

# Compilers Project 1: Scanner Generator

M. BARNEY, J. COLLARD, AND S. PATEL

March 21, 2013

## 1 Introduction

This is the final report for project 1, CS454/CS554, on lexical analysis. It includes all of the source code for our Haskell implementation of a scanner generator. Our team consists of the authors listed above. In preparing this document, the work was split equally among the members of the group, in addition to the coding and testing duties. Approximately 60 man hours went into finishing the project.

Our first design decision was to use Haskell’s literate mode to prepare all of our code. Secondly, we decided to use the distributed revision control software `git` for collaborative coding.

We decided to write each algorithm in the assignment as its own module, in addition to modules describing finite state automata (FSA), regular expressions, and similarly for the file input/output.

Lastly, we decided to write a scanner generator for our final output, instead of a scanner “interpeter”. That is, we parse a lexical description, and return a Haskell module to be compiled with an appropriate parser. Once suitably compiled, the binary scans text files and produces a stream of tokens for the language given in the lexical description.

## 2 Finite State Automaton

In this module we give our data structure for modelling a finite state automaton.

The formal definition of an FSA is a 5-tuple, where:

1. a finite set of states ( $Q$ )
2. a finite set of input symbols called the alphabet ( $\Sigma$ )
3. a transition function ( $\delta : Q \times \Sigma \rightarrow Q$ )
4. a start state ( $q_0 \in Q$ )
5. a set of accept states ( $F \subseteq Q$ )

We tried to have our data structure mirror the mathematical definition of an FSA as closely as possible.

```
{-# LANGUAGE TypeFamilies, FlexibleContexts, FlexibleInstances #-}
module FiniteStateAutomata (
    FSA (.),
    NFA' (.),
    NFAMap,
    DFA' (.),
    DFAMap,
    epsilon, ppfsa) where

import qualified Data.Map as M
import qualified Data.Set as S
class (Ord (Alpha f),
    Show (Alpha f),
    Show f,
    Show (FSAVal f),
    Listable (FSAVal f)) => FSA f where
    type Alpha f
    type FSAVal f
    alphabet :: (Ord (Alpha f), Show (Alpha f)) =>
        f -> S.Set (Alpha f)
    accepting :: f -> S.Set Int
    start     :: f -> Int
    trans     :: f -> M.Map Int (FSAVal f)
    states    :: f -> S.Set Int
    states fsa = S.unions [(S.fromList o M.keys o trans $ fsa),
        (accepting fsa),
        (S.fromList o
```

```

concatMap sndList ◦
M.elems ◦ trans $ fsa)]
data DFA' a = DFA' { alpha :: S.Set a,
                    ss      :: DFAMap a,
                    accept :: S.Set Int,
                    st      :: Int } deriving (Show, Read, Eq)
data NFA' a = NFA' { nalpha :: S.Set a,
                    nss     :: NFAMap a,
                    naccept :: S.Set Int,
                    nst     :: Int }
type DFAMap a = M.Map Int (M.Map a Int)
type NFAMap a = M.Map Int (S.Set (Maybe a, Int))
class (Show (Elem m)) ⇒ Listable m where
  type Elem m
  toList :: m → [(Elem m, Int)]
instance (Show a) ⇒ Listable (M.Map a Int) where
  type Elem (M.Map a Int) = a
  toList = M.toList
instance (Show a) ⇒ Listable (S.Set (Maybe a, Int)) where
  type Elem (S.Set (Maybe a, Int)) = Maybe a
  toList = S.toList
sndList :: Listable m ⇒ m → [Int]
sndList = map snd ◦ toList
fsaShow :: (FSA f) ⇒ f → String
fsaShow fsa = "{alphabet="
             ++ (show ◦ S.toList ◦ alphabet $ fsa)
             ++ ", " ++
             "states=" ++
             (show ◦ S.toList ◦ states $ fsa) ++ ", " ++
             "start=" ++ (show ◦ start $ fsa) ++ ", " ++
             "accepting="
             ++ (show ◦ S.toList ◦ accepting $ fsa)
             ++ ", " ++ "trans="
             ++ (show ◦ map (filter (≠ ' ')) ◦
                 showTransitions $ fsa)
pettyPrinter :: (FSA f) ⇒ f → IO ()

```

```

pettyPrinter fsa = (putStr $ "alphabet="
  ++ (show ◦ S.toList ◦ alphabet $ fsa)
  ++ "\n" ++
  "states="
  ++ (show ◦ S.toList ◦ states $ fsa)
  ++ "\n" ++
  "start=" ++ (show ◦ start $ fsa)
  ++ "\n" ++
  "accepting="
  ++ (show ◦ S.toList ◦ accepting $ fsa)
  ++ "\n") >> trans
  where trans =
    mapM_ (putStrLn ◦ filter (≠ ' '))
    $ showTransitions fsa
ppfsa :: (FSA f) ⇒ f → IO ()
ppfsa = pettyPrinter
showTransitions :: (FSA f) ⇒ f → [String]
showTransitions fsa = map showTransition ◦
  M.toList ◦ trans $ fsa where
  showTransition (from, ts) = (show from)
    ++ "  :: "
    ++ (show ◦ map showTransition' ◦ toList $ ts) where
    showTransition' (x, to) = (show x) ++ " -> " ++ (show to)
instance (Ord a, Show a) ⇒ FSA (DFA' a) where
  type Alpha (DFA' a) = a
  type FSAVal (DFA' a) = (M.Map a Int)
  alphabet = alpha
  accepting = accept
  start = st
  trans = ss
epsilon :: Maybe a
epsilon = Nothing
instance (Ord a, Show a) ⇒ FSA (NFA' a) where
  type Alpha (NFA' a) = a
  type FSAVal (NFA' a) = (S.Set (Maybe a, Int))
  alphabet = nalpha
  accepting = naccept

```

```

    start = nst
    trans = nss
instance (Ord a, Show a) ⇒ Show (NFA' a) where
    show nfa = "NFA " ++ (fsaShow nfa)
simpleNFA :: NFA' Char
simpleNFA = NFA' alpha states accepting start where
    alpha = S.fromList ['a', 'b']
    states = M.fromList
        [(0, S.fromList [(Just 'a', 1)]),
         (1, S.fromList [(Just 'b', 0), (epsilon, 2)])]
    start = 0
    accepting = S.fromList [2]
simpleDFA :: DFA' Char
simpleDFA = DFA' alpha states accepting start where
    alpha = S.fromList ['a', 'b', 'c']
    states = M.fromList
        [(0, M.fromList [('a', 1)]),
         (1, M.fromList [('b', 0), ('c', 2)])]
    start = 0
    accepting = S.fromList [2]
deadStateDFA :: DFA' Char
deadStateDFA = DFA' alpha states accepting start where
    alpha = S.fromList "ab"
    states =
        M.fromList [(0, trans0), (1, trans1), (2, trans2)] where
            trans0 = M.fromList [('a', 1), ('b', 2)]
            trans1 = M.fromList [('b', 3)]
            trans2 = M.fromList [('a', 3)]
    accepting = S.fromList [1, 2]
    start = 0

