

LiquidHaskell

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This report gives a brief overview of LiquidHaskell, a tool that extends Haskell with refinement types. Refinement types are types that extend the expressiveness of Haskell's type system by providing predicates that can verify invariants of the program. This report explains briefly how SMT solvers are leveraged by LiquidHaskell and how to use them by providing some examples. Finally, we discuss its limitations and compare it with other tools.

1 Introduction

Programming verification is an important step in software development. It is the process of verifying that a program behaves as expected. There has been a lot of research in this area and many tools have been developed. Type safety is one of the important features of programming languages that helps to prevent runtime errors. Despite catching many errors at compile time, type systems are not powerful enough to catch all the errors. On the other hand, testing is another way to verify the program, but it is not always possible to test all the possible inputs. Consider the following example:

```
average :: [Int] -> Int
average xs = sum xs 'div' length xs
```

The example above is a simple function that calculates the average of a list of integers. This can be a source of runtime error if the list is empty. While this can be caught by testing, it is not always possible to test all the possible inputs. Another way to verify the program is to use program verification tools. These tools use mathematical logic to check the program. One such tool used in the Haskell programming language is LiquidHaskell. It extends Haskell with refinement types which are types that extend the expressiveness of Haskell. With refinement types, we can provide an invariant that the program should satisfy [3].

In this report, after a short background on program verification using SMT in section 2, we will explain how LiquidHaskell works and how it uses SMT solvers to verify the program in section 3. Then, in Section 4, we provide examples of how to use LiquidHaskell Insertion sort. Finally in section 5 we discuss the limitations of LiquidHaskell and compare it with other tools.

2 Overview

2.1 Refinement Types

Refinement types extend conventional type systems by attaching logical predicates to types, generalizing Floyd-Hoare Logic for functional languages [8]. For example:

```
type Pos = \{v: Int \mid v > 0\}
type Nat = \{v: Int \mid v >= 0\}
```

These are refinements of the basic Int type, with logical predicates stating that v is strictly positive (Pos) and non-negative (Nat), respectively. We can use these refinement types to annotate functions with preconditions and postconditions, such as:

```
divide :: n:Nat -> Pos -> {v:Nat | v <= n}
```

This type signature states that the function divide takes a non-negative and a positive input, respectively, and ensures that the output is less than or equal to the first argument. If the program statically type-checks, then the function is guaranteed to be correct and will not result in a divide-by-zero runtime error [8].

2.2 LiquidHaskell and SMT

LiquidHaskell integrates refinement types with SMT solvers to perform automated verification. It encodes refinement predicates as logical formulas and delegates their satisfiability checking to an SMT solver like Z3 [8].

For example, a refined list function can ensure non-empty lists:

```
{-@ tail :: {v:[a] | 0 < len v} -> a @-}
tail :: [a] -> a
tail (x:_) = x
```

This ensures that tail is only applied to non-empty lists, preventing runtime errors. The SMT solver checks that all function applications adhere to their specifications, making LiquidHaskell a powerful tool for static verification.

2.3 SMT Solvers

SMT (Satisfiability Modulo Theories) solvers are tools that can check the satisfiability of logical formulas in a specific theory. SMT solvers extend the concept of SAT solvers by adding theories (e.g., the theory of equality, of integer numbers, of real numbers, of arrays, of lists, and so on) to the boolean logic [2]. While SAT solvers can only check the satisfiability of Boolean formulas, SMT solvers can check the satisfiability of formulas that contain variables from different theories. As an example, consider the following formula:

$$\varphi = (x \vee y) \wedge (\neg x \vee z) \tag{1}$$

An SAT solver can check the satisfiability of the formula φ by checking if there is an assignment for the variables x, y, z. For instance, x = true, y = false, z = true is an assignment that makes φ true.

