

# **A Cellular Learning Automata based Fuzzy Classifier for Color Image Segmentation**

**Mandana Hamidi<sup>3</sup>      Mohammad Reza Meybodi<sup>2</sup>**

## **ABSTRACT**

In this paper a cellular learning automata (CLA) based fuzzy classifier for color image segmentation is proposed. In the proposed classifier using a set of open asynchronous cellular learning automata, fuzzy membership functions and the rules for the fuzzy classifier are automatically generated. Each membership function is equipped with an open cellular learning automaton which is responsible for determining the best mean and variance for the corresponding membership function. In open CLA, the action of each cell in the next stage of its evolution not only depends on the local environment (actions of its neighbors) it also depends on the external environment. In order to show the performance of the proposed classifier it is compared with other methods in which the fuzzy rules are generated automatically. The result of the comparison has shown the efficiency of the proposed method. The proposed segmentation method is robust to light variation.

## **KEYWORDS**

Image Segmentation, Fuzzy Classifier, Learning Automata, Cellular Learning Automata

[2] :  
[6] [5][4] [3]  
[11][10][9][8][7]

[1][2]  
[25][24][23][22][21][20]  
[20] [27][26]

<sup>3</sup>ANFIS [21]

PSO [28][29][30]

[41]

[42]

[26][29][30]

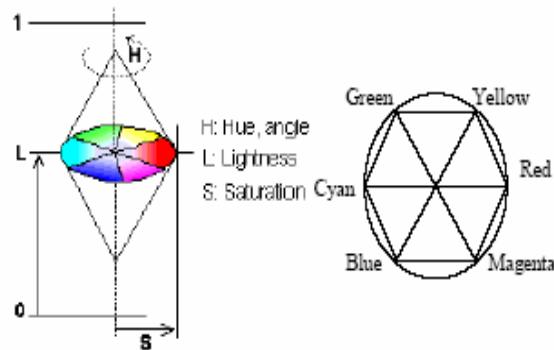
---

<sup>1</sup> Grid-type Fuzzy Partition  
<sup>2</sup> Scatter-type Fuzzy Partition  
<sup>3</sup> Adaptive Neuro-Fuzzy Inference System  
<sup>4</sup> Particle Swarm Optimization  
<sup>5</sup> Cellular Learning Automata

RGB ,HSL

.[1]

,YIQ ,HSV



**HSL**

S,L

H

HSL

HSL

[1]

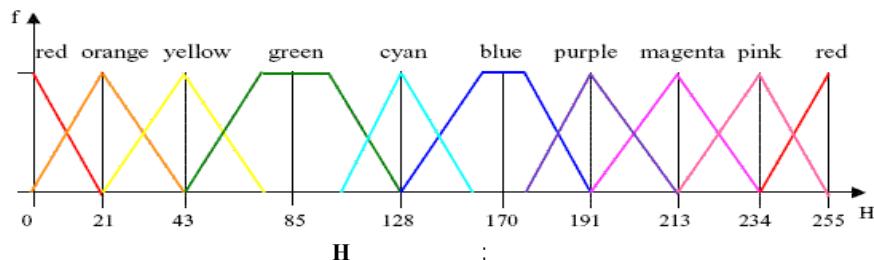
HSL

H

H

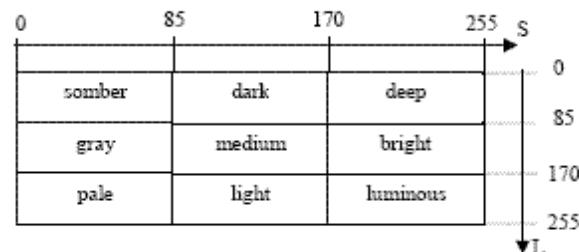
( )

[1]



S ,L

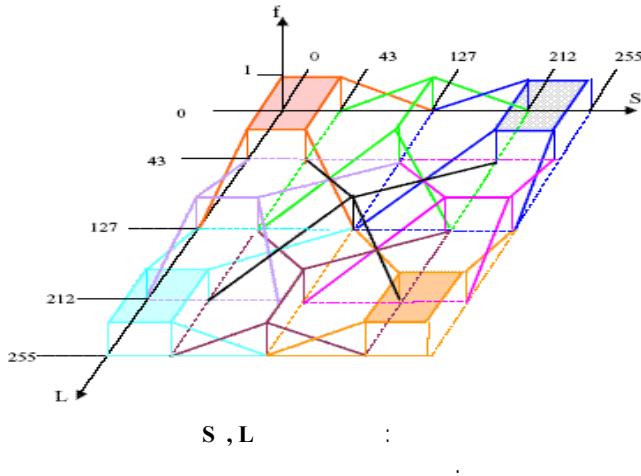
( )



