



# Lecture 4: Recursion

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# Outline

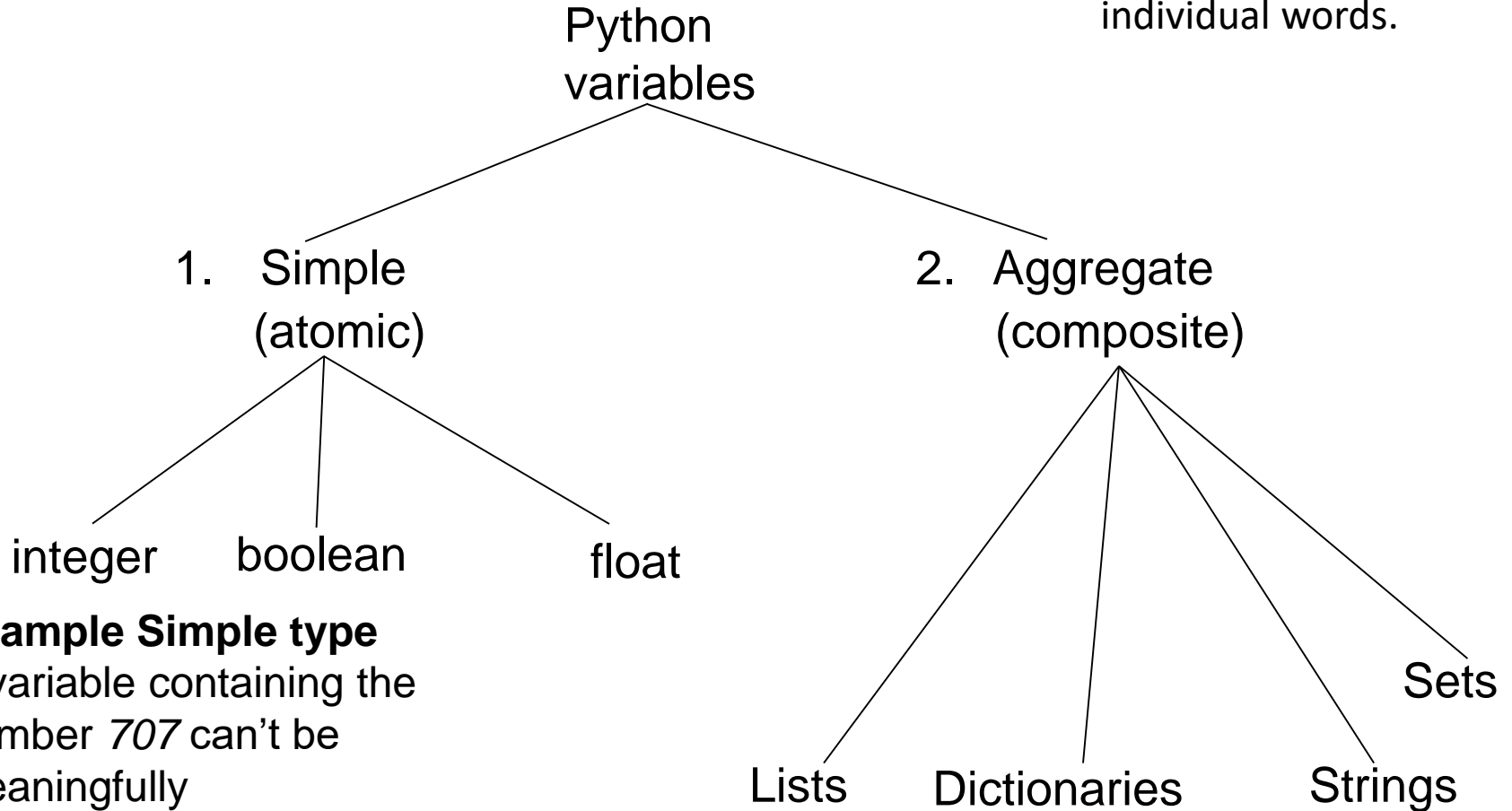
- Compound datatypes
- Recursion
- File management

# Compound datatypes

# Types Of Variables

## Example composite

A string (sequence of characters) can be decomposed into individual words.



