordance with the axes of a camera placed to face  
downwards towards the scene plane. This facilitates placement of augmenta-  
tions, since establishing the principal axes of the augmentation thus reduces to  
30 placing the downwards-facing camera in a manner such that the  $X$ - and  $Y$ -axes  
of the image align with the intended  $X$ - and  $Y$ -axes of the augmentation. We  
achieve this by warping the image to be projected using a plane-induced ho-  
mography computed to produce the effect of projecting the image not from the  
actual projector viewpoint, but in accordance with the viewpoint of a *virtual*  
35 projector (i) facing directly downwards to the target location in the scene plane  
and (ii) rotated to place the axes of the virtual projector in accordance with  
those of the camera. Moreover, our system enables specifying the dimensions  
of augmentations in metric terms, which we achieve by placing the virtual pro-  
jector at the appropriate height above the scene plane. Finally, our system set  
40 up to handle a projector equipped with a steerable mirror (without need for  
explicitly modeling the action of the steerable mirror on the projector), thereby  
enabling wide-area factory floor applications exceeding the immediate field of  
view of the projector without needing to rely on multiple projectors.

### 1.1. Related Work

45 An early spatial AR system explicitly using a projector mounted with a  
steerable mirror is the IBM Everywhere Displays prototype of Pinharez [10].  
For the purposes of the prototype, a projector mounted with a steerable mirror  
was set up with a camera to demonstrate a variety of use cases, including col-  
laborative assembly encompassing the projection of assembly instructions and  
50 an interactive projected user interface [11, 12]. The authors, however, carry out  
keystone correction manually, by interactively adjusting for the position and

orientation of a virtual scene plane and a scaling factor and computing a 2D homography accordingly.

More generally, keystone correction for planar scenes can be said to reduce  
 55 to computing a 2D homography [13], an invertible transformation that preserves  
 colinearity and is thus fittingly alternatively referred to as a ‘colineation’; this  
 is the case whether computing the homography relies on manual interaction as  
 in the case of Pinharez, or is obtained free of manual interaction as in ours.  
 The intuition for why it is that a transformation that preserves colinearity—  
 60 i.e., maps lines to lines—can serve to model an appropriate corrective image  
 warp can be drawn from considering a planar chessboard pattern: looking at an  
 image of a chessboard acquired from an oblique angle, one observes that lines  
 parallel in the chessboard appear to meet in respective vanishing points; looking  
 at an image of the same chessboard acquired frontally with respect to the plane  
 65 of the chessboard, lines parallel in the chessboard appear parallel in the image  
 (i.e., they are said to meet ‘at infinity’). To warp the former image (where lines  
 parallel in the scene meet in respective vanishing points) such that the lines of  
 the chessboard appear as in the latter image (where lines parallel in the scene  
 meet at infinity), a transformation that maps lines to lines is sufficient.

70 One way to compute a homography is by identifying at least four corre-  
 spondences between pixel positions in two images of a planar surface [13]. The  
 keystone correction approach of Sukthankar *et al.* [14] reduces to using a seg-  
 mentation approach to identify the four corners of projection screen in an image  
 acquired by a camera, and computing a homography that maps the resulting  
 75 four corners of the projection screen to the four corners of the projector’s image  
 plane. Additional sensors can be used to inform the computation of a homog-  
 raphy; Raskar and Beardsley [15] use a tilt sensor to recover the projector’s  
 gravity vector, which they use to carry out a rotational correction in projecting  
 to a wall. Still another way to compute a homography is as a function of a plane  
 80 and a pair of pinhole cameras; the effect produced by the homography is one  
 of projecting an image to the plane from the viewpoint of the one camera, and  
 acquiring the projected image from the viewpoint of the other. Such a homog-

raphy is said to be ‘induced’ by a plane [13]. We exploit the fact that cameras  
 and projectors alike can be modeled using a pinhole camera model [9], proceed  
 85 to recover the relative geometry relating the scene plane and projector, and  
 compute a particular form of plane-induced homography to effect the intended  
 corrective image warp.

## 2. Approach

Correcting for projective distortions of the sort outlined in Section 1 can  
 90 be achieved by modeling the manner in which the respective rays through the  
 pixels of the projector’s image plane fan out into the scene (i.e., by ‘calibrating’  
 the projector) and the geometry of the scene itself (i.e., by recovering the scene  
 plane relative to the projector) within at least the projector’s field of view. This  
 is because the scene point ‘illuminated’ by a pixel in the projector’s image plane  
 95 can be recovered by intersecting its corresponding ray with the geometry of the  
 scene surface. To model this interaction, we (i) carry out a one-time projector  
 calibration, which in our approach calls for additionally calibrating a camera  
 facing downwards to the scene plane and includes recovery of the scene plane as  
 a convenient side effect. Next, we use the relative camera-projector-scene plane  
 100 geometry to (ii) compute a plane-induced homography that warps the image to  
 be projected in a manner that it appear undistorted to the viewer, and placed  
 in alignment with the axes of a proxy image of the scene. These two points are  
 treated in Sections 2.1 and 2.2, respectively.