```

### 3 Regular Expressions

In this module we give the haskell data type for a regular expression; the encoding almost exactly mirrors the definition given in the assignment.

```
{-# LANGUAGE TypeFamilies, FlexibleContexts, FlexibleInstances #-}
```

```

module Regex (Regex (.)) where
data Regex a = Alt (Regex a) (Regex a)
    | Concat (Regex a) (Regex a)
    | Kleene (Regex a)
    | Term a
    | Empty deriving (Eq, Show)

```

We wrote a pretty infix printer:

```

instance Show (Regex Char) where
  show (Alt r1 r2) =
    "(" ++ (show r1) ++ "|" ++ (show r2) ++ ")"
  show (Concat r1 r2) =
    "(" ++ (show r1) ++ "+" ++ (show r2) ++ ")"
  show (Kleene r1) = "(" ++ (show r1) ++ "*" ++ ")"
  show (Term c) = '\'' : c : []
  show (Empty) = "\\epsilon"

```

However, it was determined that writing a scanner generator would be easier if we used the default show for regular expressions.

## 4 Algorithms

Our solutions to the “in-memory” algorithms given in §1.2 have been modularized in the following way.

```

module Algorithms (module Thompson,
    module SubsetConstruction,
    module Hopcroft,
    module Recognize
) where
import Thompson
import SubsetConstruction
import Hopcroft
import Recognize

```

In this way we encapsulated (and named) the solutions individually, as the assignment requested.

## 4.1 Thompson's Algorithm

In this module we provide our solution for converting a regular expression to an NFA.

```
module Thompson (thompson) where  
import Prelude hiding (concat)  
import qualified Data.Set as S  
import qualified Data.Map as M  
import FiniteStateAutomata (FSA (trans), NFA' (..), epsilon)  
import Regex
```

The function *thompson* returns the result of converting a regular expression to a non-deterministic finite state automaton. It uses Thompson's algorithm for doing so.

```
thompson :: (Ord a, Show a) => Regex a -> NFA' a  
thompson = fst o thompson' 0  
thompson' :: (Ord a, Show a) =>  
  Int -> Regex a -> (NFA' a, Int)  
thompson' lab (Alt r1 r2) = union lab'' fsa fsa' where  
  (fsa, lab') = thompson' lab r1  
  (fsa', lab'') = thompson' lab' r2  
thompson' lab (Concat r1 r2) = concat lab'' fsa fsa' where  
  (fsa, lab') = thompson' lab r1  
  (fsa', lab'') = thompson' lab' r2  
thompson' lab (Kleene r1) = mrKleene lab' fsa where  
  (fsa, lab') = thompson' lab r1  
thompson' lab (Term x) = symbol lab x  
thompson' lab Empty = expression lab
```

The following functions individually convert particular regular expressions to their NFA equivalents. For example, *concat* takes two regular expressions, say *a* and *b*, and returns an NFA where the NFA corresponding to *a*'s accepting states are now transitions to the NFA corresponding to *b*'s start state.

The other functions perform similar operations, according to the algorithm.

```
expression :: (Ord a, Show a) => Int -> (NFA' a, Int)  
expression label = (fsa, label + 2) where
```

```

fsa = NFA' S.empty (M.fromList [n1])
      (S.singleton (label + 1)) label
n1 = (label, S.singleton (epsilon, (label + 1)))
symbol :: (Ord a, Show a) => Int -> a -> (NFA' a, Int)
symbol label sym = (fsa, label + 2) where
  fsa = NFA' (S.singleton sym)
      (uncurry M.singleton n1) (S.singleton (label + 1)) label
  n1 = (label, S.singleton (Just sym, label + 1))
union :: (Ord a, Show a) =>
  Int -> NFA' a -> NFA' a -> (NFA' a, Int)
union label nfa0 nfa1 = (fsa, label + 2) where
  (NFA' a0 m0 as0 st0) = updateAccepting [(label + 1)] nfa0
  (NFA' a1 m1 as1 st1) = updateAccepting [(label + 1)] nfa1
  fsa = NFA' alpha newMap (S.singleton (label + 1)) label
  alpha = S.union a0 a1
  newMap = M.unions [m0, m1, epsilonEdges]
  epsilonEdges =
    M.singleton label
    (S.fromList [(epsilon, st0), (epsilon, st1)])
concat :: (Ord a, Show a) =>
  Int -> NFA' a -> NFA' a -> (NFA' a, Int)
concat label fsa0@(NFA' s0 m0 as0 st0) (NFA' s1 m1 as1 st1) =
  (fsa, label) where
  fsa = NFA' (S.union s0 s1) (M.union updated m1) as1 st0
  updated = trans $ updateAccepting [st1] fsa0
mrKleene :: (Ord a, Show a) => Int -> NFA' a -> (NFA' a, Int)
mrKleene label nfa@(NFA' a _ as st) = (fsa, label + 2) where
  (NFA' _ m _ _) = updateAccepting [st, (label + 1)] nfa
  fsa = NFA' a m' (S.singleton (label + 1)) label
  m' = M.union m epsilons
  epsilons =
    M.singleton label
    (S.fromList [(epsilon, (label + 1)), (epsilon, st)])
  epsilons' = M.fromList o map func o S.toList $ as
  func x = (x, S.singleton (epsilon, label + 1))
updateAccepting :: (Ord a) => [Int] -> NFA' a -> NFA' a
updateAccepting is nfa@(NFA' a ts as st) =

```



```

NFA' a newTrans (S.empty) st where
  newTrans = M.union ts nts
  nts = M.fromList ◦ map func ◦ S.toList $ as
  func x =
    (x, S.fromList ◦ map (λi → (epsilon, i)) $ is)

```

## 4.2 Subset Construction

In this module we provide our solution for converting a given non-deterministic finite state automaton to an equivalent deterministic finite state automaton.

```

{-# LANGUAGE FlexibleInstances #-}
module SubsetConstruction (subsetConstruction) where
import Data.Maybe
import FiniteStateAutomata
import qualified Data.Map as M
import qualified Data.Set as S
import Debug.Trace
type LabelMap = M.Map (S.Set Int) Int
subsetConstruction :: (Ord a, Show a) ⇒ NFA' a → DFA' a
subsetConstruction nfa =
  DFA' (alphabet nfa) dfamap' accept start' where
    start' = labelsM. ! startStateSet
    accept = findAccepting nfa labelmap
    (−, labelmap, dfamap') =
      subsetConstruction' nfa next
      labels dfamap outSets
    startStateSet = closure nfa (start nfa)
    (labels, next) =
      labelSets 0 M.empty
      (S.fromList (startStateSet : outSets))
    edges = edgeMap labels edgeSet
    dfamap =
      M.singleton (labelsM. ! startStateSet) edges
    outSets =
      map (closure' ◦ flip move' startStateSet)