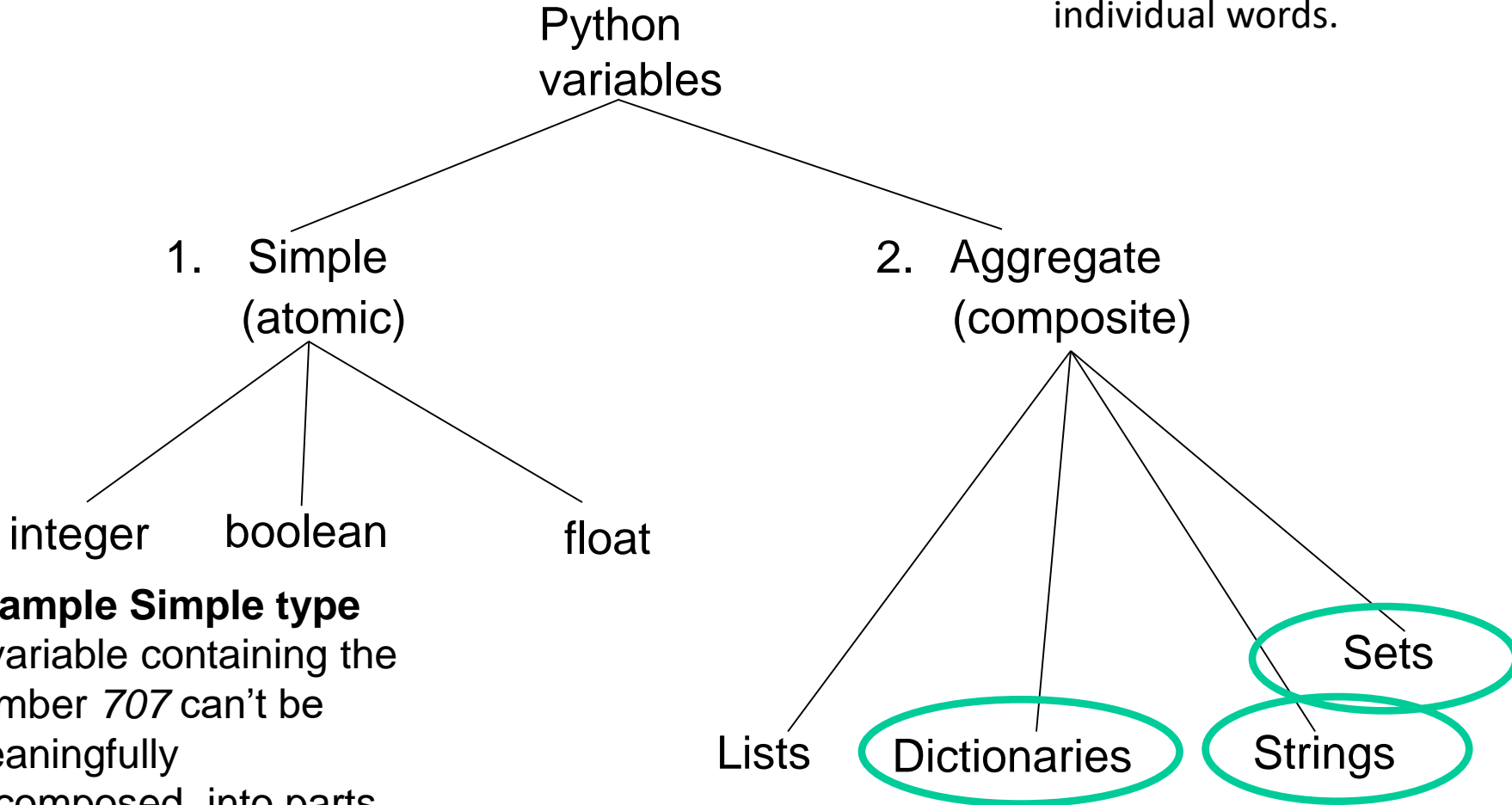
## Example Simple type

A variable containing the number 707 can't be meaningfully decomposed into parts

# Types Of Variables

## Example composite

A string (sequence of characters) can be decomposed into individual words.



## Example Simple type

A variable containing the number 707 can't be meaningfully decomposed into parts

# **Compound datatypes**

## **Strings**

# What are strings?

- Strings are a list of characters
- Almost all operations on lists also work on strings!

# **Compound datatypes**

## **Dictionaries**



# What is a dictionary?

- You can think of it as a list of pairs, where the first element of the pair, the **key**, is used to retrieve the second element, the **value**.
- Thus we ***map a key to a value***
- Example:
  - Telephone book

# Key Value pairs

- The key acts as an index to find the associated value.
- Just like a dictionary, you look up a word by its spelling to find the associated definition
- A dictionary can be searched to locate the value associated with a key

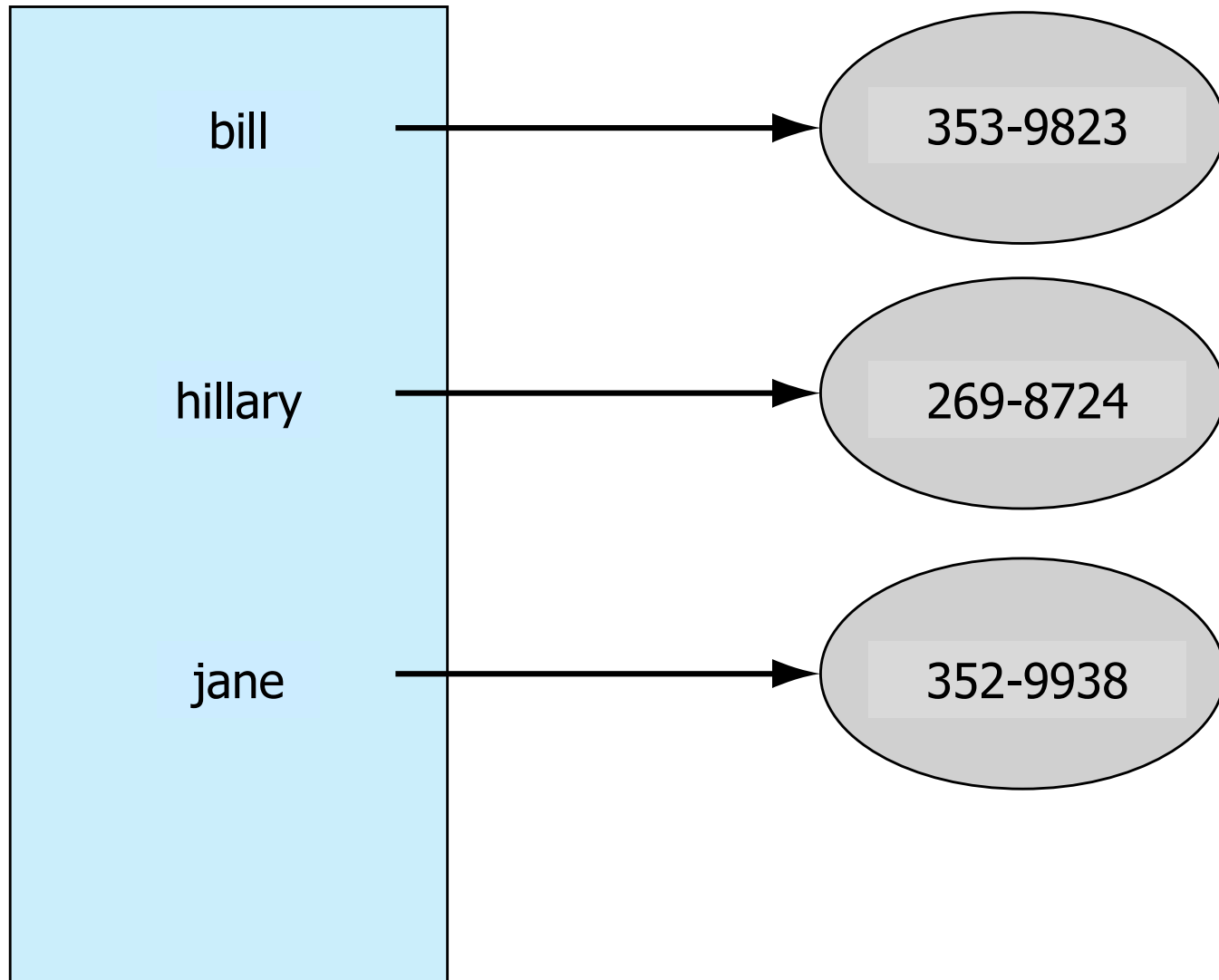
# Python Dictionary

- Use the { } marker to create a dictionary
- Use the : marker to indicate key:value pairs

```
contacts= {'bill':'353-9823',  
          'hillary':'269-8724', 'jane':'352-9938'}  
print (contacts)  
{'jane':'352-9938',  
  'bill':'353-9823',  
  'hillary':'369-8724'}
```

## Contacts

## Phone numbers



# Keys and values

- Key must be immutable
  - strings, integers, tuples are fine
  - lists are NOT
- Value can be anything

# Collections but not a sequence

- dictionaries are collections but they are not sequences such as lists, strings or tuples
  - there is no order to the elements of a dictionary
  - in fact, the order (for example, when printed) might change as elements are added or deleted.
- So how to access dictionary elements?