On the other hand, SMT solvers can check the satisfiability of formulas that contain variables that require arithmetic theory as the following formula:

$$x + y \le 10 \quad and \quad x = y - 7 \tag{2}$$

2.4 Z3 SMT Solvers

Overall System Architecture of Z3

The overall system architecture of Z3 is aimed at efficiently solving Satisfiability Modulo Theories (SMT) problems. Here's a detailed breakdown of the major components and their interactions:

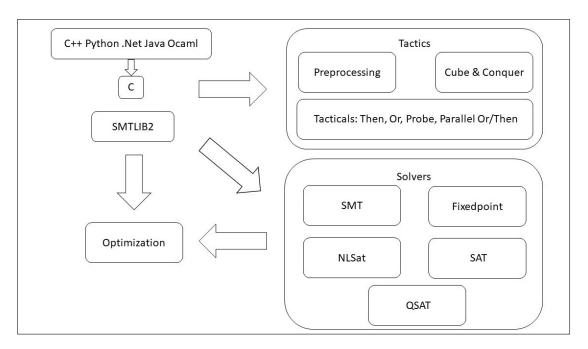


Figure 1: Overall system architecture of Z3 [5]

2.4.1 Interfaces to Z3

Z3 can be interacted with using SMT-LIB2 scripts supplied as text files or through a pipe. Besides this, high-level programming languages can make API calls to Z3, which are proxies for calls over a C-based API [5].

2.4.2 Logical Formulas

Z3 accepts logical formulas built from atomic variables and logical connectives, which can include symbols defined by various theories. These formulas use basic building blocks like Boolean variables, integers, and reals, combined with logical operators such as And, Or, Not, Implies, and Xor. Z3 handles complex logical expressions by integrating symbols from multiple theories, such as arrays and arithmetic, allowing it to model a wide range of problems. The formulas generally follow the SMT-LIB2 standard, ensuring interoperability between different SMT solvers. This versatility makes Z3 a powerful tool for solving diverse logical problems efficiently [5].

2.4.3 Theories

Z3 supports multiple theories, including Equality and Uninterpreted Functions (EUF), Arithmetic (both linear and non-linear), Arrays, Bit-Vectors, Algebraic Datatypes, Sequences, and Strings. Each theory has specialized decision procedures for solving related formulas [5].

2.4.4 **Solver**

Z3 provides services for deciding the satisfiability of formulas. This includes handling incrementality, scopes, assumptions, cores, models, and other methods like statistics, proofs, and retrieving solver state. Specialized solvers are included for different types of problems [5].

SMT Solver

The SMT solver in Z3 is a general-purpose solver that integrates various theories to decide the satisfiability of logical formulas. It uses the CDCL(T) architecture, which combines Conflict-Driven Clause Learning (CDCL) with theory solvers [5].

Fixedpoint Solver

The Fixedpoint solver in Z3 is used for reasoning about recursive definitions and fixed-point computations. It includes a Datalog engine and supports relational algebra and Property Directed Reachability (PDR) algorithms [5]

NLSat Solver

The NLSat solver is specialized for non-linear arithmetic problems. It uses a combination of algebraic methods and SAT-solving techniques to handle polynomial constraints [5].

SAT Solver

The SAT solver in Z3 is designed for propositional logic problems. It uses advanced techniques like in-processing and co-processing to efficiently solve Boolean satisfiability problems [5].

QSAT Solver

The QSAT solver handles quantified Boolean formulas (QBF). It extends the capabilities of the SAT solver to deal with quantifiers, providing solutions for more complex logical problems [5].

2.4.5 Tactics

Tactics in Z3 are used for preprocessing, formula simplification, and the generation of sub-goals. They are essential for decomposing complex problems into relatively simple fragments. The preprocess tactics simplify the input formulae before they are fed into the main solver. It can include heuristics such as the propagation of constants, arithmetic simplification, and removal of redundant constraints. The Cube and Conquer tactic is used to split the search space into smaller sub-problems. (cubes) that can be solved independently. This is a very useful scheme for parallel solving and the sum time required to solve, it greatly shortens. Tacticals are combiners that make the composition of multiple tactics [5].

2.4.6 Optimization

Z3 allows the use of optimization services along with user-defined problems in order to study the satisfiability of the problem while maximizing or minimizing objective functions. This applies to those problems which require solutions that are to be optimized under given constraints [5].

2.4.7 Applications and Example of Z3

Software analysis verification and symbolic execution along with software analysis verification rely heavily on making use of the Z3 platform. Z3 operates through SMT-LIB2 scripts as well as program application interfaces using Python, C++, and OCaml. Z3 users prefer the Python API because of its straightforward nature and SMT-LIB2 stands out for presenting logical problems with predefined logic including arithmetic, arrays, and bit-vectors.