```

```

    alphabet'
    edgeSet = zip alphabet' outSets
    alphabet' = S.toList ∘ alphabet $ nfa
    closure' = closure nfa
    move' = move nfa
findAccepting :: (Ord a, Show a) ⇒
    NFA' a → LabelMap → S.Set Int
findAccepting nfa labels = S.fromList sets where
    sets = M.elms (M.filterWithKey isAccepting labels)
    isAccepting label _ =
        S.empty ≠ (S.intersection accept label)
    accept = accepting nfa
subsetConstruction' :: (Ord a, Show a) ⇒
    NFA' a → Int → LabelMap →
    DFAMap a → [S.Set Int] →
    (Int, LabelMap, DFAMap a)
subsetConstruction' _ next labels dfamap [] =
    (next, labels, dfamap)
subsetConstruction' nfa next labels dfamap (s : ss) =
    case (s ≡ S.empty) of
    True → subsetConstruction' nfa next labels dfamap ss
    False → if done then continue else recursion where
        done = M.lookup (labelsM. ! s) dfamap ≠ Nothing
        continue = subsetConstruction' nfa next labels dfamap ss
        recursion =
            subsetConstruction' nfa next'' labels'' dfamap'' ss
            (next'', labels'', dfamap'') =
                subsetConstruction' nfa next' labels' dfamap' outSets
            (labels', next') =
                labelSets next labels (S.fromList outSets)
            dfamap' = M.insert (labelsM. ! s) edges dfamap
            edges = edgeMap labels' edgeSet
            edgeSet = zip alphabet' outSets
            outSets = map (closure' ∘ flip move' s) alphabet'
            alphabet' = S.toList ∘ alphabet $ nfa
            move' = move nfa
            closure' = closure nfa

```

```

labelSets :: Int → M.Map (S.Set Int) Int →
    S.Set (S.Set Int) →
    (M.Map (S.Set Int) Int, Int)
labelSets next labels sets =
    labelSets' next labels (S.toList sets)
labelSets' :: Int → LabelMap →
    [S.Set Int] → (LabelMap, Int)
labelSets' next labels [] = (labels, next)
labelSets' next labels (s : ss) =
    case (s ≡ S.empty) of
        True → labelSets' next labels ss
        False →
            if (M.member s labels) then
                (labelSets' next labels ss)
            else
                (labelSets' (next + 1)
                 (M.insert s next labels) ss)

edgeMap :: (Ord a, Show a) ⇒
    M.Map (S.Set Int) Int →
    [(a, (S.Set Int))] → M.Map a Int
edgeMap = edges' M.empty where
    edges' :: (Ord a, Show a) ⇒
        M.Map a Int → M.Map (S.Set Int) Int →
        [(a, (S.Set Int))] → M.Map a Int
    edges' acc [] = acc
    edges' acc labels ((alpha, set) : ss) =
        case (set ≡ S.empty) of
            True → edges' acc labels ss
            False → edges' acc' labels ss where
                acc' = M.insert alpha (labelsM. ! set) acc

class Constructable c where
    closure :: (Show a, Ord a) ⇒ NFA' a → c → S.Set Int
    move :: (Show a, Ord a) ⇒ NFA' a → a → c → S.Set Int

instance Constructable Int where
    closure nfa state =
        fst ∘ closure' nfa (S.singleton state) M.empty $ state where
            closure' nfa acc memoize state =

```

```

case (M.lookup (acc, state) memoize) of
  Nothing →
    if done then (acc', memoize') else (acc'', memoize'') where
      done = edges ≡ Nothing ∨ eps ≡ S.singleton state
      edges = M.lookup state ∘ trans $ nfa
      eps = S.union (S.singleton state)
        (S.map snd ∘ S.filter isEpsilon ∘
         fromJust $ edges)
      eps' = S.difference eps acc
      isEpsilon (label, _) = label ≡ epsilon
      acc' = S.union acc (S.singleton state)
      acc'' = S.union acc' ∘ S.unions $ sets
      memoize' = M.insert (acc, state) acc' memoize
      (memoize''', sets) = memoMap memoize (closure' nfa acc') ∘ S.toList $ eps'
      memoize'' = M.insert (acc, state) acc'' memoize'''
  Just set → (set, memoize)

move nfa sym state =
  if (edges ≡ Nothing) then S.empty else eps where
    edges = M.lookup state ∘ trans $ nfa
    eps = S.map snd ∘ S.filter isSym ∘ fromJust $ edges
    isSym (label, _) =
      label ≠ Nothing ∧ sym ≡ fromJust label
  -- func x = S.map (fst . (closure' memoize acc' nfa))
memoMap :: tbl → (tbl → a → (b, tbl)) → [a] → ((tbl), [b])
memoMap = memoMap' [] where
  memoMap' acc m _ [] = (m, acc)
  memoMap' acc m f (x : xs) = memoMap' (a : acc) m' f xs where
    (a, m') = f m x

instance Constructable (S.Set Int) where
  closure nfa states = concatMap' (closure nfa) states
  move nfa sym states = concatMap' (move nfa sym) states
concatMap' :: (Ord a, Ord b) ⇒
  (a → S.Set b) → S.Set a → S.Set b
concatMap' f = S.unions ∘ S.toList ∘ S.map f
simpleNFA :: NFA' Char
simpleNFA = NFA' alpha trans accept st where

```

```

    alpha = S.empty
    accept = S.fromList [0]
    st     = 0
    trans  = M.fromList [(0, trans0), (1, trans1)] where
        trans0 = S.fromList [(Nothing, 1)]
        trans1 = S.fromList [(Nothing, 0)]

testNFA :: NFA' Char
testNFA = NFA' alpha trans accept st where
    alpha = S.empty
    accept = S.fromList [0, 1]
    st     = 0
    trans  = M.fromList [(0, trans0), (1, trans1), (2, trans2)] where
        trans0 = S.fromList [(Nothing, 1), (Nothing, 2)]
        trans1 = S.fromList [(Nothing, 2), (Nothing, 0)]
        trans2 = S.fromList [(Nothing, 0), (Nothing, 1)]

testNFA' :: NFA' Char
testNFA' = NFA' alpha trans accept st where
    alpha = S.fromList "a"
    accept = S.fromList [0, 1]
    st     = 0
    trans  = M.fromList [(0, trans0), (1, trans1), (2, trans2)] where
        trans0 = S.fromList [(Nothing, 1), (Just 'a', 1), (Just 'a', 2)]
        trans1 = S.fromList [(Just 'a', 2), (Just 'a', 0)]
        trans2 = S.fromList [(Just 'a', 0), (Just 'a', 1)]

```

### 4.3 Hopcroft's Algorithm

In this module we provide our solution for minimizing a given deterministic finite state automaton.