### 2.1. Recovering Geometry

Calibration of a projector (or camera) in the sense we employ the term  
 here<sup>1</sup> renders one able to project a scene point  $\mathbf{X} \in \mathbb{R}^3$  to its corresponding  
 pixel  $\mathbf{x} \in \mathbb{R}^2$  in the projector’s (or camera’s) image plane, or to compute the  
 ‘back-projection’ of  $\mathbf{x}$ , i.e., the ray from the projector’s (or camera’s) center  
 of projection through  $\mathbf{x}$  along which a projecting point  $\mathbf{X}$  must lie. Such a

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<sup>1</sup>We are referring to a geometric calibration; not, e.g., to a color calibration.

calibration can be expressed in terms of (i) a  $3 \times 3$  calibration matrix  $\mathbf{K}$  derived from the projector's (or camera's) focal length  $f$  and principal point  $\mathbf{p}_0 = (x_0, y_0)^\top \in \mathbb{R}^2$  [13], and (ii) the coefficients of a lens distortion model used to correct for radial or tangential distortions caused by the lens system [16, 17]; the calibration matrix  $\mathbf{K}$  is then

$$\mathbf{K} = \begin{bmatrix} f & 0 & x_0 \\ 0 & f & y_0 \\ 0 & 0 & 1 \end{bmatrix}, \quad (1)$$

105 where  $f$  and  $(p_x, p_y)^\top$  are both expressed in units of pixels. The calibration matrix  $\mathbf{K}$  models a so-called pinhole camera; such a model is applicable to an image acquired using a real-world camera assuming the image has been corrected for lens distortion effects, by having applied the appropriate lens distortion model coefficients.

Calibrating a camera can be carried out by (i) establishing 2D-3D correspondences between pixels in the camera's image plane and the corresponding points in the scene, and on (ii) using those correspondences as input to an optimization procedure that relies on bundle adjustment [18] to output maximum likelihood estimates of the calibration matrix, the associated lens distortion model coefficients, and, for each calibration image, the pose (i.e., position and orientation) of the camera relative to the 3D scene points from among the 2D-3D correspondences [13, 19]. Calibration images containing a calibration surface such as a chessboard pattern of known dimensions and scale are acquired from varying viewpoints using the camera, to be used to establish the 2D-3D correspondences  $\{\mathbf{x}_{i,j} \leftrightarrow \mathbf{X}_{i,j}\}$ ,  $i \in \{1, \dots, n_{\text{pt}}\}$ ,  $j \in \{1, \dots, n_{\text{im}}\}$ , where  $n_{\text{pt}}$  gives the number of correspondences obtained from one calibration image of the pattern,  $n_{\text{im}}$  the number of such images, and  $\mathbf{X}_{i,j} = \mathbf{X}_{i,j'}$ , for  $j, j' \in \{1, \dots, n_{\text{im}}\}$ . Bundle adjustment is then used to obtain the maximum likelihood estimates  $(\hat{\omega}, \hat{\mathbf{K}}, \{(\hat{\mathbf{R}}_j, \hat{\mathbf{t}}_j)\})$ ,  $j \in \{1, \dots, n_{\text{im}}\}$  of the lens distortion model coefficients  $\omega$ , calibration matrix  $\mathbf{K}$ , and rigid body transformations  $(\mathbf{R}_j, \mathbf{t}_j) \in SE(3)$ ,  $j \in \{1, \dots, n_{\text{im}}\}$  that minimize the cumulative reprojection

tion error

$$\sum_{i=1}^{n_{\text{pt}}} \sum_{j=1}^{n_{\text{im}}} d_{\hat{\omega}}(\mathbf{x}_{i,j}, \hat{\mathbf{x}}'_{i,j}), \quad (2)$$

