CSCE4133/5133 – Algorithms Fall 2024

Assignment 4 Graph Theory Minimum Spanning Tree and Shortest Path

Out Date: Nov. 8, 2024 Due Date: **Nov. 22, 2024**

Instructions:

- Written Format & Template: Students can use either Google Doc or Latex
- Write your full name, email address and student ID in the report.
- Write the number of "Late Days" the student has used in the report.
- Submission via BlackBoard
- Policy: Can be solved in individual & review the late-day policy.
- **Submissions:** Your submission should be a PDF for the written section & a zip file with your source code implementation.
- For more information, please visit course website for the homework policy.

1. Overview

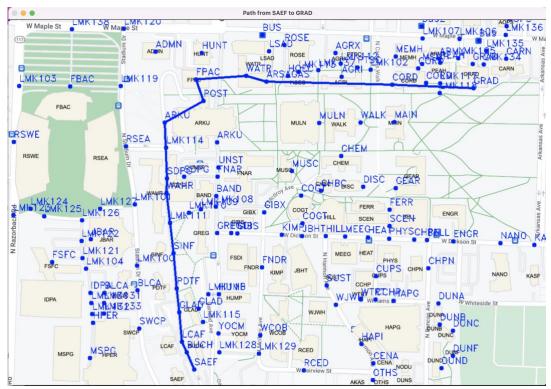


Figure 1: The shortest path from the SAEF building to the GRAD building searched by the Dijkstra's Algorithm

In this assignment, we will implement the minimum spanning tree algorithms and the shortest path algorithm, i.e., Prim's Algorithm, Kruskal's Algorithm, and Dijkstra Algorithm. In this assignment, you are given a Graph where each node represents a building or a landmark and the weight between two nodes equals the Euclidian distance between them.

In this assignment, you are **REQUIRED** to implement **Prim's Algorithm**, **Kruskal's Algorithm**, and **Dijkstra's Algorithm**. If you think the homework is too long, don't worry; it is long because we provide you with the details of the descriptions. There are some hints that may help to be successful in this homework:

- You should start your homework early.
- You should read the homework descriptions carefully before you start working on the homework.
- Before implementing the required functions, you should try to compile the source code first. Basically, the source code with an empty implementation can be compiled successfully. This step will help you to understand the procedure of each problem.
- If you forgot these algorithms, you are encouraged to revise the lecture slides.

The source code is organized as follows:

File or Folder	Required Implementati on	Purpose	
assets/	No	Contain the data of homework	
include/	No	Contain headers files	
src/	No	Contain source code files	
bin/	No	Contain an executable file	
include/graph.hpp	No	Define the graph structure	
include/sort.hpp	No	Define the header of sorting algorithms	
src/algorithms	No	Implement the algorithms (i.e., Kruskal, Prim, and Dijkstra)	
src/sort	No	Contain the source files of sorting algorithms	
<pre>src/sort/msort.cpp</pre>	No	Implement the Merge Sort algorithm	
<pre>src/algorithms/prim.cpp</pre>	Yes	Implement Prim's Algorithm	
<pre>src/algorithms/kruskal.cpp</pre>	Yes	Implement Kruskal's Algorithm	
<pre>src/algorithms/dijkstra.cpp</pre>	Yes	Implement Dijkstra's Algorithm	
<pre>src/main.cpp</pre>	No	Implement the main program	
Makefile	No	Define compilation rules	

2. Implementation

a. Graph Before you start implementing algorithms, you first investigate the usages of

Graph. This class has already been implemented in the *src/graph.cpp*.

Class	Method	Meaning	Sample Code	
Graph	Graph	Initialize a graph with n vertices	Graph G(6);	
	insertEdge	Insert an undirected (or	G.insertEdge(0, 1);	
		directed) edge into the graph	G.insertEdge(0, 1, directed=true);	
	search	Perform the search	G.search(start, destination, bfs);	
		algorithm to find a path		
		from start to destination		
	exportEdges	Export a list of edges	std::vector <edge> edges =</edge>	
			G.exportEdges()	

b. Prim's Algorithm

You are given a method in *src/algorithms/prim.cpp* as follows:

```
std::vector<Edge> constructMSTPrim(Graph G)
{
    // YOUR CODE HERE
}
```

