Corregidum to "Novel whitening approaches in functional settings"

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Due to production errors, Equation 3 in pp. 3 is written as

$$\langle f,g
angle_{\mathbb{M}}=\sum_{j=1}^{\infty}\lambda_{j}^{-1}\left\langle f,\gamma_{j}
ight
angle \left\langle g,\gamma_{j}
ight
angle =\left\langle \Gamma^{1/2\dagger}f,\Gamma^{1/2\dagger}g
ight
angle f,\quad g\in\mathbb{M},$$

while it was originally written as

$$\langle f,g
angle_{\mathbb{M}}=\sum_{i=1}^{\infty}\lambda_{j}^{-1}\left\langle f,\gamma_{j}
ight
angle \left\langle g,\gamma_{j}
ight
angle =\left\langle \Gamma^{1/2\dagger}f,\Gamma^{1/2\dagger}g
ight
angle \quad f,g\in\mathbb{M}.$$

In §3, the statement reads, "Then, we can use the inner product (3) to construct a space of isotropic functions (i.e., their covariance operator satisfies the identity), so that the space ends up having a certain Gaussian appearance..." The term *space of isotropic functions* is unclear in the current context. Since our whitening operators are mappings defined through elements over T, this does not necessarily imply that the realizations of $\mathbb X$ are on the unit sphere $S = \{x \in \mathbb H \mid ||x||^2 = 1\}$. The isotropy property would be satisfied when whitening the coefficients A in the direction of its transpose, assuming dependencies in a secondary domain exist. Therefore, one could use the following instead: "...to construct a space of white/orthogonalized functions (i.e., their covariance operator satisfies the identity), so that the space ends up having a certain Gaussian appearance...".

In §4, the sentence "As 2tr (Γ_{XX}) is the only dependence between the original and the whitened variable, the minimization problem can be reduced to the maximization of tr (Γ_{XX}) ." reads also as ".. is the only *dependent term*...".

In the Technical proofs (first paragraph), due to abuse of notation, in the sentence "Note that Condition 1 cannot be reached when $\langle X, \gamma_j \rangle^2 = \lambda_j$, or for $c_j \to c > 0$, $\langle X, \gamma_j \rangle^2 = \lambda_j c_j$...", X stands for a deterministic function.

REFERENCES

Vidal, M. and Aguilera, M. (2023). Novel whitening approaches in functional settings. *Stat.*, 12(1):e516. Vidal, M., Rosso, M., and Aguilera, A. M. (2021). Bi-smoothed functional independent component analysis of EEG data. *Mathematics*, 9:1243.

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