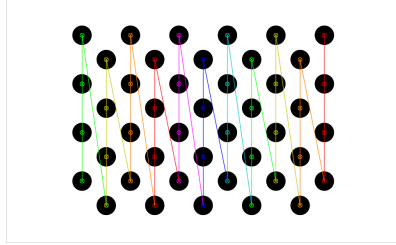
110 where  $\hat{\mathbf{R}}_j \mathbf{X}_{i,j} + \hat{\mathbf{t}}_j \in \mathbb{R}^3$  expresses  $\mathbf{X}_{i,j}$  in the camera coordinate frame of the camera corresponding to the  $j^{\text{th}}$  calibration image and  $(\hat{\mathbf{x}}'_{i,j}, 1)^{\top} \sim \hat{K}(\hat{\mathbf{R}}_j \mathbf{X}_{i,j} + \hat{\mathbf{t}}_j) \in \mathbb{P}^2$  gives the projection  $\hat{\mathbf{x}}'_{i,j} \in \mathbb{R}^2$  in pixels of the point  $\mathbf{X}_{i,j}$  to that image. The function  $d_{\hat{\omega}}$  is a distance function that computes a distance with respect to two pixel positions that it first corrects for lens distortions, in accordance  
 115 with the lens distortion model coefficients  $\hat{\omega}$  [16, 17]. The inverse rigid body transformation  $(\hat{\mathbf{R}}_j^{-1}, -\hat{\mathbf{R}}_j^{-1} \hat{\mathbf{t}}_j) \in SE(3)$  gives the pose of the  $j^{\text{th}}$  camera relative to the 3D scene points of the calibration pattern.

Calibration of a projector can be carried out in precisely the same manner as calibrating a camera insofar as step (ii) is concerned; the major difference in  
 120 projector calibration relative to the calibrating a camera concerns the manner in which 2D-3D correspondences are identified, i.e., between pixels in the image plane of the projector and the corresponding points in the scene [20, 21, 22]. What remains of this section is concerned primarily with the recovery of 2D-3D correspondences in support of calibrating cameras and projectors. A conse-  
 125 quence of the approach we take to identifying the 3D points of the 2D-3D correspondences we use for projector calibration is, for each target location, recovery of the local scene plane.

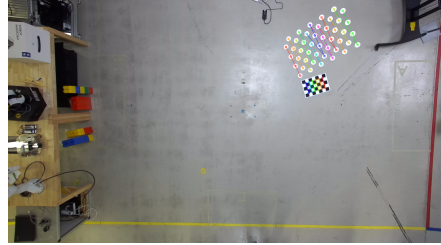
*Camera calibration.* We recover 2D-3D correspondences in support of calibrating the downwards-facing camera by relying on a planar calibration surface to  
 130 automatically identify correspondences between the 3D points on the calibration surface and their 2D correspondences in the image plane. The classical calibration surface is a chessboard pattern. The 3D corner points of the chessboard are obtained *a priori* in a coordinate system defined in the plane of the chessboard<sup>2</sup>, requiring knowledge only of the dimensions of the chessboard pat-

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<sup>2</sup>E.g.,  $(0, 0, 0), (1.5, 0, 0), (3, 0, 0), \dots, (9, 7.5, 0)$  for a chessboard with  $7 \times 6$  corners ( $8 \times 7$  squares), with each square of length and width of 1.5 unit, respectively. Note that the units of



(a) Asymmetrical circle pattern image, in image plane of projector (detections overlain).



(b) Projector calibration image (one for each target location), in image plane of camera (detections overlain).

Figure 1: Recovering 2D positions in support of projector calibration. (a) 2D positions of the 2D-3D correspondences to be used for calibrating the projector are obtained by detecting—in the image plane of the projector—the circle centers in the asymmetrical circle pattern image, to be projected to each of the target locations in the scene plane. (b) For each such target location, an image is acquired from the viewpoint of the camera and the circle centers of the projected asymmetrical circle pattern are detected, in the image plane of the camera. A chessboard pattern to be used for recovering the local scene plane is placed near the projected pattern, whose corners are likewise detected. Detected 2D projected asymmetrical circle pattern circle center points and chessboard corners overlain for illustration.

tern and of the length of a side of a chessboard square. The corresponding 2D  
 135 points are obtained, in the same order, using a specialized algorithm [23]. A set  
 of calibration images is acquired, each with the calibration pattern visible in a  
 different part of the image plane, and such that the center and all corners and  
 edges of the image plane are covered, the camera’s autofocus setting be off, and  
 140 the camera’s zoom factor remain fixed. 2D-3D correspondences are then recov-  
 ered for each calibration image, and the resulting list is passed on as input to  
 an optimization procedure that relies on bundle adjustment to yield the camera  
 calibration matrix  $K_{\text{cam}}$ .

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the chessboard’s 3D points give the units in terms of which the camera calibration is carried  
 out, and—owing to how our projector calibration relies on the camera calibration—the units  
 of the projector calibration as well.



