

# Fundamentals of Computer and Programming

## Lecture 8

# Functions

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# What We Will Learn

---

- Introduction
- Passing input parameters
- Producing output
- Scope of variables
- Storage Class of variables
- Function usage example
- Recursion



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# Introduction

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- Until now, we learned to develop simple algorithms
  - Interactions, Mathematics, Decisions, and Loops
- Real problems: very complex
  - Compressing a file
  - Calculator
  - Games, MS Word, Firefox, ...
- Cannot be developed at once
  - Divide the problem into smaller sub-problems
  - Solve the sub-problems
  - Put the solutions altogether to get the final solution
- **Modular** programming



# Modular programming

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- Solving a large and complex problem
- Design the overall algorithm
- Some portions are **black-box**
  - We know **what** each box does
  - But we do not worry **how**
  - Later, we think about the **black-boxes** and develop them
- Black-boxes are implemented by **functions**



# Modular programming: Advantages

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- Easy to develop and understand
  - Reusability
    - Something is used frequently
      - Mathematic: Square, Power, Sin, ...
      - Programming: Printing, Reading
    - Develop it **one time**, use it **many times**
  - Multiple developers can work on different parts
  - Each module can be tested and debugged separately
- 



# Functions in C

---

## ➤ Functions in mathematics

□  $z = f(x, y)$

## ➤ Functions in C

➤ **Queries**: Return a value

➤ `sin()`, `fabs()`

➤ **Commands**: do some tasks, do not return any value

➤ `printf_my_info(...)`



# Functions in C

---

- Three steps to use functions in C
- Function **prototype** (declaration) (اعلان تابع)  
(معرفی الگوی تابع)
  - Introduce the function to the compiler
- Function **definition** (تعریف تابع)
  - What the function does
- Function **call** (فراخوانی تابع)
  - Use the function





# Function prototype

---

`<output type> <function name>(<input parameter types>);`

- `<output type>`
  - **Queries**: `int, float, ...`
  - **Command**: `void`
- `<function name>` is an identifier
- `<input parameter list>`
  - `<type>, <type>, ...`
    - `int, float, ...`
  - `void`



# Function definition

---

```
<output type> <function name>(<input parameters>) {  
    <statements>  
}
```

➤ <output type>

- Queries: `int`, `float`, ...
- Command: `void`

➤ <function name> is an identifier

➤ <input parameters>

- <type> **<identifier>**, <type> **<identifier>**, ...
  - `int in`, `float f`, ...
- `void`

➤ Function definition should be out of other functions

- Function in function is not allowed



# Function call

---

- Command function

`<function name> (inputs);`

- Query function

`<variable> = <function name>(inputs);`

- Inputs should match by function definition

- Functions are called by *another* function

- Function call comes inside in a function



# Example

---

```
/* Function declaration */  
void my_info(void);  
  
int main(void){  
    printf("This is my info");  
    my_info(); /* Function call */  
    printf("=====");  
    return 0;  
}  
/* Function definition */  
void my_info(void){  
    printf("Student name is Dennis Ritchie\n");  
    printf("Student number: 9822222\n");  
}
```

---



# Function declaration

---

- Function declaration is **optional** if program is developed in a single file

```
void my_info(void){  
    printf("My name is Dennis Ritchie\n");  
    printf("My student number: 98222222\n");  
}  
  
int main(void){  
    my_info();  
    printf("-----\n");  
    my_info();  
    return 0;  
}
```



# Function Declaration?!!!!

---

- Is function declaration needed?
- Is there any useful application of function declaration?
- **Yes!**
- Libraries are implemented using it
  - .h files contains the function declarations
    - and also other definitions
  - .so, .a, .dll, ... are the compiled function definitions



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# Input Parameters

---

- Inputs of function
  - No input: **void**
  - One or multiple inputs
- Each input should have a type
- Input parameters are split by “ , ”  
`void f(void)`  
`void f(int a)`  
`void f(int a, float b)`  
`void f(int a, b) //compile error`





# Example: 'print\_sub' function

```
#include <stdio.h>
```

```
void print_sub(double a, double b){  
    double res;  
    res = a - b;  
    printf("Sub of %f and %f is %f\n", a, b, res);  
}
```

```
int main(void){  
    double d1 = 10, d2 = 20;  
    print_sub(56.0, 6.0);    //What is the output?  
    print_sub(d1, d2);       //output?  
    print_sub(d1, d2 + d2);  //output?  
    return 0;  
}
```

تابعی که دو عدد را بگیرد  
و تفاضل آنها را چاپ کند .



# How Does Function Call Work?

---

- Function call is implemented by “**stack**”
- Stack is a **logical** part of the main memory
- Variables of function and its input variables are in stack
- When a function calls
  - Its variables including the inputs are allocated in stack
  - The value of input parameters from caller function is pushed to stack of called function
    - They are **copied** in to the variables of function
- When function finished, its stack is freed.