L

S

( )



$j$ -th rule:

if  $x_1$  is  $A_{j1}$  and  $x_2$  is  $A_{j2}$  and ... and  $x_m$  is  $A_{jm}$   
then  $x = (x_1, x_2, \dots, x_m)$  belongs to class  $H_j$  with  $CF = CF_j$   
 $j = 1, 2, \dots, R$

$$CF_j = [0, 1] \quad , \quad M_j \quad , \quad H_j \in \{1, 2, \dots, M\} \quad , \quad m_j \quad , \quad R_j$$

$$m_{(ji,1)}, m_{(ji,2)}, m_{(ji,3)}$$

$$\mu_{A_{ji}}(m_{(ji,1)}, m_{(ji,2)}, m_{(ji,3)}; x_i) = \begin{cases} \exp\left(-\left(\frac{x_i - m_{(ji,1)}}{m_{(ji,2)}}\right)^2\right), & \text{if } x_i \leq m_{(ji,1)} \\ \exp\left(-\left(\frac{x_i - m_{(ji,1)}}{m_{(ji,3)}}\right)^2\right), & \text{if } x_i > m_{(ji,1)} \end{cases}$$

$$p \quad j \quad i \quad \underline{m}_{ji} = [m_{(ji,1)}, m_{(ji,2)}, \dots, m_{(ji,p)}]$$

$$r = [r_1, r_2, \dots, r_R] \quad \underline{r}_j = [\underline{m}_{j1}, \underline{m}_{j2}, \dots, \underline{m}_{jM}]$$

$$\underline{a} = [H_1, CF_1, H_2, CF_2, \dots, H_R, CF_R]$$

$$x = (x_1, x_2, \dots, x_m)$$

$$q_j(x) = \prod_{i=1}^M \mu_{A_{ji}}(x_i)$$

$$y = \arg \max_{j=1}^R q_j(x).CF_j$$

[33]

[17]

[31] . ( )



$$\alpha = \{\alpha_1, \dots, \alpha_r\}$$

$$\{\alpha, \beta, p, T\}$$

$$p = \{p_1, \dots, p_r\}$$

$$\beta = \{\beta_1, \dots, \beta_m\}$$

$$p(n+1) = T[\alpha(n), \beta(n), p(n)]$$

P

$$\beta_i$$

$$\beta_i$$

( )

$$\beta_i(n) = 0$$

$$\beta_i(n) = 1$$

---

<sup>6</sup> Cellular Automata

<sup>7</sup> Learning Automata

<sup>8</sup> P-model

<sup>9</sup> Unfavorable

<sup>10</sup> Failure

<sup>11</sup> Favorable

$\beta_i(n) \in [0,1]$	$S - L_{RP}$	$\beta_i(n)$
$S - L_{RP}$	$\alpha_i$	n
$\beta_i(n)$	$\alpha_i$	n
$p_i(k+1) = p_i(k) + a(1 - \beta_i(k))(1 - p_i(k)) - b\beta_i(k)p_i(k)$	$\forall j \quad j \neq i$	( )
$p_j(k+1) = p_j(k) - a(1 - \beta_i(k))p_j(k) + b\beta_i(k)\left[\frac{1}{r-1} - p_j(k)\right]$		
b a	b	a ( )
$L_{RP}$	$L_{RI}$	b a

[33]

[34][36][35]

[36]