*Projector calibration.* As in camera calibration, we calibrate the projector by relying on 2D-3D correspondences, yet for projector calibration we obtain them by *projecting* a calibration pattern that we detect using the calibrated downwards-facing camera. The pattern we project is one of circles (cf. Figure 1(a)), and we rely on an algorithm to detect the circle center points in the asymmetrical circle pattern in the image plane of the projector [23], giving the 2D positions of our 2D-3D correspondences for calibrating the projector. We project the asymmetrical circle pattern to each of the target locations, and use the calibrated downwards-facing camera to acquire a projector calibration image for each. Given a projector calibration image acquired using camera, we detect the circle centers of the *projected* asymmetrical circle pattern (cf. Figure 1(b)); given the scene plane (the recovery of which we shall return to in the paragraph that follows) and such a 2D circle center  $\mathbf{x}$ , we obtain its 3D correspondence by intersecting the back-projection  $\mathbf{K}_{\text{cam}}^{-1}(\mathbf{x}^\top, 1)^\top \in \mathbb{P}^2$  of  $\mathbf{x}$  with the recovered scene plane (cf. Figure 2). Since the algorithm that yields 2D circle centers does so in a consistent ordering, we thus obtain the 2D-3D correspondences between the projector’s image plane and the scene required for projector calibration, yielding the projector calibration matrix  $\mathbf{K}_{\text{proj}}$ .

We recover the scene plane via spatial resection by applying a PnP algorithm [24] to the 2D-3D correspondences obtained using a chessboard pattern. Note that this step is separate from camera calibration, yet could well be carried out using the same calibration pattern used in the camera calibration step.<sup>3</sup> While a single image of such a chessboard pattern placed on the floor could be sufficient if the floor is even, we place a chessboard pattern in close proximity to the projected asymmetrical circle pattern in each projector calibration image in order to recover the scene plane locally to each target location, in order to account for the possibility of an uneven floor (cf. Figure 1(b)). Note that in principle, we could project a chessboard pattern instead of an asymmetrical circle pat-

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<sup>3</sup>The critical point is that the pattern should ideally be coplanar with the local scene plane, meaning its height above the scene plane should not exceed a few millimeters.

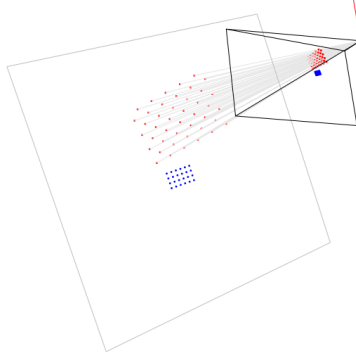


Figure 2: Scene plane (gray) recovered via spatial resection with respect to 2D-3D correspondences obtained using a chessboard pattern (blue); 3D circle center points of the asymmetrical circle pattern—i.e., the 3D positions of the 2D-3D correspondences to be used for calibrating the projector—obtained by intersection with the scene plane of back-projections (likewise gray) of the 2D circle center points of the asymmetrical circle pattern detected in the image plane (red). Note that as in the figures of this section that follow, the rendering in the figure corresponds to the projection calibration image in Figure 1(b), acquired by the downwards-facing camera (frustum of the camera in black, with up vector in red).

tern to obtain the 2D-3D correspondences needed for projector calibration; it is, however, because we rely on detecting the corners of a chessboard pattern to recover the scene plane that we opt instead for a alternative pattern.

175 The pose of the projector, for each projector calibration image, is provided relative to the 3D points of the pattern—and thus in the coordinate frame of the camera—alongside  $K_{\text{proj}}$  by the aforementioned optimization procedure. Note that for a fixed projector with steerable mirror, given a projector calibration image, the recovered projector’s pose is the pose the projector would have to  
 180 have had to project to the given target location *in the absence of the mirror*. This is sufficient for our needs in Section 2.2, and it is in this sense that our system is able to handle a projector equipped with a steerable mirror, without need for modeling the steerable mirror explicitly.

## 2.2. Correcting for Projective Distortion

185 If the projector is calibrated and its pose relative to the scene plane is known, a ‘virtual’ projector (with the same calibration  $K$  and lens distortion model coef-

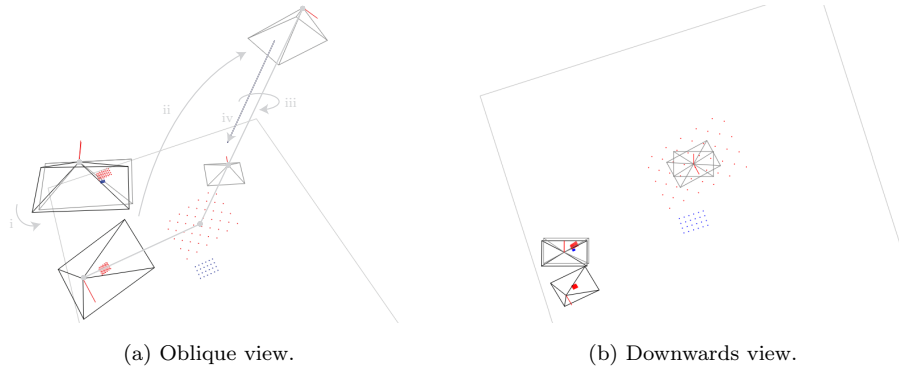


Figure 3: The virtual camera is obtained by (i) rotating the camera (top left, black) about its center of projection such that its optical axis be made parallel with the normal vector of the scene plane. The virtual projector is obtained by (ii) rotating the projector (bottom left, black) about the point of intersection of its optical axis with the scene plane such that the optical axis be made parallel with the scene plane’s normal vector, (iii) rotating the  $X$ - and  $Y$ -axes to align them with those of the virtual camera, and (iv) translating along the normal direction to achieve the desired metric projected image dimensions.

