Assignment 3

RedBlack Trees

Introduction

- Most of the BST operations (e.g., search, max, min, insert,) take O(h) time where h is the height of the BST.
- The cost of these operations may become O(n) for a skewed Binary tree.
- If we make sure that the height of the tree remains O(log n) after every insertion and deletion, then we can guarantee an upper bound of O(log n) for all these operations.
- The height of a Red-Black tree is always O(log n) where n is the number of nodes in the tree.

2. Lab Goal

- This lab assignment focuses on balanced binary search trees and focusing on one of Balanced BST RedBlack trees.

3. Red Black Trees Implementation

3.1 Requirements

You are required to implement the Red-Black Tree data structure supporting the following operations:

1. **Search:** Search for a specific element in a Red-Black Tree.
2. **Insertion:** Insert a new node in a Red-Black tree. Tree balance must be maintained via the rotation operations.
3. **Print Tree Height:** Print the height of the Red-Black tree. This is the longest path from the root to a leaf-node.
4. **Print Black Height:** number of black nodes in any path from root to leaf.
5. **Print Tree size:** Print the number of elements in Red-Black tree.

4. Application

4.1 Introduction

English Dictionary As an application based on your Red-Black Tree implementation.

4.2 Requirements

You are required to implement a simple English dictionary, with a simple text-based user interface, supporting the following functionalities:

1. **Load Dictionary:** You will be provided with a text file, “dictionary.txt", containing a list of words. Each word will be in a separate line. - You should load the dictionary into a Red-Black Tree data structure to support efficient insertions and search operations.
2. **Insert Word:** Takes a word from the user and inserts it, only if it is not already in the dictionary. Otherwise, print the appropriate error message (e.g. “ERROR: Word already in the dictionary!"). The dictionary file must be updated with the newly inserted word.
3. **Look-up a Word:** Takes a word from the user and prints “YES" or “NO" according to whether it is found or not.

Note: For validation purposes, you are required to print both the size of the dictionary, height, and the black height of your Red-Black tree after each insertion.

5. Notes

- Implement your algorithms using (Python, Java, or C/C++) Preferably Python
- You should work in groups **of members.**
- Discussion will have higher weight than implementation, so you should understand your implementation well to get discussion marks.
- Late submissions are not allowed unless there is a valid documented excuse.