# Access dictionary elements

Access requires [ ], but the *key* is the index!

```
my_dict={}
```

- an empty dictionary

```
my_dict['bill']=25
```

- added the pair 'bill':25

```
print(my_dict['bill'])
```

- prints 25

# Dictionaries are mutable

- Like lists, dictionaries are a mutable data structure
  - you can change the object via various operations, such as index assignment

```
my_dict = {'bill':3, 'hillary':10}
print(my_dict['bill'])           # prints 3
my_dict['bill'] = 100
print(my_dict['bill'])           # prints 100
```



# Common operators with Lists

Like others, dictionaries respond to these

- `len(my_dict)`
  - number of key:value **pairs** in the dictionary
- `element in my_dict`
  - boolean, is `element` a **key** in the dictionary
- `for key in my_dict:`
  - iterates through the **keys** of a dictionary

# Dictionary content methods

- `my_dict.items()` – List of all the key/value pairs
- `my_dict.keys()` – List of all the keys
- `my_dict.values()` – List of all the values

How to print all values in a dictionary, each value in a separate row?



# Example: Word frequencies

We are given a list of words

```
word_list=['she','dog','cat','hello','he','she','good','dog']
```

and want to compute the word frequencies using a dictionary



## Example: Word frequencies

```
count_dict = {}  
for word in word_list:  
    if word in count_dict:  
        count_dict[word] += 1  
    else:  
        count_dict[word] = 1
```

# **Compound datatypes**

## **Sets**

# Sets, as in Mathematical Sets

- in mathematics, a set is a collection of objects, potentially of many different types
- in a set, no two elements are identical. That is, a set consists of elements each of which is unique compared to the other elements
- there is no order to the elements of a set
- a set with no elements is the empty set

# Creating a set

Set can be created in one of two ways:

- constructor:

```
my_set = set('abc')  
my_set → {'a', 'b', 'c'}
```

- shortcut: { }

```
my_set = {'a', 'b', 'c'}
```

# Diverse elements

- A set can consist of a mixture of different types of elements

```
my_set = {'a', 1, 3.14159, True}
```

- as long as the single argument can be iterated through, you can make a set of it



# No duplicates

- duplicates are automatically removed

```
my_set = set("aabbccdd")  
print(my_set)  
→ {'a', 'c', 'b', 'd'}
```

# Example

```
>>> null_set = set()           # set() creates the empty set
>>> null_set
set()

>>> a_set = {1,2,3,4}          # no colons means set
>>> a_set
{1, 2, 3, 4}

>>> b_set = {1,1,2,2,2}        # duplicates are ignored
>>> b_set
{1, 2}

>>> c_set = {'a', 1, 2.5, (5,6)} # different types is OK
>>> c_set
{(5, 6), 1, 2.5, 'a'}

>>> a_set = set("abcd")        # set constructed from iterable
>>> a_set
{'a', 'c', 'b', 'd'}          # order not maintained!
```

# Common operators

Most data structures respond to these:

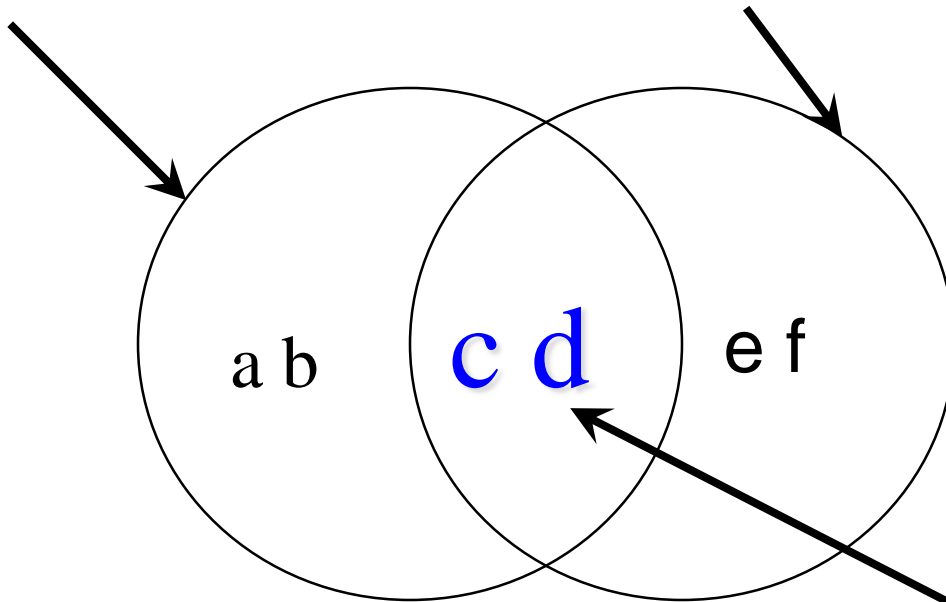
- `len(my_set)`
  - the number of elements in a set
- `element in my_set`
  - boolean indicating whether element is in the set
- `for element in my_set:`
  - iterate through the elements in `my_set`

# Set operators

- The set data structure provides some special operators that correspond to the operators you learned in middle school.
- These are various combinations of set contents
- These operations have both a method name and a shortcut binary operator

## method: intersection, op: &

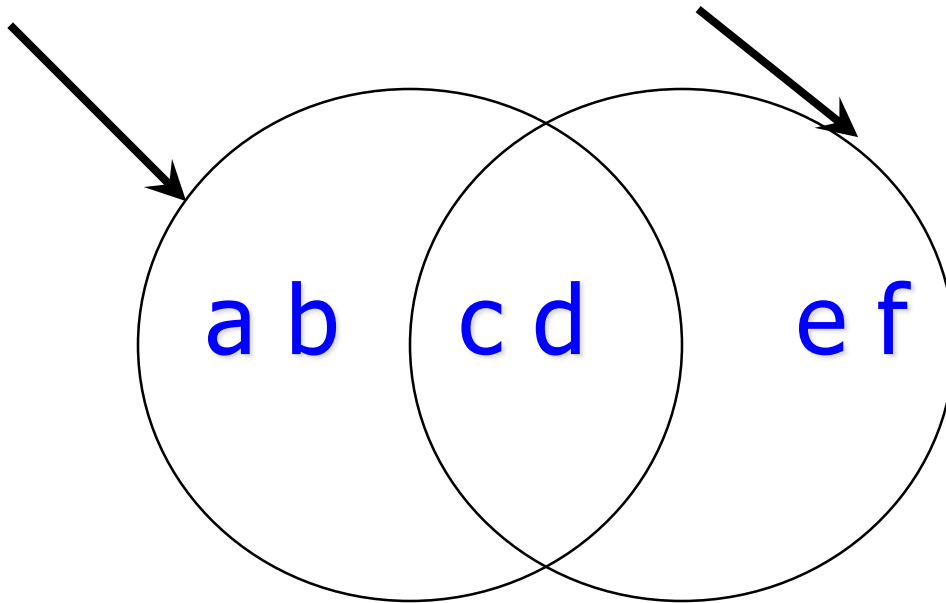
```
a_set=set("abcd") b_set=set("cdef")
```



```
a_set & b_set → {'c', 'd'}  
b_set.intersection(a_set) → {'c', 'd'}
```

