Method#02 - PID control: Tuning PID controller of the LTI, SISO system

Let's consider the following UAV stabilization system

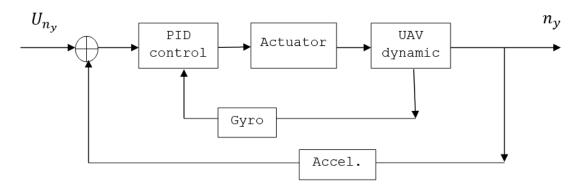


Fig.2.01 - Functional block-diagram of the UAV stabilization system

Assumptions

Measurment noise&errors of the Gyro and Accelerometer aren't taking into account in the model: $W_{\rm evro}(s)=1$, $W_{\rm accel}(s)=1$.

...

PID controller

$$\delta(t) = K_P e(t) + K_D \omega_z(t) + K_I \int_0^T e(t) dt , \qquad (2.01)$$

Actuator

$$W_{act} = \frac{1}{T_{act}s + 1},\tag{2.02}$$

where $T_{act} = \frac{1}{K_{act}}$ is actuator time constant, $K_{act} = 20$.

UAV dynamics

$$W_{\delta}^{\omega_{z}} = \frac{K(T_{1}s+1)}{T_{2}^{2}s^{2} + 2\xi T_{2} + 1}, \quad W_{\omega_{z}}^{\dot{\theta}} = \frac{1}{T_{1}s+1}, \quad W_{\dot{\theta}}^{n_{y}} = \frac{V}{g}, \tag{2.03}$$

where

$$K = 1$$
,
 $T_1 = 0.7$ (s), $T_2 = 0.5$ (s),
 $\xi = 0.3$.