February 25, 2024

1 Auswertung Versuch 234

```
[1]: %matplotlib inline
import numpy as np
import matplotlib.pyplot as plt
from scipy.optimize import curve_fit
from scipy.stats import chi2
from tabulate import tabulate
```

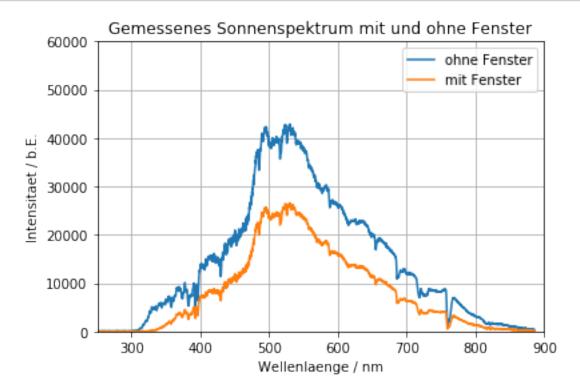
2 Himmelsmessungen

2.0.1 Import & Formatierung der Messungen

2.0.2 Vergleich der Spektren

```
[5]: plt.plot(lamb_og, inten_og, label='ohne Fenster')
   plt.plot(lamb_mg, inten_mg, label='mit Fenster')
   plt.title('Gemessenes Sonnenspektrum mit und ohne Fenster')
   plt.xlabel('Wellenlaenge / nm')
   plt.ylabel('Intensitaet / b.E.')
   plt.legend()
   plt.grid()
   plt.ylim((0,60000))
```

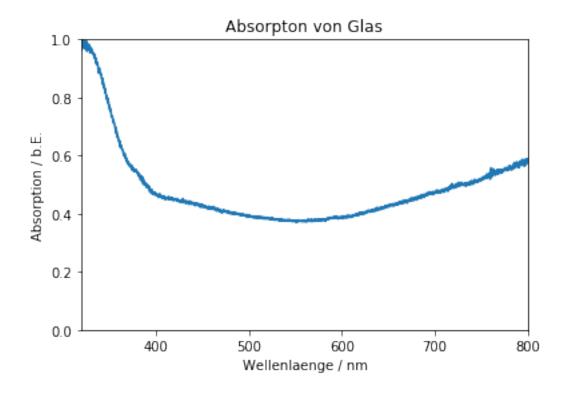
```
plt.xlim((250,900))
plt.savefig("./output/Himmel_m_o_G.pdf", format="pdf")
```



2.0.3 Absorption vom Glas

```
[6]: A=1-inten_mg/inten_og

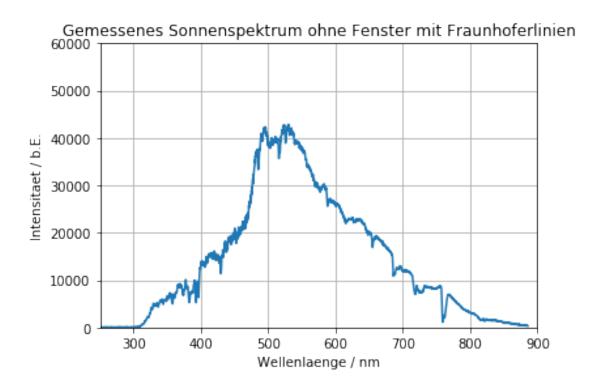
plt.plot(lamb_mg, A)
plt.title('Absorpton von Glas')
plt.xlabel('Wellenlaenge / nm')
plt.ylabel('Absorption / b.E.')
plt.ylim((0,1))
plt.xlim((320,800))
plt.savefig("./output/Absorption_Glas.pdf", format="pdf")
```



2.0.4 Fraunhofer Linien

```
[7]: plt.plot(lamb_og, inten_og)
    plt.title('Gemessenes Sonnenspektrum ohne Fenster mit Fraunhoferlinien')
    plt.xlabel('Wellenlaenge / nm')
    plt.ylabel('Intensitaet / b.E.')
    plt.grid()
    plt.ylim((0,60000))
    plt.xlim((250,900))
```