We followed the algorithm given on page 30 of *Basics of Compiler Design*.

```

module Hopcroft (hopcroft) where
import FiniteStateAutomata (FSA (..), DFA' (..))
import Data.Maybe (fromJust, isJust, isNothing)
import qualified Data.Map as M
import qualified Data.Set as S
hopcroft :: (Ord a, Show a) => DFA' a -> DFA' a

```

```

hopcroft dfa = hopcroft' (dropUnreachable dfa)
                parts partMap where
    accept'      = accepting dfa
    notAccept    = S.difference (states dfa) accept'
    parts        = S.fromList [accept', notAccept]
    partMap      = toPartitionMap parts
hopcroft' :: (Ord a, Show a) =>
    DFA' a → S.Set (S.Set Int) →
    M.Map Int Int → DFA' a
hopcroft' dfa set eqMap =
    if done then dfa' else recurse where
    done          = consistent' ≡ S.empty
    consistent'   = consistent dfa eqMap ∘ S.toList $ set
    dfa'          = buildDFA dfa eqMap
    recurse       = hopcroft' dfa set' eqMap' where
        set'      = S.union (S.delete consistent' set)
        (partition dfa eqMap consistent')
    eqMap'        = toPartitionMap set'
consistent :: (Ord a, Show a) =>
    DFA' a → M.Map Int Int →
    [S.Set Int] → S.Set Int
consistent _ _ [] = S.empty
consistent dfa eqMap (s:ss') =
    if continue then recurse else s where
    continue = (isConsistent dfa eqMap (S.toList s))
    recurse  = consistent dfa eqMap ss'
buildDFA :: (Ord a, Show a) => DFA' a →
    M.Map Int Int → DFA' a
buildDFA dfa eqMap = DFA' alphabet' ss' accept' st' where
    alphabet'    = alphabet dfa
    ss'          = M.fromList oldStates
    accept'      = S.map lookup' (accepting dfa)
    st'          = lookup' (start dfa)
    newStates    = S.toList ∘ S.fromList ∘ M.elems $ eqMap
    oldStates     = zip newStates ∘
        map (updateState dfa eqMap) ∘ map check $ newStates
    check ns      = M.keys ∘ M.filter (≡ ns) $ eqMap

```

```

lookup'          = (eqMapM.!)
updateState :: (Ord a, Show a) =>
  DFA' a → M.Map Int Int →
  [Int] → M.Map a Int
updateState dfa eqMap oldStates = update where
  update = M.map (eqMapM.!) ∘
    M.unions ∘ map fromJust ∘
    filter isJust ∘ map lookup' $ oldStates
  lookup' = flip M.lookup (trans dfa)

-- Builds a partition map for equivalence look up
toPartitionMap :: S.Set (S.Set Int) → M.Map Int Int
toPartitionMap = toPartitionMap' 0 M.empty ∘ S.toList
where
  toPartitionMap' _ acc [] = acc
  toPartitionMap' next acc (s : ss') =
    toPartitionMap' (next + 1) acc' ss' where
      acc' = S.fold insert acc s
      insert = flip M.insert next

-- Partitions a given equivalence group
partition :: (Ord a, Show a) => DFA' a →
  M.Map Int Int → S.Set Int → S.Set (S.Set Int)
partition dfa parts toPart =
  partition' S.empty dfa parts (S.toList toPart)
where
  partition' acc _ _ [] = acc
  partition' acc dfa parts (s : ss) =
    partition' acc' dfa parts ss' where
      acc' = S.insert set acc
      sMap = eqMap s
      matches = filter ((sMap ≡) ∘ eqMap) ss
      set = S.fromList (s : matches)
      ss' = filter elems ss
      elems x = ¬ (S.member x set)
      eqMap x = eqMap' where
        map' = M.lookup x (trans dfa)
        eqMap' =
          if isNothing map' then

```

```

        M.empty
    else
        equivalenceMap parts ◦ fromJust $ map'
-- Determines if a set of states all have the same edges
isConsistent :: (Ord a, Show a) =>
    DFA' a → M.Map Int Int → [Int] → Bool
isConsistent _ _ [] = True
isConsistent dfa partitions (s:ss) =
    isConsistent' dfa partitions eqMap ss where
    map = M.lookup s (trans dfa)
    eqMap =
        if isNothing map then
            M.empty
        else
            equivalenceMap partitions ◦ fromJust $ map
equivalenceMap :: M.Map Int Int →
    M.Map a Int → M.Map a Int
equivalenceMap partitions map' =
    M.mapWithKey updateKey map' where
    updateKey _ v = partitionsM. ! v
isConsistent' :: (Ord a, Show a) =>
    DFA' a → M.Map Int Int →
    M.Map a Int → [Int] → Bool
isConsistent' _ _ _ [] = True
isConsistent' dfa partitions eqMap (s:ss') =
    if consistent' then
        recurse
    else
        False where
    consistent' = map' ≡ eqMap
    mMap = M.lookup s (trans dfa)
    map' =
        if isNothing mMap then
            M.empty
        else equivalenceMap partitions ◦ fromJust $ mMap
    recurse = isConsistent' dfa partitions eqMap ss'
-- Removes all unreachable states in a DFA'

```



```

dropUnreachable :: (Ord a, Show a) => DFA' a -> DFA' a
dropUnreachable dfa = dropUnreachable' set set dfa where
    set = S.singleton $ start dfa
dropUnreachable' :: (Ord a, Show a) =>
    S.Set Int -> S.Set Int -> DFA' a -> DFA' a
dropUnreachable' reachable_states new_states dfa =
    if done then dfa' else recurse where
        reachable' =
            S.unions o S.toList o S.map (reachable dfa) $ new_states
        new_states' =
            S.difference reachable' reachable_states
        reachable_states' =
            S.union reachable_states new_states'
        recurse =
            dropUnreachable' reachable_states' new_states' dfa
        dfa' =
            updateDFA dfa reachable_states'
        done = new_states' == S.empty
updateDFA :: (Ord a, Show a) =>
    DFA' a -> S.Set Int -> DFA' a
updateDFA dfa reachable_states =
    DFA' alphabet' trans' accept' start' where
        unreachable_states =
            S.difference (states dfa) reachable_states
        accept' =
            S.difference (accepting dfa) unreachable_states
        alphabet' = alphabet dfa
        start' = start dfa
        trans' = M.filterWithKey removeKey (trans dfa)
        removeKey k _ = S.member k reachable_states
reachable :: (Ord a, Show a) => DFA' a -> Int -> S.Set Int
reachable fsa state = S.fromList ns where
    trans' = M.lookup state (trans fsa)
    ns = if isNothing trans' then [] else ns'
    ns' = M.elems o fromJust $ trans'
-- A test DFA that has several unreachable states: [3,4,5,6]
testDFA :: DFA' Char