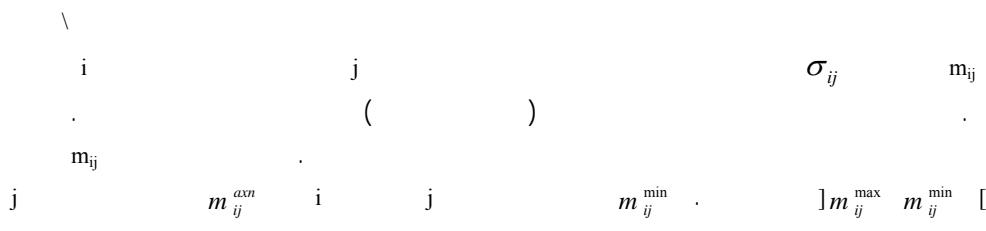
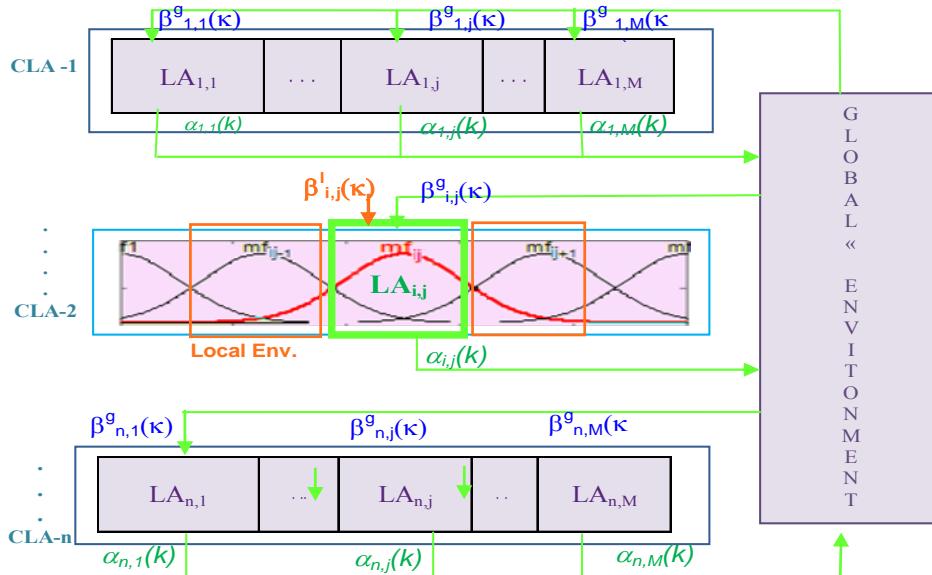
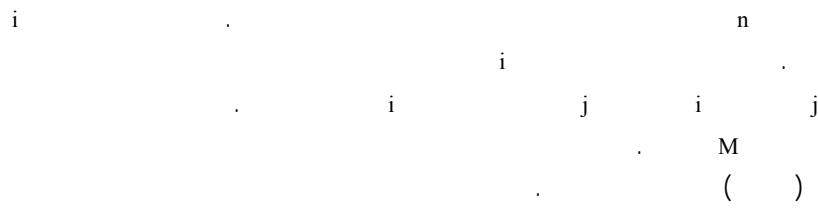
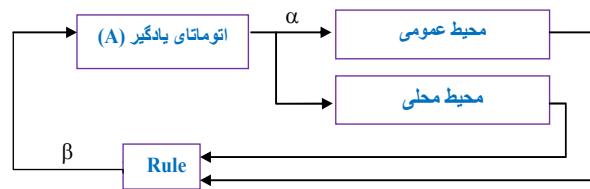
CLA

<sup>12</sup> Q-Model

<sup>13</sup>S-Model

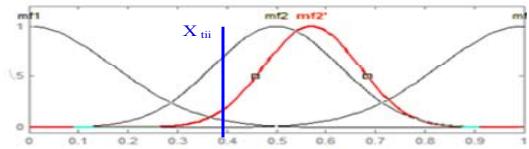
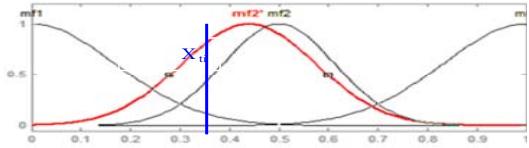
## <sup>14</sup> Local Environment

<sup>15</sup> Global Environment



$$m_{ij}^{axn} \quad m_{ij}^{\min} \quad m_{ij}^{\max} \quad m_{ij}^{\min} \quad [$$

$$\sigma_{ij} \quad m_{ij}$$



(

( :

