## Kitaev Algorithm

The magnetic moment of our artificial atom is:

$$\mu = S\hbar |d\omega_{01}/d\Phi|,$$

which is directly proportional to the area S and the rate change with flux  $\Phi$  of the transition frequency  $\omega_{01}$ . For our device we obtain  $d\omega_{01}/d\Phi = -2\pi \times 5.3 GHz/\Phi_0$  at the bias point, resulting in  $\mu = 1.10 \times 10^5 \mu_B$ .

Operating away from the bias point leads to a reduction of the decoherence time  $T_2: T_2^{-1} = (2T_1)^{-1} + T_{\Phi}^{-1}$ , where  $2T_1$  is a sum of relaxation time and  $T_{\Phi}$  is a dephasing time. The dephasing rate appreciably increases at our bias point, which reduces  $T_2$  and thus the number of available steps that can be implemented in the Kitaev algorithm.

In the experiment we apply a Ramsey sequence of two consecutive  $\pi/2$  pulses separated by a time delay  $\tau$ , which corresponds to an effective spin-1/2 precession around the z-axis of the Bloch sphere. The precession angle  $\phi = \Delta\omega(\Phi)\tau$  is defined by the frequency mismatch  $\Delta\omega(\Phi) = \omega_d - \omega_{01}(\Phi)$  between the transition frequency  $\omega_{01}(\Phi)$  of the transmon qubit and the fixed drive frequency  $\omega_d$  of the  $\pi/2$  pulses.