```

```

testDFA = DFA' alpha' ss' accept' st' where
  alpha' = S.fromList "ab"
  ss'    =
    M.fromList [(0,trans0),
                (1,trans1),
                (2,trans2),
                (3,trans3)]
  trans0 = M.fromList [( 'a' ,1), ( 'b' ,2)]
  trans1 = M.empty
  trans2 = M.empty
  trans3 = M.fromList [( 'a' ,4), ( 'b' ,5)]
  accept' = S.fromList [1,2,3,6]
  st'     = 0

-- Tests the removal of unreachable states
testDroppable :: Bool
testDroppable = alphabet' ∧ states'
                ∧ start' ∧ accepting' where
  alphabet' = (alphabet dfa) ≡ (S.fromList "ab")
  states'   = (states dfa) ≡ (S.fromList [0,1,2])
  start'    = (start dfa) ≡ 0
  accepting' = (accepting dfa) ≡ (S.fromList [1,2])
  dfa       = dropUnreachable testDFA

-- A test DFA that can be reduced
-- to a single node with two edges
-- it recognizes strings of the language (a|b)*
testDFA' :: DFA' Char
testDFA' = DFA' alpha' ss' accept' st' where
  alpha' = S.fromList "ab"
  ss'    = M.fromList
    [(0,trans'),
     (1,trans'),
     (2,trans')]
  trans' = M.fromList [( 'a' ,1), ( 'b' ,2)]
  accept' = S.fromList [0,1,2]
  st'     = 0

-- Tests that hopcroft reduces testDFA' to a minimal dfa
testHopcroft :: Bool

```

```

testHopcroft = alphabet' ∧ states'
               ∧ accepting' ∧ trans' where
alphabet'      = (alphabet dfa) ≡ (S.fromList "ab")
states'        = (states dfa) ≡ (S.fromList [start'])
start'         = (start dfa)
accepting'     = (accepting dfa) ≡ (S.fromList [start'])
trans'         = (trans dfa) ≡ (M.fromList [(start', trans0)])
trans0         = M.fromList [('a', start'), ('b', start')]
dfa           = hopcroft testDFA'

testPartition :: Bool
testPartition = partition' ≡ correctPartition where
partition' = partition dfa parts toPart
correctPartition = S.fromList [s1, s2, s3]
s1          = S.fromList [1, 2, 5]
s2          = S.fromList [3]
s3          = S.fromList [4, 7]
parts       = M.fromList
              [(0, 0), (6, 0),
               (1, 1), (2, 1),
               (3, 1), (4, 1),
               (5, 1), (7, 1)]
toPart      = S.fromList [1, 2, 3, 4, 5, 7]
dfa         = nonMinimalDFA

nonMinimalDFA :: DFA' Char
nonMinimalDFA = DFA' alpha' ss' accept' st' where
alpha' = S.fromList "ab"
ss'    = M.fromList
        [(0, trans0), (1, trans1), (2, trans2),
         (3, trans3), (4, trans4), (5, trans5),
         (6, trans6), (7, trans7)]
trans0 = M.fromList [('a', 1)]
trans1 = M.fromList [('a', 4), ('b', 2)]
trans2 = M.fromList [('a', 3), ('b', 5)]
trans3 = M.fromList [('b', 1)]
trans4 = M.fromList [('a', 6), ('b', 5)]
trans5 = M.fromList [('a', 7), ('b', 2)]
trans6 = M.fromList [('a', 5)]

```

```

trans7 = M.fromList [('a',0),('b',5)]
accept' = S.fromList [0,6]
st'      = 0

```

#### 4.4 Recognize a string for a given DFA

In this module we test whether a “string” from an alphabet for a DFA is accepted by that DFA or not. It also includes the function `tokenize` which is utilized by the generated scanner in tokenizing a string for a particular lexical description.

```

module Recognize (match, match', tokenize) where
import FiniteStateAutomata
import qualified Data.Map as M
import qualified Data.Set as S
import Data.Maybe

```

The function `match` takes an  $\alpha$  DFA and list of  $\alpha$  as input (a “string” in the language of that DFA), and returns true if the string is accepted by that DFA, and false otherwise. It is fairly straightforward.

```

match :: (Ord a, Show a) => DFA' a -> [a] -> Bool
match dfa = match' dfa (start dfa) where
  match' dfa curr [] = S.member curr (accepting dfa)
  match' dfa curr (c : cs) =
    let labelMap = M.lookup curr (trans dfa) in
    case labelMap of
      Nothing -> False
      Just map -> let labels = M.lookup c map in
        case labels of
          Nothing -> False
          Just next -> match' dfa next cs
match' :: (Ord a, Show a) =>
  DFA' a -> a -> (Bool, Maybe (DFA' a))
match' dfa@(DFA' alpha ss accept st) sym =
  (isAccepting, dfa') where
    curr = start dfa
    lookup = M.lookup curr (trans dfa)

```

```

nextStart =
  if isNothing lookup then
    Nothing
  else
    M.lookup sym (fromJust lookup)
dfa' =
  if isNothing nextStart then
    Nothing
  else
    Just (DFA' alpha ss accept (fromJust nextStart))
isAccepting =
  if isNothing nextStart then
    False
  else
    S.member (fromJust nextStart) (accepting dfa)

```

The second function *tokenize* matches a dfa against a string, and produces a token if possible, as required for the final generated scanner.

```

type Match a = (Int, [a], [a])
tokenize :: (Ord a, Show a) =>
  [a] -> DFA' a -> (Int, [a], [a])
tokenize toScan dfa =
  tokenize' (0, [], toScan) (0, [], toScan) dfa toScan where
    tokenize' :: (Ord a, Show a) =>
      Match a -> Match a -> DFA' a -> [a] -> (Int, [a], [a])
    tokenize' (consumed, token, rem) _ _ [] =
      (consumed, reverse token, rem)
    tokenize' currentMatch candidate dfa (x : xs) =
      if done then
        finalize currentMatch
      else recurse where
        done = isNothing dfa'
        (consumed, acc, _) = candidate
        (matches, dfa') = match' dfa x
        acc' = (x : acc)
        consumed' = consumed + 1
        candidate' = (consumed', acc', xs)
        currentMatch' =

```

```

    if matches then
        candidate'
    else
        currentMatch
recurse = tokenize' currentMatch'
candidate' (fromJust dfa') xs
finalize (c,t,m) = (c,reverse t,m)

```

## 5 Alphabet

This module provides functions for lexing and parsing alphabets found in input files, in addition to an alphabet token data structure.

```

module Alphabet (parseElement,
                 parseAlphabet,
                 getAlphabet,
                 gotoGetAlphabet) where

import Data.List
import Parselib
import GHC.Unicode (isPrint)
import Data.Char (ord)

```

A formal description of an alphabet is:

```

Alphabet -> alphabet Elements end;
Elements -> 'Subset_ascii
Elements -> Elements
Subset_ascii ->
    a|b|c|d|e|f|g|h|i|j|k|l|m|n|o|p|q|r|s|t|u|v|
    w|x|y|z|A|B|C|D|E|F|G|H|I|J|K|L|M|N|O|P|Q|R|S|
    T|U|V|W|X|Y|Z|\n|\t|\r| |+|-|=|_|)|(|*|&|^|%|$|
    #|@|!|~|`|\"'|;|:|/|?|.|>|,<|||{|}|{||\0|1|2|
    3|4|5|6|7|8|9|\a\b\v\f\r