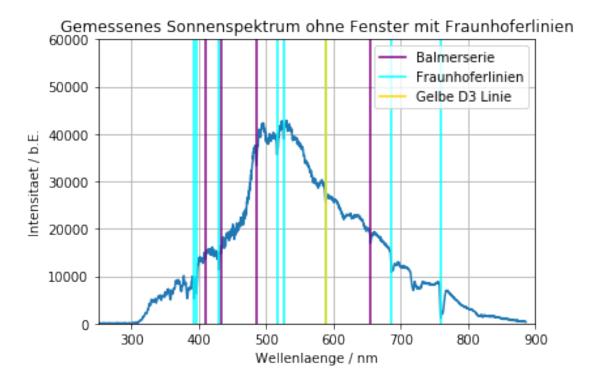
[7]: (250, 900)



```
[8]: balmer=np.array([655.1, 485.2, 433.4, 409.7])
balmererr=np.array([0.5, 0.5, 0.5, 0.5])
fraunh=np.array([759.3, 686.0, 588.2, 525.8, 515.9, 429.8, 396.5, 393.0])
fraunherr=np.array([0.5, 0.5, 0.5, 1.0, 1.0, 0.5, 0.5, 0.5])

litbalmer=np.array([656.3, 486.1, 434.0, 410.1])
litfraunh=np.array([759.4, 686.7, 587.6, 527.0, 518.4, 430.8, 396.8, 393.4])
```

```
[9]: plt.plot(lamb_og, inten_og)
     plt.title('Gemessenes Sonnenspektrum ohne Fenster mit Fraunhoferlinien')
     plt.xlabel('Wellenlaenge / nm')
     plt.ylabel('Intensitaet / b.E.')
     for i in range(0, len(balmer)-1):
         plt.axvline(x=balmer[i], color='purple')
     plt.axvline(x=balmer[3], color='purple', label='Balmerserie')
     for i in range(0, len(fraunh)-1):
         plt.axvline(x=fraunh[i], color='cyan')
     plt.axvline(x=fraunh[7], color='cyan', label='Fraunhoferlinien')
     plt.axvline(x=fraunh[2], color='gold', label='Gelbe D3 Linie')
     plt.legend()
     plt.grid()
     plt.ylim((0,60000))
     plt.xlim((250,900))
     plt.savefig("./output/Fraunhoferlinien.pdf", format="pdf")
```



```
[10]: #Signifikanztest
sigmaBalmer = abs(balmer-litbalmer) / balmererr
sigmaFraunh = abs(fraunh-litfraunh) / fraunherr
print(sigmaBalmer)
print(sigmaFraunh)
```

[2.4 1.8 1.2 0.8] [0.2 1.4 1.2 1.2 2.5 2. 0.6 0.8]

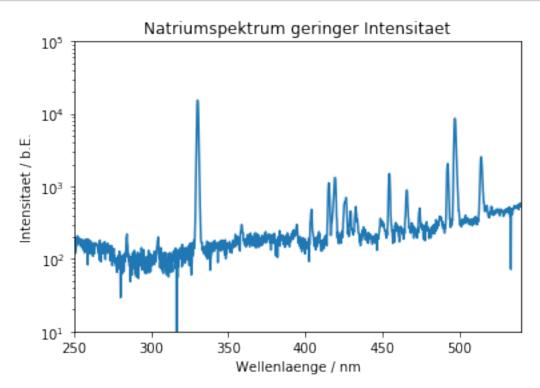
3 Natriumspektrum

3.0.1 Bereich: 400 - 540nm

```
[11]: lamb_low_full, inten_low_full=np.loadtxt('./data/400-540 full.txt', skiprows=14, converters= {0:comma_to_float, 1:comma_to_float}, comments='>', unpack=True)
```

```
[12]: #%matplotlib ipympl
    plt.plot(lamb_low_full, inten_low_full)
    plt.title('Natriumspektrum geringer Intensitaet')
    plt.xlabel('Wellenlaenge / nm')
    plt.ylabel('Intensitaet / b.E.')
    plt.yscale('log')
    plt.ylim((10,100000))
```

```
plt.xlim((250,540))
plt.savefig("./output/NA_low_full.pdf", format="pdf")
```



