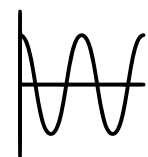
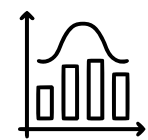


Overview



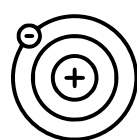
Classical light Raman spectroscopy is limited by the time–frequency trade-off: short pulses give high temporal but poor spectral resolution, and vice versa. Femtosecond Adaptive Spectroscopic Technique via Coherent Anti-Stokes Raman Scattering (**FAST CARS**) [1] addresses this by combining ultrashort broadband excitation with a narrowband probe, boosting resonant signals and reducing background, though it remains bound by classical uncertainty.

Quantum protocols overcome these limits by exploiting entanglement. Quantum Induced Coherence LiDAR (**QuIC LiDAR**) [2] uses SPDC photon pairs in an **SU(1,1)** interferometer, where induced coherence makes idler-only detection possible. This grants access to spectral or spatial information with strong resilience to noise.



Quantum Femtosecond Raman Spectroscopy (**QFRS**) [3] applies **entangled photons** to extend FAST CARS: the signal interacts with the sample while the idler provides a temporal reference. Coincidence detection retrieves vibrational coherences without the classical trade-off, but needs heterodyne detection to recover phase information.

The present study proposes a **interferometric scheme** that merges QFRS with QuIC LiDAR. Using SU(1,1) interference, it preserves vibrational coherence without heterodyne detection and inherits noise immunity from induced coherence. This points toward a robust quantum Raman protocol with applications in spectroscopy.



Theoretical Framework

Entangled photon pairs allow quantum-enhanced spectroscopy. They exhibit strong time–frequency correlations enabling Raman signals to surpass the classical Fourier limit of simultaneous temporal and spectral resolution.

The quantum state of a photon pair can be written as

$$|\Phi\rangle = \sum_k \int d\omega_s d\omega_i \Phi_k(\omega_s, \omega_i) a_{\omega_s, k}^\dagger a_{\omega_i, k}^\dagger |0\rangle, \quad (1)$$

where the joint spectral amplitude $\Phi(\omega_s, \omega_i)$ defines correlations between signal (s) and idler (i) photons.

The light–matter interaction in the off-resonant Raman regime is modeled as

$$V(t) = \sum_j \sum_b \alpha_{bg}^{(j)} |b\rangle\langle g|_j(t) E_s(t) E_s^\dagger(t) + h.c., \quad (2)$$

with α_{bg} the Raman polarizability.

The measurable spectroscopic response is given by the four-point field correlation function

$$S(\omega_s, \omega_i) = \langle \Phi | E_s^\dagger E_i^\dagger E_i E_s | \Phi \rangle, \quad (3)$$

which captures coincidence detections and encodes molecular coherence.

QFRS Model

Here the spectroscopic signal that carries the nonlinear dispersion information is expressed as

$$S_{QV}(\omega, \omega_i; T) = \frac{N(N-1)}{4\pi^2} |\mathcal{E}_{AS, \omega}|^6 |\mathcal{E}_{i, \omega_i}|^2 \left| \sum_b \alpha_{bg}^* \rho_{bg}(T) \Phi(\omega - \omega_{bg} - i\gamma_{bg}, \omega_i) \right|^2, \quad (4)$$

where $\rho_{bg}(T)$ carries the vibrational coherence and γ_{bg} the dephasing rate.

The time evolution of the coherence between levels b and g is

$$\rho_{bg}(\tau) = \rho_{bg} e^{-[i(\omega_b - \omega_g) + \text{sgn}(\tau)\gamma_{bg}]\tau}, \quad (5)$$

which encodes oscillation at the vibrational frequency and exponential decay.

The Raman line-shape function probed in QFRS is

$$f_{bg}(T) = 2\pi \theta(t - T) \rho_{bg}(T) \Phi(\omega - \omega_{bg} - i\gamma_{bg}, \omega_i), \quad (6)$$

linking the vibrational coherence to the entangled two-photon spectrum.

In heterodyne detection, one accesses the phase-sensitive part of the signal:

$$S_{QVHD} = \frac{N}{\pi} |\mathcal{E}_{s, \omega}|^2 |\mathcal{E}_{i, \omega_i}|^2 \text{Im} \left[\sum_b \alpha_{bg}^* \Phi^*(\omega, \omega_i) f_{bg}(T) \right], \quad (7)$$

where interference with a local oscillator retrieves vibrational phase information.