```

The Haskell version of this might be written as follows:

```

data Alphabet =
    AlphabetToken |

```

```

Symbol Char |
EndToken deriving (Show, Eq)

```

The remaining functions find an alphabet in a file, tokenize, and generate a list of the symbols in the alphabet.

```

gotoAlphabet [] = []
gotoAlphabet cs | isPrefixOf "alphabet" cs = cs
gotoAlphabet (c:cs) = gotoAlphabet cs

-- old scanner
scanAlphabet [] = []
scanAlphabet ('a': 'l': 'p': 'h': 'a': 'b': 'e': 't': cs) =
    AlphabetToken : scanAlphabet cs
scanAlphabet ('\" : c:cs) =
    Symbol c : scanAlphabet cs
scanAlphabet ('e': 'n': 'd': cs) =
    [EndToken]
scanAlphabet (_:cs) =
    scanAlphabet cs

-- old parser
parseAlphabet' [] = []
parseAlphabet' (AlphabetToken : ts) =
    parseAlphabet' ts
parseAlphabet' (Symbol c : ts) =
    c : parseAlphabet' ts
parseAlphabet' (EndToken : ts) =
    []
getAlphabet' = parseAlphabet' o scanAlphabet o gotoAlphabet

-- this was not a fun bug to track down
parseEscapedChar =
    do {string "\\n"; return ' \n' }
    ++ do {string "\\t"; return ' \t' }
    ++ do {string "\\v"; return ' \v' }
    ++ do {string "\\r"; return ' \r' }
    ++ do {string "\\b"; return ' \b' }
    ++ do {string "\\a"; return ' \a' }
    ++ do {string "\\f"; return ' \f' }
    ++ do {string "\\\"; return ' \\' }

```

```

printablePlus char =
  let ascii = ord char in
    (ascii ≥ 7 ∧ ascii ≤ 13)
    ∨ (ascii ≥ 32 ∧ ascii ≤ 126)
parseElement :: Parser Char
parseElement = do
  space
  char ' \'
  c ←
    parseEscapedChar +++
    sat printablePlus
  return c
parseAlphabet :: Parser [Char]
parseAlphabet = do
  space
  string "alphabet"
  alphabet ← many parseElement
  space
  string "end;" +++ string "end" -- need because test file
  return alphabet
getAlphabet file =
  case (parse parseAlphabet) file of
    [] → error "Alphabet is empty (no alphabet provided)."
    regex → (fst ∘ head) regex
  -- to skip beginning contents and read alphabet
gotoGetAlphabet file =
  case (parse parseAlphabet) (gotoAlphabet file) of
    [] → error "Alphabet is empty (no alphabet provided)."
    regex → (fst ∘ head) regex

```

## 6 Input

Similar to the Algorithms module, in this module we gather all of our solutions for problems 5-8, which deals with file input/output.

Module *ParseFSA* parses either DFAs or FSAs from text file descriptions; *ParseReg* parses regular expressions from text files (with an alphabet)



and tests whether symbols occurring in the regular expression are elements of the alphabet provided in the file; and lastly *ParseLang* provides a data structure for lexical descriptions, reads in a complete lexical description from a text file, and transforms it into our internal representation, for use with the algorithms in the *Algorithms* module.

```
module Input (  
    module ParseFSA,  
    module ParseReg,  
    module ParseLang) where  
  
import ParseFSA  
import ParseReg  
import ParseLang
```

## 6.1 Parse a Regular Expression

This module inputs, lexes, and parses a regular expression from a text file. It uses Hutton's Parselib library.

Parsing is divided into a function for each regular expression. It handles ascii spaces, newlines, tabs, etc. In other words, the printable subset of ascii, as required by the spec.

It uses the functions provided by the *Alphabet* module to lex elements from the alphabet properly (escapes, newlines, etc.), and additionally, correctly error checks whether a terminal symbol is an element of the alphabet provided in either a regular expression file or a lexical description.

```
module ParseReg (getRegex, parseRegex) where  
  
import Alphabet  
import Regex  
  
import Parselib  
  
type Alphabet = [Char]  
parseAlt :: Alphabet → Parser (Regex Char)  
parseAlt alphabet = do  
    string " | "  
    space  
    regex ← parseRegex alphabet  
    space
```

```

    regex' ← parseRegex alphabet
    return (Alt regex regex')
parseConcat :: Alphabet → Parser (Regex Char)
parseConcat alphabet = do
    string "+"
    space
    regex ← parseRegex alphabet
    space
    regex' ← parseRegex alphabet
    return (Concat regex regex')
parseKleene :: Alphabet → Parser (Regex Char)
parseKleene alphabet = do
    string "*"
    space
    regex ← parseRegex alphabet
    return (Kleene regex)
parseTerm :: Alphabet → Parser (Regex Char)
parseTerm alphabet = do
    c ← parseElement
    if ¬ (elem c alphabet) then
        let msg = "Regular expression contains terminal "
            ++ show c
            ++ " which is not an element of the"
            ++ " alphabet provided." in
            error msg
    else
        return (Term c)
parseRegex :: Alphabet → Parser (Regex Char)
parseRegex alphabet = do
    space
    parseAlt alphabet + + +
    parseConcat alphabet + + +
    parseKleene alphabet + + +
    parseTerm alphabet
-- takes an alphabet
getRegex :: String → Alphabet → Regex Char
getRegex file alphabet =

```

```

case (parse (parseRegex alphabet)) file of
  [] → error "Could not parse regular expression."
  regex → (fst ∘ head) regex
-- example, should error
readRegex1 = do
  source ← readFile "regexp3.txt"
  -- get alphabet before, because alphabet is after
  let alphabet = gotoGetAlphabet source
  let regex = getRegex source alphabet
  putStrLn $ show regex
readRegex file = do
  source ← readFile file
  let alphabet = gotoGetAlphabet source
  let regex = getRegex source alphabet
  putStrLn $ show regex

```

## 6.2 Parse an FSA

In this module we parse a description of an DFA or an NFA and return the appropriate data structure.

Since the formal definition of a lexical description of a language does not contain a description of an NFA or a DFA (only regular expressions), this module was simply used on the provided test cases, and for a basic sanity check on whether our implementation for NFAs and DFAs was correct.