Consider the satisfiability problem 3 involving three clauses. We aim to determine whether there exists an assignment of Boolean variables Tie and Shirt such that the conjunction of the following clauses holds:

$$(Tie \lor Shirt) \land (\neg Tie \lor Shirt) \land (\neg Tie \lor \neg Shirt)$$

$$(3)$$

Formula 3 can be solved in SMTLIB2 as the following code:

When we must this 72 responds:

When we run this, Z3 responds:

```
sat
(model
  (define-fun Tie () Bool false)
  (define-fun Shirt () Bool true)
)
```

This SMT-LIB2 script sets up the problem, declares the variables, asserts the constraints, checks for satisfiability, and retrieves the model, just like the Python code does for Formula 3 with z3 in the following example.

```
(set-logic QF_UF)
(declare-const Tie Bool)
(declare-const Shirt Bool)
(assert (or Tie Shirt))
(assert (or (not Tie) Shirt))
(assert (or (not Tie) (not Shirt)))
(check-sat)
(get-model)
```

The output of the code is:

```
Sat
[Tie = False, Shirt = True]
```

When calling s.check(), the solver determines that the assertions are satisfiable (sat)—meaning there is a way to assign values to the Tie and Shirt that make all the conditions true. One possible solution is Tie = false and Shirt = true, which can be retrieved using s.model().

The next example shows how Z3 reasons across multiple mathematical theories such as array theory, arithmetic, and uninterpreted functions. Z3's API analyzes the following Python snippet:

```
Z = IntSort()
f = Function('f', Z, Z)
x, y, z = Ints('x y z')
A = Array('A', Z, Z)
fml = Implies(x + 2 == y, f(Store(A, x, 3)[y - 2]) == f(y - x + 1))
solve(Not(fml))
unsat
```

The integrated theories enabling this reasoning are:

• Linear Integer Arithmetic (LIA): Handles integer constraints:

$$x + 2 = y$$
 and $y - x + 1$

• Array Theory: Manages array operations through Store and select operators:

$$Store(A, x, 3)[y - 2] \equiv ite(y - 2 = x, 3, A[y - 2])$$

where ite denotes the if-then-else operator.

• Uninterpreted Functions: Treats function f as a black box respecting functional consistency:

$$\forall a, b : (a = b) \implies (f(a) = f(b))$$

This example illustrates Z3's theory combination mechanism, which:

- Ensures coherence across different mathematical domains
- Handles cross-theory constraints (e.g., array indices as arithmetic expressions)
- Enables verification of systems with mixed abstractions (memory, arithmetic, and black-box components)

This capability makes Z3 particularly useful for software verification, as real-world programs inherently integrate these concepts [5].

3 Working with LiquidHaskell

In this section, we will explain how LiquidHaskell works. LiquidHaskell is available as a GHC plugin. To use it, you need to add its dependencies to the cabal file as following [1]:

```
name: lh-plugin-demo
version: 0.1.0.0
...
build-depends:
    liquid-prelude,
    liquid-vector,
    liquidhaskell,
    base,
    containers,
    vector

default-language: Haskell2010
ghc-options: -fplugin=LiquidHaskell
```

With these dependencies, LiquidHaskell can check your program at compile time or through a code linter in your preferred IDE. Note that there are options such as --reflection and --ple, which enable reflection and Proof by Logical Evaluation (PLE) in LiquidHaskell. You can either add them as plugin options in the Cabal file or use them directly in the source code as follows:

```
{-@ LIQUID "--reflection" @-}
{-@ LIQUID "--ple" @-}
```

In the following sections, we will use both options, so we do not include them explicitly in the code snippets.

3.1 Type Refinement

Refinement types allow constraints to be placed on variables by adding predicates to their types [3]. For example, we can define natural numbers as follows:

```
{-@ type Nat = {v:Int | 0 <= v} @-}
```

Now if you configure your IDE to use Haskell LSP, it will show the following error if you try to assign a negative number to a variable of type Nat.

The error message shows that the inferred type of the variable x is not a subtype of the required type.