ficients) can be placed elsewhere relative to the scene plane. If we for a moment imagine that the projector—at its recovered pose—functions as a camera,<sup>4</sup> then (i) projecting an image to the scene plane *from the viewpoint of the virtual pro-*  
190 *jector* and (ii) acquiring the resulting projected image from the viewpoint of the recovered projector gives the desired corrective warp. Projecting an image warped in this manner to the scene plane *from the viewpoint of the recovered projector* then has the same effect as projecting the original image to the scene plane from the viewpoint of the virtual projector. This warp can be effected  
195 using a plane-induced homography, computed analytically as a function of the scene plane, the projector, and the virtual projector.

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<sup>4</sup>Recall that the calibration matrix  $K$  enables computing both (i) the projection of a scene point to the image plane (the function of a camera), or (ii) the back-projection of a pixel in the image plane, giving a ray into the scene (along which a projector illuminates the scene with the given pixel).

*Virtual projector.* The placement of the virtual projector is to determine from which pose the image to be projected is to *appear* to have been projected. We carry out this placement according to a small handful of steps. First, we (i) rotate the camera about its center of projection to align its optical axis<sup>5</sup> with the normal vector of the scene plane, giving a virtual camera likewise facing directly<sup>6</sup> downwards to the scene plane (cf. Figure 3). Next, we (ii) intersect the scene plane with the optical axis (i.e., the ray from the projector’s center of projection through the center of the image plane) and rotate the projector’s placement about that point of intersection, aligning the optical axis with the scene plane’s normal vector and giving an initial virtual projector. Finally, we (iii) align the  $X$ - and  $Y$ -axes of the initial virtual projector with those of the virtual camera, which gives the virtual projector (cf. again Figure 3). The virtual projector is thus rendered fronto-parallel with the scene plane, enabling projection to the scene plane absent of projective distortions. We additionally (iv) adjust the height above the scene plane of the virtual projector, in order to satisfy desired projected image dimensions provided in metric units.

Owing to the manner in which we place the virtual projector, the virtual projector’s axes and thus the augmentation are aligned with the axes of the downwards-facing camera; the placement of the camera thereby intuitively determines the principal axes according to which augmentations are to be placed. Note further that a consequence of placing the virtual projector by rotating about the point of intersection of the projector’s optical axis with the scene plane is that *the center of the projector’s image plane remains invariant* to the placement of the virtual projector, i.e., a steerable mirror can be aimed with respect to a point projected from the center of the projector’s image plane,

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<sup>5</sup>Strictly speaking, the optical axis is the back-projection of the principal point; in our usage, we understand it to refer to the back-projection of the center of the image to be projected.

<sup>6</sup>A physical camera placed to face downwards is almost certain to not face downwards precisely; in contrast, the virtual camera’s optical axis is aligned exactly with the scene plane’s normal vector, rendering it genuinely fronto-parallel with respect to the scene plane.

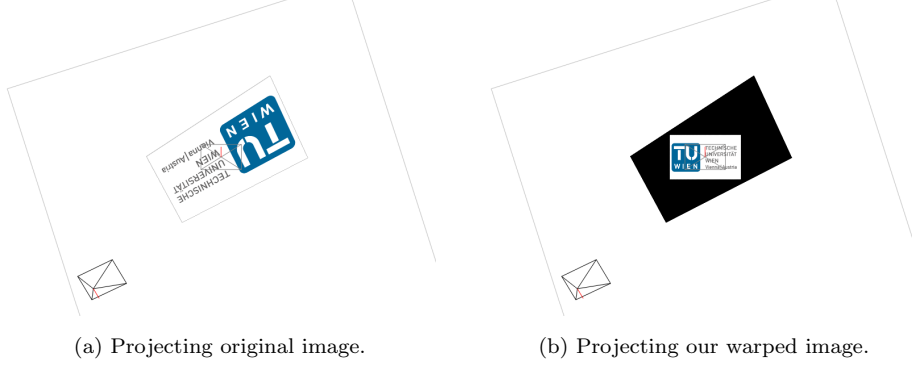


Figure 4: Projection to the scene plane from the recovered projector viewpoint (bottom left, black; virtual projector in center, gray) of the original image and of the warped image. (a) Projecting the original image to the scene plane. (b) After warping the original image according to our plane-induced homography for the given target location, the image is projected in a manner that appears free of projective distortions, aligned with the axes of the virtual camera (via the virtual projector), and to have the desired dimensions in the scene plane, expressed in metric units. Note that unprojected background is shown set to black.

further facilitating placement of augmentations.

