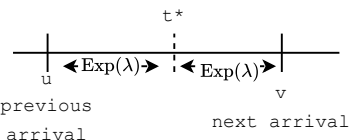
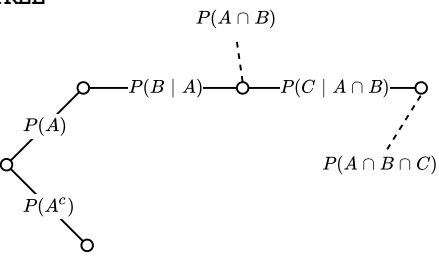


MISC	PROB BASICS	CONT. DISTROS	COND. DISTROS same for PDF	EXPECTATIONS
Log $\ln(mn) = \ln(m) + \ln(n)$ $\ln\left(\frac{m}{n}\right) = \ln(m) - \ln(n)$ $\ln(m^r) = r \ln(m)$ Exponent $(ab)^x = a^x b^x$ $(a^x)^y = a^{xy}$ $a^x a^y = a^{x+y}$ Summation $\sum_{i=1}^n ar^{i-1} = a \frac{1-r^n}{1-r}$ Integrals $\int \frac{1}{x} dx = \ln x $ $\int e^{ax} dx = \frac{1}{a} e^{ax}$ $\int a^x dx = \frac{a^x}{\ln(a)}$ $\int \ln(x) dx = x \ln(x) - x$ $\int \cos(x) dx = \sin(x)$ $\int \sin(x) dx = -\cos(x)$ Derivatives $(e^x)' = e^x$ $(\ln(x))' = \frac{1}{x}$ $\sin(x) = \cos(x)$ $\cos(x) = -\sin(x)$ $(fg)' = fg' + f'g$ $\frac{1}{f} = -\frac{f'}{f^2}$ $(f(g(x)))' = f'(g(x))g'(x)$ $\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$	Properties $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ $P(A \cup B) \leq P(A) + P(B)$ Conditional $P(A \mid B) = \frac{P(A \cap B)}{P(B)}$ $P(A \cap B) = P(B)P(A \mid B)$ Total Prob Theorem $P(B) = P(A_1 \cap B) + \dots + P(A_n \cap B)$ $ = P(A_1)P(B \mid A_1) + \dots$ Bayes $P(A \mid B) = \frac{P(A)P(B \mid A)}{P(B)}$ Independence $P(A \mid B) = P(A)$ $P(A \cap B) = P(A)P(B)$	$P(a \leq x \leq b) = \int_a^b f_X(x) dx$ Disjoint $P(1 \leq x \leq 3 \text{ or } 4 \leq x \leq 5)$ $\phantom{P(1 \leq x \leq 3 \text{ or } 4 \leq x \leq 5)} = P(1 \leq x \leq 3) + P(4 \leq x \leq 5)$ Properties $f(x) \geq 0$ and $\int_{-\infty}^{\infty} f_X(x) dx = 1$ CDF Properties · $\rightarrow_{x \rightarrow \infty} 1$ and $\rightarrow_{x \rightarrow -\infty} 0$ · increasing/monotonic · right-continuous ____*--- Uniform $f_X(x) = \frac{1}{b-a}$ $F_X(x) = \frac{x-a}{b-a}$ $E[X] = \frac{a+b}{2}$ $Var(X) = \frac{(b-a)^2}{12}$ Exponential <i>time to wait for something</i> $f_X(x) = \lambda e^{-\lambda x}$ $P(X \geq a) = \int_a^{\infty} \lambda e^{-\lambda x} dx = e^{-\lambda a}$ $F_X(x) = 1 - e^{-\lambda x}$ $E[X] = \frac{1}{\lambda}$ $E[X^2] = \frac{2}{\lambda^2}$ $Var(X) = \frac{1}{\lambda^2}$	$p_{X Y}(x \mid y) = \frac{p_{X,Y}(x, y)}{p_Y(y)}$ Multiplication Rule $p_{X,Y}(x, y) = p_Y(y)p_{X Y}(x \mid y)$ $p_{X,Y,Z}(x, y, z) = p_X(x)p_{Y X}(y \mid x)p_{Z X,Y}(z \mid x, y)$ $p_{X,Y Z}(x, y \mid z) = \frac{p_{X,Y,Z}(x, y, z)}{p_Z(z)}$	Expected Value $E[g(x)] = \sum g(x)p_X(x)$ $E[g(x)] = \int_{-\infty}^{\infty} g(x)f_X(x)dx$ Linearity of Expectations $E[aX + b] = aE[X] + b$ $E[X + Y] = E[X] + E[Y]$ Total Expectation Th. $E[X] = \sum_y p_Y(y)E[X \mid Y = y]$ $E[X] = \int_{-\infty}^{\infty} f_Y(y)E[X \mid Y = y]dy$ $E[X] = \sum_i P(A_i)E[X \mid A_i]$ Cond. Expectation $E[g(x) \mid Y = y] = \sum_x g(x)p_{X Y}(x \mid y)$ Iterated Expectation $E[E[X \mid Y]] = E[X]$