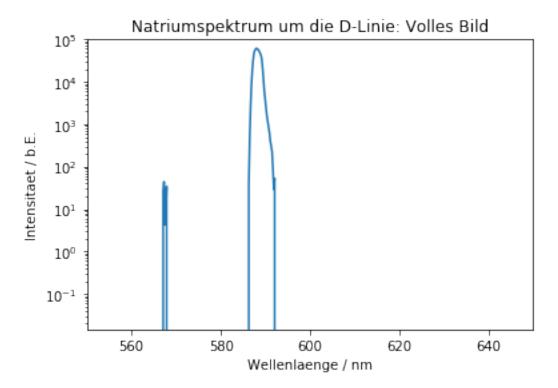
```
[13]: #Gemessene Linien:
NaLow=np.array([284.2, 304.3, 329.8, 404.0, 415.2, 419.2, 426.2, 429.3, 432.8, 449, 454.4, 465.8, 474.2, 492.2, 496.9, 514.1, 517.3])
NaLowErr=np.array([0.6, 0.9, 1.5, 0.5, 0.7, 1.0, 1.2, 0.5, 1.0, 3, 0.7, 1.0, 0. 7, 1.0, 1.7, 1.3, 1.0])
```

3.0.2 Bereich: D-Linie

```
[14]: lamb_d_full, inten_d_full=np.loadtxt('./data/natrium d linie full.txt', u ⇒skiprows=14, converters= {0:comma_to_float, 1:comma_to_float}, comments='>', unpack=True)
```

```
[44]: plt.plot(lamb_d_full, inten_d_full)
    plt.title('Natriumspektrum um die D-Linie: Volles Bild')
    plt.xlabel('Wellenlaenge / nm')
    plt.ylabel('Intensitaet / b.E.')
    plt.yscale('log')
    plt.ylim((0,100000))
    plt.xlim((550,650))
```

```
plt.savefig("./output/NA_D_full.pdf", format="pdf")
```



```
[16]: #gemessene Linien
NaDFull=np.array([567.2, 588])
NaDFullErr=np.array([0.6, 5])
```

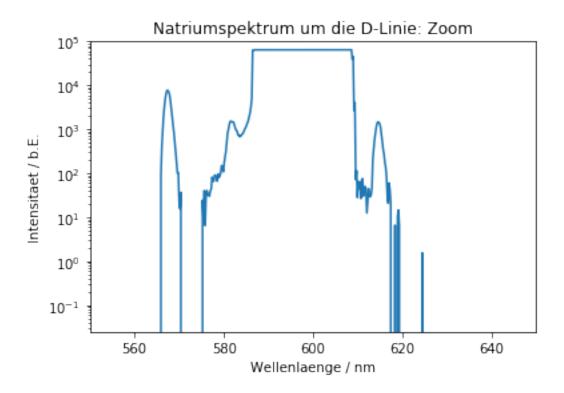
```
[17]: lamb_d_zoom, inten_d_zoom=np.loadtxt('./data/natrium d linie zoom.txt', u

→skiprows=14,

converters= {0:comma_to_float, 1:comma_to_float},

comments='>', unpack=True)
```

```
[18]: plt.plot(lamb_d_zoom, inten_d_zoom)
    plt.title('Natriumspektrum um die D-Linie: Zoom')
    plt.xlabel('Wellenlaenge / nm')
    plt.ylabel('Intensitaet / b.E.')
    plt.yscale('log')
    plt.ylim((0,100000))
    plt.xlim((550,650))
    plt.savefig("./output/NA_D_zoom.pdf", format="pdf")
```

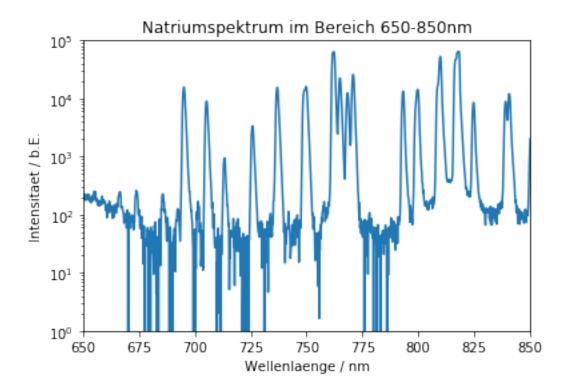


```
[19]: #gemessene Linien
NaDZoom=np.array([567, 614.5])
NaDZoomErr=np.array([3, 1.3])
```

