CS454 Project 1: « Lexer Generator »

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1 Introduction

This is the final report for project 1, CS454, on lexical analysis.

Our first design decision was to use Haskell's literate mode to prepare all of our code. Secondly, we decided to use the distributed revision control software git for collaborative coding.

We decided to write each algorithm in the assignment as its own module, in addition to modules describing finite state automata (FSA) and regular expressions.

Lastly, we decided to write a lexer generator for our final output. That is, we parse a lexical description, and return a Haskell source file to be compiled. Once suitably compiled, the binary will accept text files which are accepted if and only if they are strings accepted by the language given in the lexical description.

2 Finite State Automaton

In this module we give our data structure for modelling a finite state automaton.

The formal definition of an FSA is a 5-tuple, where:

- 1. a finite set of states (Q)
- 2. a finite set of input symbols called the alphabet (Σ)
- 3. a transition function $(\delta: Q \times \Sigma \to Q)$

- 4. a start state $(q0 \in Q)$
- 5. a set of accept states $(F \subset Q)$

We tried to have our data structure mirror the mathematical definition of an FSA as closely as possible.

```
{-# LANGUAGE TypeFamilies, FlexibleContexts,FlexibleInstances #-}
module FiniteStateAutomata (
                              FSA (..),
                             NFA'(..),
                             NFAMap,
                              DFA'(..),
                              DFAMap,
                             epsilon, ppfsa) where
import qualified Data.Map as M
import qualified Data.Set as S
type DFAMap\ a = M.Map\ Int\ (M.Map\ a\ Int)
type NFAMap \ a = M.Map \ Int \ (S.Set \ (Maybe \ a, Int))
class (Show (Elem m)) \Rightarrow Listable m where
  type Elem m
  toList :: m \rightarrow [(Elem \ m, Int)]
instance (Show a) \Rightarrow Listable (M.Map a Int) where
  type Elem(M.Map\ a\ Int) = a
  toList = M.toList
instance (Show a) \Rightarrow Listable (S.Set (Maybe a, Int)) where
  type Elem (S.Set (Maybe\ a, Int)) = Maybe\ a
  toList = S.toList
class (Ord (Alpha f),
  Show (Alpha f),
  Show f,
  Show (FSAVal\ f),
  Listable (FSAVal\ f)) \Rightarrow FSA\ f where
  type Alpha f
  type FSAVal f
  alphabet :: (Ord (Alpha f), Show (Alpha f)) \Rightarrow
            f \rightarrow S.Set (Alpha f)
  accepting :: f \rightarrow S.Set Int
```

```
:: f \rightarrow Int
   start
           :: f \rightarrow M.Map Int (FSAVal f)
   trans
   states :: f \rightarrow S.Set Int
   states\ fsa = S.unions\ [(S.fromList \circ M.keys \circ trans\ \$\ fsa),
      (accepting fsa),
      (S.fromList \circ
     concatMap sndList ∘
     M.elems \circ trans \$ fsa)
sndList :: Listable \ m \Rightarrow m \rightarrow [Int]
sndList = map \ snd \circ toList
fsaShow :: (FSA f) \Rightarrow f \rightarrow String
fsaShow fsa = "{alphabet="
            ++ (show \circ S.toList \circ alphabet \$ fsa)
            #","#
           "states=" ++
           (show \circ S.toList \circ states \$ fsa) + "," +
           "start=" ++ (show o start $ fsa) ++ "," ++
            "accepting="
            ++ (show \circ S.toList \circ accepting \$ fsa)
            ++ "," ++ "trans="
            ++ (show \circ map (filter (\not\equiv """)) \circ
              showTransitions $ fsa)
pettyPrinter :: (FSA f) \Rightarrow f \rightarrow IO ()
pettyPrinter fsa = (putStr $ "alphabet="
   ++ (show \circ S.toList \circ alphabet \$ fsa)
   # "\n" #
   "states="
   ++ (show \circ S.toList \circ states \$ fsa)
   # "\n" #
   "start=" ++ (show \circ start \$ fsa)
   # "\n" #
   "accepting="
   ++ (show \circ S.toList \circ accepting \$ fsa)
   ++ "\n") \gg trans
         where trans =
           mapM\_(putStrLn \circ filter (\not\equiv """))
               $ showTransitions fsa
```

```
ppfsa :: (FSA f) \Rightarrow f \rightarrow IO ()
ppfsa = pettyPrinter
showTransitions :: (FSA f) \Rightarrow f \rightarrow [String]
showTransitions\ fsa=map\ showTransition\ \circ
  M.toList \circ trans \$ fsa  where
  showTransition (from, ts) = (show from)
     #"::"
     ++ (show \circ map \ show Transition' \circ to List \$ ts) \ \mathbf{where}
       showTransition'(x, to) = (show x) + " \rightarrow " + (show to)
data DFA' a = DFA' { alpha :: S.Set a,
                              :: DFAMap a,
  accept :: S.Set Int,
                              :: Int } deriving (Show, Read)
instance (Ord a, Show a) \Rightarrow FSA (DFA' a) where
  type Alpha (DFA'a) = a
  type FSAVal(DFA'a) = (M.Map\ a\ Int)
  alphabet = alpha
  accepting = accept
  start = st
  trans = ss
 {-instance (Ord a, Show a) => Show (DFA' a) where show dfa = "DFA" ++ (fsaShow dfa) -
data NFA' a = NFA' { nalpha :: S.Set a,
  nss
                                :: NFAMap a,
  naccept :: S.Set Int,
  nst
                                :: Int }
epsilon :: Maybe a
epsilon = Nothing
instance (Ord a, Show a) \Rightarrow FSA (NFA' a) where
  type Alpha (NFA'a) = a
  type FSAVal (NFA' a) = (S.Set (Maybe a, Int))
  alphabet = nalpha
  accepting = naccept
  start = nst
  trans = nss
instance (Ord a, Show a) \Rightarrow Show (NFA' a) where
  show nfa = "NFA" + (fsaShow nfa)
```

```
simpleNFA:: NFA' Char
simpleNFA = NFA' alpha states accepting start where
  alpha = S.fromList['a', 'b']
  states = M.fromList
     [(0, S.fromList [(Just 'a', 1)]),
          (1, S.fromList [(Just 'b', 0), (epsilon, 2)])]
  start = 0
  accepting = S.fromList [2]
simpleDFA:: DFA' Char
simpleDFA = DFA' alpha states accepting start where
  alpha = S.fromList['a', 'b', 'c']
  states = M.fromList
     [(0, M.fromList [('a', 1)]),
          (1, M. from List [('b', 0), ('c', 2)])]
  start = 0
  accepting = S.fromList [2]
deadStateDFA:: DFA' Char
deadStateDFA = DFA' alpha states accepting start where
  alpha = S.fromList "ab"
  states =
    M.fromList [(0, trans0), (1, trans1), (2, trans2)] where
       trans0 = M.fromList[('a',1),('b',2)]
       trans1 = M.fromList[('b',3)]
       trans2 = M.fromList[('a',3)]
  accepting = S.fromList [1,2]
  start = 0
```

