

CS 278 Lab7: Functions

Due: Thursday 10/11 by 11:30pm

Your task is to generate all possible functions from $X=\{a, b, c\}$ to a set Y . Set Y contains integers $0, 1, \dots, n$ for some integer $n \geq 0$. The value of n is provided by the user. To define a function you need to specify what it outputs for each element of X . For instance, if $Y = \{0, 1\}$, then $f(a)=0, f(b)=1, f(c)=1$ defines function f from X to Y .

Write a program that prompts the user to enter the size of Y , then generates, enumerates, and prints out in a neat format all possible functions from X to Y . Your program should number generated functions f_1, f_2, f_3, f_4 , etc. For each generated function, output whether or not it is one-to-one, onto, or a bijection. Compute total number of functions generated, how many of them are one-to-one, how many of them are onto, and how many of them are bijections.

Sample dialog with the user may look like the following:

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The program will generate all functions from  $X=\{a,b,c\}$  to  $Y=\{0,1,\dots,n\}$ .
Please enter the value of n: 1
f1(a)=0    f1(b)=0    f1(c)=0
    f1 is not one-to-one, not onto, and not a bijection.
f2(a)=0    f2(b)=0    f2(c)=1
    f2 is not one-to-one, onto, and not a bijection.
f3(a)=0    f3(b)=1    f3(c)=0
    f3 is not one-to-one, onto, and not a bijection.
f4(a)=0    f4(b)=1    f4(c)=1
    f4 is not one-to-one, onto, and not a bijection.
f5(a)=1    f5(b)=0    f5(c)=0
    f5 is not one-to-one, onto, and not a bijection.
f6(a)=1    f6(b)=0    f6(c)=1
    f6 is not one-to-one, onto, and not a bijection.
f7(a)=1    f7(b)=1    f7(c)=0
    f7 is not one-to-one, onto, and not a bijection.
f8(a)=1    f8(b)=1    f8(c)=1
    f8 is not one-to-one, not onto, and not a bijection.
There are 8 functions total.
0 of them are one-to-one.
6 of them are onto.
0 of them are bijections.
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Implementation details:

All possible functions must be automatically generated by your program (e.g., use nested loops to do it). Your program must work for any value of n ($n \geq 0$) entered by the user (you may assume that n is no more than 10).

What to submit:

- Submit the source code of your program using Canvas.
- If you write your program in a programming language other than Java, then submit instructions on how to compile and run your program on CS machines.