## method: union, op: |

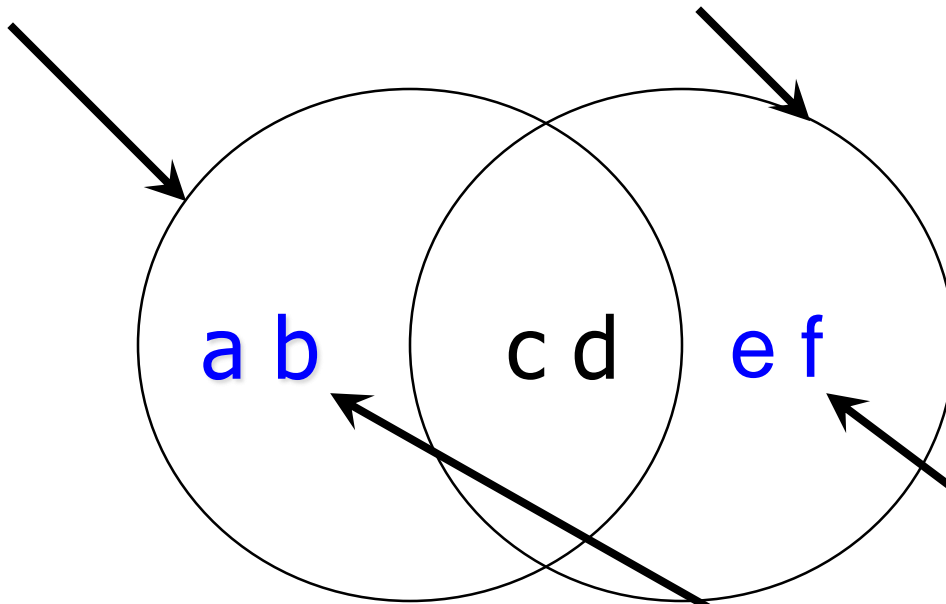
`a_set=set("abcd") b_set=set("cdef")`



`a_set | b_set → {'a', 'b', 'c', 'd', 'e', 'f'}`  
`b_set.union(a_set) → {'a', 'b', 'c', 'd', 'e', 'f'}`

## method: difference op: -

`a_set=set("abcd") b_set=set("cdef")`



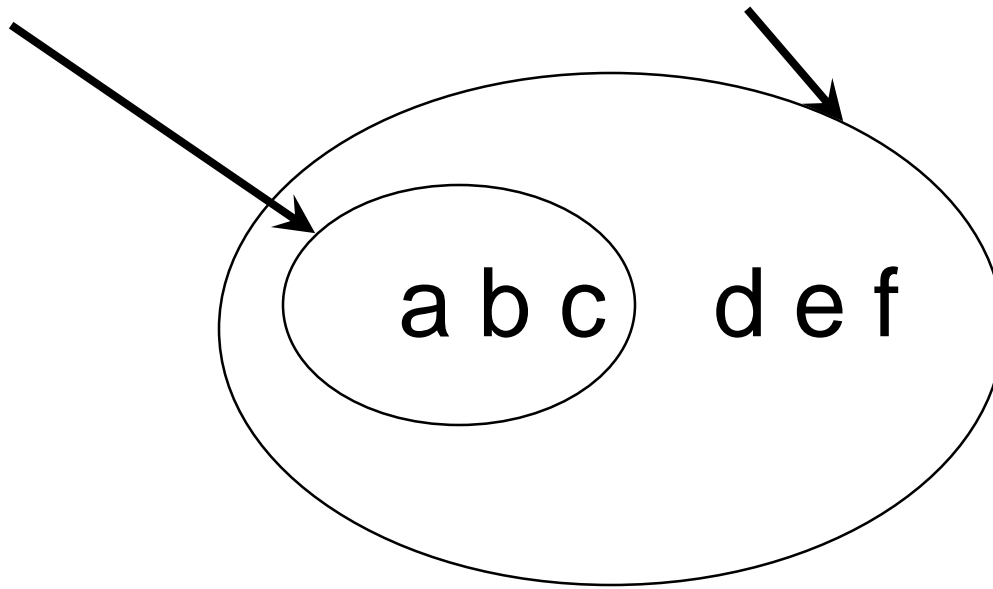
`a_set - b_set → {'a', 'b'}`

`b_set.difference(a_set) → {'e', 'f'}`

**method: issubset, op: <=**

**method: issuperset, op: >=**

```
small_set=set("abc"); big_set=set("abcdef")
```



```
small_set <= big_set → True
```

```
big_set >= small_set → True
```



## Other Set Ops

- `my_set.add("g")`
  - adds to the set, no effect if item is in set already
- `my_set.clear()`
  - empties the set
- `my_set.remove("g")` **versus** `my_set.discard("g")`
  - `remove` throws an error if "g" isn't there. `discard` doesn't care. Both remove "g" from the set
- `my_set.copy()`
  - returns a shallow copy of `my_set`

# Recursion

# What Is Recursion?

*"the determination of a succession of elements by operation on one or more preceding elements according to a rule or formula involving a finite number of steps"* (Merriam-Webster online)

# What This Really Means

*Breaking a problem down into a sequence of steps. The final step is reached when some basic condition is satisfied.*

***The solution for each step is used to solve the previous step.***

*The solution for all the steps together form the solution to the whole problem.*

# Recursion In Real Life?

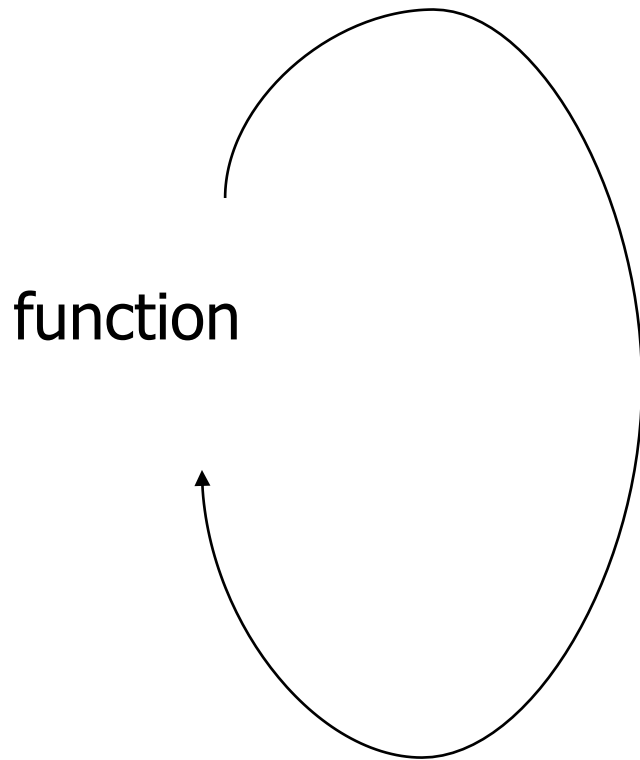
Do you have an example for recursion in real life?