3 Regular Expressions

In this module we give the haskell data type for a regular expression; the encoding almost exactly mirrors the definition given in the assignment.

```
{-# LANGUAGE TypeFamilies, FlexibleContexts,FlexibleInstances #-}

module Regex (Regex (..)) where

data Regex a = Alt (Regex a) (Regex a)

| Concat (Regex a) (Regex a)

| Kleene (Regex a)
```

```
| Term a
| Empty deriving Show
```

We wrote a pretty infix printer:

```
instance Show (Regex Char) where
    show (Alt r1 r2 ) =
        "(" ++ (show r1) ++ "|" ++ (show r2) ++ ")"
    show (Concat r1 r2) =
        "(" ++ (show r1) ++ "+" ++ (show r2) ++ ")"
    show (Kleene r1) = "(" ++ (show r1) ++ "*" ++ ")"
    show (Term c) = "\'':c:[]
    show (Empty) = "\\epsilon"
```

However, it was determined that writing a lexer generator would be easier if we used the default show for regular expressions.

4 Algorithms

Our solutions to the "in-memory" algorithms given in §1.2 have been modularized in the following way.

```
module Algorithms (module Thompson, module SubsetConstruction, module Hopcroft, module Recognize
) where import Thompson import SubsetConstruction import Hopcroft import Recognize
```

In this way we encapsulated (and named) the solutions individually, as the assignment requested.

4.1 Thompson's Algorithm

In this module we provide our solution for converting a regular expression to an NFA.

```
module Thompson (thompson) where import Prelude hiding (concat) import qualified Data.Set as S import qualified Data.Map as M import FiniteStateAutomata (FSA (trans), NFA' (..), epsilon) import Regex
```

The function *thompson* returns the result of converting a regular expression to a non-deterministic finite state automaton. It uses Thompson's algorithm for doing so.

```
thompson :: (Ord\ a, Show\ a) \Rightarrow Regex\ a \rightarrow NFA'\ a

thompson = fst \circ thompson' 0

thompson' :: (Ord\ a, Show\ a) \Rightarrow

Int \rightarrow Regex\ a \rightarrow (NFA'\ a, Int)

thompson' lab (Alt\ r1\ r2) = union\ lab'' fsa fsa' where

(fsa, lab') = thompson'\ lab\ r1

(fsa', lab'') = thompson'\ lab'\ r2

thompson' lab (Concat\ r1\ r2) = concat\ lab''\ fsa\ fsa'\ where

(fsa', lab'') = thompson'\ lab\ r1

(fsa', lab'') = thompson'\ lab'\ r2

thompson' lab (Kleene\ r1) = mrKleene\ lab'\ fsa\ where

(fsa, lab') = thompson'\ lab\ r1

thompson' lab (Term\ x) = symbol\ lab\ x

thompson' lab Empty = expression\ lab
```

The following functions individually convert particular regular expressions to their NFA equivalents. For example, *concat* takes two regular expressions, say a and b, and returns an NFA where the NFA corresponding to a's accepting states are now transitions to the NFA corresponding to b's start state.

The other functions perform similar operations, according to the algorithm.

```
expression :: (Ord\ a, Show\ a) \Rightarrow Int \rightarrow (NFA'\ a, Int)

expression label = (fsa, label + 2) where

fsa = NFA'\ S.empty\ (M.fromList\ [n1])

(S.singleton\ (label + 1))\ label

n1 = (label, S.singleton\ (epsilon, (label + 1)))
```

```
symbol :: (Ord\ a, Show\ a) \Rightarrow Int \rightarrow a \rightarrow (NFA'\ a, Int)
symbol\ label\ sym = (fsa, label + 2) where
  fsa = NFA' (S.singleton sym)
     (uncurry M.singleton n1) (S.singleton (label + 1)) label
  n1 = (label, S.singleton (Just sym, label + 1))
union :: (Ord a, Show a) \Rightarrow
  Int \rightarrow NFA' \ a \rightarrow NFA' \ a \rightarrow (NFA' \ a, Int)
union label nfa0 nfa1 = (fsa, label + 2) where
   (NFA' \ a0 \ m0 \ as0 \ st0) = updateAccepting [(label + 1)] \ nfa0
   (NFA' \ a1 \ m1 \ as1 \ st1) = updateAccepting [(label + 1)] \ nfa1
  fsa = NFA' alpha newMap (S.singleton (label + 1)) label
  alpha = S.union \ a0 \ a1
  newMap = M.unions [m0, m1, epsilonEdges]
  epsilonEdges =
     M.singleton label
        (S.fromList [(epsilon, st0), (epsilon, st1)])
concat :: (Ord \ a, Show \ a) \Rightarrow
  Int \rightarrow NFA' \ a \rightarrow NFA' \ a \rightarrow (NFA' \ a, Int)
concat label fsa0@(NFA' s0 m0 as0 st0) (NFA' s1 m1 as1 st1) =
   (fsa, label) where
  fsa = NFA' (S.union s0 s1) (M.union updated m1) as1 st0
  updated = trans $ updateAccepting [st1] fsa0
mrKleene :: (Ord\ a, Show\ a) \Rightarrow Int \rightarrow NFA'\ a \rightarrow (NFA'\ a, Int)
mrKleene\ label\ nfa@(NFA'\ a\ \_as\ st)=(fsa,label+2)\ \mathbf{where}
   (NFA' \_ m \_ \_) = updateAccepting [st, (label + 1)] nfa
  fsa = NFA' a m' (S.singleton (label + 1)) label
  m' = M.union m epsilons
  epsilons =
     M.singleton label
        (S.fromList [(epsilon, (label + 1)), (epsilon, st)])
  epsilons' = M.fromList \circ map func \circ S.toList \$ as
  func x = (x, S. singleton (epsilon, label + 1))
updateAccepting :: (Ord \ a) \Rightarrow [Int] \rightarrow NFA' \ a \rightarrow NFA' \ a
updateAccepting is nfa@(NFA' a ts as st) =
  NFA' a newTrans (S.empty) st where
     newTrans = M.union ts nts
     nts = M.fromList \circ map func \circ S.toList \$ as
```

```
func x = (x, S. fromList \circ map (\lambda i \rightarrow (epsilon, i)) \$ is)
```