# print\_sub: What happen?

---

```
print_sub(56.0, 6.0);
```

- 56.0 is copied the memory location **a**
- 6.0 is copied to memory location **b**

```
double a = 56.0;
```

```
double b = 6.0;
```

```
double res;
```

```
res = a - b;
```



# print\_sub: What happen?

---

```
print_sub(d1, d2);
```

- **Value** of **d1** is copied to memory location **a**
- **Value** of **d2** is copied to memory location **b**

```
double a = 10.1;
```

```
double b = 20.2;
```

```
double res;
```

```
res = a - b;
```

Call by Value



# Call by value

---

- In call by value mechanism
  - The values are copied to the function
- If we change values in the function
  - The copied version is changed
  - The original value does not affect
- Call by value inputs **cannot** be used to produce output.



# add function (**wrong** version)

---

```
void add(double a, double b, double res){  
    res = a + b;  
    return;  
}
```

```
int main(void){  
    double d1 = 10.1, d2 = 20.2;  
    double result = 0;  
    add(56.0, 6.7, result);  
    printf("result = %f\n", result);           // result = 0  
    add(d1, d2, result);  
    printf("result = %f\n", result);           // result = 0  
}
```



# Stack in C/C++

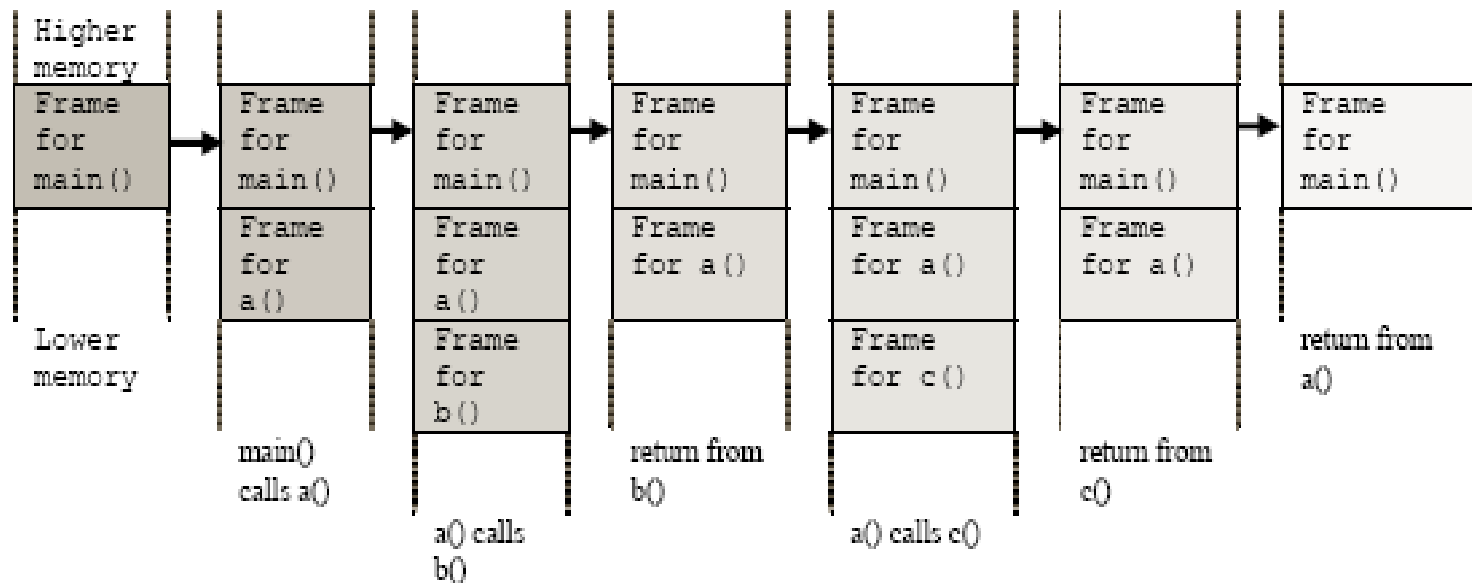
```
#include <stdio.h>
```

```
int b(int i){ return i; }
```

```
int c(int j){  
    return j; }
```

```
int a(int i, int j){  
    b(i);  
    c(j);  
    return 0;  
}
```

```
int main(){  
    a(3, 5);  
    return 0;  
}
```



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# Producing output

---

- What we have seen are the “Command”
- Query functions
  - Produce output
  - Output **cannot** be produced by the “call by value” parameters
- To produce an output
  - Declare output type
  - Generate the output by **return**



# The return command

---

- To generate a result by a function

**return <value>;**

- Only one value can be returned
- **return** finishes the running function
- Function can have multiple return
  - Only one of them runs each time
- The type of the returned value = the result type
  - Otherwise, cast



# Exmaple: my\_fabs (Version 1)

---

```
double my_fabs(double x){
    double res;
    if(x >= 0)
        res = x;
    else
        res = -1 * x;
    return res;
}

void main(void){
    double d = -10;
    double b;
    b = my_fabs(d);
    printf("%lf\n", b);                // 10
    printf("%lf\n", my_fabs(-2 * b));  // 20
}
```