*Plane-induced homography.* Let  $K_{\text{proj}}$  express the calibration matrix of the recovered projector and  $(R, \mathbf{t}) \in SE(3)$  the rigid body transformation that transforms points from the coordinate frame of the recovered projector to that of the virtual projector, for a given target location. Moreover, let  $(\mathbf{n}^\top, -d)^\top$  give the scene plane, expressed in the coordinate frame of the recovered projector, where  $\mathbf{n} \in \mathbb{R}^3$  is the scene plane’s normal vector and  $d = \mathbf{n}^\top \mathbf{X}$  for any point  $\mathbf{X}$  in the plane, so that  $(\mathbf{n}^\top, -d)(\mathbf{X}^\top, 1)^\top = 0$ . The transformation that warps the image to be projected to the scene plane by the recovered projector such that it appear as if were projected to the scene plane by the virtual projector (cf. Figure 4(b)) is given the by the  $3 \times 3$  matrix

$$H = K_{\text{proj}} \left( R - \frac{\mathbf{t}\mathbf{n}^\top}{d} \right) K_{\text{proj}}^{-1}, \quad (3)$$

a form of ‘plane-induced’ 2D homography [13]. For convenience, we enable optional rotation of the image to be projected *before* applying  $H$ , about the

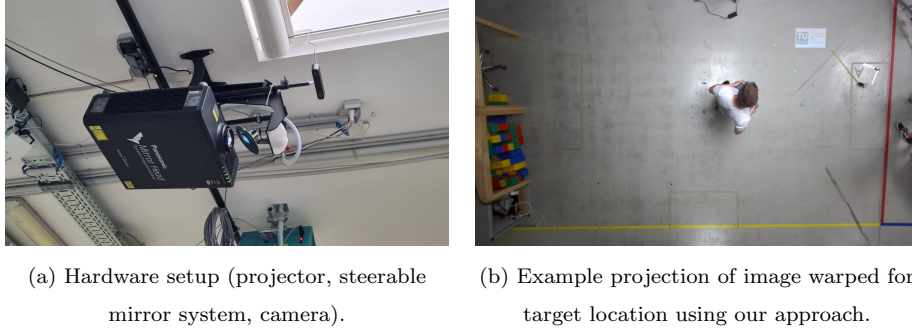


Figure 5: Evaluation scenario. (a) Our hardware setup, comprised of a Panasonic PT-RZ660BE projector, a steerable mirror system manufactured by Dynamic Projection Institute, and a Stereolabs Zed 2 stereo camera, of which we used only the left view. (b) Example augmentation produced by projecting—to one of our 15 target locations—an image warped using our approach, as seen from the downwards-facing camera. Note that the warp places the axes of the augmentation in accordance with the axes of the camera, and that the dimensions of the augmentation are in line with the desired target dimensions ( $50 \text{ cm} \times 31.25 \text{ cm}$ ). Corners of the full projected image extent projected to the floor in light green.

image center; that rotation, parameterized in degrees, is thus in effect likewise carried out intuitively in accordance with the placement of the camera.

### 3. Evaluation

We evaluate our approach by using a  $960 \text{ pixel} \times 600 \text{ pixel}$  image of the TU Wien logo (cf. Figure 4) to augment 15 locations across the floorspace at the Pilotfabrik<sup>7</sup> of TU Wien, a collaborative space for research on Industry 4.0 topics situated in Vienna, Austria. We contrast our approach with a baseline approach involving manual keystone correction, by aiming with both approaches to place the same image for each location aligned with the principal axes of the floorspace, absent of projective distortions, and with the same metric dimensions of  $50 \text{ cm} \times 31.25 \text{ cm}$ <sup>8</sup>. All experiments were carried out by the same technician,

<sup>7</sup><https://www.pilotfabrik.at/>

<sup>8</sup>The dimensions in pixels of the image we project are  $960 \times 600$ ; we chose for our experiments to set the projected metric length of the horizontal axis of the image to 50 cm, which

experienced in both approaches.

