

A General Call Admission Policy for Next Generation Wireless Networks

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Abstract

In this paper, we consider the call admission problem in next generation wireless networks, which must handle multi-media traffics. We first introduce a multi-threshold guard channel policy. The limiting behavior of this policy is analyzed under the stationary traffic. Then we give an algorithm, which finds the optimal number of guard channels, which minimizes the blocking probability calls with lowest level of QoS subject to the hard constraint on the blocking probabilities of other calls.

Keywords

Next Generation Wireless Networks, Call Admission Control, Guard Channel Policy, Multi-Threshold Guard Channels

1. Introduction

During the last decade, there has been a rapid growth of wireless communication technology. The next generation wireless networks are expected to eventually carry multi-media traffics. In order to support such wide range of traffics on a network, the network must be capable of satisfying various quality of service (QoS) requirements. The satisfying QoS means that the various traffics should get predictable service from the available resources in the network. Since wireless spectrum remains as the prime limited resource in the next generation networks, hence, it is necessary to develop mechanisms that can provide effective bandwidth management while satisfying the QoS requirement for incoming calls. In order to satisfy the QoS requirements, call admission control is needed. The

call admission control policies determine whether a call should be either accepted or rejected at the base station and assign the required channel(s) to the admitted call. In order to satisfy the level of QoS for each type of call, the call admission control policies usually use the prioritized methods. This priority is usually implemented through allocation of more resources to calls with higher level of QoS [1]. Several call admission control policies have been proposed to reduce the dropping of voice calls in wireless networks [2, 3, 4, 5, 6].

Suppose that the given cell has C full duplex channels. The guard channel (GC) policy reserves a subset of channels, called *guard channels*, allocated to the cell for sole use of handoff calls (say $C - T$ channels) [2]. Whenever the channel occupancy exceeds a certain threshold T , the GC policy rejects new calls until the channel occupancy goes below the threshold. The GC policy accepts handoff calls as long as channels are available. If only the dropping probability of handoff calls is considered, the GC policy gives very good performance, but the blocking probability of new calls is degraded to a great extent. In order to have more control on both the dropping probability of handoff calls and the blocking probability of new calls, *limited fractional guard channel policy* (LFG) is proposed [4]. The LFG policy reserves non-integral number of guard channels for handoff calls. The limited fractional guard channel policy uses an additional parameter π and operates the same as the guard channel policy except when T channels are occupied in the cell, in which case new calls are accepted with probability π . In [6], *uniform fractional guard channel policy* (UFG) is introduced, which accepts new calls with probability of π independent of channel occupancy. The uniform fractional guard channel policy performs better than guard channel policy in low handoff traffic conditions. In [7], two traffic classes of voice and transactions are considered and static and

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dynamic guard channel schemes are proposed to maintain the upper bound of dropping probability of handoff transaction calls. In this approach, $(C - T)$ guard channels are reserved for handoff transaction calls, but new calls and handoff voice calls have the same priority. Thus, this scheme fails to maintain the upper bound for dropping probability of handoff voice calls.

All of the above mentioned call admission control policies consider only one threshold to decide for accepting/rejecting of new calls. These policies fail when there is several classes of traffics with different level of QoS. In such cases, we need multi-threshold scheme, which provides different thresholds for different classes. In [8], *dual-threshold reservation* (DTR) scheme is given for integrated voice/data wireless networks. In this scheme, three classes of calls in ascending order of level of QoS are considered which are data calls, new voice calls and handoff voice calls. The basic idea behind the DTR scheme is to use two thresholds, one for reserving channels for handoff voice, while the other is used to block data traffic into the network in order to preserve the voice performance in terms of handoff dropping and call blocking probabilities. DTR assumes that the bandwidth requirement of voice and data are the same. The equations for blocking probabilities of DTR are derived but no algorithm for finding the optimal number of guard channels is given. In [9], a *two-threshold guard channel* (TTGC) policy, which uses two sets of guard channels, is introduced in which three classes of traffics in ascending order of level of QoS are considered. The limiting behavior of TTGC policy is analyzed under stationary traffic and an algorithm for finding the optimal number of guard channels is given.

In this paper, the idea given in [9] is generalized to multi-class traffics. In the proposed model, there are N classes of traffics each of which with different level of QoS. Each class may contain either new calls or handoff calls but having the same level of QoS. For example, class 1 can contain new voice calls and class 2 can contain handoff voice and new data calls. Our proposed model, referred to as *multi-threshold guard channel* (MTGC) scheme, builds upon guard channel scheme by using $N - 1$ thresholds in which each threshold is used to reserve channels for satisfying the specified level of QoS for that class. The limiting behavior of MTGC is analyzed under stationary traffics using one dimensional Markov chain. Then we give an algorithm that finds the optimal number of guard channels.