	DISCRETE DISTROS Bernouilli $P(X = 1) = p$ $E[X] = p$ $Var(X) = p(1 - p)$ Uniform $p_X(x) = \frac{1}{b-a+1}$ $E[X] = \frac{a+b}{2}$ $Var(X) = \frac{(b-a+1)^2 - 1}{12}$ Binomial <i>k successes in n trials</i> $p_X(k) = \binom{n}{k} p^k (1-p)^{n-k}$ $E[X] = np$ $Var(X) = np(1 - p)$ Geometric <i>number of trials until success</i> $p_X(k) = (1-p)^{k-1} p$ $E[X] = \frac{1}{p}$ $Var(X) = \frac{1-p}{p^2}$ Poisson <i>how many occurrences k in τ given rate λ</i> $P(k, \tau) = \frac{(\lambda \tau)^k e^{-\lambda \tau}}{k!}$ $E[N_\tau] = \lambda \tau$ $Var(N_\tau) = \lambda \tau$	NORMALS $f_X(x) = \frac{1}{\sigma \sqrt{2\pi}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$ $E[X] = \mu$ $Var(X) = \sigma^2$ Linear Functions $Y = aX + b$ with $X \sim N(\mu, \sigma^2)$ $Y = N(a\mu + b, a^2 \sigma^2)$ Indie Sum $Z \sim N(\mu_X + \mu_Y, \sigma_X^2 + \sigma_Y^2)$ Tables $\Phi(-2) = P(Y \leq -2)$ $ = 1 - P(Y \leq 2) = 1 - \Phi(2)$ Standardising $X \sim N(\mu, \sigma^2)$ and $Y \sim N(0, 1)$ $Y = \frac{X - \mu}{\sigma}$ $X = \mu + \sigma Y$	MULTIPLE VARS $\sum_x \sum_y p_{X,Y}(x, y) = 1$ $P((X, Y) \in B) = \iint_{(x,y) \in B} f_{X,Y}(x, y) dx dy$ Marginals $p_X(x) = \sum_y p_{X,Y}(x, y)$ $f_X(x) = \int f_Y(y) f_{X Y}(x \mid y) dy$ ranges: what values can Y take when X = x? $ = \int f_{X,Y}(x, y) dy$ Expected Value Rule $E[g(X, Y)] = \sum_x \sum_y g(x, y) p_{X,Y}(x, y)$ $E[g(X, Y)] = \int E[g(x, y) \mid Y = y] f_Y(y) dy$ $E[g(X, Y) \mid Y = y] = \int g(x, y) f_{X Y}(x \mid y) dy$ CDF $F_{X,Y}(x, y) = P(X \leq x, Y \leq y)$ $\phantom{F_{X,Y}(x, y)} = \int_{-\infty}^y \int_{-\infty}^x f_{X,Y}(s, t) ds dt$	INDEPENDENCE If Indie $E[XY] = E[X]E[Y]$ $Var(X + Y) = Var(X) + Var(Y)$ $p_{X,Y Z}(x, y \mid z) = p_{X Z}(x \mid z)p_{Y Z}(y \mid z)$ $f_{X,Y}(x, y) = f_X(x)f_Y(y)$ $f_{X Y}(x \mid y) = f_X(x)$ $Cov(X, Y) = 0$
COUNTING n choose k nb of combinations (any order) $\binom{n}{k} = \frac{n!}{k!(n-k)!}$ permutations nb of ways of ordering n elements (order matters) $n!$ subsets of n elements 2^n partitions n objects into r groups $\frac{n!}{n_1! n_2! \dots n_r!}$			VARIANCE $Var(x) = E\left[(x - \mu)^2\right]$ and $\sigma = \sqrt{Var(X)}$ Properties $Var(aX + b) = a^2 Var(X)$ $Var(X) = E[X^2] - (E[X])^2$ Dependent Sum $Var(X_1 + \dots + X_n) = \sum_{i=1}^n Var(X_i) + \sum_{\{i,j\}: i \neq j} Cov(X_i, X_j)$ Independent Sum $Var(X + Y) = Var(X - Y) = Var(X) + Var(Y)$	Law of Total Var $Var(X) = E[Var(X \mid Y)] + Var(E[X \mid Y])$

