

Seeing is NOT Always Believing

Our lives are filled with electronic signs that display time, temperature, or a game score; however, what we see is not always what is really happening.

Most displays cycle through individual display signals so that only one display is on at a time.

The cycle speed is so fast that the human eye perceives all signals are on all at once.

Multiplexers and Demultiplexers can be used to control this.

2's Complement Arithmetic

Binary Addition

Single Bit Addition:

$$\begin{array}{r} \text{Carry} \\ 0 \ 0 \ 1 \ 1 \\ + 0 \ 1 \ 0 \ 1 \\ \hline 0 \ 1 \ 1 \ 10 \end{array}$$

Multiple Bit Addition:

$$\begin{array}{r} 6 \ 0110 \\ + 3 \ 0011 \\ \hline 9 \ 1001 \end{array}$$

Negative Numbers?

Digital Electronics requires frequent addition and subtraction of numbers.

A subtractor is not needed with the 2's complement system.

The 2's complement system allows you to easily calculate a positive number and its negative equivalent.

Since subtracting one number from another is the same

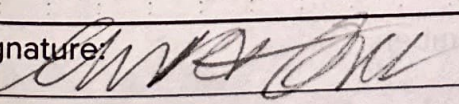
as adding one number negative and adding, a subtractor is not needed.

How to create a negative number?

In Digital Electronics, you cannot simply put a negative sign in front of a number to make it negative.

You must represent a negative number in a fixed-length binary number system. All digital arithmetic must be performed in a fixed-length system.

A physical fixed-length device (adding memory) contains a fixed number of bits (usually 4-bits, 8-bits, 16-bits) to hold the number.

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3-Digit Decimal Number System

A bicycle odometer with only three digits is an example of a Fixed-length system

The problem is without a negative sign, you cannot tell the difference between a +998 from a -2

Note: Car odometers do not work this way

Negative Decimal

Cut the number system in half

Use 001-999 to represent positive

units

Use 000-999 to represent negative

units

"Odometer" math examples

$$\begin{array}{r}
 3 \\
 + 2 \\
 \hline
 5
 \end{array}
 \quad
 \begin{array}{r}
 003 \\
 + 002 \\
 \hline
 005
 \end{array}
 \quad
 \begin{array}{r}
 6 \\
 + (-3) \\
 \hline
 3
 \end{array}
 \quad
 \begin{array}{r}
 006 \\
 + 997 \\
 \hline
 1003
 \end{array}
 \quad
 \begin{array}{r}
 -5 \\
 + 2 \\
 \hline
 (-3)
 \end{array}
 \quad
 \begin{array}{r}
 998 \\
 + 002 \\
 \hline
 999
 \end{array}$$

Complex Problems

How do we easily convert a number into it's negative equivalent?

Counting backwards is not too easy for large numbers.

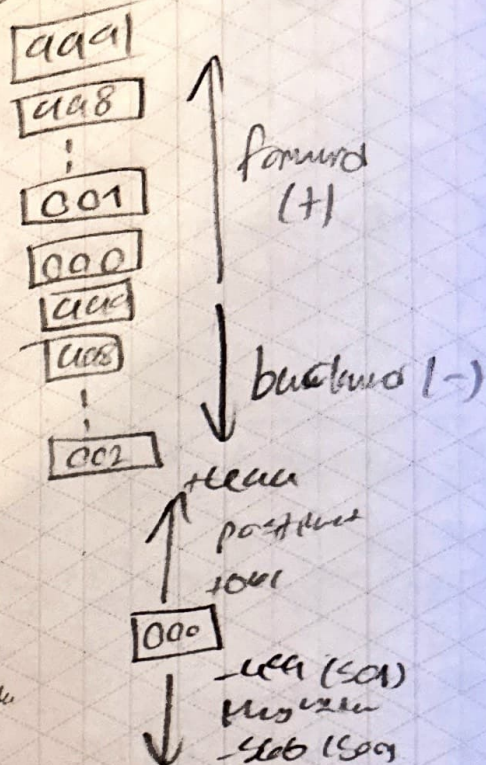
10's Complement System

Uses base - 10 (decimal) numbers

Complement all of the digits in a number

- A digit's complement is the number you add to the digit to make it equal the largest digit in the base.

Add 1.



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10's Example 1

$$\begin{array}{r} -003 \\ \downarrow \downarrow \downarrow \\ \text{cell 6} \\ + \quad 1 \\ \hline \text{cell 7} \end{array}$$

2's Example 1

$$\begin{array}{r} -214 \\ \downarrow \downarrow \downarrow \\ 785 \\ + \quad 1 \\ \hline 786 \end{array}$$

S = 00000101
 $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$
 11111010
 + 1
 S = 11111011

8-Bit Binary System

Apply to binary numbers.

Use 00000001 - 01111111 for positive values

Use 10000000 - 11111111 for negative values

Sign Bit

The MSB is (0) for all positive values.

The MSB is (1) for all negative values.

In a signed number system, this allows you to directly observe the sign of a number.

2's Complement Process

1. Complement all digits of a number
2. Add 1

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