4.2 Subset Construction

In this module we provide our solution for converting a given non-deterministic finite state automaton to an equivalent deterministic finite state automaton.

```
{-# LANGUAGE FlexibleInstances #-}
module SubsetConstruction (subsetConstruction) where
import Data.Maybe
import FiniteStateAutomata
import qualified Data. Map as M
import qualified Data.Set as S
import Debug.Trace
type LabelMap = M.Map (S.Set Int) Int
subsetConstruction :: (Ord a, Show a) \Rightarrow NFA' a \rightarrow DFA' a
subsetConstruction nfa =
     DFA' (alphabet nfa) dfamap' accept start' where
         start' = labelsM. ! startStateSet
         accept = findAccepting nfa labelmap
         (\_, labelmap, dfamap') =
            subsetConstruction' nfa next
              labels dfamap outSets
         startStateSet = closure nfa (start nfa)
          (labels, next) =
            labelSets 0 M.empty
            (S.fromList (startStateSet : outSets))
         edges = edgeMap labels edgeSet
         dfamap =
            M.singleton (labelsM.!startStateSet) edges
         outSets =
            map (closure' ∘ flip move' startStateSet)
                 alphabet'
         edgeSet = zip alphabet' outSets
         alphabet' = S.toList \circ alphabet \$ nfa
         closure' = closure nfa
```

```
move' = move nfa
findAccepting :: (Ord a, Show a) \Rightarrow
                   NFA' a \rightarrow LabelMap \rightarrow S.Set Int
findAccepting nfa labels = S.fromList sets where
  sets = M.elems (M.filterWithKey isAccepting labels)
  isAccepting label _ =
        S.empty \not\equiv (S.intersection \ accept \ label)
  accept = accepting nfa
subsetConstruction' :: (Ord \ a, Show \ a) \Rightarrow
  NFA' a \rightarrow Int \rightarrow LabelMap \rightarrow
  DFAMap \ a \rightarrow [S.Set \ Int] \rightarrow
  (Int, LabelMap, DFAMap a)
subsetConstruction' _ next labels dfamap [] =
     (next, labels, dfamap)
subsetConstruction' nfa next labels dfamap (s:ss) =
     case (s \equiv S.empty) of
  True \rightarrow subsetConstruction' nfa next labels dfamap ss
  False \rightarrow if done then continue else recursion where
     done = M.lookup (labelsM.!s) dfamap \not\equiv Nothing
     continue = subsetConstruction' nfa next labels dfamap ss
     recursion =
           subsetConstruction' nfa next" labels" dfamap" ss
      (next'', labels'', dfamap'') =
           subsetConstruction' nfa next' labels' dfamap' outSets
      (labels', next') =
           labelSets next labels (S.fromList outSets)
     dfamap' = M.insert (labelsM.!s) edges dfamap
     edges = edgeMap \ labels' \ edgeSet
     edgeSet = zip alphabet' outSets
     outSets = map (closure' \circ flip move' s) alphabet'
     alphabet' = S.toList \circ alphabet \$ nfa
     move' = move nfa
     closure' = closure nfa
labelSets :: Int \rightarrow M.Map (S.Set Int) Int \rightarrow
                S.Set (S.Set Int) \rightarrow
              (M.Map (S.Set Int) Int, Int)
labelSets next labels sets =
```

```
labelSets' next labels (S.toList sets)
labelSets' :: Int \rightarrow LabelMap \rightarrow
   [S.Set\ Int] \rightarrow (LabelMap, Int)
labelSets' next \ labels \ [\ ] = (labels, next)
labelSets' next labels (s:ss) =
  case (s \equiv S.empty) of
      True \rightarrow labelSets' next labels ss
     False \rightarrow
              if (M.member s labels) then
                 (labelSets' next labels ss)
              else
                 (labelSets' (next + 1)
                    (M.insert s next labels) ss)
edgeMap :: (Ord a, Show a) \Rightarrow
              M.Map (S.Set Int) Int \rightarrow
                 [(a, (S.Set\ Int))] \rightarrow M.Map\ a\ Int
edgeMap = edges' M.empty where
  edges' :: (Ord \ a, Show \ a) \Rightarrow
              M.Map \ a \ Int \rightarrow M.Map \ (S.Set \ Int) \ Int \rightarrow
              [(a, (S.Set\ Int))] \rightarrow M.Map\ a\ Int
  edges' acc _ [] = acc
  edges' acc labels ((alpha, set) : ss) =
        case (set \equiv S.empty) of
      True \rightarrow edges' \ acc \ labels \ ss
     False \rightarrow edges' \ acc' \ labels \ ss \ where
        acc' = M.insert alpha (labels M.! set) acc
class Constructable c where
  closure :: (Show a, Ord a) \Rightarrow NFA' a \rightarrow c \rightarrow S.Set Int
  move :: (Show a, Ord a) \Rightarrow NFA' a \rightarrow a \rightarrow c \rightarrow S.Set Int
instance Constructable Int where
  closure nfa state =
        fst ∘ closure' nfa (S.singleton state) M.empty $ state where
     closure' nfa acc memoize state =
        case (M.lookup (acc, state) memoize) of
           Nothing \rightarrow
              if done then (acc', memoize') else (acc'', memoize'') where
                 done = edges \equiv Nothing \lor eps \equiv S.singleton state
```

```
edges = M.lookup state \circ trans \$ nfa
                eps = S.union (S.singleton state)
                  (S.map \ snd \circ S.filter \ isEpsilon \circ
                     fromJust $ edges)
                eps' = S.difference eps acc
                isEpsilon\ (label,\_) = label \equiv epsilon
                acc' = S.union acc (S.singleton state)
                acc'' = S.union \ acc' \circ S.unions \$ sets
                memoize' = M.insert (acc, state) acc' memoize
                (memoize''', sets) = memoMap memoize (closure' nfa acc') ∘ S.toList $ eps'
                memoize" = M.insert (acc, state) acc" memoize"
          Just set \rightarrow (set, memoize)
  move nfa sym state =
     if (edges \equiv Nothing) then S.empty else eps where
     edges = M.lookup state \circ trans \$ nfa
     eps = S.map \ snd \circ S.filter \ isSym \circ fromJust \$ \ edges
     isSym (label, \_) =
          label \not\equiv Nothing \land sym \equiv from Just \ label
  -- func x = S.map (fst . (closure' memoize acc' nfa))
memoMap :: tbl \rightarrow (tbl \rightarrow a \rightarrow (b, tbl)) \rightarrow [a] \rightarrow ((tbl), [b])
memoMap = memoMap' [] where
  memoMap' acc m = [] = (m, acc)
  memoMap' acc m f (x:xs) = memoMap' (a:acc) m' f xs where
     (a, m') = f m x
instance Constructable (S.Set Int) where
  closure\ nfa\ states = concatMap'\ (closure\ nfa)\ states
  move nfa sym states = concatMap' (move nfa sym) states
concatMap' :: (Ord\ a, Ord\ b) \Rightarrow
  (a \rightarrow S.Set \ b) \rightarrow S.Set \ a \rightarrow S.Set \ b
concatMap' f = S.unions \circ S.toList \circ S.map f
simpleNFA :: NFA' Char
simpleNFA = NFA' alpha trans accept st where
  alpha = S.empty
  accept = S.fromList[0]
  st
          = 0
  trans = M.fromList [(0, trans0), (1, trans1)] where
```

```
trans0 = S.fromList [(Nothing, 1)]
    trans1 = S.fromList [(Nothing, 0)]
testNFA :: NFA' Char
testNFA = NFA' alpha trans accept st where
  alpha = S.empty
  accept = S.fromList[0,1]
  st
         = 0
  trans = M.fromList [(0, trans0), (1, trans1), (2, trans2)] where
    trans0 = S.fromList [(Nothing, 1), (Nothing, 2)]
    trans1 = S.fromList [(Nothing, 2), (Nothing, 0)]
    trans2 = S.fromList [(Nothing, 0), (Nothing, 1)]
testNFA' :: NFA' Char
testNFA' = NFA' alpha trans accept st where
  alpha = S.fromList "a"
  accept = S.fromList[0,1]
  trans = M.fromList[(0, trans0), (1, trans1), (2, trans2)] where
    trans0 = S.fromList [(Nothing, 1), (Just 'a', 1), (Just 'a', 2)]
    trans1 = S.fromList [(Just 'a', 2), (Just 'a', 0)]
    trans2 = S.fromList [(Just 'a', 0), (Just 'a', 1)]
```