# Exmample: my\_fabs (Version 2)

---

```
double my_fabs(double x){
    if(x >= 0)
        return x;
    return (-1 * x);
}

void main(void){
    double d = -10;
    double b;
    b = my_fabs(d);
    printf("b  = %lf\n", b);
    b = my_fabs(-2 * d);
    printf("b  = %lf\n", b);
}
```



# Output of functions

---

- A function can produce **at most one** output
- Output of functions can be **dropped**

`double f;`

`sin(f);`      **//we drop the output of sin**

`gcd(10, 20);` **//we drop the output of gcd**



# Casting in functions

---

## ➤ Cast for input

- Prototype: `void f(int a, double b);`
- Call: `f(10.1, 20.2);`

## ➤ Cast for output

- Prototype: `int f(int a);`
- Call: `double d = f(10);`
- Cast in return

```
int f(int a){  
    ...  
    return 10.20  
}
```



# Be careful: empty input/output type

- If output or input type is not specified → int
  - Casting may not work

```
f1(a){  
    printf("a = %d\n", a);    return a / 2;  
}  
f2(int a){  
    printf("a = %d\n", a);    return a / 2;  
}  
f3(float a){  
    printf("a = %f\n", a);    return a / 2;  
}  
int main(){  
    printf("%d\n", f1(10.5));  
    printf("%d\n", f2(10.5));  
    printf("%d\n", f3(10.5));  
    return 0;  
}
```

// a = 1  
// 0  
// a = 10  
// 5  
// a = 10.500000  
// 5



# Inline Functions and Macro's

---

- Function call using stack has its overhead
  - 2 approaches to reduce the overhead
- **inline** function
  - To ask from compiler to compile it as inline, but no guarantee.

**inline int f(float x)**

- **Macros**

**#define PRINT\_INT(X) printf("%d\n", X)**





# Example: GCD (بزرگترین مقسوم علیه مشترک)

---

```
# define PRINT_INT(x) printf("%d\n",x); \
                        printf("=====\n");
inline int gcd(int a, int b){ /* return gcd of a and b */
    int temp;
    while(b != 0){
        temp = a % b;
        a = b;
        b = temp;
    }
    return a;
}

void main(void){
    int i = 20, j = 35, g;
    g = gcd(i, j);
    printf("GCD of %d and %d = ", i , j);
    PRINT_INT(g);
    g = gcd(j, i);
    printf("GCD of %d and %d = ", j , i);
    PRINT_INT(g);}
```



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- **Scope of variables**
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# Scope of Variables

---

## ➤ Variables

- Are declared in the start of functions
- Are used any where in the function **after declaration**
- Cannot be used outside of function
- Cannot be used in other functions

## ➤ **Scope** of variable

- A range of code that the variable can be used
- ## ➤ Variable **cannot** not be used outside of its scope
- Compile error



# Scopes and Blocks

---

- Scopes are determined by Blocks
  - Start with `{` and finished by `}`
  - Example: statements of a **function**, statement of a **if** or **while**, ...
- Variables
  - **Can be** declared in a block
  - **Can be** used in the declared block
  - **Cannot be** used outside the declared block
- The declared block is the scope of the variable



# Variables in Blocks

---

```
#include <stdio.h>
int main(void){
    int i;
    for(i = 1; i <= 10; i++){
        int number;
        printf("Enter %d-th number: ", i);
        scanf("%d", &number);
        if((number % 2) == 0)
            printf("Your number is even\n");
        else
            printf("Your number is odd\n");
    }
    /* compile error: */
    // printf("The last number is %d\n", number);
    return 0;
}
```



# Nested Scopes/Blocks

---

- Scopes can be nested
  - Example: Nested **if**, nested **for**, ...

```
void main(){ // block 1
    int i;
    { // block 2
        int j;
        { // block 3
            int k;
        }
        int m;
    }
}
```



# Variables in Nested Blocks

---

- All variables from outer block can be used in inner blocks
  - Scope of outer block contains the inner block
- Variables in inner block **cannot** be used in outer block
  - Scope of the inner block does **not** contains the outer block



# Variables in Nested Blocks: Example

---

```
int k = 0;
for(int i = 0; i < 10; i++){
    /* block 1 */
    if(i > 5){
        /* block 2 */
        int j = i;
        ...
    }
    while(k > 10){
        /* block 3 */
        int l = i;
        /* int m = j; compile error */
        ...
    }
    /* k = 1; compile error */
}
```





# Same Variables in Nested Block

---

- If a variable in inner block has the same identifier of a variable in outer block
  - The inner variable **hides** the outer variable
  - Changing inner variables **does not** change outer variable

```
int j = 20, i = 10;
printf("outer i = %d, %d\n", i, j);
while(...){
    int i = 100;
    j = 200;
    printf("inner i = %d, %d\n", i, j);
    ...
}
printf("outer i = %d, %d\n", i, j);
```

