

- WE ARE GIVEN THAT $x_1 > x_0$. THAT IS, THE FLATTER BUDGET LINE DESCRIBES A MORE REMOTE LOCATION.
- WHEN $h=0$, WE HAVE
 $c_0 = w - \bar{x}x_0$, $c_1 = w - \bar{x}x_1$,
 THESE ARE Y-INTERCEPTS OF THE BUDGET LINES.
- SINCE $x_1 > x_0$, WE MUST HAVE $c_1 < c_0$, AS DRAWN
- IN SPATIAL EQUILIBRIUM, HOMOTHETIC'S OPTIMIZE
 \Rightarrow BUDGET LINE IS TANGENT TO INDIF. CURVE FOR OUTSIDE OPTION, \bar{U} .
- THIS CAN ONLY HAPPEN IF $p_1 < p_0$. THIS WE HAVE $p \downarrow$ AS $x \uparrow$

$$2. \text{ (a) } \underset{\text{S.T.}}{\underset{\text{Max}}{\max}} \quad c^{\frac{1}{2}} h^{\frac{1}{2}}$$

$$\tilde{\omega} = c + ph \quad \tilde{\omega} = \omega - 2\zeta x$$

$$\Rightarrow \underset{\text{Max}}{(\tilde{\omega} - ph)^{\frac{1}{2}} h^{\frac{1}{2}}}$$

$$\text{F.O.C.} \Rightarrow \frac{1}{2} (\tilde{\omega} - ph)^{-\frac{1}{2}} (-p) h^{-\frac{1}{2}} + \frac{1}{2} (\tilde{\omega} - ph)^{\frac{1}{2}} h^{-\frac{1}{2}} = 0$$

$$\Rightarrow -ph + (\tilde{\omega} - ph) = 0$$

$$\Rightarrow -2ph = -\tilde{\omega}$$

$$\Rightarrow h^* = \frac{\tilde{\omega}}{2p}$$

$$\Rightarrow c^* = \tilde{\omega} - ph^*$$

$$c^* = \tilde{\omega} - p \frac{\tilde{\omega}}{2p}$$

$$c^* = \frac{\tilde{\omega}}{2}$$

$$(b) \text{ Using } u(c, h) = 3 \Rightarrow$$

$$c^{*\frac{1}{2}} h^{*\frac{1}{2}} = 3$$

$$\Rightarrow \left(\frac{\tilde{\omega}}{2} \right)^{\frac{1}{2}} \left(\frac{\tilde{\omega}}{2p} \right)^{\frac{1}{2}} = 3$$

$$\Rightarrow \frac{\tilde{\omega}}{2\sqrt{p}} = 3$$

$$\Rightarrow \sqrt{p} = \frac{\tilde{\omega}}{2}$$

$$\Rightarrow P^* = \left(\frac{\tilde{\omega}}{2} \right)^2 = \left(\frac{\omega - 2\zeta x}{2} \right)^2$$

$$(c) \underset{s}{\text{Max}} \quad P s^{\frac{2}{3}} - i s - R$$

$$\text{F.O.C.} \Rightarrow \sum_3 P s^{-\frac{1}{3}} - i = 0$$

$$\Rightarrow s^{-\frac{1}{3}} = \frac{3}{2} \frac{i}{P}$$

$$\Rightarrow s^* = \left(\frac{3}{2} \frac{i}{P} \right)^{-3}$$

$$\Rightarrow s^* = \left(\frac{2}{3} \frac{P}{i} \right)^3$$

SUBSTITUTING INTO $h_s(s)$

$$\Rightarrow h_s^*(s^*) = \left[\left(\frac{2}{3} \frac{P}{i} \right)^3 \right]^{\frac{2}{3}}$$

$$= \left(\frac{2}{3} \frac{P}{i} \right)^2$$

(d) POPULATION DENSITY IS

$$\frac{h_s^*}{h^*} = \frac{\cancel{\text{Housing}}}{\cancel{\text{Area}}} = \frac{\text{Personal}}{\cancel{\text{Area}}}$$

$$= \frac{\left(\frac{2}{3} \frac{P^*}{i} \right)^2}{\frac{\tilde{\omega}}{2P^*}} = \frac{4}{9i^2} \cdot \frac{2P^{*3}}{\tilde{\omega}}$$