Given a Graph G, you have to implement Prim's Algorithm and return a list of edges as the minimum spanning tree of G.

c. Kruskal's Algorithm

You are given a method in *src/algorithms/kruskal.cpp* as follows:

```
std::vector<Edge> constructMSTKruskal(Graph G)
{
   std::vector<Edge> edges = G.exportEdges(); // Graph's edges
   // YOUR CODE HERE
}
```

Given a Graph G, you have to implement Kruskal's Algorithm and return a list of edges as the minimum spanning tree of G.

d. Dijkstra's Algorithm

You are given a method in *src/algorithms/dijkstra.cpp* as follows:

```
std::vector<int> searchShortestPath(Graph &G, int start, int passBy,int destination)
{
    // YOUR CODE HERE
}
```

Given a Graph G, you have to implement Dijkstra's Algorithm and return a list of vertices that is the shortest path from start to destination on graph G. In addition, on the path from start to destination, you have to go through the vertex passBy.

e. Requirements

In this homework, we have a strict requirement of the complexity of each algorithm that you implement. The complexity of your algorithms should not be **no more than**:

Algorithm	Undergrad Student	Graduate Student	
Prim's Algorithm	$O(V ^2)$	$O((V + E)\log V)$	
Kruskal's Algorithm	O(E V)	$O((V + E)\log V)$	
Dijkstra's Algorithm	$O(V ^2)$	$O(E \log E)$	

3. Compilation and Testing

In this homework, we use the same environment (Make, GCC/G++, OpenCV Library) used in the previous ones to compile the source code. For Windows users, you have to make sure that you set the correct paths for MINGW_BIN and OPENCV_DIR:

```
MINGW_BIN=<path to mingw64>/bin
OPENCV_DIR=<path to opencv>/build/install
```

For example, if we stored mingw64 and opency in C:/, we edit these paths as follows:

MINGW_BIN=C:/mingw64/bin

OPENCV_DIR=C:/opency/build/install

OpenCV Library: In our homework, OpenCV is OPTIONAL and only used for the visualization purpose, you can work on your homework WITHOUT installing and using OpenCV. If you do not want to use OpenCV for visualization, open file *Makefile* and edit line *OPENCV=1* to *OPENCV=0*. If you use OpenCV 4+, you need to turn on the flag *OPENCV4=1* in makefile.

To compile and test your source code, you open the terminal and go to the source code folder and type the following commands:

- **make prim** (or **mingw32-make prim** on Windows): To compile and run Prim's algorithm.
- **make kruskal** (or **mingw32-make kruskal** on Windows): To compile and run Kruskal's algorithm.
- **make dijkstra** (or **mingw32-make dijkstra** on Windows): To compile and run Dijkstra's algorithm.

If you compile and run successfully, you should pass the unit test of the sorting algorithm and are going to see an output as follows:

Prim	Perform unit test of the Prim's algorithm			
	Total Cost of Minimum Spanning Tree: 16			
	Total Cost of Minimum Spanning Tree: 9315			
Kruskal	Perform unit test of the Kruskal's algorithm			
	Total Cost of Minimum Spanning Tree: 16			
	Total Cost of Minimum Spanning Tree: 9315			
Dijkstra	Perform unit test of the Dijkstra algorithm			
	Path from 0 to 5 pass by 3: 0 1 3 4 5			
	Path from SAEF to HAPG Pass By GRAD: SAEF -> BUCH -> LCAF ->			
	GLAD2 -> PDTF -> SINF -> LMK111 -> WAHR -> SDPG2 -> ARKU2			
	-> POST -> FPAC -> WATR -> ARSAGAS -> CORD1 -> PTSC ->			
	MEMH2 -> ARMY -> GRAD -> ARMY -> MEMH2 -> PTSC -> CORD1			
	-> WALK -> GEAR -> FERR -> SCEN -> PHYS -> CHPN1 -> BELL -			
	> CHPN2 -> DUNA -> HAPG			

For Windows users, if you would like to compile with OpenCV, you have to copy the following files from *C:\opencv-3.4.13\build\bin* to your Homework folder:

- libopencv_core3413.dll
- libopency highgui3413.dll
- libopency_imgcodecs3413.dll
- libopency_imgproc3413.dll