Refinement types allow defining function preconditions and postconditions [3]. For example, consider the following function:

```
tail :: [a] -> [a]
tail (_:xs) = xs
tail [] = error "tail: empty list"
```

The function defined above is a partial function because it does not handle the case when the list is empty. Typical Haskell types only allow the introduction of the Maybe type, which postpones error handling to another part of the program [3]. Using refinement types, we can define the type of tail function as follows:

```
{-@ tail :: {v:[a] | 0 < len v} -> a @-}
tail :: [a] -> [a]
tail (x:_) = x
```

Now, our function is total, as it does not allow an empty list to be passed to tail.

```
x :: [Int]
x = tail (tail [1, 2])
```

When calling functions, LiquidHaskell won't look into the body of the function to see if the first application of the *tail* gives the valid non-empty list to the second *tail*. To allow LiquidHaskell consider the above example as safe, we need to also specify the post-condition for our function as following:

```
{-@ tail :: xs: {v:[a] | 0 < len v} -> {v:[a] | len v == len xs - 1} @-}
tail :: [a] -> [a]
tail (x:_) = x
```

3.2 Refined Data Types

In the above examples, we saw how refinements of input and output of function allow us to have stronger arguments about our program. We can take this further by refining the data types. Consider the following example [3]:

```
data Slist a = Slist { size :: Int, elems :: [a] }
{-@ data Slist a = Slist { size :: Nat, elems :: {v:[a] | len v == size} } @-}
```

This refined *Slist* data type ensures the stored 'size' always matches the length of the 'elems' list, as formalized in the refinement annotation [3]. This ensures that the size of the list is always correct.

The only thing that is missing is the definition of *len*. Fortunately, this function has already reflected by LiquidHaskell. In the following section, we show how can we use reflection or measure directives to define and execute any user-defined Haskell function in the refinement logic and reason about them.

3.3 Lifting Functions to the Refinement Logic

When our programs become more complex, we need to define our own functions in the refinement logic and reason about a function within another function. Refinement Reflection allows deep specification and verification by reflecting the code implementing a Haskell function into the function's output refinement type [7]. There are two ways to define and reason about a function in the refinement logic: reflection and measure.

Measure can be used on a function with one argument that is pattern-matched in the function body. Then, LiquidHaskell copies the function to the refinement logic, adds a refinement type to the constructor of the function's argument, and emits inferred global invariants related to the refinement [6]. Consider the following example:

```
data Bag a = Bag { toMap :: M.Map a Int } deriving Eq
{-@ measure bag @-}
{-@ bag :: Ord a => List a -> Bag a @-}
bag :: (Ord a) => List a -> Bag a
bag Nil = B.empty
bag (Cons x xs) = B.put x (bag xs)
```

This code adds the bag refinement type to the List data type. The measure directive is used to define the bag function, which is then copied to the refinement logic. It means that now the type of list constructors would have:

```
Nil :: \{v: \text{List a} \mid bag\ v = B.empty\}
Cons :: x: a \rightarrow 1: \text{List } a \rightarrow \{v: \text{List a} \mid bag\ v = B.put\ x\ (bag\ 1)\}
```

So then we can use the bag function in the refinement logic to reason about the program. For instance, in the following example, we can use the bag function to reason about the program:

```
{-@ equalBagExample1 :: { bag(Cons 1 (Cons 3 Nil)) == bag( Cons 2 Nil) } @-}

>> VV : {v : () | v == GHC.Tuple.Prim.()}
>> .

>> is not a subtype of the required type
>> VV : {VV##2465 : () | bag (Cons 1 (Cons 3 Nil)) == bag (Cons 2 Nil)}
```

The $\{x=y\}$ is shorthand for $\{v:()\mid x=y\}$, where x and y are expressions. Note that equality for bags is defined as the equality of the underlying maps that already have a built-in equality function. LiquidHaskell can reason about the equality of bags by using the equality of the underlying maps and issuing a type error if the bags are not equal. If we define multiple measures for the same data type the refinements are conjoined together [6].

Reflection is another useful feature that allows the user to define a function in the refinement logic, providing the SMT solver with the function's behavior [10]. This has the advantage of allowing the user to define a function that is not pattern-matched in the function body. Additionally, with the use of a library of combinators provided by LiquidHaskell, we can leverage the existing programming constructs to prove the correctness of the program and use the principle of propositions-as-types (known as Curry-Howard isomorphism) [10] [11].

```
{-@ infixr ++ @-}

{-@ reflect ++ @-}

{-@ (++) :: xs:[a] -> ys:[a] -> { zs:[a] | len zs == len xs + len ys } @-}

(++) :: [a] -> [a] -> [a]

[] ++ ys = ys

(x : xs) ++ ys = x : (xs ++ ys)
```

The ++ function is defined in the refinement logic using the reflect directive. Now we can use the ++ function in the refinement logic to reason about the program. In the following subsection, we will show how to use LiquidHaskell to verify that the ++ function is associative.