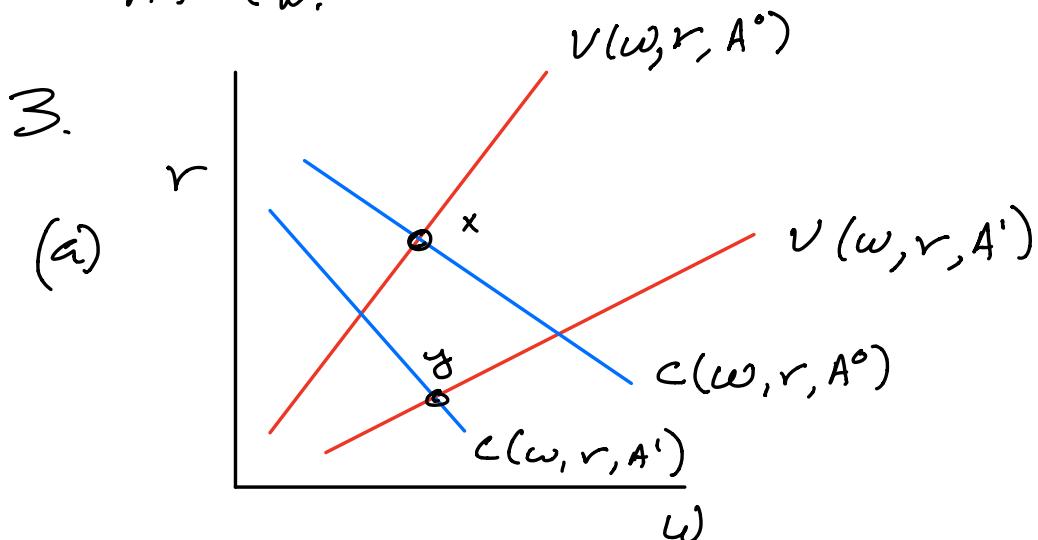
$$= \frac{4}{9i^2} \cdot \frac{2}{\omega - 2\epsilon_x} \left[\left(\frac{\omega - 2\epsilon_x}{2} \right)^2 \right]^3$$

$$= \frac{8}{9\pi^2} \cdot \left(\frac{w - 2\epsilon x}{z} \right)^5$$

$$= \frac{1}{36\pi^2} (w - 2\epsilon x)^5$$

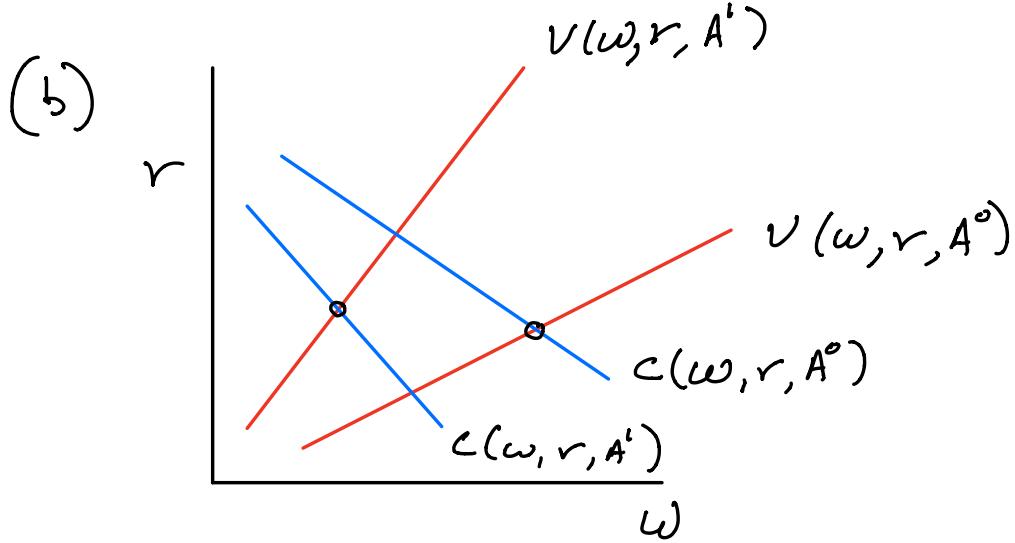
(e) • WE SEE IN (d) THAT POPULATION DECLINES WITH DISTANCE TO THE CENTER. JUST LIKE BOTH THE 1900 AND 1940 DENSITY GRADIENT.