The rest of this paper is organized as follows: Section 2. presents the limiting behavior of multi-

threshold guard channel scheme under stationary traffics. Section 3. gives an algorithm to find the optimal value of thresholds and section 4. concludes the paper.

2. Multi-Threshold Guard Channel Scheme

In this section, we first introduce the multi-threshold guard channel policy and then give the blocking probabilities of multi-threshold guard channel policy. These blocking probabilities are computed based on the following assumptions.

1. There are N class of calls in the network. Each class can contain either new calls or handoff calls but having the same level of QoS. For example, class 2 can contain handoff voice and new data calls and class 1 can contain new voice calls. Every call requests only one channel. Class k (for $k = 1, 2, \dots, N$) has a level of QoS, q_k , which must be satisfied. Without loss of generality, it is assumed that $q_1 \geq q_2 \geq \dots \geq q_N$. Thus, the priority of calls for class k (for $k = 1, 2, \dots, N - 1$) is less than the priority of calls for class $(k + 1)$.
2. The arrival process of calls for class k (for $k = 1, 2, \dots, N$) is Poisson with rate λ_k . Let $\Lambda_k = \sum_{j=k+1}^N \lambda_j$ and $\alpha_k = \frac{\lambda_k}{\Lambda_0}$.
3. The channel holding time of calls for class k (for $k = 1, 2, \dots, N$) is exponentially distributed with mean μ_k^{-1} . Let $\mu^{-1} = \sum_{j=1}^N \mu_j^{-1}$ and $\rho = \frac{\Lambda_0}{\mu}$.
4. The time interval between two calls from a mobile computer is much greater than the mean call holding time.
5. Only mobile to fixed calls are considered.
6. The network is homogenous.

The assumptions 2 through 4 have been found to be reasonable as long as the number of mobile computers in a cell is much greater than the number of channels allocated to that cell. The fifth assumption makes our analysis easier and the sixth one let us to examine the performance of a single network cell in isolation. Suppose that the given cell has a limited number of full duplex channels, C , in its channel pool. We define the state of a particular cell at time t to be the number of busy channels in that cell, which is denoted by $c(t)$. In order to provide the specified level of QoS for calls of each class, channels which are allocated to the given cell are partitioned into (N) subsets. In order to partition the channel sets, $(N - 1)$ thresholds, T_1, \dots, T_{N-1} ($0 < T_1 \leq T_2 \leq \dots \leq T_{N-1}$) are defined. For the sake of simplicity, we use two additional fixed

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Algorithm MinBlock
1.   set  $T_0 \leftarrow -1$ ,  $T_1 \leftarrow T_2 \leftarrow \dots T_N \leftarrow C$ 
2.   if  $B_N(T) \leq q_N$  then
3.     return  $T$ 
4.   end if
5.   for  $k \leftarrow N$  downto 2 do
6.     while ( $T_{k-1} > 0$  and  $B_k(T) > q_k$ ) do
7.       if not MinBlockCheck( $T, k + 1$ ) then
8.         set  $T \leftarrow T - E_1^{k-1}$ 
9.       end if
10.      end while
11.    end for
12.    if at least one of constraints  $q_2, \dots, q_N$ 
        isn't satisfied then
13.      return Number of channels is too small.
14.    end if
end Algorithm

function MinBlockCheck ( $T, k$ )
1.   if  $k = N$  and  $T_{k-1} < T_k$ 
      and  $B_k(T + e_{k-1}) \leq q_k$  then
2.     set  $T \leftarrow T + e_{k-1}$ 
3.     return true
4.   end if
5.   if  $k < N$  and not MinBlockCheck( $T, k + 1$ )
      and  $T_{k-1} < T_k$  and  $B_k(T + e_{k-1}) \leq q_k$  then
6.     set  $T \leftarrow T + e_{k-1}$ 
7.     return true
8.   end if
9.   return false
end function

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Fig. 2. Algorithm for finding the optimal parameters of multi-threshold guard channel scheme

Induction step:

Consider any $N > 2$ and assume that the induction hypothesis is true for all m traffic classes ($1 \leq m \leq N$). In order to prove the correctness of MinBlock for $N + 1$ traffic classes, we consider finding of T_k (for $k = 1, \dots, N$). The statements in lines 6 through 10 of MinBlock algorithm uses a sequential search for finding the largest value of T_k . Since B_j (for $2 \leq j \leq N + 1$) is an increasing function of T_k ($k < j$), thus decreasing T_k ($k < j$) also decreases B_j . This contradicts with the objective of MinBlock which must find the largest value of T_k . This side effect is removed by using MinBlockCheck function. Since in each iteration of the while-loop in line 6, MinBlockCheck is called and on each of its call at most one T_j ($j > k$) is increased, then the above side effect is removed. Thus the while-loop in line 6 finds the largest value of T_j ($j > k$) and hence the algorithm finds the largest value for T_1 while satisfying the specified levels of QoS. From property 1, it is

concluded that the MinBlock algorithm minimizes B_1 . This completes the proof of this theorem.

3.1 A Numerical Example

In table 2, the usefulness of multi-threshold guard channel policy is shown for four traffic classes ($N = 4$). This example assumes that the given cell has 20 full duplex channels ($C = 20$) and constraints are $q_2 = 0.035$, $q_3 = 0.02$ and $q_4 = 0.01$. The table 1 shows the normalized arrival rate Λ_k . The columns of table 2 show the optimal number of guard channels and blocking probabilities for different classes, respectively.

Table 1. The input traffic

Case	Λ_0	Λ_1	Λ_2	Λ_3
1	17	12	7	2
2	18	8	7	2
3	20	10	5	2
4	20	12	7	2
5	20	10	7	2
6	21	11	3	2
7	22	12	7	2
8	25	15	7	2

Table 2. Results of the proposed algorithm for finding the optimal number of guard channels

Case	T_1	T_2	T_3	T_4	B_1	B_2	B_3	B_4
1	18	18	18	20	0.015822	0.015822	0.015822	0.001438
2	18	18	18	20	0.018911	0.018911	0.018911	0.001719
3	15	17	18	20	0.267492	0.027544	0.002858	0.000260
4	13	17	18	20	0.513851	0.031402	0.003259	0.000296
5	14	17	18	20	0.346408	0.025677	0.002665	0.000242
6	16	17	18	20	0.196272	0.030776	0.003194	0.000290
7	13	17	18	20	0.540299	0.033018	0.003426	0.000311
8	9	18	19	20	0.940582	0.034587	0.003144	0.003144

4. Conclusions

In this paper, we have studied the problem of call admission control in the next generation cellular mobile networks, which supports multi-classes of services. We introduced a multi-threshold guard channel policy and derived blocking probabilities of the network. We also studied their behavior and compared analytical results with simulation results. Then we gave an algorithm which finds the optimal number of guard channels.

thresholds $T_0 = -1$ and $T_N = C$. The procedure for accepting calls in multi-threshold guard channel scheme can be described as follows. A call from class k (for $k = 1, \dots, N$) will be accepted when the number of busy channels is smaller than T_k . In the multi-threshold guard channel scheme, $\{c(t)|t \geq 0\}$ is a continuous-time Markov chain (birth-death process) with states $0, 1, \dots, C$. The state transition diagram of a particular cell in the network, which has C full duplex channels and uses multi-threshold guard channel scheme is shown in figure 1.

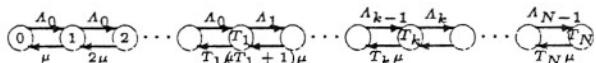


Fig. 1. Markov chain model of cell

Define the steady state probability $P_n = \lim_{t \rightarrow \infty} \text{Prob}[c(t) = n]$, for $n = 0, 1, \dots, T_N$. P_n is expressed by

$$P_n = P_0 \frac{(\rho \alpha_k)^n}{n!} \prod_{j=1}^k \left(\frac{\alpha_{j-1}}{\alpha_j} \right)^{T_j}, \quad (1)$$

for $T_k < n \leq T_{k+1}$ and P_0 is obtained from equation $\sum_{n=0}^C P_n = 1$ and is given by

$$P_0 = \left[\sum_{k=0}^{N-1} \prod_{j=1}^k \left(\frac{\alpha_{j-1}}{\alpha_j} \right)^{T_j} \sum_{n=T_{k+1}}^{T_{k+1}} \frac{(\rho \alpha_k)^n}{n!} \right]^{-1} \quad (2)$$

Define T as $[T_0, T_1, \dots, T_N]$, e_j as the unit $((N+1) \times 1)$ vector with 1 as the j^{th} element and the rest zero and E_i^j as $\sum_{k=i}^j e_k$. Thus, the blocking probability of class N is equal to

$$\begin{aligned} B_N(T) &= P_C, \\ &= \prod_{i=1}^{N-1} \left(\frac{\alpha_{i-1}}{\alpha_i} \right)^{T_i} \frac{(\rho \alpha_{N-1})^{T_N}}{T_N!} P_0. \end{aligned} \quad (3)$$