**Do NOT  
Use It!!!**



# Local Variables

---

- All variables defined in a function are the **local variable** of the function
- Can **ONLY** be used in the function, not other functions

```
void func(void){  
    int i, j;  
    float f;  
    /* These are local variables */  
}  
int main(void){  
    i = 10; /* compile error, why? */  
    f = 0;  /* compile error, why? */  
}
```



# Global/External Variables

---

- Global variables are defined outside of all functions
- Global variables are *initialized* to zero
- Global variables are available to all **subsequent** functions

```
void f(){  
    i = 0; // compile error  
}  
int i;  
void g(){  
    int j = i; // g can use i  
}
```



# Global/External Variables: Example

---

```
int i, j;
float f;
void func(void){
    printf("i = %d \n", i);           // i = 0
    printf("f = %f \n", f);           // f = 1000
    i = 20;
}
void f1(){
    printf("%d", i);
}
int main(void){
    f = 1000;
    func();
    f1();
    return 0;
```



## Parameter Passing by Global Variables: my\_fabs (V.3)

---

```
double x;
```

```
void my_fabs(void){  
    x = (x > 0) ? x : -1 * x;  
}
```

```
void main(void){  
    double b, d = -10;  
    x = d;  
    my_fabs();  
    b = x;  
    printf("b = %f\n", b);  
}
```

Do not use this method.  
Parameters should be passed by  
input parameter list.

Global variable are used to  
define (large) variables that are  
used in many functions



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# Storage Classes

---

## ➤ Storage class:

- How memory is allocated for the variable
- Until when the variable exists
- How it is initialized

## ➤ Storage classes in C:

- Automatic (اتوماتیک) → **auto**
- External (خارجی) → **extern**
- Static (ایستا) → **static**
- Register (ثبات) → **register**



# Storage Classes: Automatic

---

- All local variables are automatic by default
  - Input parameters of a function
  - Variables defined inside a function/block
  - The keyword “**auto**” is optional before them
- Generated at the **start of each run of the block**
- Destroyed at the **end of each run of the block**
- Are not initialized





# Storage Classes: External

---

- All global variables are external by default
  - Are initialized by 0
  - Are generated when the program starts
  - Are destroyed when the program finishes
- Usage of keyword “extern”
  - To use global variables in other files
  - To use global variables before definition
  - To emphasize that the variable is global
    - This usage is optional
  - Access to a global variable with the same name



# extern Example

---

```
#include <stdio.h>
int x=50;
int main()
{
    int x=100;
    {
        extern int x;
        printf("x= %d\n",x);
    }
    printf("x= %d\n",x);
    return 0;
}
// x = 50
// x = 100
```



# Use a global variable in another file in C

---

- ❑ To use a global variable in another file in C using **extern**, you need to do the following steps:
  - Declare the global variable in one source file (for example, **file1.c**) and initialize it with a value.
    - For example: **int global\_var = 42;**
  - Declare the same global variable in a header file (for example, **file1.h**) using the **extern** keyword. This tells the *compiler* that the variable is defined elsewhere, and it should not allocate storage for it.
    - For example: **extern int global\_var;**
  - Include the header file in any other source file (for example, **file2.c**) that needs to access the global variable.
    - For example: **#include "file1.h"**



# Use a global variable in another file in C

---

- Use the global variable in any function in the other source file as you normally do. For example:  
`printf("Global variable: %d\n", global_var);`
- This way, you can share the same global variable across multiple source files without redefining it or causing conflicts.
- You can also modify the value of the global variable in **any source file**; the changes will be reflected in **all the other source** files that use it.



# Storage Classes: Static

---

- The keyword “**static**” comes before them
- For **local** variables:
  - 1) Generated in **the first run of the block**
  - 2) Destroyed **when program finishes**
  - 3) Initialized
    - If no value → initialized by 0
  - **Only initialized in the first run of the block**



# Storage Classes: Static

---

- The keyword “**static**” comes before them
- For **global** variables:
  - 1) Generated **when program starts**
  - 2) Destroyed **when program finishes**
  - 3) Always initialized
    - If no value → initialized by 0
  - 4) *Is not accessible for other files*



# Storage Classes: Register

---

- The keyword “**register**” comes before them
- Can be used for local variables
- The compiler tries to allocate the variable in registers of CPU.
  - But does **not** guarantee
  - Registers are very fast and small memories
- Improve performance



# Storage Classes, Auto: Examples

---

```
void f(int i, double d){  
    int i2;  
    auto int i3;  
    double d2;  
    auto double d3;  
}
```

All variables (i, d, i2, i3, d2, d3) are **auto** variables





# Storage Classes, Extern: Examples

---

```
int i = 10, j = 20;

void print(void){
    printf("i = %d, j = %d\n", i, j);
}

int main(void){
    extern int i;    // i refers the global i
    int j;           // j is new variable

    print();         // i = 10, j = 20
    i = 1000;
    j = 2000;
    print();         // i = 1000, j = 20
    return 0;
}
```



# Storage Classes: Examples

---

```
int i;
void func(void){
    int j;
    printf("i = %d \n", i);
    printf("j = %d \n", j);
    i = 20;
}
int main(void){
    func();
    func();
    i = 30;
    func();
    return 0;
}
```

// i = 0  
// j = ???  
// i = 20  
// j = ??  
// i = 30  
// j = ??