$$\begin{array}{ll} \sigma_{ij} & m_{ij} \\ x_{ti} & mf_{ij} \end{array}$$

$$LA_{ij}$$

$$\begin{array}{llll} " & " & " & " \\ CF_r & \sigma_{ij} & & \end{array}$$

if  $m_{ij} > x_{ti}$  then

$$m_{ij} = m_{ij} + d_{fm} \cdot CF_r$$

$$\sigma_{ij} = \sigma_{ij} + d_{fs} \cdot CF_r$$

if  $m_{ij} < x_{ti}$  then

$$m_{ij} = m_{ij} - d_{fm} \cdot CF_r$$

$$\sigma_{ij} = \sigma_{ij} - d_{fs} \cdot CF_r$$

$$\begin{array}{ll} \sigma_{ij} & m_{ij} \\ x_{ti} & mf_{ij} \end{array}$$

$$LA_{ij}$$

$$\begin{array}{llll} " & " & " & " \\ & & & \sigma_{ij} \end{array}$$

if  $m_{ij} > x_{ti}$  then

$$m_{ij} = m_{ij} - d_{fm} \cdot CF_r$$

$$\sigma_{ij} = \sigma_{ij} + d_{fs} \cdot CF_r$$

if  $m_{ij} < x_{ti}$  then

$$m_{ij} = m_{ij} + d_{fm} \cdot CF_r$$

$$\sigma_{ij} = \sigma_{ij} - d_{fs} \cdot CF_r$$

$$x_{ti}$$

$$x_{ti}$$

$$M$$

$$n$$

$$[0.5 \ 0.5]$$

$$( \quad \quad \quad )$$

$$\underline{x}_t = (x_{t1}, x_{t2}, \dots, x_{tn})$$

i

$$\beta_{ij}^g(k) = \begin{cases} CF_r & \text{if } x_{ti} \text{ classifies correctly} \\ 1 - CF_r & \text{if } x_{ti} \text{ doesn't classify correctly} \end{cases}$$

( )

$$\beta_{ij}^l(k) = \beta_{ij}^g(k) + \beta_{ij+1}^g(k)$$

k                     $\beta_{ij}^l$

If  $LA_{ij-1}$  is Active

$$\beta_{ij}^l(k) = 1 - \beta_{ij-1}^g(k)$$

( )

Elseif  $LA_{ij+1}$  is Active

$$\beta_{ij}^l(k) = 1 - \beta_{ij+1}^g(k)$$

$$k \quad \beta_{ij}$$

$$\beta_{ij}(k) = \beta_{ij}^l(k) + \beta_{ij-1}^g(k)$$

( )

$\varepsilon$

$$\text{"if } x_1 \text{ is } A_{j1} \text{ and } x_2 \text{ is } A_{j2} \text{ and...and } x_n \text{ is } A_{jn} \text{ "}$$

xi                    j                    ( )

"then  $\underline{x} = (x_1, x_2, \dots, x_n)$  belongs to class  $H_j$  with  $CF = CF_j$ "

$$\underline{x}_i = (x_{i1}, x_{i2}, \dots, x_{in}) \quad (\underline{x}_i, \underline{y}_i), \quad i = 1, 2, \dots, N$$

[20]                    CF   H   j                    i                     $y_i$

$$\theta_t = \sum_{\underline{x}_p \in Class_t} q_j(\underline{x}_p), t = 1, 2, \dots, M$$

( )

$$H_j = \arg \max_{t=1}^M \theta_t$$

( )

$$CF_j = \frac{\theta_{H_j} - \theta}{\sum_{t=1}^M \theta_t} \quad ( )$$

$$\theta = \sum_{\substack{t=1 \\ t \neq H_j}}^M \frac{\theta_t}{M-1} \quad ( )$$

$$F [ ] . \quad PT . \quad A \quad (tr) \quad A-F^*PT$$

$$(t_1, t_2, t_3, t_4, t_5, t_6, t_7, t_8, t_9, t_{10}, t_{11}, t_{12})$$

L H,S

	رائدمنان	تعداد قانون
ANFIS	%81,49	٩٠
PSO-based Fuzzy	%73,34	٣٩
CLPSO-based Fuzzy	%89	٣٦
LA-based Fuzzy (LRP)	%85,49	٦٣
	%87,4	٥٦
	%85,3	٤٧
LA-based Fuzzy (LRI)	%85,01	٦٥
	%86,34	٥٠
	%84,6	٤٢
CLA-based Fuzzy (LRP)	%93,3	٥٢
	%95,7	٤٥
	%92	٣٠
CLA-based Fuzzy (LRI)	%94	٤٩
	%95,9	٤٦
	%93,1	٣٦