# Recursion In Programming

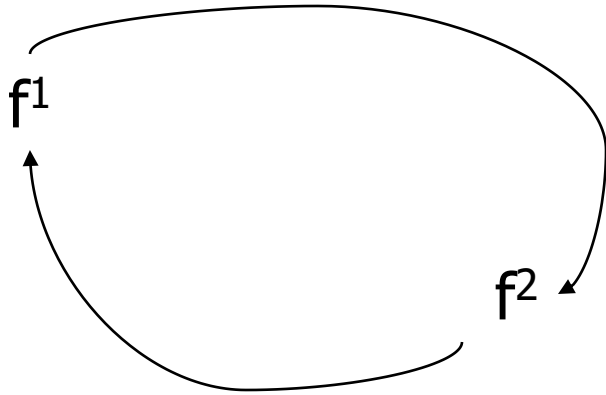
*"A programming technique whereby a function calls itself either directly or indirectly."*

# Direct Call



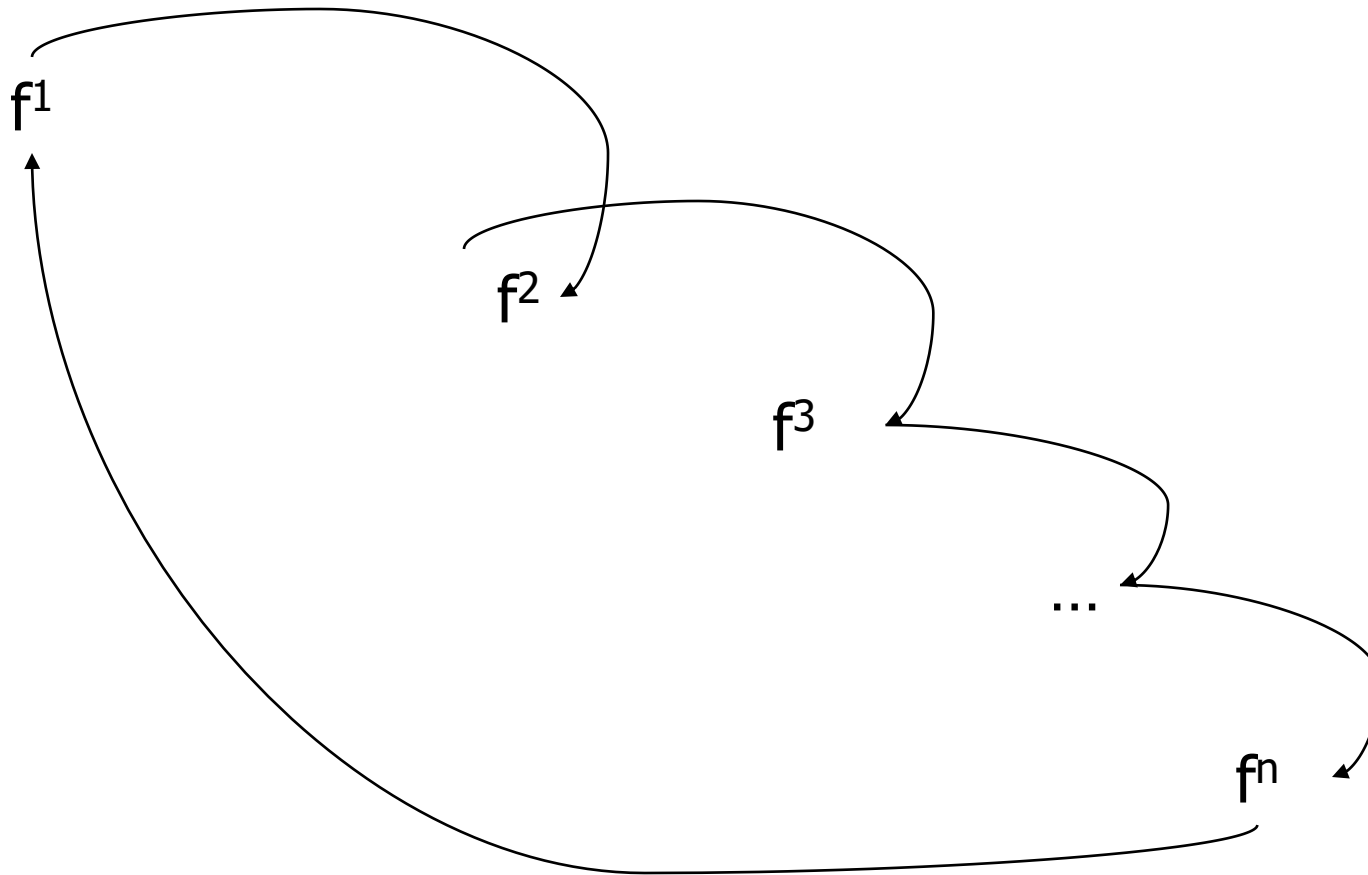
```
def fun ():  
    ...  
    fun ()  
    ...
```

# Indirect Call





# Indirect Call



# Indirect Call (2)

Example for indirect call:

```
def fun1():  
    fun2()
```

```
def fun2():  
    fun1()
```

```
fun1()
```

# Requirements For *Sensible* Recursion

- 1) Base case (similar to termination criterion for loops)
- 2) Progress is made (towards the base case)

