

# Image Analysis

(SE3IA11 + SEMIP12)

## Lectured by

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Room 145 (HW) and Room 123 (JMF)  
the SSE Building

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## Reference books

- Rafael Gonzalez & Richard Woods, *Digital Image Processing*, 2<sup>nd</sup> edition, Prentice Hall, 2002
- S G Hoggar, *Mathematics of Digital Images – Creation, Compression, Restoration, Recognition*, Cambridge Univ. Press, 2006
- Anil K. Jain, *Fundamentals of Digital Image Processing*, Prentice Hall, 1989
- Milan Sonka, Vaclav Hlavac, and Roger Boyle, *Image Processing, Analysis, and Machine Vision*, Thomson Learning, 2007

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## Recommended Journals

- *IEEE Transaction on Image Processing*
- *Image and Vision Computing*
- *IEEE Transaction on Pattern Analysis and Machine Intelligence (PAMI)*
- Many conference proceedings, *e.g.*
  - International Conference of Image Processing (ICIP)
  - International Conference of Pattern Recognition (ICPR)
  - International Conference of Computer Vision (ICCV)
  - Computer Vision and Pattern Recognition (CVPR)
  - British Machine Vision Conference (BMVC)
  - More .....

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## Arrangements for the module

- This is a 10 credit module running through the autumn term. Two lectures a week.
  - 14:00-16:00 Fridays for 10 weeks (HARB164)
  - Week 3 is used for a tutorial in a lab (SSE G21)
  - Week 11 is for a demonstration in a lab (SSE G21)
- Two pieces of coursework associated with lab practicals (unsupervised)
  - Assignment 1: image enhancement (15% assessment)
  - Assignment 2: image compression (15% assessment)
- One 2-hour written examination in May/June 2016. It counts 70% of the final assessment.

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## Contents covered in this module

- Fundamentals of digital images
- Image enhancement
- Colour image processing
- Image compression
- Mathematical morphology in image processing
- Image segmentation

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## Detailed scheduling

Week	Topic	Lecturer
Week 1 (2 <sup>nd</sup> October)	Fundamentals of Image Analysis	HW
Week 2 (9 <sup>th</sup> October)	Image Enhancement (Spatial)	JMF
Week 3 (16 <sup>th</sup> October)	Tutorial (MatLab+OpenCV)	HW
Week 4 (23 <sup>rd</sup> October)	Image Enhancement (Frequency)	JMF
Week 5 (30 <sup>th</sup> October)	Colour Image Processing	HW
Week 7 (13 <sup>th</sup> November)	Image Compression (IC)	JMF
Week 8 (20 <sup>th</sup> November)	IC2 / Symbolic Feature Extraction	JMF
Week 9 (27 <sup>th</sup> November)	Morphological Image Processing	HW
Week 10 (4 <sup>th</sup> December)	Image Segmentation	HW
Week 11 (11 <sup>th</sup> December)	Compression coursework assessment	HW&JMF

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## Digital image analysis

- Questions to be answered in this module
  - What is digital image?
  - How is a digital image formed mathematically?
  - Are there any applications where image analysis is required?
  - How to make the applications feasible?
    - Various techniques and processes

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## Applications of image analysis (1)

- Medical and biomedical images



(a) Gastric body  
from endoscope

(b) Hip joints  
from X-ray

(c) Cells from  
microscope

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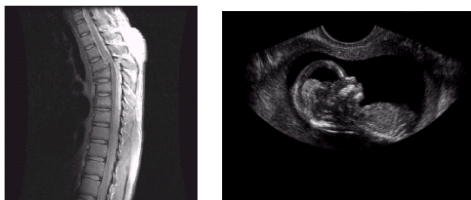
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## Applications of image analysis (2)

- Further medical images



(a) MRI of human spine

(b) Ultrasound image of a baby

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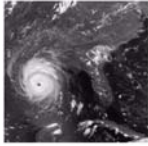
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### Applications of image analysis (3)

- Remotely sensed data in climate and environment research – observation



(a) Multispectral image of hurricane (from GEO Satellite)



(b) SAR image: surface of Venus (from Magellan probe)



(c) LIDAR data (from airborne laser scanning)

