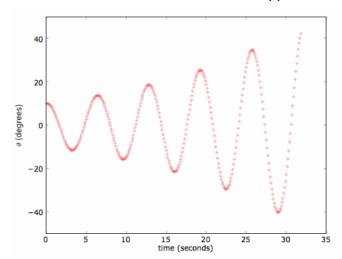
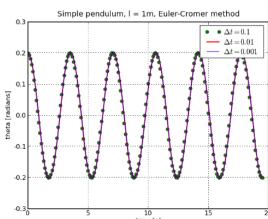
- The perpendicular force through a string in a basic pendulum SHO is given by:
- $F_{\theta} = mgsin(\theta)$
- Angular velocity of the pendulum:  $\omega_{i+1} = \omega_i \frac{g}{l}\theta_i \Delta t$ ,  $\theta_{i+1} = \theta_i + \omega \Delta t$
- A lower  $\Delta t$  makes the errors in a Euler approximation system smaller.



Graph similar to the example in the

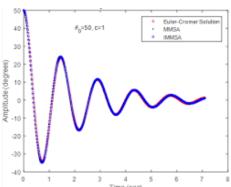
book which was used to graphically describe an Euler approximation of a SHO system.

- Total Energy of the pendulum:  $E = 1/2 ml^2 \omega^2 + mgl(1 cos(\theta))$
- The Euler-Cromer method of approximation takes a different approach to the same method as the Euler method and in SHO problems tends to better conserve energy.



Graph similar to the example in the book

which was used to graphically describe an Euler-Cromer approximation of a SHO system.



Graph similar to the example in the book which was used to graphically describe an Euler-Cromer approximation of a damped pendulum system.

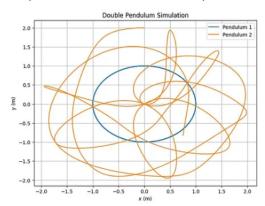
Underdamped system:  $\theta(t) = \theta_0 e^{-qt/2} sin(\sqrt{\Omega^2 - q^2/4t + \phi})$ 

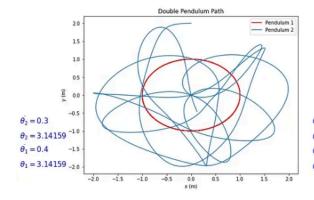
Overdamped system:  $\theta(t) = \theta_0 e^{-q/2 \pm \sin(\sqrt{q^2/4 - \Omega^2})t}$ 

Critically:  $\theta(t) = (\theta_0 + Ct)e^{-qt/2}$ 

Chaotic behavior in a pendulum has to do with the driving force in the pendulum.

Examples of chaotic behavior in pendulums:





15 0.5 E 0.0  $\theta_2 = 3.14159^{-1.0}$  $\dot{\theta_1} = 0.4$ -1.5  $\theta_1 = 2.61799_{-2.0}$ 