The hardware setup employed in the evaluation (cf. Figure 5(a)) comprised a Panasonic PT-RZ660BE projector with a steerable mirror system—used in our experiments to point the projection to each of the 15 locations—manufactured  
240 by Dynamic Projection Institute [7, 8]. The steerable mirror system was bundled with the MDC-X software for steering the mirror, loading imagery, and optionally carrying out manual keystone correction, such that each position and (warped) image can be registered as a preset. In addition, we used a downwards-facing Zed 2 stereo camera manufactured by Stereolabs, yet relied only on the  
245 left view. The floorspace used for our experiments measured dimensions of ca. 6 m  $\times$  4 m; the projector was mounted at approximately the center of this space, at a height of ca. 3.5 m.

*Manual approach.* Having pointed the steerable mirror to the desired location, manual keystone correction using the MDC-X software involves warping the  
250 image to be projected by manipulating the corners of the image until the desired effect is produced on the projection surface. In order to provide a template for manually carrying out keystone correction, we prepared a 50 cm  $\times$  31.25 cm piece of cardboard. For each target location, we placed this piece of cardboard in a manner that its axes were aligned with the principal axes of the scene (cf.  
255 the yellow and red lines in Figure 5(b)); we then manually warped the image for the given target location so that any corner of the augmentation deviated by at most 1 cm from the corresponding corner of the template. End-to-end, the process of setting the presets in the MDC-X software having carried out keystone correction manually took ca. 32 min for the 15 target locations.

260 *Our approach.* We began by carrying out a calibration of the camera, acquiring 10 camera calibration images (cf. Section 2.1) of a chessboard calibration pattern with 6  $\times$  4 corners (7  $\times$  5 squares) and feeding the images as input to our camera calibration module. Separately, for each of the 15 target locations,

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implies 31.25 cm for the vertical axis if aspect ratio is to be preserved.

we produced a projector calibration image (cf. again Section 2.1) by projecting  
 265 a  $11 \times 4$  asymmetrical circle pattern image to the location in question using  
 the steerable mirror, placing a chessboard pattern beside the projected pattern,  
 and acquiring the image using the downwards-facing camera. We then fed these  
 images alongside the output of the camera calibration module to our projec-  
 tor calibration module. For each of the target locations, the steerable mirror  
 270 was made to point to that location, the asymmetrical circle pattern image was  
 projected to the scene plane, an image was acquired using the camera, and  
 the location was registered in the MDC-X software as a preset. The output  
 of the projector calibration module is a homography per input projector cali-  
 bration image (cf. Section 2.2). Next, we warped the images to be projected  
 275 to the respective locations using their corresponding homography, using a third  
 dedicated custom module. These warped images were finally imported into  
 the MDC-X software and associated with their respective location presets (cf.  
 Figure 5(b)).

The total amount of time to carry out all the above steps amounted to ca.  
 280 20 min, with ca. 2 min going to acquisition of the camera calibration images,  
 and ca. 5 min going to that of projector calibration images. The remainder of  
 the time was spent running our modules or working with the MDC-X software.  
 Note that once the camera is calibrated, that calibration can be reused if the  
 camera’s intrinsics remain fixed, in particular if no change is made to the zoom  
 285 factor of the camera.

#### 4. Conclusion

We presented a spatial AR system for planar scenes that produces the effect  
 of keystone correction analytically, in a manner that enables intuitive place-  
 ment the augmentations in accordance with the axes of an image of the scene  
 290 acquired by a downwards-facing camera, and such that the desired dimensions  
 of augmentations can be specified in metric terms. Moreover, we showed our  
 system to be able to handle a projector equipped with a steerable mirror, en-



abling factory floor augmentation exceeding the bounds of the projector’s own  
immediate field of view. Our evaluation demonstrated our approach to produce  
295 compelling results at less time than the more cumbersome traditional manual  
approach to keystone correction.

A natural extension of this work would be to address non-planar scenes.  
To handle non-planar scenes would call for a change in how scene geometry  
is recovered and how warping of the image to be projected is carried out; the  
300 methodology we proposed for projector calibration could, however, be left un-  
changed.

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## References

- [1] D. Van Krevelen, R. Poelman, A survey of augmented reality technologies,  
applications and limitations, *International Journal of Virtual Reality* 9 (2)  
(2010) 1–20.
- 310 [2] F. Zhou, H. B.-L. Duh, M. Billinghurst, Trends in augmented reality track-  
ing, interaction and display: A review of ten years of ISMAR, in: 2008 7th  
IEEE/ACM International Symposium on Mixed and Augmented Reality,  
IEEE, 2008, pp. 193–202.
- [3] S. Schlund, W. Mayrhofer, P. Rupprecht, Möglichkeiten der Gestaltung  
315 individualisierbarer Montagearbeitsplätze vor dem Hintergrund aktueller  
technologischer Entwicklungen, *Zeitschrift für Arbeitswissenschaft* 72 (4)  
(2018) 276–286.

