

因为:  $(\text{前后})' = \text{前}' \cdot \text{后} + \text{前} \cdot \text{后}'$

即:  $\text{前} \cdot \text{后}' = (\text{前后})' - \text{前}' \cdot \text{后}$

$$\begin{aligned}\text{两边积分, 即: } \int (\text{前} \cdot \text{后}') dx &= \int [(\text{前后})' - \text{前}' \cdot \text{后}] dx \\ &= \underbrace{\int \left[ \underbrace{(\text{前后})'}_{\text{导函数}} \right] dx}_{\text{原函数, 就 = 前后}} - \int [\text{前}' \cdot \text{后}] dx \\ &= \text{前后} - \int [\text{前}' \cdot \text{后}] dx \quad (1)\end{aligned}$$

$$\int \text{前} \cdot \underbrace{\text{后}'}_{=d(\text{后})} dx = \text{前后} - \int \text{后} \cdot \underbrace{\text{前}'}_{=d(\text{前})} dx$$

$$\text{即: } \int \text{前} d(\text{后}) = \text{前后} - \int \text{后} d(\text{前}) \quad (2)$$

上面 (1) 和 (2) 式, 就是“分部积分法”公式