Similarly, the blocking probability of class k ($K < N$) is given by

$$\begin{aligned} B_k(T) &= \sum_{n=T_k+1}^C P_n, \\ &= \sum_{j=k}^{N-1} \prod_{i=1}^j \left(\frac{\alpha_{i-1}}{\alpha_i} \right)^{T_i} \sum_{n=T_{j+1}}^{T_{j+1}} \frac{(\rho \alpha_j)^n}{n!} P_0. \end{aligned} \quad (4)$$

$B_k(\cdot)$ has interesting properties some of which are listed below and proved in [10].

Property 1. For any given value of T , we have $B_k(T) \geq B_{k+1}(T)$.

Property 2. For any given value of T , $B_k(\cdot)$ is a monotonically decreasing function of T_k .

Property 3. For any given value of T , $B_k(\cdot)$ is a monotonically increasing function of T_j ($j < k$).

Property 4. For any given values of T , $B_k(\cdot)$ is a monotonically increasing function of T_j ($j > k$).

3. Optimal Number of Guard Channels

In this section, we consider problem of finding the optimal values of thresholds T_1, \dots, T_{N-1} , which can be described as: Given C channels allocated to a cell, the objective is to find T^* that minimizes $B_1(\cdot)$ with constraints $B_k(\cdot) \leq q_k$ for $k = 2, \dots, N$. Thus, we have the following nonlinear programming problem.

Problem 1. Minimize $B_1(T)$ subject to the hard constraint $B_k(T) \leq q_k$, where q_k is the level of QoS to be satisfied for calls of class $k = 2, \dots, N$.

We now present an algorithm called *MinBlock*, which is shown in figure 2, for solving problem 1. The *MinBlock* algorithm uses a function called *MinBlockCheck*. Function *MinBlockCheck* (T, k) increments T_j ($j > k$) by one if the specified level of QoS for class j is satisfied and returns *true*; otherwise it returns *false*, where j ($k-1 \leq j \leq N-1$) is the largest possible value which satisfies the specified level of QoS.

Theorem 1. Algorithm *MinBlock* minimizes $B_1(\cdot)$ while satisfying constraints $B_k(\cdot) \leq q_k$ for $k = 2, \dots, N$.