5 Hopcroft's Algorithm

In this module we provide our solution for minimizing a given deterministic finite state automaton.

The pseudocode for this algorithm from https://en.wikipedia.org/wiki/DFA_minimization is as follows:

```
Y is nonempty do
                   replace Y in P by the
                    two sets X - Y and Y \setminus X
                   if Y is in W
                          replace Y in W by the same two sets
                   else
                          if |X
                                  Y | <= | Y \ X |
                                add X Y to W
                          else
                                add Y \ X to W
             end;
      end;
end;
    module Hopcroft (hopcroft) where
    import FiniteStateAutomata (FSA (..), DFA' (..))
    import Data.Maybe (from[ust, is[ust, isNothing)]
    import qualified Data.Map as M
    import qualified Data.Set as S
    hopcroft :: (Ord\ a, Show\ a) \Rightarrow DFA'\ a \rightarrow DFA'\ a
    hopcroft dfa = hopcroft' (dropUnreachable dfa)
                   parts partMap where
       accept'
                   = accepting dfa
       notAccept = S.difference (states dfa) accept'
       parts
                   = S.fromList [accept', notAccept]
       partMap
                   = toPartitionMap parts
    hopcroft' :: (Ord \ a, Show \ a) \Rightarrow
             DFA' \ a \rightarrow S.Set \ (S.Set \ Int) \rightarrow
                M.Map\ Int\ Int \rightarrow DFA'\ a
    hopcroft' dfa set eqMap =
             if done then dfa' else recurse where
       done
                        = consistent' \equiv S.empty
       consistent' = consistent \ dfa \ eqMap \circ S.toList \$ set
                        = buildDFA dfa eqMap
       dfa'
       recurse
                        = hopcroft' dfa set' eqMap' where
            set' = S.union (S.delete consistent' set)
              (partition dfa eqMap consistent')
```

```
eqMap' = toPartitionMap set'
consistent :: (Ord \ a, Show \ a) \Rightarrow
           DFA' a \rightarrow M.Map Int Int \rightarrow
            [S.Set\ Int] \rightarrow S.Set\ Int
consistent \_ \_ [] = S.empty
consistent dfa eqMap (s:ss') =
            if continue then recurse else s where
  continue = (isConsistent dfa eqMap (S.toList s))
  recurse = consistent dfa eqMap ss'
buildDFA :: (Ord a, Show a) \Rightarrow DFA' a \rightarrow
         M.Map\ Int\ Int \rightarrow DFA'\ a
buildDFA dfa eqMap = DFA' alphabet' ss' accept' st' where
  alphabet'
                    = alphabet dfa
  ss'
                    = M.fromList oldStates
                    = S.map lookup' (accepting dfa)
  accept'
  st'
                    = lookup' (start dfa)
  newStates
                    = S.toList \circ S.fromList \circ M.elems \$ eqMap
  oldStates
                    = zip newStates \circ
     map (updateState dfa eqMap) ∘ map check $ newStates
  check ns
                    = M.keys \circ M.filter (\equiv ns) \$ eqMap
  lookup'
                       = (eqMapM.!)
updateState :: (Ord a, Show a) \Rightarrow
              DFA' \ a \rightarrow M.Map \ Int \ Int \rightarrow
                 [Int] \rightarrow M.Map \ a \ Int
updateState dfa eqMap oldStates = update where
  update = M.map (eqMapM.!) \circ
     M.unions ∘ map fromJust ∘
     filter is[ust ○ map lookup' $ oldStates
  lookup' = flip M.lookup (trans dfa)
  -- Builds a partition map for equivalence look up
toPartitionMap :: S.Set (S.Set Int) \rightarrow M.Map Int Int
toPartitionMap = toPartitionMap' 0 M.empty o S.toList
  toPartitionMap' \_acc[] = acc
  toPartitionMap' next acc (s:ss') =
     toPartitionMap' (next + 1) acc' ss' where
       acc' = S.fold insert acc s
```

```
insert = flip M.insert next
  -- Partitions a given equivalence group
partition :: (Ord \ a, Show \ a) \Rightarrow DFA' \ a \rightarrow
         M.Map\ Int\ Int \rightarrow S.Set\ Int \rightarrow S.Set\ (S.Set\ Int)
partition dfa parts toPart =
         partition' S.empty dfa parts (S.toList toPart)
         where
  partition' acc \_ \_ [] = acc
  partition' acc dfa parts (s:ss) =
     partition' acc' dfa parts ss' where
        acc'
              = S.insert set acc
        sMap = eqMap s
        matches = filter ((sMap \equiv) \circ eqMap) ss
               = S.fromList (s: matches)
        ss'
               = filter elems ss
        elems x = \neg (S.member \ x \ set)
        eqMap x = eqMap' where
          map' = M.lookup x (trans dfa)
          eqMap' =
             if isNothing map' then
                M.empty
             else
                equivalenceMap parts o from Just $ map'
  -- Determines if a set of states all have the same edges
isConsistent :: (Ord a, Show a) \Rightarrow
                 DFA' \ a \rightarrow M.Map \ Int \ Int \rightarrow [Int] \rightarrow Bool
isConsistent \_ \_ [] = True
isConsistent\ dfa\ partitions\ (s:ss) =
                 isConsistent' dfa partitions eqMap ss where
  map = M.lookup s (trans dfa)
  eqMap =
     if isNothing map then
          M.empty
     else
          equivalenceMap partitions o fromJust $ map
equivalenceMap :: M.Map Int Int \rightarrow
  M.Map \ a \ Int \rightarrow M.Map \ a \ Int
```

```
equivalence Map partitions map' =
                      M.mapWithKey updateKey map' where
  updateKey v = partitionsM.!v
isConsistent' :: (Ord a, Show a) \Rightarrow
