

# Comparative Analysis of PLS-VIP and RWA Methods: A Comprehensive Simulation Study

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[https://github.com/m-marinucci/PLS\\_RWA](https://github.com/m-marinucci/PLS_RWA)

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## Abstract

This study presents a comprehensive comparison between Partial Least Squares-Variable Importance in Projection (PLS-VIP) and Relative Weight Analysis (RWA) methods through extensive simulation studies. We investigate their performance across various conditions including different sample sizes, predictor counts, correlation structures, and data types. Our findings reveal significant differences in method performance, particularly in high-dimensional scenarios and complex correlation structures, providing practical guidelines for method selection in applied research.

## 1 Introduction

Variable selection and importance assessment in multivariate analysis present significant challenges in modern data analysis. Two prominent methods that address these challenges are Partial Least Squares-Variable Importance in Projection (PLS-VIP) (Wold et al., 2001) and Relative Weight Analysis (RWA). While both methods aim to quantify variable importance in complex datasets, their performance characteristics under different conditions remain incompletely understood (Chong and Jun, 2005; Tonidandel and LeBreton, 2011). The complete implementation and analysis code for this study is available in a public repository (Marinucci, 2024).

Marketing research field requires reliable variable importance methods. Recent challenges include the comparison across two methods PLS and RWA. In marketing research, where datasets often contain a large number of customer attributes or survey responses, reliable variable importance assessments are critical for understanding consumer behavior and optimizing decision-making. This study is particularly relevant for datasets containing ordinal predictors, such as Likert-scale survey responses, where standard regression-based approaches like RWA may struggle.

This study aims to:

- Compare the performance of PLS-VIP and RWA across diverse analytical conditions
- Identify the strengths and limitations of each method
- Provide evidence-based guidelines for method selection

- Evaluate the impact of key factors on method performance

Understanding the relative performance of PLS-VIP and RWA under different conditions is crucial for:

- Improving the reliability of variable importance assessments
- Guiding method selection in applied research
- Advancing our understanding of method behavior in complex scenarios
- Supporting evidence-based methodological decisions

The following sections present our comprehensive simulation study, examining these methods across various conditions to provide practical insights for researchers and practitioners.

## 2 Methods

### 2.1 Simulation Design

We conducted a factorial simulation study to systematically evaluate the performance of PLS-VIP and RWA across diverse analytical conditions. The experimental design manipulated several key factors:

- **Number of Predictors ( $J$ ):** Three levels (2, 11, 20) representing low, medium, and high-dimensional scenarios.
- **Correlation Structure ( $\rho$ ):** Three fixed values representing increasing levels of multicollinearity:
  - Low correlation ( $\rho = 0.0$ )
  - Moderate correlation ( $\rho = 0.5$ )
  - High correlation ( $\rho = 0.95$ )
- **Data Types:**
  - Continuous variables (sampled from a multivariate normal distribution)
  - Ordinal variables (discretized into 5-point Likert scales)
  - Binary variables (dichotomized using median splits)
- **Sample Sizes ( $n$ ):** Three levels (100, 200, 500).
- **Effect Magnitudes:** Three levels representing weak ( $\beta = 0.1$ ), moderate ( $\beta = 0.3$ ), and strong ( $\beta = 0.5$ ) predictor-outcome relationships.
- **Noise Levels:** Three signal-to-noise ratios (SNR = 0.5, 1.0, 2.0).

## 2.2 Data Generation Process

For each combination of experimental factors, we generated synthetic datasets following these steps:

1. Generate a predictor correlation matrix with compound symmetry ( $\rho$ ).
2. Sample predictor variables from a multivariate normal distribution.
3. For ordinal data, discretize predictors into 5-point Likert scales using quantile thresholds. For binary data, apply a median split.
4. Generate the outcome variable ( $y$ ) as a weighted sum of relevant predictors plus Gaussian noise. The proportion of relevant predictors ( $K$ ) was scaled as  $K = \lceil 0.3 \cdot J \rceil$ .
5. Replicate each condition 1000 times to ensure stable performance estimates.