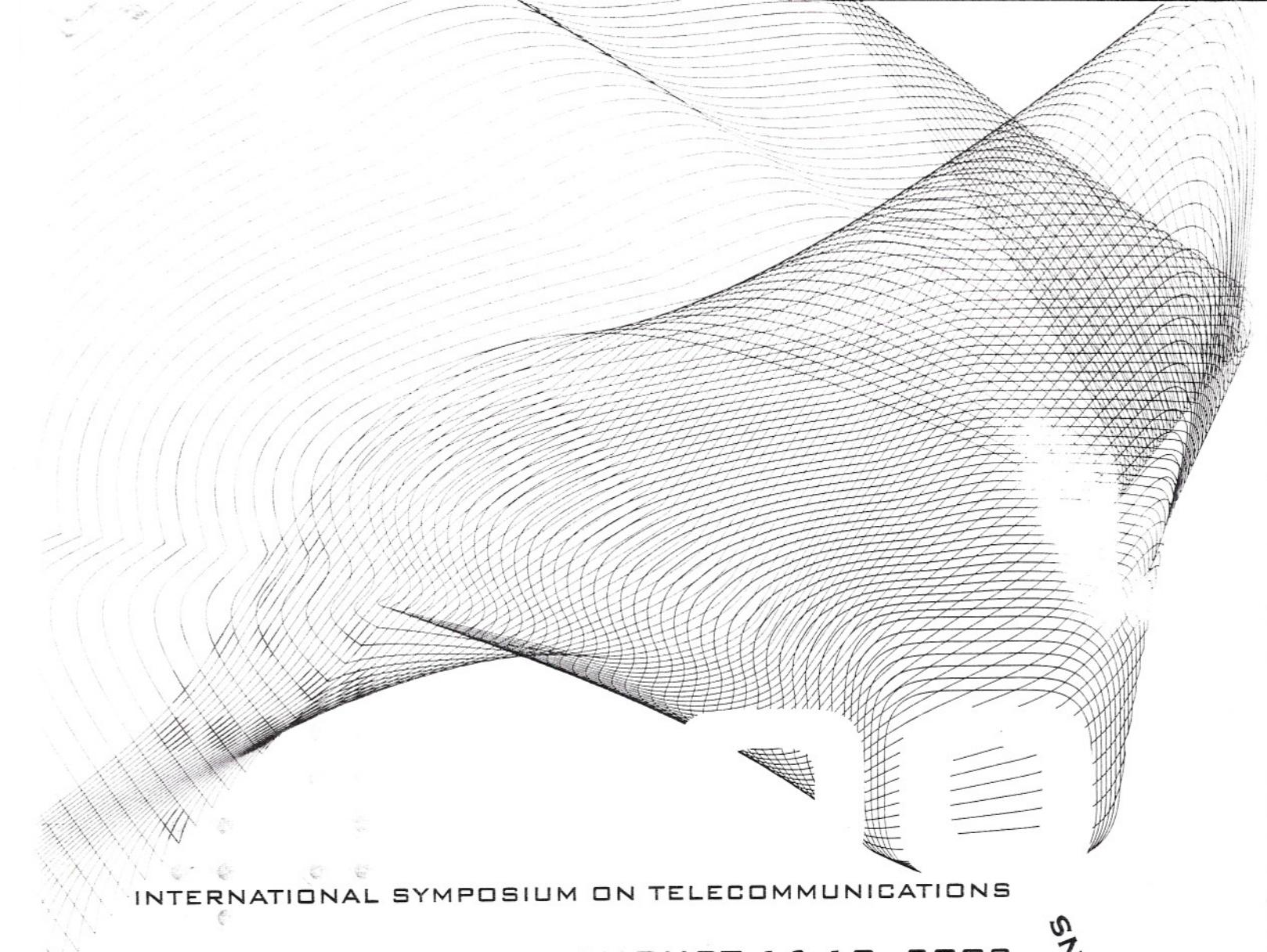
Proof. Since B_k (for $k = 1, \dots, N$) is a decreasing function of T_k (property 2), it is sufficient to show that the *MinBlock* algorithm maximizes T_1 while satisfying the specified levels of QoS. The proof is by induction on the number of traffic classes, N . We shall show that if the *MinBlock* algorithm minimizes $B_1(\cdot)$ for N classes, then it still minimizes $B_1(\cdot)$ for $N+1$ classes and when the algorithm stops, T gives the optimal solution to problem 1.

Basis:

When we have 2 traffic classes ($N = 2$), the *MinBlockCheck* function always return *false*. Hence, the statements in lines 6 through 10 performs a linear search and finds the largest value of T_1 satisfying level of QoS, q_2 . Since B_1 is a decreasing function of T_1 , thus the *MinBlock* algorithm minimizes B_1 .

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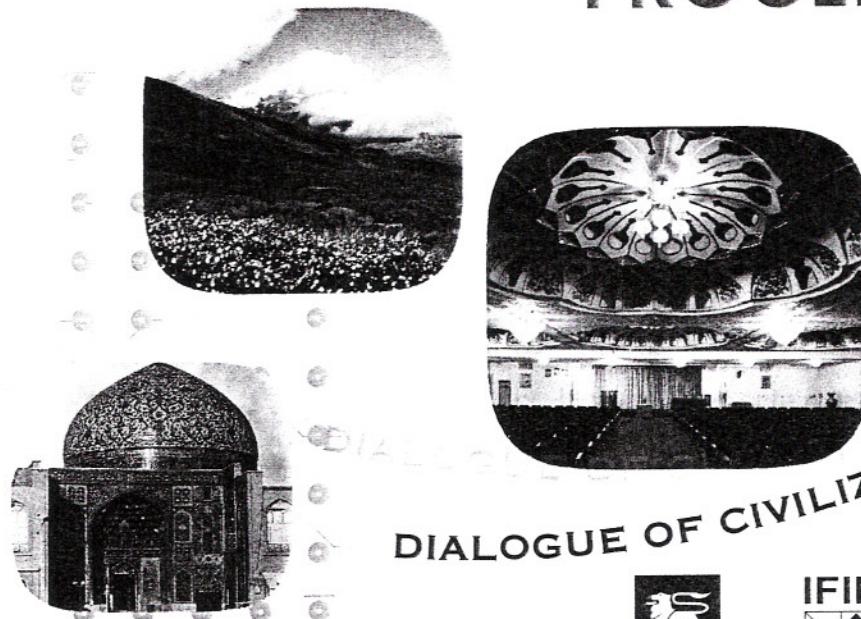
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