It uses Haskell's Parsec library for parsing.

```

{-# LANGUAGE FlexibleContexts #-}
module ParseFSA (parseNFA, parseDFA) where

import Data.Functor
import qualified Data.Set as S
import qualified Data.Map as M
import FiniteStateAutomata
import Text.Parsec

data Transition = NFAT {fromState :: String,
  symbols :: [Char],
  toState :: String}

```

```

    | DFAT {fromState :: String,
           symbol :: Char,
           toState :: String}

instance Show Transition where
    show (NFAT f ss t) = "NFAT " ++ f ++ " " ++ (show ss) ++ " -> " ++ t
    show (DFAT f s t) = "DFAT " ++ f ++ " " ++ (show s) ++ " -> " ++ t

data Description = Description {states' :: [String],
                                startState :: String,
                                acceptStates :: [String],
                                trans' :: [Transition]} deriving Show

parseNFA :: [Char] → String → NFA' Char
parseNFA = parseFSA "nfa" (NFA') (toNFAMap)

parseDFA :: [Char] → String → DFA' Char
parseDFA = parseFSA "dfa" (DFA') (toDFAMap)

parseFSA typ constr toMap alpha s =
    case parse (description typ isNFA) "Syntax Error" of
        Left er → error ◦ show $ er
        Right desc → convertToFSA alpha desc constr toMap
    where isNFA = if typ ≡ "nfa" then True else False

convertToFSA :: FSA f ⇒ [Alpha f] → Description →
    (S.Set (Alpha f) → M.Map Int (FSAVal f) → S.Set Int → Int → f) →
    (M.Map String Int → [Transition] → M.Map Int (FSAVal f)) →
    f

convertToFSA alpha desc const toMap = const alphabet nfaMap accepting start where
    normal = M.fromList $ zip (states' desc) [0..]
    alphabet = S.fromList alpha
    nfaMap = (toMap normal) ◦ trans' $ desc
    accepting = S.fromList ◦ map (normalM.!) ◦ acceptStates $ desc
    start = normalM.!(startState desc)

toNFAMap :: M.Map String Int → [Transition] → NFAMap Char
toNFAMap m ts = M.fromList ◦ map convert ◦ M.toList ◦ go ts $ M.empty where
    convert (s, es) = (mM.!(s), S.fromList ◦ map (λ(c, s2) → (c, mM.!(s2))) $ es)
    toM "" = [Nothing]
    toM s = map Just s
    go [] acc = acc
    go ((NFAT f syms t) : ts) acc = case M.lookup f acc of

```

```

    Nothing → go ts $ M.insert f (zip (toM syms) (repeat t)) acc
    Just es → go ts $ M.insert f ((zip (toM syms) (repeat t)) ++ es) acc
toDFAMap :: M.Map String Int → [Transition] → DFAMap Char
toDFAMap m ts = M.fromList ∘ map convert ∘ M.toList ∘ go ts $ M.empty where
    convert (s, es) = (mM.!s, M.fromList ∘ map (λ(c, s2) → (c, mM.!s2)) $ es)
    go [] acc = acc
    go ((DFAT f symb t) : ts) acc = case M.lookup f acc of
        Nothing → go ts $ M.insert f [(symb, t)] acc
        Just es → go ts $ M.insert f ((symb, t) : es) acc
description :: Stream s m Char ⇒
    String →
    Bool →
    ParsecT s u m Description
description keyword isNFA = do
    spaces >> string keyword >> spaces
    stats ← statelist "states" "end; " identifier
    initState ← initialState "initial"
    acceptStates ← statelist "accept" "end; " identifier
    trans ← statelist "transitions" "end; " (transition isNFA)
    return $ Description stats initState acceptStates trans
transition :: Stream s m Char ⇒
    Bool →
    ParsecT s u m Transition
transition isNFA = do
    from ← identifier
    syms ← option [] symbolList
    string "->" >> spaces
    to ← identifier
    return $ case isNFA of
        True → NFAT from syms to
        False → DFAT from (head syms) to
initialState :: Stream s m Char ⇒ String → ParsecT s u m String
initialState keyword = string keyword >> spaces >> identifier
parseStringOrTerm :: Stream s m Char ⇒ String →
    ParsecT s u m a →
    ParsecT s u m (Either String a)
parseStringOrTerm term s = do

```

```

    ter ← try $ optionMaybe $ string term
case ter of
    Just t → return $ Left t
    Nothing → Right < $ > s
statelist :: Stream s m Char ⇒
String →
String →
ParsecT s u m a →
ParsecT s u m [a]
statelist startTok endTok elem = do
    string startTok >> spaces
    reverse < $ > parseSets' [] where
        parseSets' acc = do
            sOrT ← parseStringOrTerm endTok elem
            spaces
            case sOrT of
                Left _ → return acc
                Right str → parseSets' $ str : acc
identifier :: Stream s m Char ⇒ ParsecT s u m String
identifier = do
    i ← many1 alphaNum
    spaces
    return i
sym :: Stream s m Char ⇒ ParsecT s u m Char
sym = do
    char ' \'
    c ← anyChar
    case c of
        ' \' → do
            c2 ← anyChar
            return $ read $ "' \' " ++ [c2] ++ "' "
        _ → return c
symbolList :: Stream s m Char ⇒ ParsecT s u m [Char]
symbolList = sym 'sepEndBy1' (spaces)

```

### 6.3 Parse a Lexical Description of a Programming Language

In this module we parse a lexical description of a language, and prepare it for parsing with respect to our previous data structures and algorithms.

It also uses Hutton's Parselib.

```
{-# LANGUAGE TypeFamilies, FlexibleContexts, FlexibleInstances #-}
module ParseLang where
import Parselib
import Regex
import ParseReg
import FiniteStateAutomata
import Alphabet
import Data.Char (isSpace)
import Data.List (intersperse)
```

We use a data structure *Desc* to internally represent a lexical description. *Desc* is a basic record type, with three functions, *language*, *symbols*, and *classes* which return the name of the language as a string, the alphabet, and a list of classes given by the lexical description, respectively.

The data structure *Class* is another record type with three functions, *name*, *regex*, and *relevance*, which return the name of the class, the regular expression which describes it, and its semantic relevance, respectively.

Thus to obtain an NFA equivalent of the regular expression for the first class given in a parsed lexical description *l*, we write:  $(thompson \circ regex \circ head \circ classes) \, l$ .

```
type Identifier = String
data Relevance = Relevant | Irrelevant | Discard deriving (Eq, Show)
data Class = Class {
  name :: Identifier,
  regex :: Regex Char,
  relevance :: Relevance} deriving Eq
instance Show Class where
  show c = "class " ++ name c ++ " " ++
    show (regex c) ++ " " ++
    show (relevance c) ++
    " end; "
```

```

data Desc = Desc {
    language :: String,
    symbols :: [Char],
    classes :: [Class]
}

showAlphabet a = "' " ++ (intersperse ' \' a)

instance Show Desc where
    show desc =
        "language: " ++ language desc ++ "\n" ++
        "alphabet: " ++
        showAlphabet (symbols desc) ++
        " end; " ++ "\n" ++
        "classes: " ++ "\n" ++
        unlines (map show (classes desc)) ++
        " end; "

```

The remaining functions parse a text file of a lexical description, and deposit that description (if it is well-formed) into our data structure.

```

parseLangIdentifier :: Parser String
parseLangIdentifier = do
    ident ← many $ sat (¬ ∘ isSpace)
    return ident

parseRelevance :: Parser Relevance
parseRelevance =
    do {string "relevant"; return Relevant} +++
    do {string "irrelevant"; return Irrelevant} +++
    do {string "discard" ; return Discard}

parseClass :: [Char] → Parser Class
parseClass alphabet = do
    space
    string "class"
    space
    name ← parseLangIdentifier
    space
    string "is"
    regex ← parseRegex alphabet
    space