# Example: Summing up numbers 1 to N

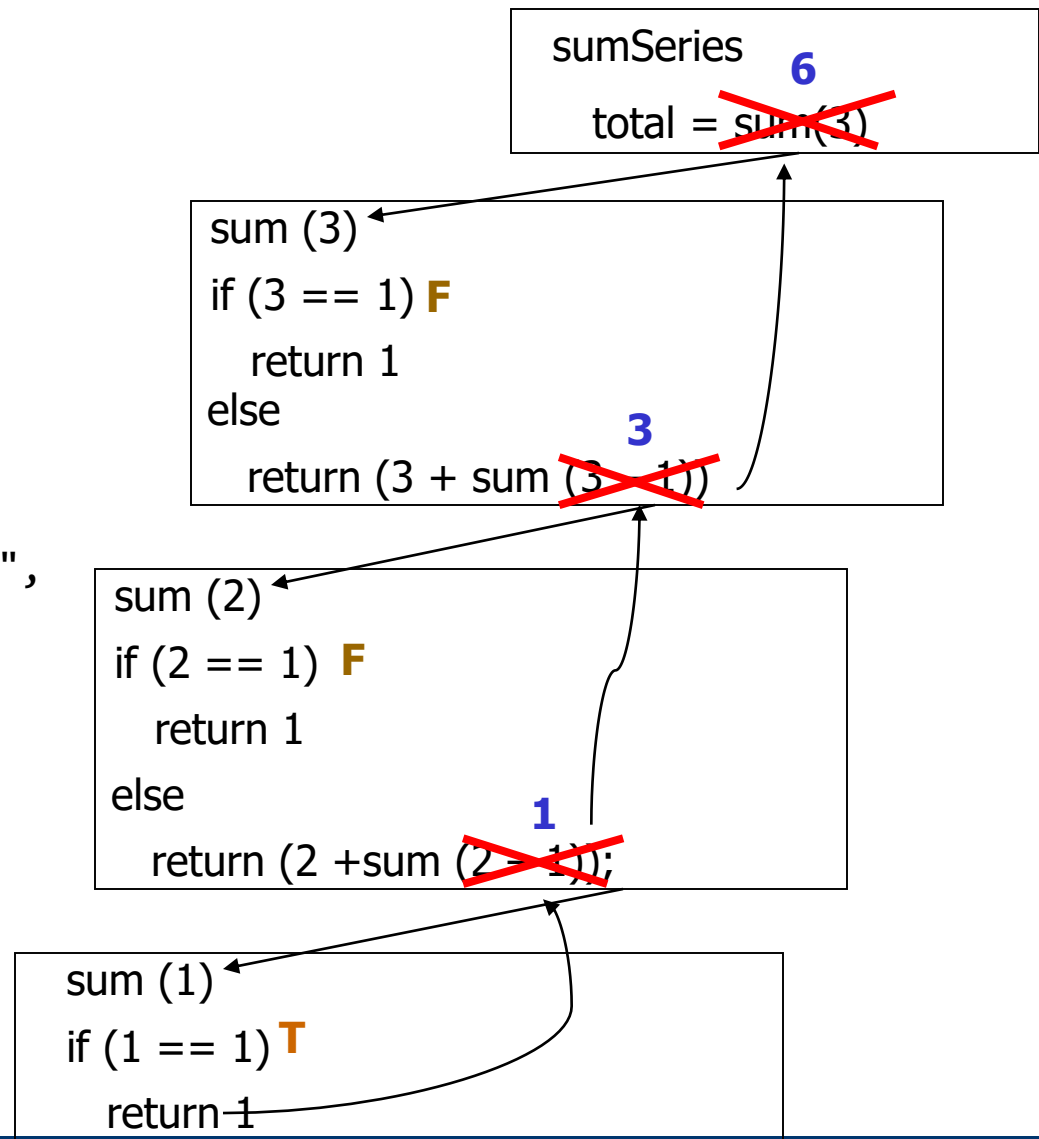
Easy to do with loops (see Exercise session).

How to achieve this with recursion?



# Example Program: sumSeries.py

```
def sum(no):  
    if (no == 1):  
        return 1  
    else:  
        return (no + sum(no-1) )  
  
def start():  
    last = input ("Enter the last  
                  number: ")  
    last = (int)last  
    total = sum(last)  
    print ("The sum of the series  
          from 1 to", last, "is",  
          total)  
  
start()
```



# When To Use Recursion

- When a problem can be divided into steps.
- The result of one step can be used in a previous step.
- There is a scenario when you can stop sub-dividing the problem into steps (step = recursive call) and return to a previous step.
  - Algorithm goes back to previous step with a partial solution to the problem (back tracking)
- All of the results together solve the problem.

# When To Consider Alternatives To Recursion

- When a loop will solve the problem just as well
- Types of recursion (for both types a return statement is excepted)
  - **Tail recursion**
    - The last statement in the function is another recursive call to that function This form of recursion can easily be replaced with a loop.
  - **Non-tail recursion**
    - The last statement in the recursive function is not a recursive call.
    - This form of recursion is very difficult (read: impossible) to replace with a loop.

## Second Example for Recursion

- Consider the mathematical definition of  $b^n$ , where  $n$  is a non-negative integer:

$$b^n = 1 \quad \text{if } n = 0$$

$$b^n = b \times b^{n-1} \quad \text{if } n > 0$$

- This definition is recursive, and immediately suggests a recursive function:

```
def power (b, n):  
    if n == 0:  
        return 1  
    else:  
        return b * power(b, n-1)
```



# Error Handling Example Using Recursion

- Name of the example program: `errorHandling.py`
    - Iterative/looping solution (month must be between 1 – 12)
- ```
month = -1
while ((month < 1) or (month > 12)):
    month = int(input("Enter birth month (1-12): "))
```

# Error Handling Example Using Recursion (2)

- Iterative/looping solution (day must be between 1 – 31)

```
def promptDay():  
    day = int(input("Enter day of birth (1-31): "))  
    if ((day < 1) or (day > 31)):  
        day = promptDay()  
    return(day)  
  
...  
day = promptDay()
```

# Drawbacks Of Recursion

Function calls can be costly

- Uses up memory
- Uses up time

# Benefits Of Using Recursion

- Simpler solution that's more elegant (for many standard problems)
- Easier to visualize solutions (for some people and certain classes of problems – typically require either: non-tail recursion to be implemented or some form of “backtracking”)

# Common Pitfalls When Using Recursion

- These three pitfalls can result in a runtime error
  - No base case
  - No progress towards the base case
  - Using up too many resources (e.g., variable declarations) for each function call

# No Base Case

```
def sum(no):  
    return(no + sum (no - 1))
```

# No Base Case

```
def sum (no):
```

```
    return (no + sum (no - 1))
```

When does it stop???



# No Progress Towards The Base Case

```
def sum (no):  
    if (no == 1):  
        return 1  
    else:  
        return (no + sum (no))
```




# No Progress Towards The Base Case

```
def sum (no):  
    if (no == 1):  
        return 1  
    else:
```

```
        return (no + sum (no))
```

The recursive case  
doesn't make any  
progress towards the  
base (stopping) case



# Using Up Too Many Resources

- Name of the example program: recursiveBloat.py

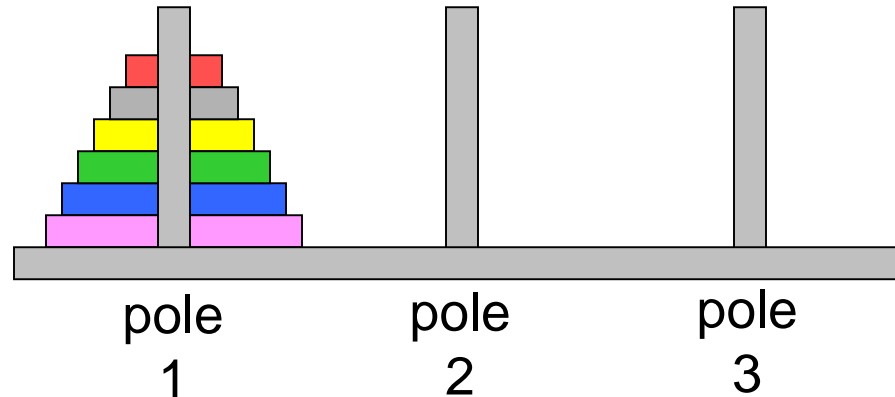
```
def fun(no):  
    print(no)  
    aList = []  
    for i in range (0, 10000000, 1):  
        aList.append("*")  
    no = no + 1  
    fun(no)  
  
fun(1)
```

# You Should Now Know

- What is a recursive computer program
- How to write and trace simple recursive programs
- What are the requirements for recursion/What are the common pitfalls of recursion

# Larger example: Towers of Hanoi (1)

- Three vertical poles are mounted on a platform.
- A number of discs are provided, all with different diameters. Each disc has a hole in its centre.
- All discs are initially threaded on to pole 1, forming a tower with the largest disc at the bottom and the smallest disc at the top.