3.0.3 Bereich: 650 - 800nm

```
[20]: lamb_high, inten_high=np.loadtxt('./data/natrium 650-850.txt', skiprows=14, converters= {0:comma_to_float, 1:comma_to_float}, comments='>', unpack=True)
```

```
[21]: plt.plot(lamb_high, inten_high)
   plt.title('Natriumspektrum im Bereich 650-850nm')
   plt.xlabel('Wellenlaenge / nm')
   plt.ylabel('Intensitaet / b.E.')
   plt.yscale('log')
   plt.ylim((1,100000))
   plt.xlim((650,850))
   plt.savefig("./output/NA_high.pdf", format="pdf")
```



[22]: #gemessene Linien
NaHigh=np.array([694.9, 705.0, 713.1, 725.6, 736.6, 749.4, 761.7, 764.8, 768.2, □ →770.8, 793.2, 799.6, 809.7, 817.9, 824.5, 839.0, 840.7])
NaHighErr=np.array([2.0, 1.8, 1.2, 1.4, 2.0, 1.7, 1.2, 1.0, 0.8, 1.3, 1.2, 1.5, □ →2.0, 2.2, 0.8, 1.2, 1.3])

3.0.4 Erwartete Linien 1.NS

```
[23]: #Berechnung von E_3p

#Verwende gemessene Linie NaHigh[13] = 817,9 und m=3

E_Ry = -13.605 #eV

hc = 1.2398 * 10**3 #nm eV

E_3p = (E_Ry / 9) - (hc / 817.9)

#Fehler:

dE_3p = (hc / 817.9**2) * NaHighErr[13]

print(E_3p, dE_3p)
```

-3.027499898113054 0.0040773115407532114

```
[24]: NS1 = [] #Array, in dem alle erwarteten Linien mit Qunatenzahl und Fehler⊔

→ gespeichert Werden

NS11 = [] #Array mit nur den Linien
```

```
NS11Err = [] #Array mit nur den Fehlern
      for m in range (3,13):
          l=1.2398E3/(-13.605/m**2-E_3p)
          print('m={m:2d}, lambda={1:6.2f}'.format(m=m,l=1))
          dl = abs(1.2398E3/((-13.605/m**2-E_3p)**2) * dE_3p)
          a = (m, round(1, 2), round(d1, 2))
          NS1.append(a)
          NS11.append(1)
          NS11Err.append(d1)
     m= 3, lambda=817.90
     m= 4, lambda=569.45
     m= 5, lambda=499.26
     m= 6, lambda=467.92
     m= 7, lambda=450.86
     m= 8, lambda=440.44
     m= 9, lambda=433.57
     m=10, lambda=428.78
     m=11, lambda=425.31
     m=12, lambda=422.70
[25]: print(tabulate(NS1, tablefmt="latex", floatfmt=".2f"))
     \begin{tabular}{rrr}
     \hline
       3 & 817.90 & 2.20 \\
       4 & 569.45 & 1.07 \\
       5 & 499.26 & 0.82 \\
       6 & 467.92 & 0.72 \\
       7 & 450.86 & 0.67 \\
       8 & 440.44 & 0.64 \\
       9 & 433.57 & 0.62 \\
      10 & 428.78 & 0.60 \\
      11 & 425.31 & 0.59 \\
      12 & 422.70 & 0.59 \\
     \hline
     \end{tabular}
[26]: #Zugeordnete Linien
      NS1zug = np.array([817.9, 567, 496.9, 465.8, 449, 999, 432.8, 429.3, 426.2,
      →999]) #Eiträge '999' stehen für nicht zuordbare Linien
      NS1zugErr = np.array([2.2, 3, 1.7, 1.0, 3, 0, 1.0, 0.5, 1.2, 0])
      #Signifikanztest:
      SignNS1 = []
      for i in range(0, len(NS11)):
          a = abs(NS11[i] - NS1zug[i]) / (np.sqrt(NS11Err[i]**2 + NS1zugErr[i]**2))
```

```
SignNS1.append(a)
print(SignNS1)

[0.0, 0.7695859513727448, 1.247829841684202, 1.7225498848940328,
0.6056368808730319, 875.5442670581631, 0.6521456633760835, 0.6609517706768887,
```