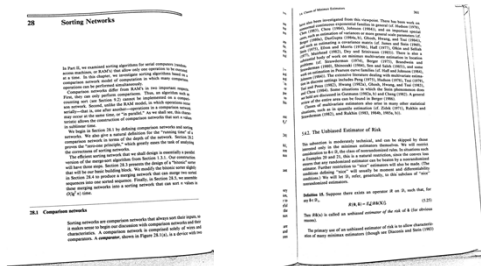
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### Applications of image analysis (4)

- Image-based document analysis



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### Applications of image analysis (5)

- Security (CCTV): visual surveillance
- Webcam application: looking after elders through mobile phones
- London congestion control: automatic number plate recognition (ANPR)
- Biometrics: face images, finger prints, iris images,...
- Information retrieve in the Internet: image based information search (Google Goggles).
- The *Google Book Search* project unveiled in late 2004 aims to make all the world's books discoverable online.
- And more .....

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### Typical processes in image analysis (from perception to cognition)

- Image acquisition
- Image enhancement and restoration
- Image compression
- Morphological processing
- Image segmentation and description
- Recognition: understanding and interpretation (intelligent?)

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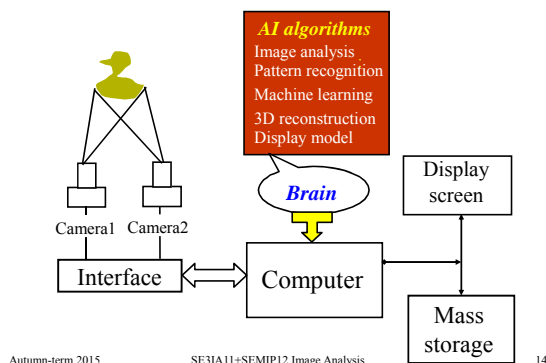
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### A computer imaging system



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### Image acquisition: lighting (electromagnetic radiation – EMR)

- “Light” in imaging covers a part of the electromagnetic spectrum beyond the visible spectrum (wavelength 380-760 nm).
- Light has two forms of energy: electricity and magnetism which are transmitted together as EMR in the speed of  $2.998 \times 10^8 \text{ m/s}$ .
- The electromagnetic spectrum can be expressed in terms of wavelength, frequency (or energy), and speed as

$$\lambda = \frac{c}{\nu} \quad \text{and} \quad \text{energy } E = h\nu \quad \text{with } h \text{ a constant.}$$

where  $\lambda$  is wavelength,  $\nu$  frequency, and  $c$  speed.

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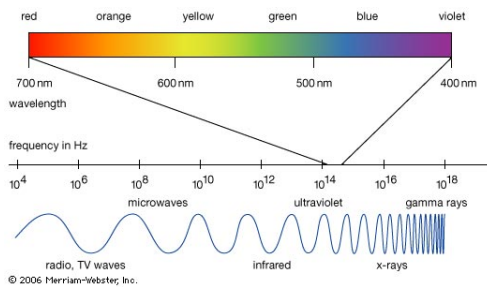
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## The electromagnetic spectrum



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## Image acquisition: sensors (1)

- Imaging is a process in which the reflected energy from illuminated scenes is received (or collected) by sensing elements or materials, called sensors.
- Four components: light source, scene, **sensors**, and **lens** – **optical systems**.
- Sensors must be responsive to light sources, *e.g.* X-ray, infrared, visible lights, etc. by using different sensing materials (*e.g.* different CCD or CMOS).
- Sensing: transform incoming illumination energy (reflected from scene) into a voltage by sensors, from which the output voltage is digitised to generate a value of a pixel in a digital image.

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## Image acquisition: sensors (2)

- Three principal sensor arrangements
  - *Single sensor*: sensor moving, *e.g.* raster scanning
  - *Line sensor*: sensor strip in linear motion
  - *Sensor arrays*: popularly used in normal digital cameras and cam-recorders.
- Outputs of all the above different sensors could be arranged to a 2D array reflecting illumination energy of a scene.

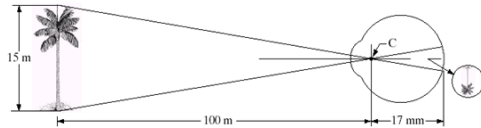
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### Image acquisition: optical systems

- An optical system (lens) plays the role to refract an observed scene onto an imaging plane (i.e. a focal plane in the pin-hole model).