Interferometric Proposal

When two SPDC sources ($k = 2$) are employed, the signal includes cross-terms:

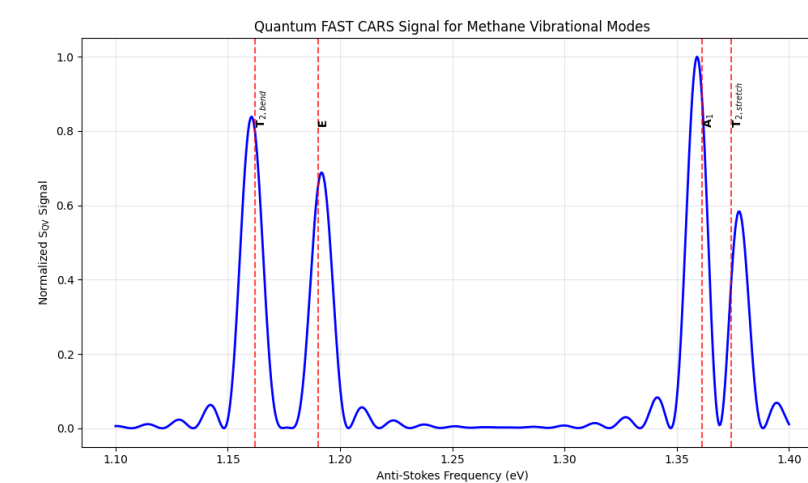
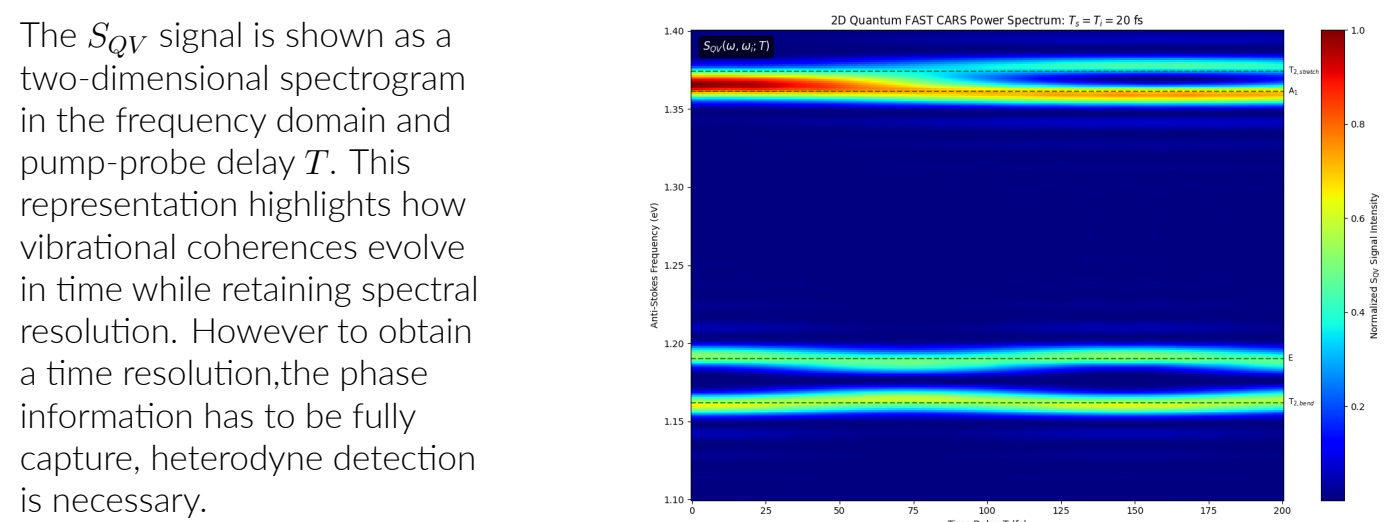
$$\begin{aligned} S_I(\omega_s, \omega_i) &= \langle \Phi_1 | E_s^\dagger E_i^\dagger E_i E_s | \Phi_1 \rangle + \langle \Phi_2 | E_s^\dagger E_i^\dagger E_i E_s | \Phi_2 \rangle \\ &\quad + \langle \Phi_1 | E_s^\dagger E_i^\dagger E_i E_s | \Phi_2 \rangle + \langle \Phi_2 | E_s^\dagger E_i^\dagger E_i E_s | \Phi_1 \rangle \\ &= S_{QV1} + S_{QV2} + 2 \text{Re}(S_{QV12}), \end{aligned} \quad (8)$$

where S_{QV1} and S_{QV2} are QFRS-like contributions from each source, and S_{QV12} is the interference term that carries induced coherence.