<div>DERIVED DISTROS</div> <div>PMF function of discrete RV</div> $p_Y(y) = P(g(x) = y) = \sum_{x:g(x)=y} p_X(x)$ <div>Linear Functions</div> $Y = aX + b$ $p_Y(y) = p_X\left(\frac{y-b}{a}\right)$ $f_Y(y) = \frac{1}{ a } f_X\left(\frac{y-b}{a}\right)$ <div>g is monotonic</div> $f_Y(y) = f_X(h(y)) \left \frac{dh}{fy}(y) \right $ <div>general case</div> <div>1) find CDF: $F_Y(y) = P(g(x) \leq y)$</div> <div>2) derive CDF for PDF</div>	<div>BERNOUILLI PROCESS</div> <div>requires indie, time homogen.</div> <div>Properties</div> $S = X_1 + \dots + X_n$ $P(S = K) = \binom{n}{k} p^k (1-p)^{n-k}$ $E[S] = np$ $Var(S) = np(1-p)$ <div>Time until 1st success</div> $T_1 = \min \{i: X_i = 1\}$ $P(T_1 = k) = (1-p)^{k-1} p$ <div>Time of kth arrival</div> $p_{Y_k}(t) = \binom{t-1}{k-1} p^k (1-p)^{t-k}$ $E[Y_k] = \frac{k}{p}$ $Var(Y_k) = \frac{k(1-p)}{p^2}$ <div>Merging</div> $Z_t = g(X_t, Y_t) \sim Ber(p+q-pq)$ $\Rightarrow \text{prob either or both have arrival at time } t$ <div>Splitting</div> <div>flip a coin with prob q</div> $A \sim Ber(qp)$ $B \sim Ber((1-q)p)$ <div>Δ these streams are not indie</div>	<div>POISSON PROCESS</div> <div>indie, time homogen. seq of exp</div> <div>λ: arrival rate</div> $P(k, \tau) = \frac{(\lambda \tau)^k e^{-\lambda \tau}}{k!}$ $E[N_\tau] = \lambda \tau$ $Var(N_\tau) = \lambda \tau$ $\lambda = \frac{E[N_\tau]}{\tau}$ <div>Time of kth arrival / Erlang</div> $f_{Y_k} = \frac{\lambda^k y^{k-1} e^{-\lambda y}}{(k-1)!}$ $= Erlang(k)$ $= Erlang\left(\frac{k}{2}\right) + Erlang\left(\frac{k}{2}\right)$ <div>Sum</div> <div>Δ must be indie</div> <div>M: $Poisson(\mu)$ N: $Poisson(v)$</div> <div>M+N: $Poisson(\mu + v)$</div> <div>Merging</div> <div>A: λ_A B: λ_B</div> $\lambda = \lambda_A + \lambda_B$ $P(k^{th} \text{ arrival is A}) = \frac{\lambda_A}{\lambda_A + \lambda_B}$ $P(k \text{ arrivals are A}) \text{ is Binomial}\left(\frac{\lambda_A}{\lambda_A + \lambda_B}\right)$ <div>Splitting</div> <div>flip a coin with prob q</div> <div>Δ these streams <u>are</u> indie</div> <div>A: $\lambda_A = \lambda q$</div> <div>B: $\lambda_B = \lambda(1-q)$</div> <div>Multiple Engine Example</div> <div>3 engines with death rate λ_e</div> <div>rate until 1st dies is $\lambda = 3\lambda_e$</div> <div>then rate until 2nd dies $\lambda = 2\lambda_e$</div> <div>Min</div> $P(\min \{X, Y, Z\} \geq t)$ $= P(X \geq t, Y \geq t, Z \geq t)$ $= e^{-3\lambda t}$ $\Rightarrow \text{have 3 merged Poissons and want to know first arrival}$ $\Rightarrow \min \{X, Y, Z\} \text{ is } Exp(3\lambda)$ $E[\min \{X, Y, Z\}] = \frac{1}{3\lambda}$ <div>Max</div> $P(\max \{T_1, T_2, T_3\} \leq t)$ $= P(T_1 \leq t) P(T_2 \leq t) P(T_3 \leq t)$ $= (1 - e^{-\lambda t})^3$ <div>then derive this to get PDF</div>	<div>Cov Matrix and MV Stuff</div> $\Sigma = \begin{pmatrix} Cov(X, X) & Cov(X, Y) \\ Cov(Y, X) & Cov(Y, Y) \end{pmatrix}$ $= E[(X - E[X])(Y - E[Y])^T]$ $Var(\mathbf{X}) = Cov(\mathbf{X})$ $Cov(\mathbf{A}\mathbf{X} + \mathbf{B}) = Cov(\mathbf{A}\mathbf{X}) = \mathbf{A}Cov(\mathbf{X})\mathbf{A}^T = \mathbf{A}\Sigma\mathbf{A}^T$ <div>Gaussian vector</div> <div>defined by $\boldsymbol{\mu}$ and Σ, $x \in R^d$</div> $f_X(x) = \frac{1}{\sqrt{(2\pi)^d \det \Sigma}} \exp\left(-\frac{1}{2}(\mathbf{x} - \boldsymbol{\mu})^T \Sigma^{-1}(\mathbf{x} - \boldsymbol{\mu})\right)$ <div>MV CLT</div> $X_i \sim R^d \quad E[\mathbf{X}_i] = \boldsymbol{\mu} \quad Cov(\mathbf{X}_i) = \Sigma$ <div>MV Delta</div> $\sqrt{n}(g(T_n) - g(\theta)) \rightarrow N\left(0, \nabla(\theta)^T \Sigma \nabla(\theta)\right)$
<div>CONVOLUTIONS</div> $Z = X + Y$ $p_Z(z) = \sum_x p_X(x) p_Y(z-x)$ $f_Z(z) = \int_{-\infty}^{\infty} f_X(x) f_Y(z-x) dx$			
<div>COVARIANCE</div> $Cov(X, Y) = E[(X - E[X])(Y - E[Y])]$ <div>Direction</div> $Cov(X, Y) > 0$ same sign <div>If Indie</div> $Cov(X, Y) = 0$ <div>Δ inverse not usually true but true for Gaussians:</div> <div>$Cov(X, Y) = 0 \rightarrow X, Y \sim N$ indie</div> <div>Properties</div> $Cov(X, X) = Var(X)$ $Cov(X, Y) = E[XY] - E[X]E[Y]$ $Cov(aX + b, Y) = aCov(X, Y)$ $Cov(X, Y + Z) = Cov(X, Y) + Cov(X, Z)$	<div>INTER-ARRIVAL TIMES / R. INCIDENCE</div> 		
<div>CORRELATION COEF.</div> $\rho(X, Y) = \frac{Cov(X, Y)}{\sigma_X \sigma_Y}$	<div>we arrive at t^*</div> <div>u, v are each $Exp(\lambda)$ away from t^*</div> $\Rightarrow E[V - U] \text{ is twice the expectation of } Exp(\lambda)$		
<div>FRESH START/MEMORYLESSNESS</div> <div>Exponential</div> $f_{X X>t}(x x > t) = f_X(x)$ <div>Bernouilli/Poisson</div> $P(A B) = P(A)$ <div>i.e. prob of two arrivals (A) after 1 arrival (B) = prob of 2 arrivals (A)</div>	<div>TREE</div> 		