3.0.5 Erwartete Lininen 2. NS

0.6657695062171897, 980.7317565116002]

```
[27]: #Bindungsenergie Grundzustand
E_3s = E_3p - (hc / 589)
dE_3s = dE_3p
#Korrekturfaktor Delta_s
Delta_s = 3 - np.sqrt(E_Ry / E_3s)
dDelta_s = 0.5 * np.sqrt(E_Ry / E_3s**3) * dE_3s

print(E_3s, dE_3s)
print(Delta_s, dDelta_s)
```

-5.132423497433937 0.0040773115407532114 1.371873928666396 0.000646709807147509

```
m= 4, lambda=1172.09
m= 5, lambda=621.78
m= 6, lambda=518.24
m= 7, lambda=477.21
m= 8, lambda=456.17
m= 9, lambda=443.79
```

[29]: print(tabulate(NS2, tablefmt="latex", floatfmt=".2f"))

```
\begin{tabular}{rrr}
\hline
4 & 1172.09 & 4.64 \\
```

```
5 & 621.78 & 1.28 \\
      6 & 518.24 & 0.88 \\
      7 & 477.21 & 0.75 \\
      8 & 456.17 & 0.68 \\
      9 & 443.79 & 0.65 \\
     \hline
     \end{tabular}
[30]: #Zugeordnete Linien
      NS2zug = np.array([999, 614.5, 517.3, 474.2, 454.4, 999]) #Eiträge '999' stehen_
      → für nicht zuordbare Linien
      NS2zugErr = np.array([0, 1.3, 1.0, 0.7, 0.7, 0])
      #Signifikanztest:
      SignNS2 = []
      for i in range(0, len(NS21)):
          a = abs(NS21[i] - NS2zug[i]) / (np.sqrt(NS21Err[i]**2 + NS2zugErr[i]**2))
          SignNS2.append(a)
      print(SignNS2)
```

[37.271791138414365, 3.9969940460289646, 0.7034891247107137, 2.9402675495457427, 1.8129757341565915, 857.177845167591]

3.0.6 Erwartete Linien HS

```
[31]: #Korrekturfaktor Delta_p
Delta_p = 3 - np.sqrt(E_Ry / E_3p)
dDelta_p = 0.5 * np.sqrt(E_Ry / E_3p**3) * dE_3p
print(Delta_p, dDelta_p)
```

 $0.8801398813843408 \ 0.0014274699285376057$

m= 4, lambda=331.97

```
m= 5, lambda=286.27
```

```
[33]: print(tabulate(HS, tablefmt="latex", floatfmt=".2f"))
     \begin{tabular}{rrr}
     \hline
      4 & 331.97 & 0.38 \\
      5 & 286.27 & 0.27 \\
     \hline
     \end{tabular}
[34]: #Zugeordnete Linien
      HSzug = np.array([329.8, 284.2])
      HSzugErr = np.array([1.5, 0.6])
      #Signifikanztest:
      SignHS = []
      for i in range(0, len(HS1)):
          a = abs(HS1[i] - HSzug[i]) / (np.sqrt(HSlErr[i]**2 + HSzugErr[i]**2))
          SignHS.append(a)
      print(SignHS)
     [1.402255655540772, 3.143046635536093]
```