                   DFA' a \rightarrow M.Map Int Int \rightarrow
                   M.Map \ a \ Int \rightarrow [Int] \rightarrow Bool
isConsistent' \_ \_ \_ [] = True
isConsistent' dfa partitions eqMap (s:ss') =
                   if consistent' then
                      recurse
                    else
                         False where
  consistent' = map' \equiv eqMap
  mMap = M.lookup s (trans dfa)
  map' =
     if isNothing mMap then
        M.empty
     else equivalenceMap partitions ∘ fromJust $ mMap
  recurse = isConsistent' dfa partitions eqMap ss'
  -- Removes all unreachable states in a DFA'
dropUnreachable :: (Ord\ a, Show\ a) \Rightarrow DFA'\ a \rightarrow DFA'\ a
dropUnreachable dfa = dropUnreachable' set set dfa where
  set = S.singleton \$ start dfa
dropUnreachable' :: (Ord\ a, Show\ a) \Rightarrow
  S.Set Int \rightarrow S.Set Int \rightarrow DFA' a \rightarrow DFA' a
dropUnreachable' reachable_states new_states dfa =
  if done then dfa' else recurse where
  reachable'
     S.unions \circ S.toList \circ S.map (reachable dfa) new_states
  new\_states' =
     S.difference reachable' reachable_states
  reachable_states' =
     S.union reachable states new states'
  recurse
     dropUnreachable' reachable_states' new_states' dfa
     updateDFA dfa reachable states'
```

```
done
                = new\_states' \equiv S.empty
updateDFA :: (Ord\ a, Show\ a) \Rightarrow
         DFA' \ a \rightarrow S.Set \ Int \rightarrow DFA' \ a
updateDFA dfa reachable states =
         DFA' alphabet' trans' accept' start' where
  unreachable_states =
     S.difference (states dfa) reachable_states
  accept'
     S.difference (accepting dfa) unreachable_states
                  = alphabet dfa
  alphabet'
  start'
                  = start dfa
  trans'
                  = M.filterWithKey removeKey (trans dfa)
  removeKey k = S.member k reachable\_states
reachable :: (Ord a, Show a) \Rightarrow DFA' a \rightarrow Int \rightarrow S.Set Int
reachable fsa state = S.fromList ns where
  trans'
               = M.lookup state (trans fsa)
               = if isNothing trans' then [] else ns'
  ns
  ns'
               = M.elems \circ from Just \$ trans'
  -- A test DFA that has several unreachable states: [3,4,5,6]
testDFA :: DFA' Char
testDFA = DFA' alpha' ss' accept' st' where
  alpha' = S.fromList "ab"
  ss'
    M.fromList [(0, trans0),
                      (1, trans1),
                      (2, trans2),
                      (3, trans3)]
  trans0 = M.fromList[('a',1),('b',2)]
  trans1 = M.empty
  trans2 = M.empty
  trans3 = M.fromList[('a',4),('b',5)]
  accept' = S.fromList [1, 2, 3, 6]
  st'
          = 0
  -- Tests the removal of unreachable states
testDroppable :: Bool
testDroppable = alphabet' \land states'
                         \land start' \land accepting' where
```

```
= (alphabet dfa) \equiv (S.fromList "ab")
  alphabet'
  states'
                 = (states dfa) \equiv (S.fromList [0,1,2])
  start'
                 = (start dfa) \equiv 0
  accepting' = (accepting dfa) \equiv (S.fromList [1,2])
  dfa
                 = dropUnreachable testDFA
  -- A test DFA that can be reduced
  -- to a single node with two edges
  -- it recognizes strings of the language (a|b)*
testDFA' :: DFA' Char
testDFA' = DFA' alpha' ss' accept' st' where
  alpha' = S.fromList "ab"
  ss'
         = M.fromList
                [(0, trans'),
                   (1, trans'),
                   (2, trans')]
  trans' = M.fromList[('a',1),('b',2)]
  accept' = S.fromList [0, 1, 2]
  st'
         = 0
  -- Tests that hopcroft reduces testDFA' to a minimal dfa
testHopcroft :: Bool
testHopcroft = alphabet' \land states'
                      \land accepting' \land trans' where
  alphabet'
                 = (alphabet dfa) \equiv (S.fromList "ab")
  states'
                 = (states dfa) \equiv (S.fromList [start'])
  start'
                 = (start dfa)
  accepting' = (accepting \ dfa) \equiv (S.fromList \ [start'])
                 = (trans \ dfa) \equiv (M.fromList \ [(start', trans0)])
  trans'
  trans0
                 = M.fromList[('a',start'),('b',start')]
                 = hopcroft testDFA'
  dfa
testPartition :: Bool
testPartition = partition' \equiv correctPartition where
  partition' = partition dfa parts toPart
  correctPartition = S.fromList [s1, s2, s3]
             = S.fromList [1, 2, 5]
  s1
  s2
            = S.fromList [3]
  s3
            = S.fromList [4,7]
            = M.fromList
  parts
```

```
[(0,0),(6,0),
                (1,1),(2,1),
                (3,1), (4,1),
                (5,1),(7,1)
  toPart
           = S.fromList [1, 2, 3, 4, 5, 7]
  dfa
           = nonMinimalDFA
nonMinimalDFA :: DFA' Char
nonMinimalDFA = DFA' alpha' ss' accept' st' where
       alpha' = S.fromList "ab"
      ss'
             = M.fromList
                    [(0, trans0), (1, trans1), (2, trans2),
                      (3, trans3), (4, trans4), (5, trans5),
                      (6, trans6), (7, trans7)]
       trans0 = M.fromList[('a',1)]
       trans1 = M.fromList[('a',4),('b',2)]
       trans2 = M.fromList[('a',3),('b',5)]
       trans3 = M.fromList[('b',1)]
       trans4 = M.fromList[('a',6),('b',5)]
       trans5 = M.fromList[('a',7),('b',2)]
       trans6 = M.fromList[('a',5)]
       trans7 = M.fromList[('a',0),('b',5)]
       accept' = S.fromList [0, 6]
       st'
             = 0
```