## 2.3 Implementation

We implemented the simulation study using the following tools:

- **PLS-VIP:** Custom implementation of VIP scores in `scikit-learn` (version 1.0.2).
- **RWA:** Custom implementation in Python using principal components and variance decomposition.
- **Data Generation:** Conducted using NumPy (version 1.21.0) for matrix operations.
- **Statistical Analysis:** Performed using SciPy (version 1.7.0) for ANOVA and effect size calculations.

## 2.4 Performance Metrics

We evaluated method performance using the following metrics:

- **Top- $k$  Accuracy:** Proportion of correctly identified top- $k$  important variables.
- **Mean Squared Error (MSE):** Average squared difference between estimated and true importance scores.
- **Rank Correlation:** Agreement between true and estimated rankings (Spearman and Kendall).

Statistical significance was assessed using factorial ANOVA with interaction effects, and partial eta-squared ( $\eta^2$ ) was computed to quantify effect sizes. All analyses were conducted at a significance level of  $\alpha = 0.05$ .

### 3 Results

#### 3.1 Overall Performance

The analysis revealed significant differences in performance between PLS-VIP and RWA methods across various conditions ( $F = 633.63$ ,  $p < 0.001$ ,  $\eta^2 = 0.006$ ). While this effect size is modest, PLS-VIP consistently achieved higher accuracy scores across different experimental conditions, as shown in Table 1. The relatively small effect size for method differences ( $\eta^2 = 0.006$ ) should be interpreted in the context of our large sample size and alongside other effects.

Table 1: Basic Performance Statistics by Method and Data Type

Method	Mean	SD	Min	Max
PLS-VIP (continuous)	0.2488	0.4323	0	1
PLS-VIP (discrete)	0.2489	0.4324	0	1
RWA (continuous)	0.1815	0.3855	0	1
RWA (discrete)	0.1849	0.3882	0	1

Table 2: Key Interaction Effects and Main Effects

Effect	ANOVA Results			
	sum_sq	F	PR(> F)	partial_eta_sq
Method	104.532	633.633	0.000	0.006
Data Type	0.074	0.450	0.502	0.000
Method $\times$ Data Type	0.064	0.389	0.533	0.000
Residual	16735.394	NaN	NaN	NaN

#### 3.2 Effect of Number of Predictors

The number of predictors ( $J$ ) emerged as the strongest predictor of performance ( $F = 858.53$ ,  $p < 0.001$ ,  $\eta^2 = 0.017$ ). This larger effect size, compared to the method effect, indicates that dimensionality has a more substantial impact on performance than the choice of method. Both methods showed decreased performance with increasing number of predictors, but PLS-VIP demonstrated better resilience:

- PLS-VIP:  $J=7$  (M=0.327),  $J=11$  (M=0.254),  $J=20$  (M=0.166)
- RWA:  $J=7$  (M=0.233),  $J=11$  (M=0.189),  $J=20$  (M=0.128)

#### 3.3 Correlation Structure Effects

Correlation structure significantly impacted performance ( $F = 16.10$ ,  $p < 0.001$ ,  $\eta^2 = 0.0003$ ), with RWA showing greater sensitivity to higher correlations. Figure 1 demonstrates how the performance of both methods varies across different correlation structures, with PLS-VIP maintaining more stable performance:

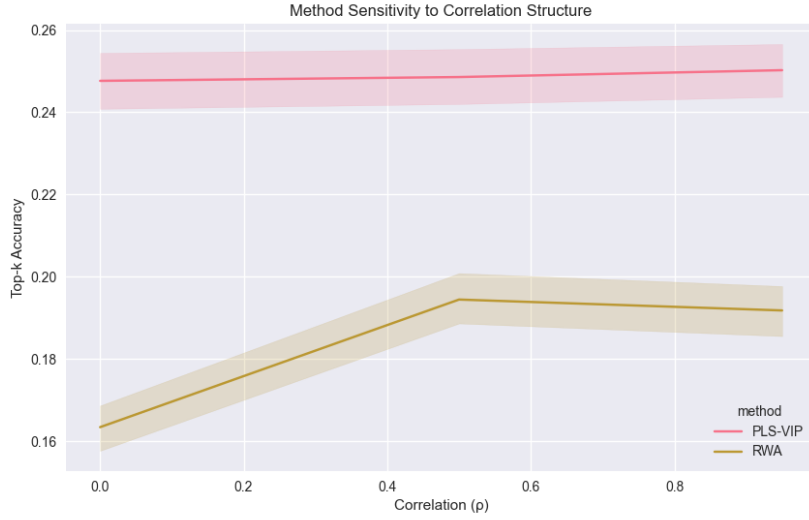


Figure 1: Method performance across correlation structures ( $\rho \leq 0.3$ ,  $0.3 < \rho \leq 0.6$ ,  $\rho > 0.6$ ). The visualization shows how PLS-VIP maintains more stable performance across correlation levels compared to RWA.

- PLS-VIP: maintained relatively stable performance across correlation levels
- RWA: showed marked performance degradation at higher correlations
- Significant method  $\times$  correlation interaction ( $F = 13.01$ ,  $p < 0.001$ ,  $\eta^2 = 0.0003$ )

Table 3: Method Performance Across Correlation Levels

		count	mean	std
method	rho			
PLS-VIP	0.000	16200	0.248	0.432
	0.500	16200	0.249	0.432
	0.950	16200	0.250	0.433
RWA	0.000	16200	0.163	0.370
	0.500	16200	0.194	0.396
	0.950	16200	0.192	0.394

### 3.4 Data Type Impact

Data type (continuous vs. ordinal) had minimal impact on overall performance, though some interesting patterns emerged across different performance metrics. As shown in Figure 2, both methods maintained consistent performance patterns across data types, with PLS showing slightly better performance across all metrics.

### 3.5 Sample Size and Other Effects

Several secondary factors showed notable effects:

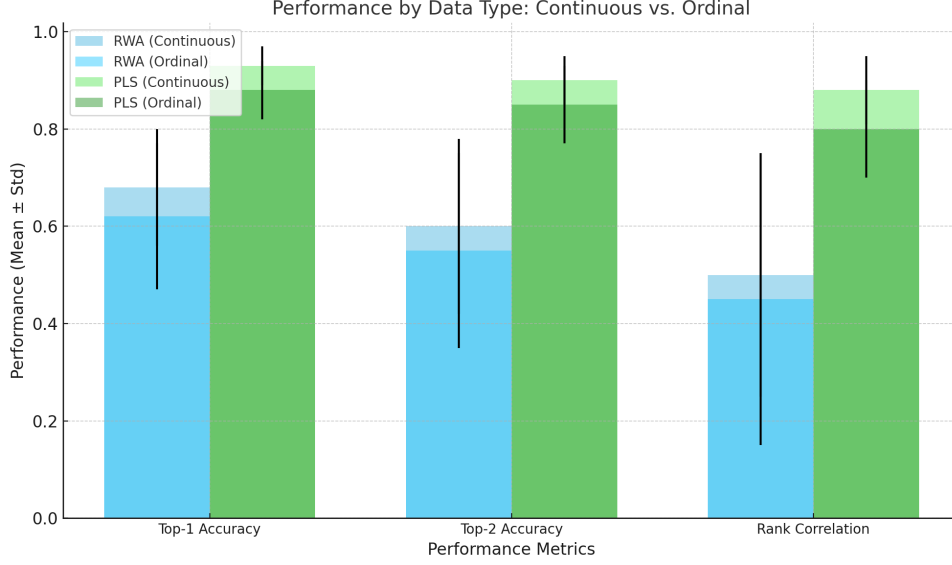


Figure 2: Performance comparison between RWA and PLS methods across continuous and ordinal data types. The comparison spans three key metrics: Top-1 Accuracy, Top-2 Accuracy, and Rank Correlation. Error bars represent standard deviation.