3.4 Verification

LiquidHaskell allows structure proofs to follow the style of calculational or equational reasoning popularized in classic texts and implemented in proof assistants like Coq and Agda . It is equipped with a family of equation combinators for logical operators in the theory QF-UFLIA

[10]. In the following example, we show how to use these combinators to verify that the ++ function is associative:

```
{-@ assoc :: xs:[a] -> ys:[a] -> zs:[a]
  -> { v: () | (xs ++ ys) ++ zs = xs ++ (ys ++ zs) } @-}
assoc :: [a] -> [a] -> ()
assoc [] ys zs =
  ([] ++ ys)
    ++ zs
    === ys
   ++ zs
    === []
   ++ (ys ++ zs)
    *** QED
assoc (x : xs) ys zs =
  ((x : xs) ++ ys)
    ++ zs
   === x : (xs ++ ys) ++ zs
    : ((xs ++ ys) ++ zs)
     ? assoc xs ys zs
     === (x : xs)
     ++ (ys ++ zs)
     *** QED
```

These combinators are defined as follows:

```
(===) :: x: a -> y: { a | x = y } -> { v: a | v = x }
data QED = QED
(***) :: a -> QED -> ()
```

As you can see, some of the steps in the proof seem trivial if we are able to unfold the definition of the ++ function. For this purpose, LiquidHaskell provides Proof by Logical Evaluation (PLE) which allows us to unfold the definition of the function. The key idea in PLE is to mimic type-level computation within SMT-logics by representing the function in a guarded form and repeatedly unfolding function application terms by instantiating them with their definition corresponds to an enabled guard [10].

4 Example Application

In this section, we discuss the insertion sort algorithm and how to verify its functional correctness using LiquidHaskell. We take an intrinsic approach, leveraging refinement types so that we do not need to prove correctness separately. Insertion sort is a simple algorithm that builds a sorted list by inserting one element at a time. Using LiquidHaskell, we aim to ensure that the sorted list is both ordered and a permutation of the input.

4.1 Definition of Insertion Sort

Insertion sort is implemented in Haskell with two main components: the insert function, which places an element in its correct position in a sorted list, and the insertSort function, which recursively sorts the input list. Below is the Haskell implementation:

```
{-@ LIQUID "--reflection" @-}
{-@ LIQUID "--ple" @-}
module InsertionSort where
-- Define the List type
data List a = Nil | Cons a (List a) deriving (Eq, Show)
-- Insert operation
{-0 reflect insert 0-}
insert :: (Ord a) => a -> List a -> List a
insert x Nil = Cons x Nil
insert x (Cons y ys)
  | x \le y = Cons x (Cons y ys)
  | otherwise = Cons y (insert x ys)
-- Insertion Sort operation
{-@ reflect insertSort @-}
insertSort :: (Ord a) => List a -> List a
insertSort Nil = Nil
insertSort (Cons x xs) = insert x (insertSort xs)
```

4.2 Specification

To verify the correctness of the insertion sort, we define specifications that ensure the following: 1. The output list is sorted. 2. The output list is a permutation of the input list.

4.2.1 Sortedness Specification

We define a helper function, isSorted, to check whether a list is sorted:

The isSorted function is then used to specify and verify the correctness of the insert and insertSort functions.

4.2.2 Insert Function Specification

The insert function places an element into a sorted list while maintaining its sortedness:

```
{-@ insert :: x:_ -> {xs:_ | isSorted xs} -> {ys:_ | isSorted ys} @-}
```

4.2.3 Insertion Sort Specification

The insertSort function ensures that the output is sorted and is a permutation of the input:

```
{-@ insertSort :: xs:_ -> {ys:_ | isSorted ys && bag xs == bag ys} @-}
```

Here, bag represents a multiset of elements, used to verify that the output is a permutation of the input.