<div>MISC</div> <div>$\sum_{k=0}^{\infty} \frac{\lambda^k}{k!} = \exp(\lambda)$</div> <div>e limits</div> <div>$\lim_{n \rightarrow \infty} \left(1 - \frac{t}{n}\right)^n = e^{-t}$</div> <div>$\lim_{n \rightarrow \infty} \left(1 + \frac{t}{n}\right)^n = e^t$</div>	<div>IDENTIFIABILITY</div> <div>θ identifiable iff mapping $\theta \in \Theta \rightarrow P_\theta$ is injective (injective: $\theta \neq \theta' \Rightarrow P_\theta \neq P_{\theta'}$)</div>	<div>TESTS</div> <div>Δ failing to reject H_0 does not mean accepting H_0</div> <div>Errors</div> <table><tr><td>test reality</td><td>H_0</td><td>H_1</td></tr><tr><td>H_0</td><td>✓</td><td>type 1 error (reject when shouldn't)</td></tr><tr><td>H_1</td><td>type 2 error (fail to reject when should)</td><td>✓</td></tr></table>	test reality	H_0	H_1	H_0	✓	type 1 error (reject when shouldn't)	H_1	type 2 error (fail to reject when should)	✓	<div>LIKELIHOODS</div> <div>Bernouilli $p^{\sum^n X_i} (1-p)^{n-\sum^n X_i}$</div> <div>Poisson $\frac{\lambda^{\sum X_i}}{x_1! \dots x_n!} \exp(-n\lambda)$</div> <div>Gaussian $\frac{1}{(2\pi\sigma^2)^{\frac{n}{2}}} \exp\left(-\frac{1}{2\sigma^2} \sum (x_i - \mu)^2\right)$</div> <div>Exponential $\lambda^n \exp\left(-\lambda \sum X_i\right)$</div> <div>Uniform $\frac{1}{b^n} \mathbf{1}\{\max X_i \leq b\}$</div>	<div>Fisher Information</div> <div>Δ use <u>ONE</u> observation not well defined if support depends on unknown (shifted exp)</div> <div>Δ $l''(\theta)$ must exist $I(\theta) = Var(l'(\theta)) = -E[l''(\theta)]$</div>	
test reality	H_0	H_1												
H_0	✓	type 1 error (reject when shouldn't)												
H_1	type 2 error (fail to reject when should)	✓												
<div>MIN/MAX</div> <div>$P(\max > x) = 1 - P(\max < x) = 1 - [P(X_i < x)]^n$</div> <div>$P(\min > x) = [P(X_i > x)]^n = [1 - P(X_i < x)]^n$</div>	<div>$\widehat{\theta}_n \rightarrow \theta$ as $n \rightarrow \infty$</div> <div>Bias $bias(\widehat{\theta}_n) = E[\widehat{\theta}_n] - \theta$</div> <div>Quadratic Risk $R(\widehat{\theta}_n) = E[\widehat{\theta}_n - \theta]^2]$</div>	<div>level α</div> <div>max type 1 error rate</div> <div>higher $\alpha \rightarrow$ more likely to reject H_0</div> <div>power β</div> <div>$\pi_\psi = \inf_{\theta \in \Theta_n} (1 - \beta_\psi(\theta))$</div> <div>example 2 sided</div> <div>coin $H_0:p = \frac{1}{2}$ and $H_1:p \neq \frac{1}{2}$</div> <div>$\psi = 1 \left\{ \sqrt{n} \frac{ \overline{X}_n - \frac{1}{2} }{\sqrt{\frac{1}{2}(1 - \frac{1}{2})}} \right\} > q_{\frac{\alpha}{2}} \right\}$</div>	<div>MAXIMIZATION</div> <div>global extremes on range</div> <div>test critical points and end points</div> <div>min/max</div> <div>$h''(x) \leq 0 \rightarrow$ concave, maximum</div> <div>$h''(x) < 0 \rightarrow$ global max</div> <div>$h''(x) \geq 0 \rightarrow$ convexe, minimum</div> <div>MV min/max</div> <div>$X^T