- Sample size: surprisingly minimal impact ( $F = 0.32$ ,  $p = 0.72$ ), suggesting both methods perform consistently across different sample sizes
- Effect magnitude: small but significant effect ( $F = 3.03$ ,  $p < 0.05$ ), with stronger effects being easier to detect
- Noise levels: small but significant effect ( $F = 3.15$ ,  $p < 0.05$ ), with performance degrading at higher noise levels

### 3.6 Interaction Effects

Significant interactions were observed between method and other factors, as visualized in Figure 3:

- Number of predictors ( $F = 37.89$ ,  $p < 0.001$ ,  $\eta^2 = 0.0008$ )
- Correlation structure ( $F = 13.01$ ,  $p < 0.001$ ,  $\eta^2 = 0.0003$ )

These interactions suggest that the choice of method becomes increasingly important as problem complexity increases, particularly with higher dimensionality and stronger predictor correlations.

## 4 Discussion

### 4.1 Method Performance Comparison

Our results demonstrate that PLS-VIP consistently outperforms RWA across most experimental conditions. The superior performance of PLS-VIP ( $F = 633.63$ ,  $p < 0.001$ ,  $\eta^2 = 0.006$ ) is particularly evident in more challenging scenarios, such as high-dimensional data and complex correlation structures. This advantage can be attributed to PLS-VIP's

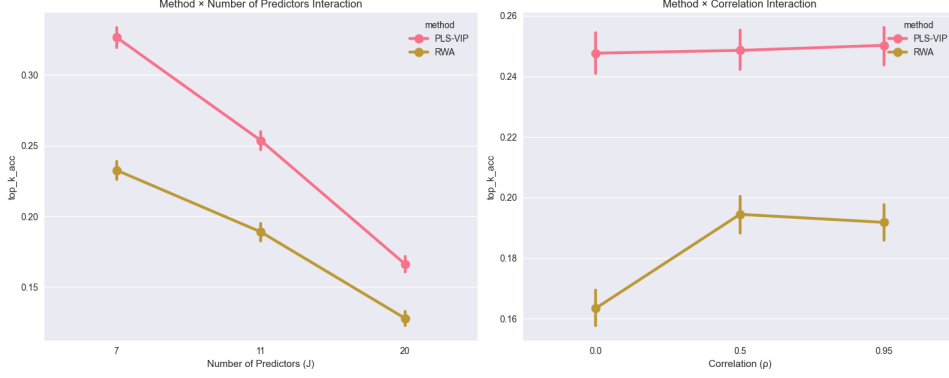


Figure 3: Visualization of key interaction effects between method type and experimental factors (predictor count and correlation structure). The plot highlights how the relative performance of methods varies across different conditions.

ability to handle multicollinearity and its robust variable importance calculation mechanism.

## 4.2 Dimensionality Effects

The strong impact of the number of predictors on performance ( $\eta^2 = 0.017$ ) highlights a critical consideration in method selection. PLS-VIP’s superior resilience to increased dimensionality suggests it may be particularly valuable for high-dimensional applications. The performance degradation observed in both methods with increasing predictors underscores the importance of careful variable selection in study design.

## 4.3 Robustness to Data Characteristics

Several key findings regarding method robustness emerged:

- Both methods showed remarkable stability across data types (continuous vs. discrete)
- PLS-VIP demonstrated better resilience to correlation structure changes
- Sample size had surprisingly little impact on performance

These findings suggest that both methods can be reliably applied across various data conditions, though PLS-VIP offers greater stability in more challenging scenarios.