# Storage Classes, Static: Examples

---

```
void func(void){  
    int j;  
    static int i = 10;  
    printf("i = %d \n", i);  
    printf("j = %d \n", j);  
    i = 20;  
}
```

```
int main(void){  
    func();  
    func();  
    return 0;  
}
```

```
// i = 10  
// j = ???  
// i = 20  
// j = ???
```



# Storage Classes, Static: Examples

---

```
void func(void){
    int j;
    static int i;
    printf("i = %d \n", i);
    printf("j = %d \n", j);
    i = 20;
}

int main(void){
    func();
    func();
    // i = 30; /* compile error, why? */
    func();
    return 0;
}
```

```
// i = 0
// j = junk
// i = 20
// j = junk
// i = 20
// j = junk
```



# Storage Classes, Register: Examples

---

```
register int i;
```

```
for(i = 0; i < 100; i++)
```

```
...
```



# Be careful: loops and automatic variables

---

➤ According to standard:

*“For such an object that does not have a variable length array type, its lifetime extends from entry into the block with which it is associated until execution of that block ends in any way.”*

➤ Variable is defined in a block of a loop

➤ 1) The variable retains its value between iterations of the loop if it is **NOT a variable length** array

➤ 2) The variable **does NOT** retain its value between iterations of the loop if it is a **variable length array**



# Loops and automatic variables

---

```
int main(){
    int i;
    for(i = 0; i < 5; i++){
        int j;
        if(i){
            printf("&j = %p, j = %d\n"
                , &j, j);

            j++;
        }
        else
            j = i;
    }
}
```

&j = 0xffffcc38, j = 0  
&j = 0xffffcc38, j = 1  
&j = 0xffffcc38, j = 2  
&j = 0xffffcc38, j = 3



# Loops and automatic variables

---

```
int main(){
    int i;
    for(i = 0; i < 5; i++){
        int j[5 * i + 1];
        if(i){
            printf("&j[0] = %p, j[0] = %d\n"
                , &(j[0]), j[0]);

            j[0]++;
        }
        else
            j[0] = i;
    }
```

```
&j[0] = 0xffffcbd0, j[0] = 12291
&j[0] = 0xffffcbc0, j[0] = 230944
&j[0] = 0xffffcbb0, j[0] = 230944
&j[0] = 0xffffcb90, j[0] = -2148
```





# Loops and automatic variables

---

```
int main(){
    int i;
    for(i = 0; i < 5; i++){
        int j[5 * 3 + 1];
        if(i){
            printf("&j[0] = %p, j[0] = %d\n"
                , &j[0]), j[0]);
            j[0]++;
        }
        else
            j[0] = i;
    }
}
```

&j[0] = 0xffffcbf0, j[0] = 0  
&j[0] = 0xffffcbf0, j[0] = 1  
&j[0] = 0xffffcbf0, j[0] = 2  
&j[0] = 0xffffcbf0, j[0] = 3



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# How to use functions: Example

---

## ➤ An Example

➤ Goldbach's Conjecture (حدس گلدباخ)

➤ Any even number larger than 2 can be expressed as the sum of two prime numbers.

## ➤ It is not proved yet!

➤ A prize of 1,000,000\$ to proof ;-)

➤ Write a program that takes a set of numbers that end with 0 and checks the correctness of the conjecture.



# Main Overall Algorithm

---

```
While(number is not zero)
  if(number >= 2 and even)
    Check Goldbach's Conjecture
  else
    Print some message
  read next number
```

**This is a module**

**It is a black-box in this step**



# Check Goldbach's Conjecture Algorithm

---

**Algorithm:** Goldbach

**Input:**  $n$

**Output:** 0 if conjecture is incorrect else 1

$i = 2$

while ( $i \leq n/2$ )

$j = n - i$

    if(**is\_prime**( $j$ ))

        conjecture is correct

        return

$i = \text{next\_prime\_number}(i)$

**This is a module**

**It is a black-box in this step**

Conjecture is incorrect



# The is\_prime algorithm

---

**Algorithm:** is\_prime

**Input:** n

**Output:** 1 if n is prime else 0

for(i from 2 to  $\sqrt{n}$ )

    if( $n \% i == 0$ )

        n is not prime

n is prime



# The next\_prime\_number algorithm

---

**Algorithm:** next\_prime\_number

**Input:** n

**Output:** prime number

if n is 2

    output is 3

else

    do

$n = n + 2$

    while(**is\_prime**(n) == 0)

    output is n



# Putting them altogether

---

```
int is_prime(int n){  
    ...  
}  
  
int next_prime_number(int n){  
    ...  
}  
  
int check_Goldbach(int n){  
    ...  
}  
  
int main(void){  
    ...  
}
```





# What We Will Learn

---

- Introduction
- Passing input parameters
- Producing output
- Scope of variables
- Storage Class of variables
- Function usage example
- **Recursion**



# Introduction

---

## ➤ Iteration vs. Recursion

- The Recursion and the Iteration both **repeatedly** execute the set of instructions.