This structure shows how QFRS can be extended into an interferometric scheme, gaining both spectral resolution and resilience against noise.

Representation of Methane S_{QV} Signal

This research in progress focuses on simulating the QFRS signal for methane, a molecule with well-characterized vibrational modes. The goal is to validate the QFRS model and establish a baseline for comparing it with the interferometric protocol.



A spectral slice at a fixed delay of $T = 150$ fs reveals the line-shape of the Raman resonance. This one-dimensional cut illustrates how vibrational features can be resolved directly from the QFRS signal, providing a clear comparison with conventional Raman spectra.

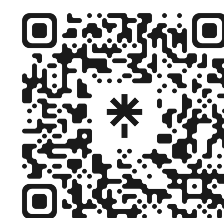
Conclusions and Perspectives

- By extending FAST CARS into the quantum domain, QFRS enables coherent vibrational sensing with entangled light.
- QFRS protocol successfully implemented and validated using methane S_{QV} signals.
- QFRS exploits off-resonant light–matter coupling to retrieve molecular fingerprints.
- SU(1,1) interferometric extension is proposed to enhance noise resilience and eliminate heterodyne detection.
- Next:** Calculate S_{QVHD} and interferometric (S_I) signals.
- Next:** Analyze espectral and time resolutions for a given molecule.
- Next:** Compare S_{QV} , S_{QVHD} , and S_I for resolution, noise resilience, and feasibility.
- Next:** Identify optimal quantum protocol for molecular spectroscopy applications.

References

- [1] Dmitry Pestov, Marlan O. Scully, et al. Optimizing the laser-pulse configuration for coherent raman spectroscopy. *Science*, 316(5822):265–268, 2007.
- [2] Gewei Qian, Da-Wei Wang, et al. Quantum induced coherence light detection and ranging. *Phys. Rev. Lett.*, 131:033603, Jul 2023.
- [3] Zhedong Zhang, Tao Peng, Xiaoyu Nie, Girish S. Agarwal, and Marlan O. Scully. Entangled photons enabled time-frequency-resolved coherent raman spectroscopy and applications to electronic coherences at femtosecond scale. *Light: Science & Applications*, 11(1):274, May 2022.

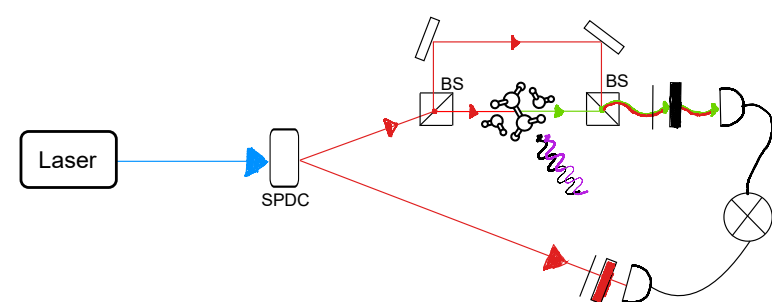
More information,
Complete references
and Contact



Spectroscopic Model Schemes

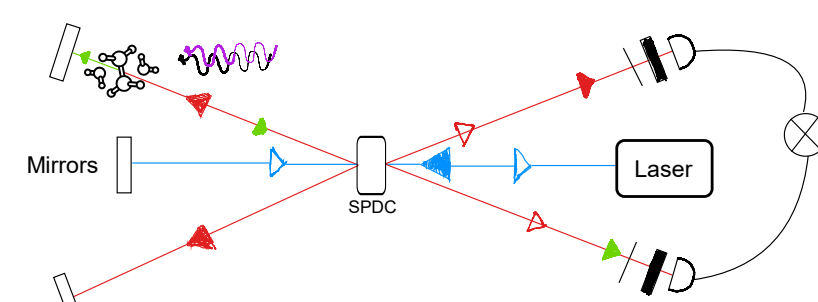
QFRS Model

- Single SPDC source ($k = 1$).
- Signal photon interacts with the molecule.
- Detection in coincidence.
- Idler photon serves as a reference.
- Heterodyne detection needed for phase estimation.
- Time delay T between entangled photons.



Interferometric Model

- Two SPDC sources ($k = 2$).
- Signal photon from one source interacts with the molecule.
- Singles detection allowed due to induced coherence.
- Phase estimation due to interference of two photon pairs.
- Time delay T between entangled photons.



Initial preparation of Coherence



Single photon Detector



Coincidence Measurement



Molecular Sample



Frequency Filter



Non-linear Crystal