

$$\int e^{-pt} dt \quad \leftarrow \text{令 } u = -pt, \text{ (} p \text{ 是常数)}$$

$$\frac{d}{dt}(u) = (-pt)' = -p$$

$$\text{即 } dt = \frac{du}{-p} = -\frac{1}{p} du$$

$$= \int e^u \cdot \left(-\frac{1}{p}\right) du$$

$$= -\frac{1}{p} \underbrace{\int e^u du}_{=e^u+C} \quad \leftarrow \text{然后把 } u \text{ 换回 } t, \text{ 因为 } u = -pt$$

$$= -\frac{1}{p} \cdot e^{-pt} + C$$