## ➤ Factorial

➤  $n! = n \times n-1 \times \dots \times 2 \times 1$

➤  $n! = n \times (n-1) !$



# Introduction

---

## ➤ Iteration vs. Recursion

- The Recursion and the Iteration both **repeatedly** execute the set of instructions.

## ➤ Factorial

➤  $n! = n \times n-1 \times \dots \times 2 \times 1$

➤  $n! = n \times (n-1) !$

## ➤ Greatest common divisor (GCD)

➤  $\text{GCD}(a, b) = \text{Euclidean Algorithm}$

➤  $\text{GCD}(a, b) = \text{GCD}(b, a \bmod b)$



# Introduction

---

- Original problem can be solved by
  - Solving a **similar** but **simpler** problem (recursion)
    - $(n-1)!$  in factorial,  $\text{GCD}(b, a \bmod b)$
- There is a simple (**basic**) problem which we can solve it directly (without recursion)
  - **Factorial:**  $1! = 1$
  - **GCD:**  $a \bmod b == 0 \rightarrow a$



# Recursion in C

---

## ➤ Recursive Algorithm

- An algorithm uses **itself** to solve the problem
- There is a basic problem with known solution

## ➤ Recursive Algorithms are implemented by **recursive functions**

## ➤ Recursive function

- **A function which calls itself**
- There is a condition that it does not call itself



# Recursive function to calculate Factorial

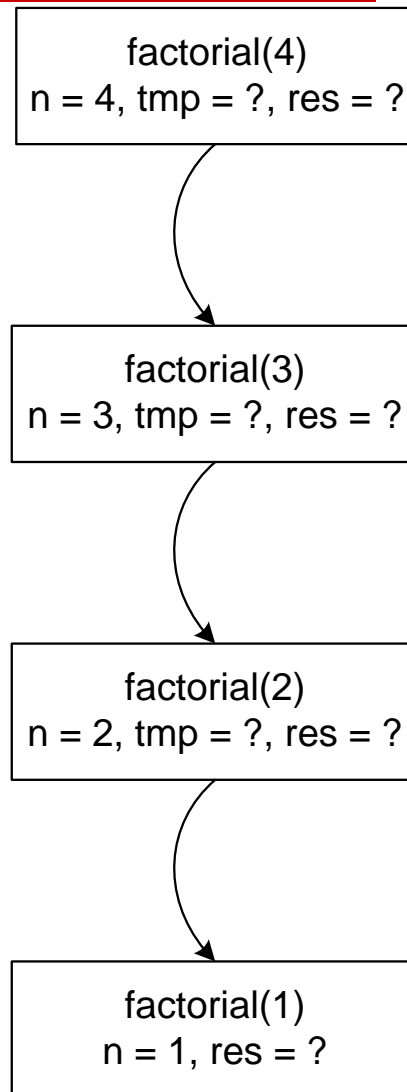
---

```
#include <stdio.h>
int factorial(int n){
    int res, tmp;
    if(n == 1)
        /* The basic problem */
        res = 1;
    else{ /* The recursive call */
        tmp = factorial(n - 1);
        res = n * tmp;
    }
    return res;
}
void main(void){
    int i = 4;
    int fac = factorial(i);
    printf("%d! = %d\n", i, fac);
}
```