5.1 Recognize a string for a given DFA

In this module we test whether a "string" from an alphabet for a DFA is accepted by that DFA or not.

```
module Recognize (match) where import FiniteStateAutomata import qualified Data.Map as M import qualified Data.Set as S
```

The function match takes an α DFA and list of α as input (a "string" in the language of that DFA), and returns true if the string is accepted by that DFA, and false otherwise. It is fairly straightforward.

```
match :: (Ord\ a, Show\ a) \Rightarrow DFA'\ a \rightarrow [a] \rightarrow Bool
match\ dfa = match'\ dfa\ (start\ dfa)\ \mathbf{where}
match'\ dfa\ curr\ [] = S.member\ curr\ (accepting\ dfa)
match'\ dfa\ curr\ (c:cs) =
\mathbf{let}\ labelMap = M.lookup\ curr\ (trans\ dfa)\ \mathbf{in}
\mathbf{case}\ labelMap\ \mathbf{of}
Nothing \rightarrow False
Just\ map \rightarrow \mathbf{let}\ labels = M.lookup\ c\ map\ \mathbf{in}
\mathbf{case}\ labels\ \mathbf{of}
Nothing \rightarrow False
Just\ next \rightarrow match'\ dfa\ next\ cs
```

6 Alphabet

This module provides functions for lexing and parsing alphabets found in input files, in addition to an alphabet token data structure.

```
module Alphabet (parseElement,
      parseAlphabet,
      getAlphabet,
      gotoGetAlphabet) where
    import Data.List
    import Parselib
    import GHC.Unicode (isPrint)
    import Data.Char (ord)
  A formal description of an alphabet is:
Alphabet -> alphabet Elements end;
Elements -> 'Subset_ascii
Elements -> Elements
Subset_ascii ->
              a|b|c|d|e|f|g|h|i|j|k|l|m|n|o|p|q|r|s|t|u|v|
              w|x|y|z|A|B|C|D|E|F|G|H|I|J|K|L|M|N|O|P|Q|R|S|
              T|U|V|W|X|Y|Z|\n|\t|\r| |+|-|=|_|)|(|*|&|^|%|$|
              #|@|!|~|`|"|'|;|:|/|?|.|>|,|<|]|[|}|{|||\|0|1|2|
              3|4|5|6|7|8|9|\a|\b|\v|\f|\r
```