3.0.7 Bestimmung der Serienenergien und der l-abhängigen Korrekturfaktoren

```
[35]: #Quantenzahl Arrays:
    NS1QZ = np.arange(3, 13)
    NS2QZ = np.arange(4, 10)

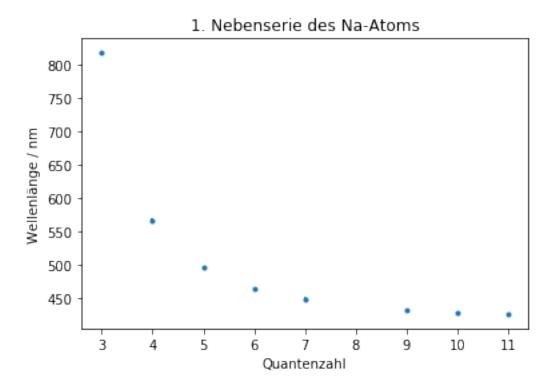
#Entferne nicht zugeordnete Wellenlängen:
    indexNS1 = [5, 9]
    NS1QZ_ = np.delete(NS1QZ, indexNS1)
    NS1zug_ = np.delete(NS1zug, indexNS1)
    NS1zugErr_ = np.delete(NS1zugErr, indexNS1)

indexNS2 = [0, 5]
    NS2QZ_ = np.delete(NS2QZ, indexNS2)
    NS2zug_ = np.delete(NS2zug, indexNS2)
    NS2zugErr_ = np.delete(NS2zugErr, indexNS2)
```

```
[36]: # 1. Nebenserie
plt.errorbar(NS1QZ_, NS1zug_, NS1zugErr_, fmt=".")
plt.xlabel('Quantenzahl')
plt.ylabel('Wellenlänge / nm')
```

```
plt.title('1. Nebenserie des Na-Atoms')
```

[36]: Text(0.5, 1.0, '1. Nebenserie des Na-Atoms')



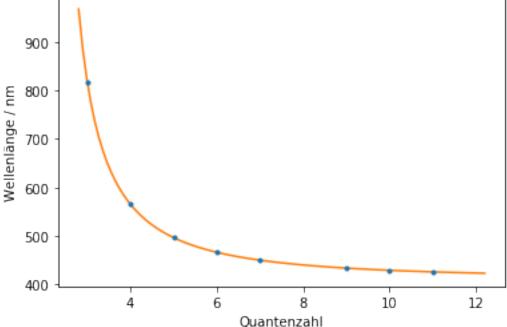
```
dof=len(NS1QZ_)-3 #dof:degrees of freedom, Freiheitsgrad
chi2_red=chi2_/dof
print("chi2=", chi2_)
print("chi2_red=",chi2_red)

#Fitwahrscheinlichkeit:
prob=round(1-chi2.cdf(chi2_,dof),2)*100
print("Wahrscheinlichkeit:", prob,"%")

#Plot des Fits:
plt.errorbar(NS1QZ_,NS1zug_,NS1zugErr_, fmt=".")
plt.xlabel('Quantenzahl')
plt.ylabel('Wellenlänge / nm')
plt.title('1. Nebenserie des Na-Atoms')
x=np.linspace(2.8,12.2, 100)
plt.plot(x, fit_funcNS1(x,*popt))
plt.savefig("output/NS1_fit.pdf", format="pdf")
```

```
\begin{split} &E\_Ry = -12.174088916181468 \text{ , Standardfehler= } 0.2803851245600611 \\ &E\_3p = -3.0147994153871127 \text{ , Standardfehler= } 0.0032031095846340937 \\ &D\_d = 0.1503829554125808 \text{ , Standardfehler= } 0.030526636698724883 \\ &\text{chi2= } 1.5970817193050355 \\ &\text{chi2\_red= } 0.3194163438610071 \\ &\text{Wahrscheinlichkeit: } 90.0 \text{ \%} \end{split}
```

1. Nebenserie des Na-Atoms



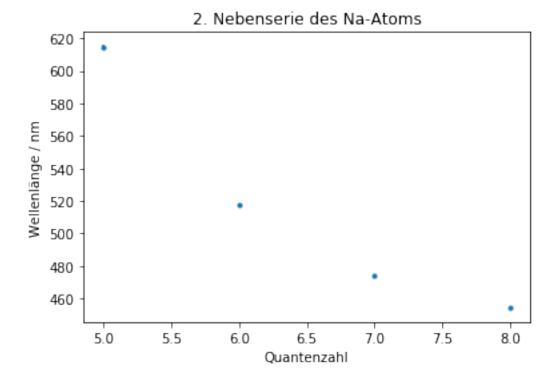
```
[38]: #Arrays mit vorherigen Werten von Oben (1.NS)
werte1 = np.array([E_Ry, E_3p, 0])
dwerte1 = np.array([0, dE_3p, 0])

#Signifikanztest
SignFit1 = []
for i in range(0, len(werte1)):
    a = abs(werte1[i] - fits1[i]) / (np.sqrt(dwerte1[i]**2 + dfits1[i]**2))
    SignFit1.append(a)
print(SignFit1)
```