H,S,L

L S H

16

0.01 0.01 0.008 dfm r dfs

<sup>16</sup> Sugeno

- [1] Amine, A. and Isis Truck and Herman A," *Color Image Profiling Using Fuzzy Sets*", Turk J Elec Engin, vol. 13, no.3, 2005.
- [2] Ruz, G. A., Estévez P. A. and Perez, C. A., "A Neurofuzzy Colour Image Segmentation Method for Wood Surface Defect Detection. Forest", Prod. J. vol. 55, no. 4, pp. 52-58, 2005.
- [3] Moghaddamzadeh, A. and Bourbakis, N., "A Fuzzy Region Growing Approach for Segmentation of Colour Images", Pattern Recognition, vol. 30, no. 6, pp. 867–881, 1997.
- [4] Robinson, G. S., "Colour Edge Detection", Opt. Eng, vol. 16, no. 5, pp. 479-484, 1977.
- [5] Canny, J., "A Computational Approach to Edge Detection", IEEE Trans. Pattern Anal. Mach. Intell, vol. 8, no. 6, pp. 679-698, 1986.
- [6] Shiji, A. and Hamada N. "Colour image segmentation method using watershed algorithm and contour information", Proc Inter. Conf. on Image Processing, no. 4, pp. 305 309, 1999.
- [7] Zhang, B., "Generalized K-harmonic Means-Boosting in Unsupervised Learning", Technical report HPL-(2000-137), Hewlett-Packard Labs, 2000.
- [8] Bezdek, J., "A Convergence Theorem for the Fuzzy ISODATA Clustering Algorithms", IEEE Trans Pattern Anal Mach Intell 2, pp.1-8, 1980.
- [9] Ball, G. and Hall, D., "A Clustering Technique for Summarizing Multivariate Data", Behav Sci 12, pp. 153–155, 1967.
- [10] Huang, K., "A Synergistic Automatic Clustering Technique (Syneract) for Multispectral Image Analysis. Photogrammetric Eng Remote Sens , vol 1, no. 1, pp. 33–40, 2002.
- [11] Mahamed G. H., Omran Ayed Salman and Andries P. Engelbrecht, "Dynamic Clustering Using Particle Swarm Optimization with Application in Image Segmentation", Pattern Anal Applic 8: 332–344 DOI 10.1007/s10044-005-0015-5, 2005.
- [12] Eberhart, R. "Fuzzy Adaptive Particle Swarm Optimization", Proceedings Congress on Evolutionary Computation, Seoul, S. Korea, 2001.
- [13] Kennedy, J. and Medes, R., "Population Structures and Particle Swarm Performance", Proceedings of the IEEE Congress on Evolutionary Computation, Hawaii, USA, 2002..
- [14] Duda, R. O. and Hart, P. E., "Pattern Classification and Scene Analysis", John Wiley & Sons, New-York, 1973.
- [15] Omran M, Engelbrecht A, Salman A , "Particle Swarm Optimization Method for Image Clustering", Int J Pattern Recogn Artif Intell vol. 19, no.3, pp. 297–322, 2005.
- [16] R Eberhart and Shi. "Comparison between Genetic Algorithms and Particle Swarm Optimization", Proceedings of the Seventh Annual Conference on Evolutionary Programming, pp. 611-619. Springer-Verlag, 1998
- [17] Chia-Chong Chen , "Design of PSO-based Fuzzy Classification Systems", Tamkang Journal of Science and Engineering, vol. 9, no 1, pp. 63\_70, 2006.
- [18] Butenkov, S. and Krivsha, V., "Classification using Fuzzy Geometric Features", Proc. IEEE Conf. ICAIS'02, Divnomorskoe, Russia, pp. 89-91. 2002.
- [19] Klose, A. and Kruse, R. "Enabling Neuro-fuzzy Classification to Learn from Partially Labeled Data", IEEE World Congress on Computational Intelligence, IEEE International Conference on Fuzzy Systems, pp. 32-42, 2002.
- [20] Ishibuchi, H., Nozaki, K., Yamamoto, N. and Tanaka,H., "Selecting Fuzzy If-Then Rules for Classification Problems Using Genetic Algorithms", IEEE Trans. Fuzzy Systems, vol. 3, pp. 260-270, 1995.
- [21] Jang, J. S., "ANFIS: Adaptive-Network-Based Fuzzy Inference Systems," IEEE Trans. on Systems, Man and Cybernetics, vol. 23, pp. 665-685, 1993.
- [22] Nozaki, K., Ishibuchi, H. and Tanaka, H., "Adaptive Fuzzy Rule-Based Classification Systems", IEEE Trans. on Fuzzy Systems, Vol. 4, No. 3, Aug., pp. 238-250, 1996.
- [23] Wong, C. C. and Chen, C. C., "A GA-Based Method for Constructing Fuzzy Systems Directly from Numerical Data", IEEE Trans. on Systems, Man and Cybernetics- Part B: Cybernetics, Vol. 30, pp. 904-911, 2000.
- [24] Wang, L. X. and Mendel, J. M., "Generating Fuzzy Rules by Learning from Examples", IEEE Trans. on Systems, Man and Cybernetics, vol. 22, pp. 1414-1427, 1992.
- [25] Yager, R. R. and Filev, D. P. "Essentials of Fuzzy Modeling and Control", John Wiley, New York, U.S.A., 1994.
- [26] Simpson, P. K., "Fuzzy Min-Max Neural Networks- Part 1: Classification", IEEE Trans. Neural Networks, vol. 3, Sep., pp. 776-786 1992.