H h(\theta) X \leq 0$ concave, max</div> <div>+1 top diag: convexe, minimum</div> <div>$\begin{pmatrix} +1 & ? \\ ? & ? \end{pmatrix}$</div>	<div>Method of Moments</div> <div>$\widehat{m}_k = \overline{X}_n^k = \frac{1}{n} \sum X_i^k$</div> <div>LLN $\widehat{m}_k \rightarrow m_k(\theta) = E_\theta[X_1^k]$</div> <div>Delta $\sqrt{n}(\hat{\theta} - \theta) \rightarrow N(0, \Gamma(\theta))$</div> <div>$\Gamma(\theta) = \left[\frac{\delta M^{-1}}{\delta \theta} \right]^T \Sigma(\theta) \left[\frac{\delta M^{-1}}{\delta \theta} \right]$</div> <div>finding $\hat{\theta}$</div> <div>write θ as function $E[X]$, $E[X^2]$... then sub for \overline{X}_n, \overline{X}_n^2</div>										
<div>LLN</div> <div>req. iid and $E[X_i] < \infty$</div> <div>$\overline{X}_n = \frac{1}{n} \sum^n X_i$</div>	<div>Confidence Interval level $1 - \alpha$</div> <div>conf.int. can't depend on unknown</div> <div>$P\left(\overline{X}_n - q_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \overline{X}_n + q_{\frac{\alpha}{2}} \frac{\sigma}{\sqrt{n}}\right) = 1 - \alpha$</div>													
<div>CLT</div> <div>req. iid, $E[X_i] < \infty$ and $Var(X_i) < \infty$</div> <div>$\sqrt{n} \frac{\overline{X}_n - \mu}{\sigma} \rightarrow N(0, 1)$</div> <div>$\sqrt{n}(\overline{X}_n - \mu) \rightarrow N(0, \sigma^2)$</div>	<div>UNBIASED ESTIMATOR</div> <div>we want $E[\widehat{\theta}_n] = 0$</div> <div>find $E[\widehat{\theta}_n]$ and use linear property of expectations to create a new estimator such that</div> <div>$E[\widehat{\theta}_n] = \frac{1}{c} E[\widehat{\theta}_n] = 0$</div>													
<div>Quantiles</div> <div>$P(X \leq q_\alpha) = 1 - \alpha$</div> <div>$\alpha = 1 \rightarrow q_\alpha$ is 90th percentile</div> <div>$P(Z > 1.96) = 0.05$</div> <table><tr><td>α</td><td>2.5%</td><td>5%</td><td>7.5%</td><td>10%</td></tr><tr><td>q_α</td><td>1.96</td><td>1.65</td><td>1.44</td><td>1.28</td></tr></table>	α	2.5%	5%	7.5%	10%	q_α	1.96	1.65	1.44	1.28	<div>1D DELTA METHOD</div> <div>g: cont. differentiable</div> <div>$\sqrt{n}(Z_n - \theta) \rightarrow N(0, \sigma^2)$</div> <div>$\sqrt{n}(g(Z_n) - g(\theta)) \rightarrow N(0, (g'(\theta))^2 \cdot \sigma^2)$</div>			
α	2.5%	5%	7.5%	10%										
q_α	1.96	1.65	1.44	1.28										
<div>Slutsky Th.</div> <div>$T_n \rightarrow T$ and $U_n \rightarrow u$</div> <div>T is r.v. and u is real</div> <div>$T_n + U_n \rightarrow T_u$</div> <div>$T_n U_n \rightarrow T_u$</div> <div>$\frac{T_n}{U_n} \rightarrow \frac{T}{U}$</div>	<div>P-VALUE</div> <div>Δ is a level α</div> <div>what is the probability of observing a result more extreme than this one under H_0?</div> <div>Δ low p-value is bad \rightarrow H_0 is unlikely</div> <div>i.e. $P(\widehat{a} \geq \widehat{a}_{\text{obs}})$</div>													