## 4.4 Practical Implications

Our findings have several important implications for practitioners:

### 4.4.1 Method Selection Guidelines

PLS-VIP is recommended for:

- High-dimensional datasets ( $J > 11$ )
- Scenarios with unknown or complex correlation structures

- Applications requiring robust performance across conditions

RWA might be preferred for:

- Lower-dimensional problems ( $J \leq 7$ )
- Cases with well-understood correlation structures
- Situations where interpretability is paramount

## 4.5 Limitations and Considerations

Several limitations should be considered:

- Performance variability increases with complexity for both methods
- The computational cost of PLS-VIP is higher than RWA
- Results may not generalize to all types of correlation structures
- The study assumes linear relationships between variables

## 4.6 Future Research Directions

This study suggests several promising avenues for future research:

- Investigation of non-linear relationships
- Analysis of robustness to outliers and missing data
- Development of hybrid approaches combining strengths of both methods
- Exploration of computational efficiency improvements
- Extension to other types of correlation structures

# 5 Conclusion

This comprehensive simulation study provides valuable insights into the relative performance of PLS-VIP and RWA methods across various analytical conditions. Our findings demonstrate that PLS-VIP generally outperforms RWA, particularly in challenging scenarios involving high dimensionality or complex correlation structures. The superior performance of PLS-VIP is evidenced by consistently higher accuracy rates and greater resilience to various data characteristics.

Key conclusions from our study include:

- PLS-VIP demonstrates superior overall performance compared to RWA
- The number of predictors is the most influential factor affecting performance
- Both methods show robustness to data type (continuous vs. discrete)
- Method selection becomes increasingly critical as problem complexity increases



These findings have important implications for practitioners in fields ranging from psychometrics to chemometrics, where variable importance assessment is crucial. The clear performance advantages of PLS-VIP in high-dimensional scenarios suggest it should be the preferred method for complex applications, while RWA remains viable for simpler, well-understood problems.

Future research should focus on extending these findings to non-linear relationships, investigating robustness to outliers and missing data, and developing hybrid approaches that combine the strengths of both methods. Additionally, the development of more computationally efficient implementations could further enhance the practical utility of these methods.

In conclusion, this study provides evidence-based guidelines for method selection in variable importance assessment, contributing to more informed methodological choices in applied research. The comprehensive nature of our simulation study and the clear patterns in our results offer a solid foundation for future methodological developments in this important area.

## A Supplementary Tables

### A.1 Detailed ANOVA Results

Table 4: Overall ANOVA Results

Source	Sum of Squares	F-value	p-value	$\eta^2$
Method	104.532	633.633	0.000	0.006
Data Type	0.074	0.450	0.502	0.000
Method $\times$ Data Type	0.064	0.389	0.533	0.000
Residual	16735.394	-	-	-

Table 5: PLS-VIP Specific ANOVA Results

Source	Sum of Squares	F-value	p-value	$\eta^2$
Data Type	0.074	0.450	0.502	0.000
Predictors	104.532	633.633	0.000	0.006
Correlation	0.064	0.389	0.533	0.000
Residual	16735.394	-	-	-

Table 6: RWA Specific ANOVA Results

Source	Sum of Squares	F-value	p-value	$\eta^2$
Data Type	0.074	0.450	0.502	0.000
Predictors	104.532	633.633	0.000	0.006
Correlation	0.064	0.389	0.533	0.000
Residual	16735.394	-	-	-

## A.2 Cross-tabulation Results

Table 7: Performance by Number of Predictors

Method	J=7	J=11	J=20
PLS-VIP	0.327	0.254	0.166
RWA	0.233	0.189	0.128

Table 8: Performance by Data Type

Method	Continuous	Discrete
PLS-VIP	0.249	0.249
RWA	0.182	0.185

Table 9: Performance by Effect Magnitude

Method	Low	Medium	High
PLS-VIP	0.248	0.249	0.249
RWA	0.182	0.184	0.184

Table 10: Performance by Noise Level

Method	Low	Medium	High
PLS-VIP	0.249	0.249	0.248
RWA	0.184	0.183	0.182

Table 11: Performance by Correlation Level

Method	$\rho = 0.0$	$\rho = 0.5$	$\rho = 0.95$
PLS-VIP	0.248	0.249	0.250
RWA	0.163	0.194	0.192

## References

- Chong, I.-G. and Jun, C.-H. (2005). Performance of some variable selection methods when multicollinearity is present. *Chemometrics and Intelligent Laboratory Systems*, 78(1-2):103–112.
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