- 320 [4] T. Masood, J. Egger, Augmented reality in support of industry 4.0—  
implementation challenges and success factors, *Robotics and Computer-  
Integrated Manufacturing* 58 (2019) 181–195.
- [5] M. Gattullo, G. W. Scurati, M. Fiorentino, A. E. Uva, F. Ferrise, M. Borde-  
goni, Towards augmented reality manuals for industry 4.0: A methodology,  
*Robotics and Computer-Integrated Manufacturing* 56 (2019) 276–286.
- 325 [6] A. E. Uva, M. Gattullo, V. M. Manghisi, D. Spagnulo, G. L. Cascella,  
M. Fiorentino, Evaluating the effectiveness of spatial augmented reality  
in smart manufacturing: a solution for manual working stations, *The In-  
ternational Journal of Advanced Manufacturing Technology* 94 (1) (2018)  
509–521.
- 330 [7] P. Rupprecht, H. Kueffner-McCauley, S. Schlund, Information provision  
utilizing a dynamic projection system in industrial site assembly, *Procedia  
CIRP* 93 (2020) 1182–1187.
- [8] P. Rupprecht, H. Kueffner-McCauley, M. Trimmel, S. Schlund, Adaptive  
spatial augmented reality for industrial site assembly, *Procedia CIRP*.
- 335 [9] O. Bimber, R. Raskar, *Spatial Augmented Reality: Merging Real and Vir-  
tual Worlds*, AK Peters/CRC Press, 2019.
- [10] C. Pinhanez, The everywhere displays projector: A device to create ubiqui-  
tous graphical interfaces, in: *International Conference on Ubiquitous Com-  
puting*, Springer, 2001, pp. 315–331.
- 340 [11] R. Kjeldsen, C. Pinhanez, G. Pingali, J. Hartman, T. Levas, M. Podlaseck,  
Interacting with steerable projected displays, in: *Proceedings of Fifth IEEE  
International Conference on Automatic Face Gesture Recognition*, IEEE,  
2002, pp. 402–407.
- [12] C. Pinhanez, R. Kjeldsen, A. Levas, G. Pingali, M. Podlaseck,  
N. Sukaviriya, Applications of steerable projector-camera systems, in: *Pro-*

- 345       ceedings of the IEEE International Workshop on Projector-Camera Sys-  
           tems at ICCV 2003, 2003.
- [13] R. I. Hartley, A. Zisserman, Multiple View Geometry in Computer Vision,  
       2nd Edition, Cambridge University Press, ISBN: 0521540518, 2004.
- [14] R. Sukthankar, R. G. Stockton, M. D. Mullin, Smarter presentations: Ex-  
 350       ploiting homography in camera-projector systems, in: Proceedings Eighth  
       IEEE International Conference on Computer Vision (ICCV), Vol. 1, IEEE,  
       2001, pp. 247–253.
- [15] R. Raskar, P. Beardsley, A self-correcting projector, in: Proceedings of the  
       2001 IEEE Computer Society Conference on Computer Vision and Pattern  
 355       Recognition (CVPR), Vol. 2, IEEE, 2001, pp. II–II.
- [16] D. C. Brown, Close-range camera calibration, Photogrammetric Engineer-  
       ing 37 (8) (1971) 855–866.
- [17] J. Weng, P. Cohen, M. Herniou, et al., Camera calibration with distortion  
       models and accuracy evaluation, IEEE Transactions on Pattern Analysis  
 360       and Machine Intelligence 14 (10) (1992) 965–980.
- [18] B. Triggs, P. F. McLauchlan, R. I. Hartley, A. W. Fitzgibbon, Bundle  
       adjustment—a modern synthesis, in: International Workshop on Vision  
       Algorithms, Springer, 1999, pp. 298–372.
- [19] Z. Zhang, A flexible new technique for camera calibration, IEEE Transac-  
 365       tions on Pattern Analysis and Machine Intelligence 22 (11) (2000) 1330–  
       1334.
- [20] D. Moreno, G. Taubin, Simple, accurate, and robust projector-camera cal-  
       ibration, in: 2012 Second International Conference on 3D Imaging, Model-  
       ing, Processing, Visualization & Transmission, IEEE, 2012, pp. 464–471.
- 370 [21] X. Zhang, L. Zhu, Projector calibration from the camera image point of  
       view, Optical Engineering 48 (11) (2009) 117208.

- [22] S. Zhang, P. S. Huang, Novel method for structured light system calibration, *Optical Engineering* 45 (8) (2006) 083601.
- [23] G. Bradski, The OpenCV library, *Dr. Dobb's Journal of Software Tools* 25 (2000) 120–125.
- [24] T. Collins, A. Bartoli, Infinitesimal plane-based pose estimation, *International Journal of Computer Vision* 109 (3) (2014) 252–286.