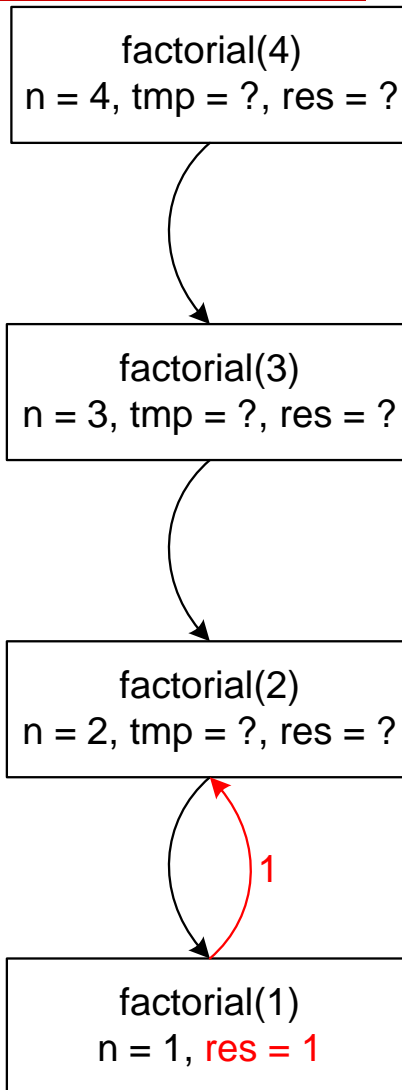


# Function Call Graph + Stacks

---

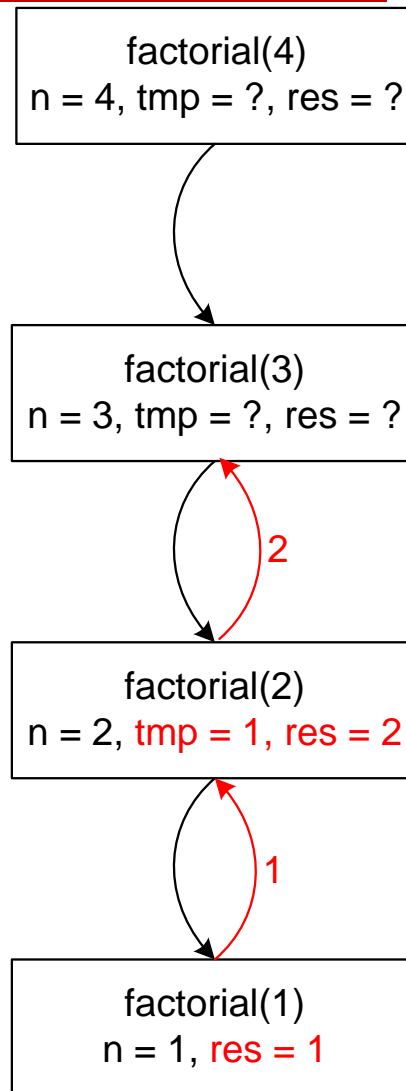


# Function Call Graph + Stacks

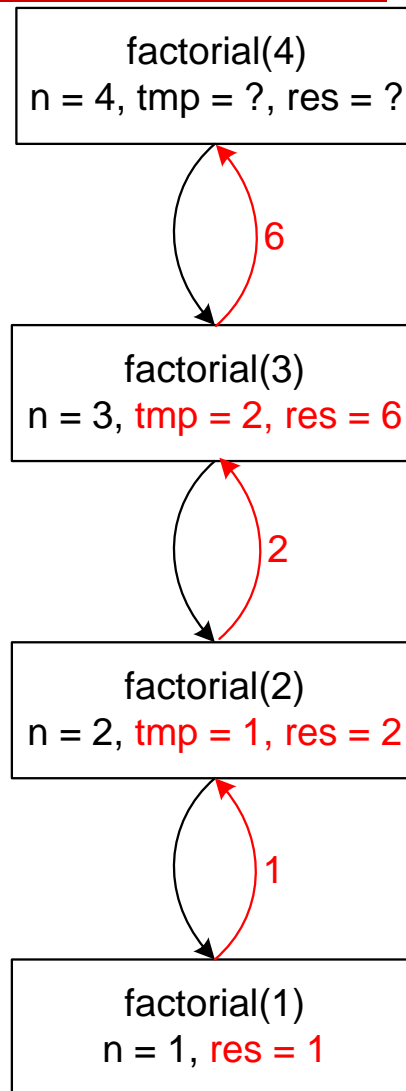




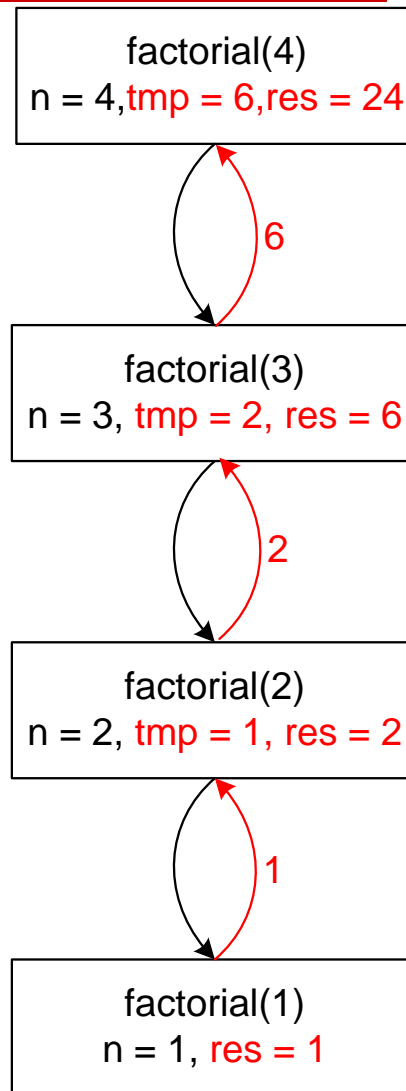
# Function Call Graph + Stacks



# Function Call Graph + Stacks



# Function Call Graph + Stacks



# Examples

---

- Recursive version of GCD?
- Recursive version of Fibonacci numbers
  - Fibonacci numbers
    - 1, 1, 2, 3, 5, 8, ...
- Print digits: left-to-right and right-to-left



# Greatest common divisor (GCD)

---

```
#include <stdio.h>
```

```
int GCD(int a, int b){
```

```
    if(b == 0)
```

```
        return a;
```

```
    else
```

```
        return GCD(b, a % b);
```

```
}
```

```
int main(void){
```

```
    printf("GCD(1, 10) = %d \n", GCD(1, 10));
```

```
    printf("GCD(10, 1) = %d \n", GCD(10, 1));
```

```
    printf("GCD(15, 100) = %d \n", GCD(15, 100));
```

```
    printf("GCD(100, 15) = %d \n", GCD(100, 15));
```

```
    printf("GCD(201, 27) = %d \n", GCD(201, 27));
```

```
    return 0;
```