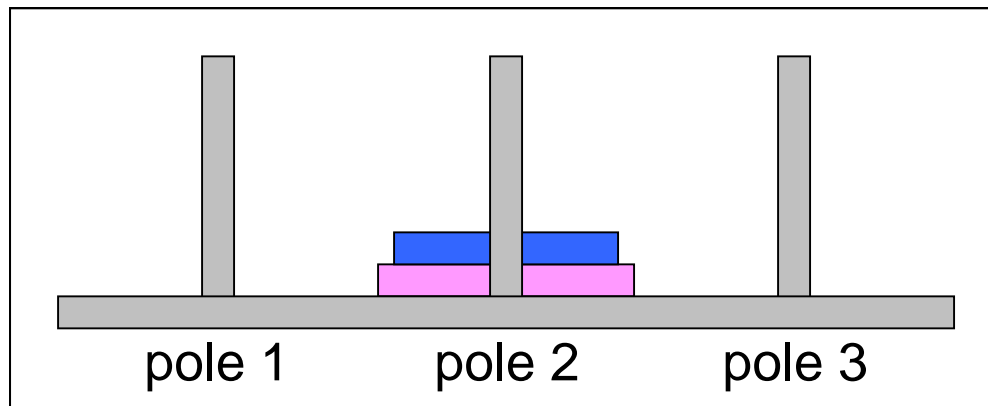


## Example: Towers of Hanoi (2)

- *One* disc may be moved at a time, from the top of one pole to the top of another pole.
- A larger disc may not be moved on top of a smaller disc.
- Problem: Move the tower of discs from pole 1 to pole 2.

## Example: Towers of Hanoi (3)

- Animation (with 2 discs):



# How to implement a solution algorithm?

- We just want to have a printout of disk movement instructions for a given number of disks  $n$ 
  - Example:

Move disc from 1 to 2.

Move disc from 1 to 3.

Move disc from 2 to 3.

Move disc from 1 to 2.

Move disc from 3 to 1.

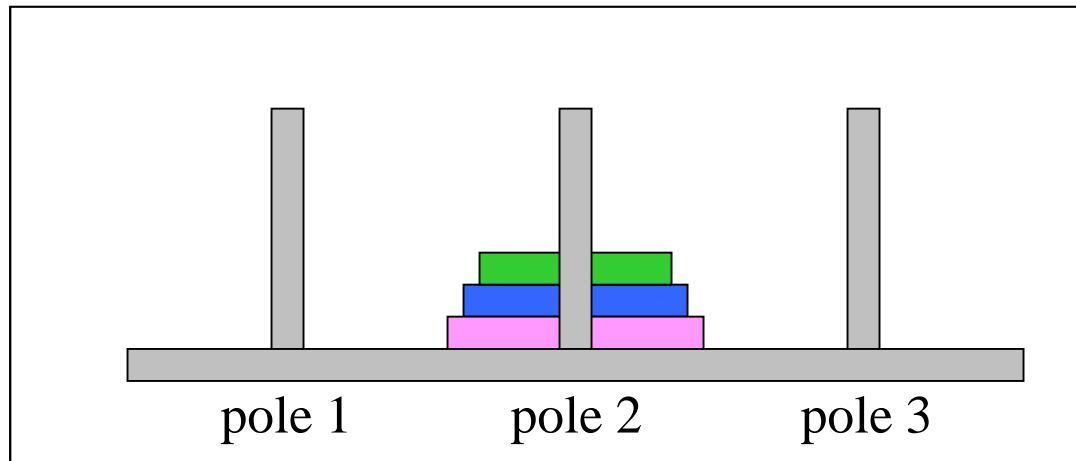
Move disc from 3 to 2.

Move disc from 1 to 2.



# Example: Towers of Hanoi (6)

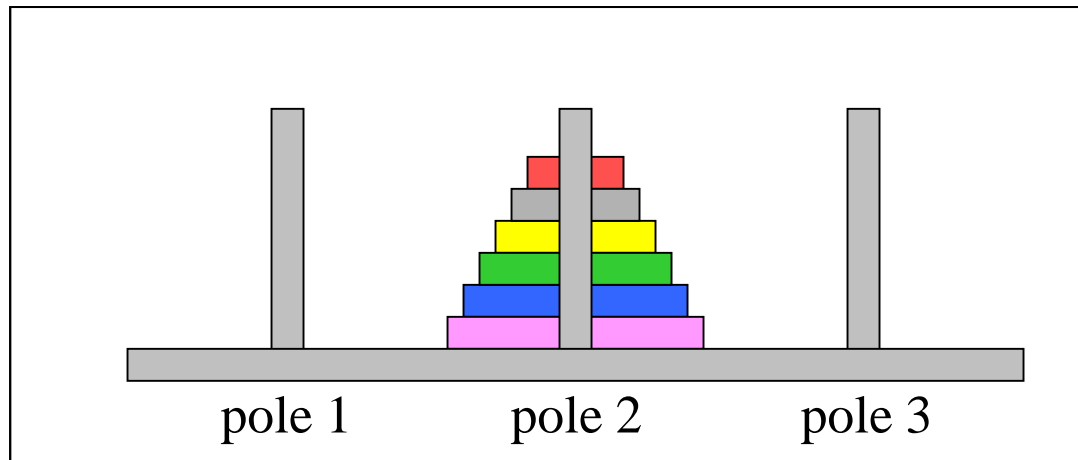
- Animation (with 3 discs):





# Example: Towers of Hanoi (7)

- Animation (with 6 discs):



# Example: Towers of Hanoi (4)

- Implementation:

```
def hanoi (n):  
    # Move a tower of n discs from tower 1 to tower 2.  
    move_tower(n, 1, 2, 3)  
  
def move_tower (n, a, b, c):  
    # Move a tower of n discs from the top of tower a  
    # to the top of tower b, using tower c as a spare.  
    if n == 1:  
        move_disc(a, b)  
    else:  
        move_tower(n-1, a, c, b)  
        move_disc(a, b)  
        move_tower(n-1, c, b, a)
```

# Example: Towers of Hanoi (5)

- Implementation (*continued*):

```
def move_disc (a, b):  
    # Move a single disc from tower a to tower b.  
    print 'Move disc from %d to %d.' \  
          % (a, b)
```

- Output (with 3 discs):

```
Move disc from 1 to 2.  
Move disc from 1 to 3.  
Move disc from 2 to 3.  
Move disc from 1 to 2.  
Move disc from 3 to 1.  
Move disc from 3 to 2.  
Move disc from 1 to 2.
```

# Files access in Python

# What You Need In Order To Read Information From A File

1. Open the file and associate the file with a file variable.
2. A command to read the information.
3. A command to close the file.