4.3 Proofs

By incorporating the specifications into the insertion sort implementation, we can verify the correctness of the algorithm. Once we define the specification, we will realize that we need to prove the correctness of the <code>insert</code> function. As the specification is not enough for the <code>LiquidHaskell</code> to verify the correctness of the <code>insert</code> function, we need to prove the following lemma:

```
{-@ lem_ins :: y:_ -> {x:_ | y < x} -> {ys:_ | isSorted (Cons y ys)}
    -> {isSorted (Cons y (insert x ys))} @-}
lem_ins :: (Ord a) => a -> a -> List a -> Bool
lem_ins y x Nil = True
lem_ins y x (Cons y1 ys) = if y1 < x then lem_ins y1 x ys else True</pre>
```

This lemma ensures that the insert function maintains the sortedness property. Then with the use of withProof, we can use the lemma to prove the correctness of the insert function:

```
{-@ reflect insert @-}
{-@ insert :: x:_ -> {xs:_ | isSorted xs}
    -> {ys:_ | isSorted ys && Map_union (singelton x) (bag xs) == bag ys } @-}
insert :: (Ord a) => a -> List a -> List a
insert x Nil = Cons x Nil
insert x (Cons y ys)
    | x <= y = Cons x (Cons y ys)
    | otherwise = Cons y (insert x ys) 'withProof' lem_ins y x ys</pre>
```

4.3.1 Proof of Insertion Sort Correctness

The correctness of insertSort is established by combining the correctness of insert and ensuring that the output satisfies both the sortedness and permutation properties.

```
{-@ insertSort :: xs:_ -> {ys:_ | isSorted ys && bag xs == bag ys} @-}
insertSort :: (Ord a) => List a -> List a
insertSort Nil = Nil
insertSort (Cons x xs) = insert x (insertSort xs)
```

By verifying these properties using LiquidHaskell, we ensure that insertion sort is functionally correct and meets the desired specifications.

5 Conclusions, Results, Discussion

LiquidHaskell, enhanced with Refinement Reflection and Proof by Logical Evaluation (PLE), combines the strengths of SMT-based and Type Theory (TT)-based verification approaches. It allows programmers to verify program correctness by leveraging a combination of refinement types, code reflection, and automated proof search [10].

Core Concepts

- Refinement Types: LiquidHaskell uses refinement types to specify program properties, extending basic types with logical predicates drawn from an SMT-decidable logic.
- Refinement Reflection: The implementation of a user-defined function is reflected in its output refinement type. This converts the function's type signature into a precise description of the function's behavior. At uses of the function, the definition is instantiated in the SMT logic [10].
- **Propositions as Types**: Proofs are written as regular Haskell programs, utilizing the Curry-Howard isomorphism. This allows programmers to use language mechanisms like branching, recursion, and auxiliary functions to construct proofs [10].
- Proof by Logical Evaluation (PLE): PLE is a proof-search algorithm that automates equational reasoning. It mimics type-level computation within SMT-logics by representing functions in a guarded form and repeatedly unfolding function application terms by instantiating them with their definition corresponding to an enabled guard [10].

Comparison with Type Theory (TT) Based Systems

- Type-Level Computation: TT-based provers use type-level computation (normalization) for reasoning about user-defined functions, often requiring explicit lemmas or rewrite hints.
- Automation: LiquidHaskell uses PLE to automate equational reasoning without explicit lemmas, by emulating type-level computation within SMT logic.
- Proof Style: Proofs in LiquidHaskell are written as Haskell programs.
- **SMT Integration**: LiquidHaskell uses SMT solvers for decidable theories, while TT-based systems often require users to handle these proofs manually.

- Expressiveness: Both systems can express sophisticated proofs. LiquidHaskell is shown to be able to express any natural deduction proof [10].
- Practicality: LiquidHaskell reuses an existing language and its ecosystem, allowing proofs and programs to be written in the same language.

Comparison with Other SMT-Based Verifiers

- Axiomatization: Existing SMT-based verifiers such as Dafny use axioms to encode user-defined functions which can lead to incomplete verification and matching loops. LiquidHaskell, uses refinement reflection to encode functions, along with PLE for complete and terminating verification [10].
- Fuel Parameter: Dafny and F* use a fuel parameter to limit the instantiation of axioms which can lead to incompleteness [10]. PLE does not require any fuel parameter and is guaranteed to terminate.

Limitations

- **Debugging**: The increased automation can make it harder to debug failed proofs.
- Interactivity: LiquidHaskell lacks strong interactivity, unlike theorem provers with tactics and scripts.
- Certificates: It does not produce easily checkable certificates, unlike theorem provers [10].
- Reflection Limitations: Not all Haskell functions can be reflected into logic due to soundness or implementation constraints [10].

Conclusion

LiquidHaskell combines refinement types, code reflection, and PLE to offer a practical approach to program verification within an existing language. By leveraging SMT solvers for decidable theories and PLE to automate equational reasoning, LiquidHaskell aims to simplify the process of verifying program correctness when compared to other tools.

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