The Haskell version of this might be written as follows:

```
data Alphabet =
  AlphabetToken |
  Symbol Char |
  EndToken deriving (Show, Eq)
```

The remaining functions find an alphabet in a file, tokenize, and generate a list of the symbols in the alphabet.

```
gotoAlphabet[] = []
gotoAlphabet cs | isPrefixOf "alphabet" cs = cs
gotoAlphabet (c:cs) = gotoAlphabet cs
scanAlphabet[] = []
scanAlphabet ('a':'l':'p':'h':'a':'b':'e':'t':cs) =
  AlphabetToken: scanAlphabet cs
scanAlphabet('\':c:cs) =
  Symbol c : scanAlphabet cs
scanAlphabet ('e':'n':'d':cs) =
  [EndToken]
scanAlphabet (\_:cs) =
  scanAlphabet cs
parseAlphabet'[] = []
parseAlphabet' (AlphabetToken: ts) =
  parseAlphabet' ts
parseAlphabet' (Symbol c:ts) =
  c: parseAlphabet' ts
parseAlphabet' (EndToken: ts) =
getAlphabet' = parseAlphabet' \circ scanAlphabet \circ gotoAlphabet
  -- this was not a fun bug to track down
parseEscapedChar =
    do { string "\\n"; return '\n' }
  + + + do \{ string " \t"; return ' \t' \}
  +++ do { string "\\v"; return '\v' }
  + + + do \{ string "\r"; return '\r' \}
  +++ do { string "\b"; return '\b' }
  +++ do { string "\\a"; return '\a' }
```

```
+++do { string "\\f"; return '\f' }
   +++ do { string "\\"; return '\\' }
printablePlus char =
  let ascii = ord char in
  (ascii \geqslant 7 \land ascii \leqslant 13)
   \lor (ascii \geqslant 32 \land ascii \leqslant 126)
parseElement :: Parser Char
parseElement = do
  space
  char '\''
     parseEscapedChar + + +
     sat printablePlus
  return c
parseAlphabet :: Parser [Char]
parseAlphabet = do
  space
  string "alphabet"
  alphabet \leftarrow many parseElement
  string "end;" + + + string "end" -- need because test file
  return alphabet
getAlphabet file =
  case (parse parseAlphabet) file of
     ] \rightarrow error "Alphabet is empty (no alphabet provided)."
     regex \rightarrow (fst \circ head) regex
  -- to skip beginning contents and read alphabet
gotoGetAlphabet file =
  case (parse parseAlphabet) (gotoAlphabet file) of
     ] \rightarrow error "Alphabet is empty (no alphabet provided)."
     regex \rightarrow (fst \circ head) regex
```

7 Input

Similar to the Algorithms module, in this module we gather all of our solutions for problems 5-8, which deals with file input/output.

Module ParseFSA parses either DFAs or FSAs from text file descriptions; ParseReg parses regular expressions from text files (with an alphabet) and tests whether symbols occuring in the regular expression are elements of the alphabet provided in the file; and lastly ParseLang provides a data structure for lexical descriptions, reads in a complete lexical description from a text file, and transforms it into our internal representation, for use with the algorithms in the Algorithms module.

```
module Input (
module ParseFSA,
module ParseReg,
module ParseLang) where
import ParseFSA
import ParseReg
import ParseLang
```

7.1 Parse a Regular Expression

This module inputs, lexes, and parses a regular expression from a text file. It uses Hutton's Parselib library.

Parsing is divided into a function for each regular expression. It handles ascii spaces, newlines, tabs, etc. I.e., the printable subset of ascii, as required by the spec.

```
module ParseReg (getRegex, parseRegex) where import Alphabet import Regex import Parselib type Alphabet = [Char] parseAlt :: Alphabet → Parser (Regex Char) parseAlt alphabet = do string "|" space regex ← parseRegex alphabet space regex' ← parseRegex alphabet return (Alt regex regex')
```

```
parseConcat :: Alphabet \rightarrow Parser (Regex Char)
parseConcat alphabet = do
  string "+"
  space
  regex \leftarrow parseRegex alphabet
  space
  regex' \leftarrow parseRegex alphabet
  return (Concat regex regex')
parseKleene :: Alphabet \rightarrow Parser (Regex Char)
parseKleene alphabet = do
  string "*"
  space
  regex \leftarrow parseRegex alphabet
  return (Kleene regex)
parseTerm :: Alphabet \rightarrow Parser (Regex Char)
parseTerm \ alphabet = \mathbf{do}
  c \leftarrow parseElement
  if \neg (elem c alphabet) then
     let msg = "Regular expression contains terminal "
        ++ show c
        + " which is not an element of the"
        + " alphabet provided." in
       error msg
  else
     return (Term c)
parseRegex :: Alphabet \rightarrow Parser (Regex Char)
parseRegex alphabet = do
  space
  parseAlt\ alphabet + + +
     parseConcat \ alphabet + + +
     parseKleene alphabet + + +
     parseTerm alphabet
  -- takes an alphabet
getRegex :: String \rightarrow Alphabet \rightarrow Regex Char
getRegex file alphabet =
  case (parse (parseRegex alphabet)) file of
     [] 
ightarrow \mathit{error} "Could not parse regular expression."
```

```
regex → (fst o head) regex
-- example, should error
readRegex1 = do
source ← readFile "regexp3.txt"
-- get alphabet before, because alphabet is after
let alphabet = gotoGetAlphabet source
let regex = getRegex source alphabet
putStrLn $ show regex
readRegex file = do
source ← readFile file
let alphabet = gotoGetAlphabet source
let regex = getRegex source alphabet
putStrLn $ show regex
```

7.2 Parse an FSA

In this module we parse a description of an DFA or an NFA and return the appropriate data structure.