C is the optical centre of the lens.

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### PSF and MTF in an optical system

- PSF: the *point spread function* indicates an optical system response to an impulse  $\delta(x, y)$ .
  - All physical optical systems blur (spread) a point of light to some degree. After an optical system,  $\delta(x, y)$  becomes to  $h(x, \alpha, y, \beta) = H[\delta(x - \alpha, y - \beta)]$ , mathematically called convolution, where  $\alpha$  and  $\beta$  are parameters related with the optical system.
- MTF: the *modulation transfer function* is defined as

$$MTF(f_s) = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$$

where  $I_{\max}$  and  $I_{\min}$  are maximum and minimum grey values of pixels in an image, respectively.  $MTF$  is a function of spatial frequency  $f_s$ . It is affected by the arrangement of sensor arrays.

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### Representation of digital images

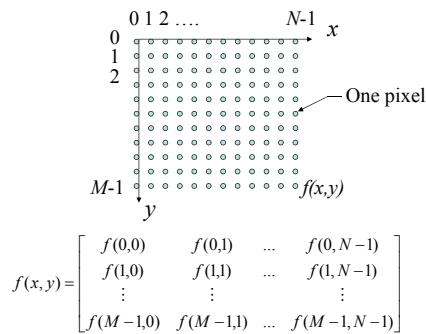
- A digital image is normally represented by a two-dimensional (2D) array, e.g.  $f(x, y)$ , where  $x=1, 2, \dots, M$  and  $y=1, 2, \dots, N$ , representing the size of the image.
- Each element in the array is a real number, called a **pixel** and represented by a finite number of bits.
- A matrix denotes a digital image in the formal mathematic term.

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### Digital image: matrix expression



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### Image sampling and quantisation (1)

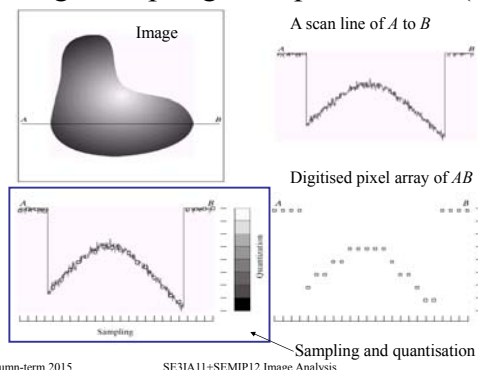
- Image sampling deals with issues of how many pixels are used to represent a scene.
  - Digitising the coordinate values: the Nyquist sampling theorem is applied.
  - The Nyquist states that the minimum sampling frequency is twice as high as the signal frequency.
- Image quantisation regards issues of how many bits used for one pixel.
  - Digitising the amplitude values of illumination energy: the visual quality should be satisfied.

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### Image sampling and quantisation (2)



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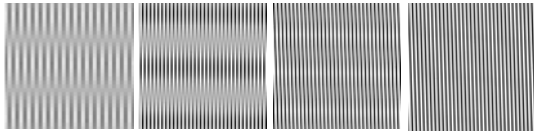
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### Example of image sampling (1)

- Sampling black and white bars with 100 lines/inch.
    - (a) 100 dpi (0.5 Nyquist-Shannon sampling rate)
    - (b) 200 dpi (with Nyquist-Shannon sampling rate)
    - (c) 300 dpi (1.5 Nyquist-Shannon sampling rate)
    - (d) 600 dpi (3 Nyquist-Shannon sampling rate)
- where dpi stands for "dots per inch".



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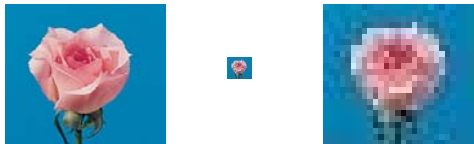
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### Example of image sampling (2)

- Pink rose in colours: details are lost in (c).
  - (a)  $599 \times 812 \times 3$  uint8
  - (b)  $82 \times 111 \times 3$  uint8
  - (c) The image in (b) re-sampled into  $599 \times 812$ .