- WE SEE THE DENSITY GRADIENT IN (e) GETS FLATTER FROM 1900 TO 1940. THIS WAS THE PERIOD WHEN THE AUTOMOBILE CAME INTO USE, SO $\epsilon \downarrow$. IN (d) THE DENSITY GRADIENT ALSO GETS FLATTER AS $\epsilon \downarrow$.



- WITH $A = A'$, EQUILIBRIUM IS AT X , WHERE $(r, w) = (r^*, w^*)$

- Households like less rent holding w constant, so, holding utility constant and wage constant, households need lower rent to live with A' than A . Since $A' > A^*$ $\Rightarrow A'$ is a good for households.
- Firm produce one unit at the same cost holding rent constant only if the wage is lower for A_1 than A_0 . Since $A_1 > A_0 \Rightarrow A_1$ is a bad for firms.



Similar to above:

- Fixing rent, firms can hold constant costs while paying a higher wage with A' than A^* $\Rightarrow A'$ is good for firms
- Fixing rent, H.H. hold utility constant at a lower rent with A' than A^* .
 \Rightarrow need more consumption at A'
 \Rightarrow A' is a bad for H.H.

4. IF WE PERFORM THE REGRESSIONS

$$\ln r = B_0 + B_1 A + \varepsilon$$

AND

$$\ln w = C_0 + C_1 A + \eta$$

THEN

$$\frac{d \ln r}{d A} = B_1$$

AND

$$\frac{d \ln w}{d A} = C_1$$

WE CAN DO THESE REGRESSIONS WITH
GIVEN DATA.

WE ARE ALSO GIVEN THAT $\frac{\ln r}{\ln w} = \frac{1}{3}$

THIS WE HAVE

$$\frac{P_A}{w} = \frac{1}{3} \cdot B_1 - C_1$$

THAT IS, WE CAN ESTIMATE THE
REAL PRICE OF A FROM THE GIVEN
DATA.

6. - THE SOLID LINE IN THE FIGURE IS
THE OBSERVED DISTRIBUTION OF PAIRWISE
DISTANCES FOR THIS INDUSTRY.

- THE TWO DASHED LINES BOUND
THE AREA WHERE WE WOULD EXPECT
THIS CURVE TO LIE IF FIRMS LOCATED
AT RANDOM.
- THE GRAPH SHOWS TOO MANY PAIRS
OF FIRMS CLOSE TOGETHER FOR
RANDOM CHOICE
 \Rightarrow FIRMS ARE MORE AGGREGATED
THAN RANDOM

7. TOP: NEW BIG GROCERY ENTERY DRIVES ABOUT
3% OF ALL FOOD EXPENDITURE
FROM FOOD DESENT RESIDENTS

MIDDLE: BIG GROCERY STORE SHARE OF
ALL FOOD EXPENDITURE FROM
FOOD DESENT RESIDENTS DOES
NOT CHANGE WITH ENTRY OF NEW
GROCERY

BOTTOM: DIET OF FOOD DESENT RESIDENT
DOES NOT CHANGE WITH ENTRY OF
STORE.

\Rightarrow ADDING GROCERIES TO FOOD DESENT
DOES NOT CHANGE DIETS OF
RESIDENTS.