	<div>KL DIVERGENCE</div> <div>$KL(P_\theta, P_{\theta'}) = \sum_{x \in E} p_\theta(x) \log\left(\frac{p_\theta(x)}{p_{\theta'}(x)}\right)$</div> <div>$KL(P_\theta, P_{\theta'}) = \int_E f_\theta(x) \log\left(\frac{f_\theta(x)}{f_{\theta'}(x)}\right) dx$</div>	<div>TOTAL VARIATION DISTANCE</div> <div>max dist between two distros</div> <div>Δ E is joint set of values of RVs</div> <div>$TV(P_\theta, P_{\theta'}) = \frac{1}{2} \sum_{x \in E} p_\theta(x) - p_{\theta'}(x)$</div> <div>$TV(P_\theta, P_{\theta'}) = \frac{1}{2} \int_{-\infty}^{\infty} f_\theta(x) - f_{\theta'}(x) dx$</div>	<div>Properties</div> <div>symmetric: $TV(P_\theta, P_{\theta'}) = TV(P_{\theta'}, P_\theta)$</div> <div>positive: $0 \leq TV \leq 1$</div> <div>definite: if $TV(P_\theta, P_{\theta'}) = 0$ then $P_\theta = P_{\theta'}$</div> <div>triangle ineq: $TV(P_\theta, P_{\theta'}) \leq TV(P_\theta, P_{\theta''}) + TV(P_{\theta''}, P_{\theta'})$</div> <div>if disjoint: $TV = 1$</div> <div>if same: $TV = 0$</div>	<div>MLE</div> <div>minimizes KL divergence</div> <div>$\hat{\theta}_n^{MLE} = \arg \max_{\theta \in \Theta} \log(L)$</div> <div>$\Delta$ function must be cont. diff. to use derivative to find extremums. use a plot and think if not</div> <div>Gaussian check Wikipedia</div> <div>Consistency and Asym. Norm.</div> <div>if:</div> <div><ul style="list-style-type: none">param is identifiablesupport of P_θ does not depend on θθ^* is not at boundary$I(\theta)$ is invertiblemore stuff</div> <div>$\hat{\theta}_n^{MLE} \rightarrow \theta^*$</div> <div>$\sqrt{n}(\hat{\theta}_n^{MLE} - \theta^*) \rightarrow N(0, I(\theta^*)^{-1})$</div>										
<div>Continuous Mapping Th.</div> <div>$T_n \rightarrow T$ then $f(T_n) \rightarrow f(T)$</div>			<div>Process to find extremum</div> <div><ul style="list-style-type: none">get l_nfind crits with $l_n'(\theta) = 0$check if crits are local min/maxcheck values at endpoints</div>											
<div>Statistical Model</div> <div>$(E, (P_\theta)_{\theta \in \Theta})$</div> <div>E: sample space Θ: Param set well specified if $\theta^* \in \Theta$</div>	<div>Properties</div> <div>not symmetric</div> <div>not negative</div> <div>definite</div> <div>triangle ineq</div>	<div>M-Estimation</div> <div>Lecture 12, tab 2</div>												