```



```

    relevance ← parseRelevance
    space
    string "end; "
    return $ Class name regex relevance
parseLang :: Parser Desc
parseLang = do
    space
    string "language"
    space
    language ← parseLangIdentifier
    alphabet ← parseAlphabet
    classes ← many $ parseClass alphabet
    space
    string "end; "
    return (Desc language alphabet classes)
getLang :: String → Desc
getLang desc = do
    case (parse parseLang) desc of
        [] → error "Could not parse lexical description."
        regex → (fst ∘ head) regex
    -- example
readLang1 = do
    source ← readFile "tests/lexdesc3.txt"
    let x = (parse parseLang) source
    putStrLn $ show x
readLang file = do
    source ← readFile file
    let x = (parse parseLang) source
    putStrLn $ show x

```

## 6.4 Scanner Generator

This module performs the work necessary to output a scanner, thus making our implementation a scanner *generator*.

From a given lexical description, we collect all the regular expressions, and then for each, we apply Thompson's algorithm, generate a dfa from

the nfa (subset construction), and finally apply Hopcroft's minimization algorithm.

We then construct a Haskell module, which when suitably compiled with a parser, will accept and tokenize only those strings given by the original language description. I.e., the scanner when imported as a module provides a function *scan* whose type is: *scan* :: *String* → [*Token*]

```
module ScannerGenerator (scannerGenerator) where
import Regex
import Algorithms
import Input
import Data.List (intersperse)
import System.Environment (getArgs)
import Data.Char (toUpper)

alternate :: [Class] → Regex Char
alternate [] = Empty
alternate (c : []) = regex c
alternate (c : cs) =
    Alt (regex c) (alternate cs)

capitalize :: String → String
capitalize [] = []
capitalize (s : ss) = (toUpper s) : ss

writeImports :: String → String
writeImports moduleName = "module "
    ++ moduleName ++ " (scan) where \n" ++
    concat ["import FiniteStateAutomata(DFA'(..))\n",
        "import ParseLang(Relevance(..))\n",
        "import Recognize(tokenize)\n",
        "import Data.List(maximumBy,lookup)\n",
        "import Data.Maybe(fromJust)\n",
        "type Location = Int\n"]

writeClasses :: [Class] → String
writeClasses classes =
    "data Class = " ++ names ++ " deriving Show\n" where
    names = concat o intersperse
        " | " o map (capitalize o name) $ classes

writeTokens :: String
```

```

writeTokens = "data Token = Token " ++
  "{kind :: Class, relevance :: Relevance, " ++
  "location :: Location, token :: String}" ++
  " deriving Show\n"

writeDFA :: Class → String
writeDFA c = name' ++ " :: DFA' Char\n" ++
  name' ++ " = read \"" ++ dfa ++ "\"\n" where
  name' = name c
  dfa = replace ' ' "\\\" " o
  show o hopcroft o
  subsetConstruction o thompson o regex $ c

writeDFAs :: [Class] → String
writeDFAs cs = "dfas :: [DFA' Char]\n" ++
  "dfas = " ++ names ++ "\n" where
  names = replace ' ' "\" " o show o map name $ cs

writeConstructor :: Class → String
writeConstructor c = name' ++
  " :: Location -> String -> Token\n" ++
  name' ++ " = Token "
  ++ capName ++ " " ++ rel ++ "\n" where
  name' = name c ++ "' "
  capName = capitalize o name $ c
  rel = show o relevance $ c

writeConstructors :: [Class] → String
writeConstructors cs = "constructors :: " ++
  "[Location -> String -> Token]\n" ++
  "constructors = " ++ names ++ "\n" where
  names = replace ' ' "\" " o
  show o map ((+ "' ") o name) $ cs

writeScan = concat [
  "table :: [(DFA' Char, Location -> String -> Token)]\n",
  "table = zip dfas constructors\n",
  "getToken :: DFA' Char -> Location -> [Char] -> Token\n",
  "getToken dfa loc token = construct loc token where\n",
  "  construct = fromJust . lookup dfa $ table\n",
  "scan :: String -> [Token]\n",
  "scan = scan' [] where\n",

```

```

"  scan' :: [Token] -> String -> [Token]\n",
"  scan' acc s = " ++
"if done then reverse (t:acc) else reCURSE where\n",
"  reCURSE = if err then error \"Could not parse.\" ++
" else scan' (t:acc) rem\n",
"  done = rem == []\n",
"  err = consumed == 0\n",
"  list = zip dfas . map (tokenize s) $ dfas\n",
"  (dfa, (consumed, token, rem)) = " ++
"maximumBy compareTrip list\n",
"  t = getToken dfa consumed token\n",
"  compareTrip (_, (i,_,_)) (_, (i2,_,_)) = compare i i2"]
scannerGenerator :: String -> String -> String
scannerGenerator moduleName desc = program where
  (Desc _ _ classes) = getLang desc
  dfas = concatMap writeDFA classes
  constructors = concatMap writeConstructor classes
  program = writeImports moduleName ++
    writeClasses classes ++ writeTokens ++
    dfas ++ writeDFAs classes ++ constructors ++
    writeConstructors classes ++ writeScan
replace :: (Eq a) => a -> [a] -> [a] -> [a]
replace a b = concatMap replace' where
  replace' x = if a == x then b else [x]

```

## 7 Module: Main.lhs

The final module, *Main*, puts everything together, by simply calling the function *scannerGenerator* on a lexical description to output a scanner *module* in Haskell source code.

```

module Main where
import System.Environment
import ScannerGenerator (scannerGenerator)
main = do
  [contents, moduleName] <- getArgs

```

```

file ← readFile contents
writeFile (moduleName ++ ".hs") ○
scannerGenerator moduleName $ file

```

Thus, given a lexical description for a language  $\mathcal{L}$  in a file `<desc.txt>`, a string in file `<string.txt>` (which may or may not be a string in the language  $\mathcal{L}$ ), and the binary `<gen>` compiled from our Haskell source code, the command `./gen desc.txt LexDesc` (in a GNU/Linux environment, for example) will produce a scanner module, `LexDesc.hs`, for  $\mathcal{L}$  which will generate tokens (if possible) from `<string.txt>`, for a suitable parser and *main* function.

Two demo binaries have been provided, `demo1` and `demo2`, which are scanners for the languages given in `lexdesc1.txt` and `lexdesc2.txt`, respectively.

The binaries simply take an ASCII text file as a command line argument, and print the tokens it consumes while reading the string in the file.

The binaries were compiled by simply importing different scanners, i.e., replacing `Scanner1` etc., in the following with the result of running our scanner generator on a lexical description:

```

module Main where
import Scanner1
import System.Environment
main = do
    [file] ← getArgs
    contents ← readFile file
    let tokens = scan contents
    putStrLn $ show tokens

```