# 1. Opening Files

Prepares the file for reading:

- A. Links the file variable with the physical file (references to the file variable are references to the physical file).
- B. Positions the file pointer at the start of the file.

**Format:**<sup>1</sup>

*<file variable> = open(<file name>, "r")*

**Example:**

(Constant file name)

```
inputFile = open("data.txt", "r")
```

OR

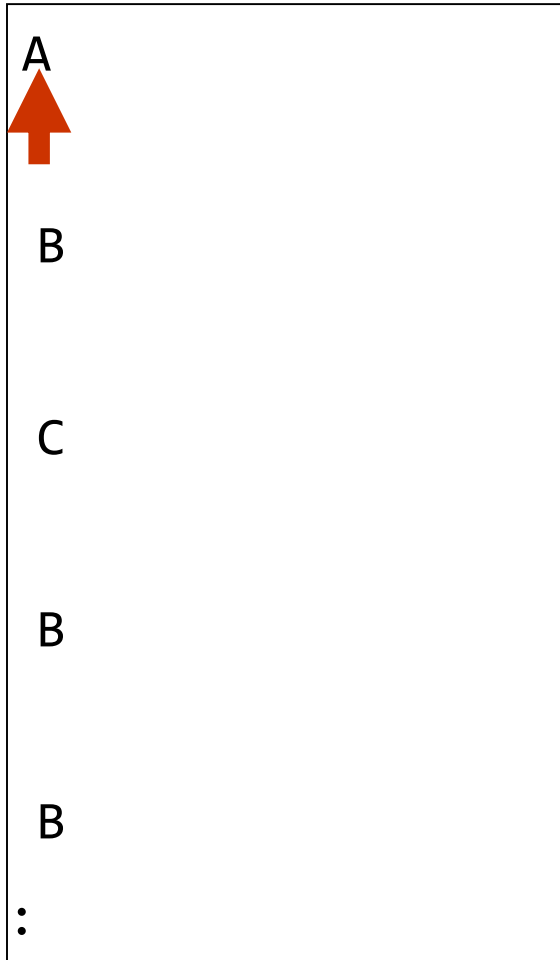
(Variable file name: entered by user at runtime)

```
filename = input("Enter name of input file: ")
```

```
inputFile = open(filename, "r")
```

## B. Positioning The File Pointer

letters.txt



## 2. Reading Information From Files

- Typically reading is done within the body of a loop
- Each execution of the loop will read a line from file into a string

### Format:

```
for <variable to store a string> in <name of file variable>:  
    <Do something with the string read from file>
```

### Example:

```
for line in inputFile:  
    print(line)  # Echo file contents back onscreen
```



# Closing The File

- Although a file is automatically closed when your program ends it is still a good style to explicitly close your file as soon as the program is done with it.
  - What if the program encounters a runtime error and crashes before it reaches the end? The input file may remain 'locked' an inaccessible state because it's still open.
- **Format:**  
*<name of file variable>.<close>()*
- **Example:**  
`inputFile.close()`

# Reading From Files: Putting It All Together

Name of the online example: grades1.py

Input files: letters.txt or gpa.txt

```
inputFileName = input("Enter name of input file: ")
inputFile = open(inputFileName, "r")
print("Opening file", inputFileName, " for reading.")

for line in inputFile:
    sys.stdout.write(line)

inputFile.close()
print("Completed reading of file", inputFileName)
```

# What You Need To Write Information To A File

1. Open the file and associate the file with a file variable (file is “locked” for writing).
2. A command to write the information.
3. A command to close the file.

# 1. Opening The File

## Format<sup>1</sup>:

*<name of file variable> = open(<file name>, "w")*

## Example:

(Constant file name)

```
outputFile = open("gpa.txt", "w")
```

(Variable file name: entered by user at runtime)

```
outputFileName = input("Enter the name of the output file  
to record the GPA's to: ")
```

```
outputFile = open(outputFileName, "w")
```

<sup>1</sup> Typically the file is created in the same directory/folder as the Python program.

### 3. Writing To A File

- You can use the `'write()'` function in conjunction with a file variable.
- Note however that this function will ONLY take a string parameter (everything else must be converted to this type first).

#### Format:

```
outputFile.write(temp)
```

#### Example:

```
# Assume that temp contains a string of characters.
```

```
outputFile.write (temp)
```

# Data Processing: Files

- Files can be used to store complex data given that there exists a predefined format.
- Format of the example input file: 'employees.txt'  
*<Last name><SP><First Name>,<Occupation>,<Income>*

# Example Program: data\_processing.py

```
inputFile = open ("employees.txt", "r")

print ("Reading from file input.txt")
for line in inputFile:
    name,job,income = line.split(',') # Divided by the comma
    first,last = name.split()
    income = int(income)
    income = income + (income * BONUS)
    print("Name: %s, %s\t\t\t\tJob: %s\t\t\tIncome $%.2f"
          %(first,last,job,income))

print ("Completed reading of file input.txt")
inputFile.close()
```

```
# EMPLOYEES.TXT
Adama Lee,CAG,30000
Morris Heather,Heroine,0
Lee Bruce,JKD master,100000
```

# Error Handling With Exceptions

- Exceptions are used to deal with extraordinary errors ('exceptional ones').
- Typically these are fatal runtime errors ("crashes" program)
- Example: trying to open a non-existent file
- Basic structure of handling exceptions

Try:

Attempt something where exception error may happen

Except:

React to the error

Else: **# Not always needed**

What to do if no error is encountered

Finally: **# Not always needed**

Actions that must always be performed



# Exceptions: File Example

- Name of the online example: `file_exception.py`
- Input file name: Most of the previous input files can be used e.g. `"input1.txt"`

```
inputFileOK = False
while (inputFileOK == False):
    try:
        inputFileName = input("Enter name of input file: ")
        inputFile = open(inputFileName, "r")
        print("Opening file" + inputFileName, " for
              reading.")
        inputFileOK = True
    for line in inputFile:
        sys.stdout.write(line)
    print("Completed reading of file", inputFileName)
```

# Exceptions: File Example (2)

```
# Still inside the body of the while loop (continued)
    inputFile.close()
    print("Closed file", inputFileName) # End of try-body
except IOError:
    print("Error: File", inputFileName, "could not be
          opened")
else:
    print("Successfully read information from file",
          inputFileName)
finally:
    print("Finished file input and output\n")
```

# What you should know after this lecture ..

- The concepts of compound data types
  - Strings, Lists, Sets, Dictionaries
- What is recursion and how it works
- How to open a file for reading/writing

**Thank you very much!**