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### Example of image quantisation



(a) Original lizard image:  
uint8×3 bits



(b) Image in 4 grey levels

(c) Image in 2 grey levels



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### Image resizing

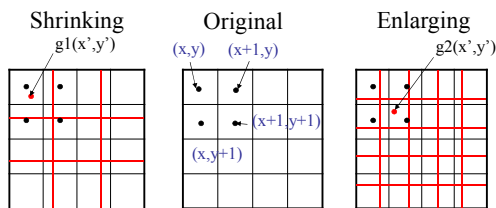
- Shrinking digital images: operation of undersampling, e.g.  $512 \times 512 \Rightarrow 256 \times 256$
- Enlarge digital images: operation of oversampling, e.g.  $256 \times 256 \Rightarrow 512 \times 512$
- Two main steps in the operations
  - Creation of new pixel locations
  - Assignment of grey levels to those new locations
- Techniques used in the image resizing operation
  - Nearest neighbour interpolation (NNI)
  - Bilinear interpolation (BLI)

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### Image resizing: interpolation (NNI)



- For NNI:  $g1(x',y')=g(x,y)$ ;  $g2(x',y')=g(x+1,y+1)$
- How about  $g1$  and  $g2$  based on the BLI algorithm?

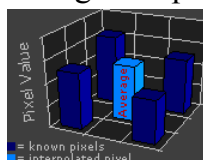
<http://www.cambridgeincolour.com/tutorials/image-interpolation.htm>

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### Image resizing: interpolation (BLI)



- Bilinear interpolation considers the closest  $2 \times 2$  neighbourhood of known pixel values surrounding the unknown pixel.
- It takes a weighted average of these 4 pixels to arrive at its final interpolated value.
- This algorithm results in much smoother looking images than NNI.

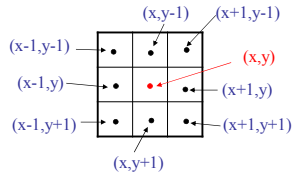
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### Relationships between pixels (1)

- Neighbours of a pixel  $p(x,y)$ 
  - 4-neighbours  $N_4(p)$ :  $(x-1,y)$ ,  $(x+1,y)$ ,  $(x,y-1)$ ,  $(x,y+1)$
  - Four diagonal neighbours  $N_D(p)$ :  $(x-1,y-1)$ ,  $(x-1,y+1)$ ,  $(x+1,y-1)$ ,  $(x+1,y+1)$



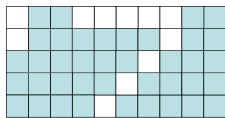
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### Relationships between pixels (2)

- Regions and boundaries: binary images have two sets  $\{1\}$  and  $\{0\}$ 
  - *Connectivity*: two pixels are neighbored, but they are connected only if they both belong to set  $\{1\}$  or set  $\{0\}$ .
  - *Connected components*: for any pixel  $p$  in set  $S$ , the set of pixels are connected to  $p$  in  $S$  is called a connected component in  $S$ .

 $S\{1\}$ : blue $S\{0\}$ : white

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### Relationships between pixels (3)

- Distance between pixels  $p(x_1,y_1)$  and  $q(x_2,y_2)$ 
  - The Euclidean distance
$$D_e = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$
  - The  $D_4$  distance:  $D_4 = |x_1 - x_2| + |y_1 - y_2|$
  - The  $D_8$  distance:  $D_8 = \max(|x_1 - x_2|, |y_1 - y_2|)$
- Image operations on a pixel basis
  - Each pixel represents an element in a matrix.
  - Image operations follow operations among matrices.

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### Image quality evaluation

- Two types of criteria for image evaluation: subjective and quantitative.
- Quantitative evaluation of image  $f(x,y)$ :
  - A reference image  $f'(x,y)$  is needed.
  - The average mean square error is used for the evaluation as

$$\sigma^2 = \frac{1}{MN} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} |f(x,y) - f'(x,y)|^2$$

- Image fidelity criteria are useful for
  - Measuring image quality
  - Rating the performance of a processing techniques.

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### Questions for further thinking

- How to express a digital image mathematically ?
- Issues of digital image visualisation (sampling and quantisation)
- Based on the concept of image resizing, work out how to deal with image rotation (matrix rotation) and shape distortion.
- Image quality evaluation: try to think about more efficient measures for the purpose. Do we need benchmarks for the purpose? If so, how to establish the benchmarks (with assumptions)?

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### End of the first two lectures

- Summary of what you have learned in the two lectures.
- Revision on matrix operations

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