GCD(1, 10) = 1  
GCD(10, 1) = 1  
GCD(15, 100) = 5  
GCD(100, 15) = 5  
GCD(201, 27) = 3



# Fibonacci numbers

```
#include <stdio.h>
int fibo(int n){
    if(n == 1)
        return 1;
    else if(n == 2)
        return 1;
    else
        return fibo(n - 1) + fibo(n - 2);
}
```

تابع بازگشتی محاسبه جمله  $n$ -ام  
اعداد فیبوناچی

```
int main(void){
    printf("fibo(1) = %d\n", fibo(1));
    printf("fibo(3) = %d\n", fibo(3));
    printf("fibo(5) = %d\n", fibo(5));
    printf("fibo(8) = %d\n", fibo(8));
    return 0;
}
```

fibo(1) = 1  
fibo(3) = 2  
fibo(5) = 5  
fibo(8) = 21



# Print digits recursive

```
#include <stdio.h>

void print_digit_right_left(int n){
    int digit = n % 10;
    printf("%d ", digit);
    if(n >= 10)
        print_digit_right_left(n / 10);
}

int main(void){
    printf("\n print_digit_right_left(123): ");
    print_digit_right_left(123);    // 3 2 1
    printf("\n print_digit_right_left(1000): ");
    print_digit_right_left (1000); // 0 0 0 1
    return 0;
}
```

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راست به چپ



# Print digits recursive

```
#include <stdio.h>

void print_digit_left_right(int n){
    if(n >= 10)
        print_digit_left_right(n / 10);
    int digit = n % 10;
    printf("%d ", digit);
}

int main(void){
    printf("\n print_digit_left_right(123): ");
    print_digit_left_right(123);    // 1 2 3
    printf("\n print_digit_left_right(1000): ");
    print_digit_left_right (1000); // 1 0 0 0
    return 0;
}
```

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چپ به راست





# Find the Largest Element in an Array

---

```
#include <stdio.h>

int max(int a, int b){
    return a > b ? a : b;
}

int findMaxRec(int A[], int n){
    if (n == 1)
        return A[0];
    return max(A[n-1], findMaxRec(A, n-1));
}

int main(){
    int arr[] = {10, 324, 45, 90, 9808};
    int n = sizeof(arr)/sizeof(arr[0]);
    printf("Largest in given array is %d", findMaxRec(arr, n));
    return 0;
}
```



# Indirect recursion

---

- What we have seen are direct recursion
  - A function calls itself directly
- Indirect recursion
  - A function calls itself using another function
  - Example:
    - Function A calls function B
    - Function B calls function A



# Determine whether input is odd or even

```
#include <stdio.h>
#include <stdbool.h>
bool is_even(int n);
bool is_odd(int n);

bool is_even(int n){
    if(n == 0)
        return true;
    if(n == 1)
        return false;
    else
        return is_odd(n - 1);
}
bool is_odd(int n){
    if(n == 0)
        return false;
    if(n == 1)
        return true;
    else
        return is_even(n - 1);
}
```

تابع بازگشتی تعیین زوج یا فرد بودن  
عدد داده شده

```
int main(void){
    if(is_even(20))
        printf("20 is even\n");
    else
        printf("20 is odd\n");

    printf("23 is %s\n",
is_odd(23) ? "odd" : "even");

    return 0;
}
```



# Bugs and Avoiding Them

---

- Be careful about the order of input parameters.

```
int diff(int a, int b){return a - b;}
```

diff(x, y) or diff(y, x)

- Be careful about **casting** in functions.
- Recursion must finish, be careful about basic problem in the recursive functions.
  - No base problem → Stack Overflow
- Static variables are useful debugging



# Questions

---

Which of the following statements about functions in C is NOT true?

- A. Function prototypes are required before the function is called in the code.
- B. The return type of a function must always be specified; it cannot be omitted.
- C. A function can be defined inside another function.
- D. Global variables can be accessed from any function from any file.

➤ **Answer: C**



# Questions

---

What is the primary advantage of using inline functions in C?

- A) Inline functions reduce the overhead of function calls by directly inserting code at the call site
- B) Inline functions allow functions to be written without specifying any return type
- C) Inline functions are mandatory for all functions with parameters
- D) Inline functions cannot be used for simple operations

➤ **Answer: A**



# Questions

---

What will be the output of the following code?

```
int func(int i)
{ if ( i%2 ) return (i++);
  else return func(func( i - 1 ));
}
int main(){
    printf(" %d ", func(2));
    return 0;
}
```

- A. 2 1 0
- B. 2 1 2
- C. 0
- D. 1

➤ **Answer: D**



# Reference

---

➤ **Reading Assignment:** Chapter 5 of “C How to Program”