- [27] Wong, C. C. and Chen, C. C., "A Hybrid Clustering and Gradient Descent Approach for Fuzzy Modeling," IEEE Trans. on Systems, Man and Cybernetics-Part B: Cybernetics, vol. 29, pp. 686-693 (1999).
- [28] Chen, C. C., "Design of PSO-based Fuzzy Classification Systems", Tamkang Journal of Science and Engineering, vol. 9, no. 1, pp. 63-70, 2006.
- [29] Borji, A., M. Hamidi, M. and Eftekhari Moghadam, A. M. "CLPSO-based Color Image Segmentation", 26th Annual Meeting of the North American Fuzzy Information Processing Society (NAFIPS'07). San Diego, California, USA, June 24-27, 2007.
- [30] Hmaidi, M., Hamidi A., Eftekhari Moghadam, A. M., Meybodi M.R. "Soccer Field Image Colour Segmentation using PSO-based Fuzzy", Proceeding of the4th International Conference on Computational Intelligence, Robotics and Autonomous Systems Massey University, Palmerston North, New Zealand, CIRAS 2007,pp. 28-30 ,2007
- [31] Narendra K. S. and Thathachar M. A. L., Learning Automata: An Introduction, Prentice Hall, 1989.
- [32] Thathachar, M.A.L. and Sastry, P.S., "Varieties of Learning Automata: An Overview", IEEE Transaction on Systems, Man, and Cybernetics-Part B: Cybernetics, vol. 32, no. 6, pp. 711-722, 2002.
- [33] Wolfram, S., "Cellular Automata", Los Alamos Science, vol. 9, pp. 2-21, Fall 1983.
- [34] Beigy, H. and Meybodi, M. R., "A Mathematical Framework for Cellular Learning Automata", Advances on Complex Systems, vol. 7, nos. 3-4, pp. 295-320, 2004.
- [35] Beigy, H and Meybodi, M. R., "Open Synchronous Cellular Learning Automata", Proceedings of the 8th world Multi-conference on Systemics, Cybernetics and Informatics(SCI2004), pp. 9-15, Orlando, Florida, USA. July 18-21, 2004.
- [36] Schönfisch B, Roos A. D.; "Synchronous and Asynchronous Updating in Cellular Automata"; BioSystems, vol 51, pp. 123-143, 1999.
- [37] Beigy, H. and Meybodi, M. R., "Asynchronous Cellular Learning Automata", Automatica, Journal of International Federation of Automatic Control, 2007, to appear.
- [38] Wong, C. C. and Chen, C. C., "A Hybrid Clustering and Gradient Descent Approach for Fuzzy Modeling", IEEE Trans. on Systems, Man and Cybernetics-Part B: Cybernetics, Vol. 29, pp. 686-693, 1999.
- [39] Blake, C., Keogh, E. and Merz, C. J., UCI Repository of Machine Learning Database, Univ. California, Irvine, 1998.  
<http://www.ics.uci.edu/~mlearn/>

[ ]

- [41] Hamidi, M. and Meybodi, M. R., "A Fuzzy Classifier based on Learning Automata", 3th International Conference on Information and Knowledge Technology, Nov. 27-29, 2007, Ferdowsi Univ. of Mashhad, Iran
- [42] Hamidi, M. and Meybodi, M. R., "A Fuzzy Classifier based on Cellular Learning Automata",,13th International CSI Computer Conference, CSICC2008, Sharif University, Iran. 2008