[5.103377313841834, 2.449459212500005, 4.926286406745306]

```
[39]: # 2. Nebenserie
plt.errorbar(NS2QZ_, NS2zug_, NS2zugErr_, fmt=".")
plt.xlabel('Quantenzahl')
plt.ylabel('Wellenlänge / nm')
plt.title('2. Nebenserie des Na-Atoms')
```

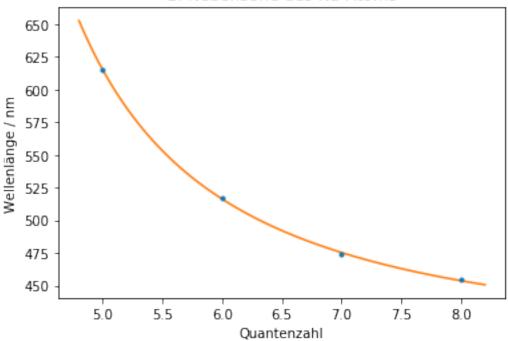
[39]: Text(0.5, 1.0, '2. Nebenserie des Na-Atoms')



```
[40]: #Definiere Fitfunktion:
      def fit_funcNS2(m,E_Ry,E_3p,D_s):
          return 1.2398E3/(E_Ry/(m-D_s)**2-E_3p)
      #Fit:
      para = [-13.6, -3, 1.3]
      popt2, pcov2 = curve_fit(fit_funcNS2, NS2QZ_, NS2zug_, sigma=NS2zugErr__
      →,p0=para)
      #Ausqabe:
      print("E_Ry=",popt2[0], ", Standardfehler=", np.sqrt(pcov2[0][0]))
      print("E_3p=",popt2[1], ", Standardfehler=", np.sqrt(pcov2[1][1]))
      print("D_s=",popt2[2], ", Standardfehler=", np.sqrt(pcov2[2][2]))
      fits2 = np.array([popt2[0], popt2[1], popt2[2]])
      dfits2 = np.array([np.sqrt(pcov2[0][0]), np.sqrt(pcov2[1][1]), np.

sqrt(pcov2[2][2])])
      #Güte des Fits:
      chi2_2=np.sum((fit_funcNS2(NS2QZ_,*popt2)-NS2zug_)**2/NS2zugErr_**2)
      dof2=len(NS2QZ_)-3 #dof:degrees of freedom, Freiheitsgrad
      chi2 red2=chi2 2/dof2
      print("chi2=", chi2_2)
      print("chi2_red=",chi2_red2)
      #Fitwahrscheinlichkeit:
      prob=round(1-chi2.cdf(chi2_2,dof2),2)*100
      print("Wahrscheinlichkeit:", prob,"%")
      #Plot des Fits:
      plt.errorbar(NS2QZ_,NS2zug_,NS2zugErr_, fmt=".")
      plt.xlabel('Quantenzahl')
      plt.ylabel('Wellenlänge / nm')
      plt.title('2. Nebenserie des Na-Atoms')
      x=np.linspace(4.8,8.2, 100)
      plt.plot(x, fit_funcNS2(x,*popt2))
     plt.savefig("output/NS2_fit.pdf", format="pdf")
     E_Ry= -15.983793260146998 , Standardfehler= 3.7763275744024076
     E_3p = -3.0677424492262095, Standardfehler= 0.04874524155986873
     D_s= 1.1001660083796412 , Standardfehler= 0.37724577768421824
     chi2= 4.460469180301559
     chi2_red= 4.460469180301559
     Wahrscheinlichkeit: 3.0 %
```

2. Nebenserie des Na-Atoms



```
[41]: #Arrays mit vorherigen Werten von Oben (1.NS)
  werte2 = np.array([E_Ry, E_3p, Delta_s])
  dwerte2 = np.array([0, dE_3p, dDelta_s])

#Signifikanztest
SignFit2 = []
for i in range(0, len(werte2)):
    a = abs(werte2[i] - fits2[i]) / (np.sqrt(dwerte2[i]**2 + dfits2[i]**2))
    SignFit2.append(a)
  print(SignFit2)
```

[0.6299223818059358, 0.8226958152229904, 0.7202400586372499]

4 Vergleich der Spektren