Since the formal definition of a lexical description of a language does not contain a description of an NFA or a DFA (only regular expressions), this module was simply used on the provided test cases, and for a basic sanity check on whether our implementation for NFAs and DFAs was correct.

It uses Haskell's Parsec library for parsing.

```
{-# LANGUAGE FlexibleContexts #-}
module ParseFSA (parseNFA, parseDFA) where
import Data.Functor
import qualified Data.Set as S
import qualified Data.Map as M
import FiniteStateAutomata
import Text.Parsec
data Transition = NFAT {fromState :: String,
    symbols :: [Char],
    toState :: String }
| DFAT {fromState :: String,
    symbol :: Char,
    toState :: String }
```

```
instance Show Transition where
  show (NFAT f ss t) = "NFAT " + f + + " " + (show ss) + + " --> " + t
  data Description = Description { states' :: [String],
  startState :: String,
  acceptStates :: [String],
  trans' :: [Transition] } deriving Show
parseNFA :: [Char] \rightarrow String \rightarrow NFA' Char
parseNFA = parseFSA "nfa" (NFA') (toNFAMap)
parseDFA :: [Char] \rightarrow String \rightarrow DFA' Char
parseDFA = parseFSA  "dfa" (DFA') (toDFAMap)
parseFSA typ constr toMap alpha s =
  case parse (description typ isNFA) "Syntax Error" s of
     Left er \rightarrow error \circ show \$ er
     Right desc \rightarrow convertToFSA alpha desc constr toMap
  where isNFA = if typ \equiv "nfa" then True else False
convertToFSA :: FSA f \Rightarrow [Alpha f] \rightarrow Description \rightarrow
  (S.Set\ (Alpha\ f) \to M.Map\ Int\ (FSAVal\ f) \to S.Set\ Int \to Int \to f) \to
  (M.Map\ String\ Int \rightarrow [Transition] \rightarrow M.Map\ Int\ (FSAVal\ f)) \rightarrow
  f
convertToFSA alpha desc const toMap = const alphabet nfaMap accepting start where
  normal = M.fromList \$ zip (states' desc) [0..]
  alphabet = S.fromList alpha
  nfaMap = (toMap normal) \circ trans' \$ desc
  accpting = S.fromList \circ map (normalM.!) \circ acceptStates \$ desc
  start = normalM.!(startState desc)
toNFAMap :: M.Map String Int \rightarrow [Transition] \rightarrow NFAMap Char
toNFAMap\ m\ ts = M.fromList \circ map\ convert \circ M.toList \circ go\ ts\ \$\ M.empty\ \mathbf{where}
  convert (s, es) = (mM.!s, S.fromList \circ map (\lambda(c, s2) \rightarrow (c, mM.!s2)) \$ es)
  toM "" = [Nothing]
  toM s = map Just s
  go[]acc = acc
  go((NFAT f syms t) : ts) acc = case M.lookup f acc of
     Nothing \rightarrow go ts $ M.insert f (zip (toM syms) (repeat t)) acc
     Just es \rightarrow go ts $ M.insert f ((zip (toM syms) (repeat t)) ++ es) acc
toDFAMap :: M.Map \ String \ Int \rightarrow [Transition] \rightarrow DFAMap \ Char
```

```
toDFAMap\ m\ ts = M.fromList \circ map\ convert \circ M.toList \circ go\ ts\ \$\ M.empty\ \mathbf{where}
  convert (s,es) = (mM.!s, M.fromList \circ map (\lambda(c,s2) \rightarrow (c,mM.!s2)) \$es)
  go[]acc = acc
  go((DFAT f symb t) : ts) acc = case M.lookup f acc of
     Nothing \rightarrow go ts $ M.insert f [(symb, t)] acc
     Just es \rightarrow go ts $ M.insert f ((symb, t) : es) acc
description :: Stream s m Char \Rightarrow
           String \rightarrow
           Bool \rightarrow
           ParsecT s u m Description
description keyword isNFA = do
  spaces \gg string \ keyword \gg spaces
  stats ← statelist "states" "end; " identifier
  initState ← initialState "initial"
  acceptStates ← statelist "accept" "end; "identifier
  trans ← statelist "transitions" "end;" (transition isNFA)
  return $ Description stats initState acceptStates trans
transition :: Stream s m Char \Rightarrow
  Bool \rightarrow
  ParsecT s u m Transition
transition isNFA = do
  from \leftarrow identifier
  syms \leftarrow option [] symbolList
  string "-->" ≫ spaces
  to \leftarrow identifier
  return $ case isNFA of
     True \rightarrow NFAT from syms to
     False \rightarrow DFAT from (head syms) to
initialState :: Stream s m Char \Rightarrow String \rightarrow ParsecT s u m String
initialState\ keyword = string\ keyword \gg spaces \gg identifier
parseStringOrTerm :: Stream s m Char \Rightarrow String \rightarrow
  ParsecT s u m a \rightarrow
  ParsecT s u m (Either String a)
parseStringOrTerm\ term\ s = \mathbf{do}
  ter \leftarrow try \$ optionMaybe \$ string term
  case ter of
     Just t \rightarrow return \$ Left t
```

```
Nothing \rightarrow Right < $ > s
statelist :: Stream s m Char \Rightarrow
   String \rightarrow
   String \rightarrow
   ParsecT s u m a \rightarrow
   ParsecT s u m [a]
statelist startTok endTok elem = do
   string\ startTok \gg spaces
   reverse < $ > parseSets' [] where
     parseSets' acc = do
         sOrT \leftarrow parseStringOrTerm\ endTok\ elem
         spaces
         case sOrT of
           Left \_ \rightarrow return acc
            Right str \rightarrow parseSets' $ str : acc
identifier :: Stream s m Char \Rightarrow ParsecT s u m String
identifier = do
   i \leftarrow many1 \ alphaNum
   spaces
   return i
sym :: Stream \ s \ m \ Char \Rightarrow ParsecT \ s \ u \ m \ Char
sym = do
   char '\''
   c \leftarrow anyChar
   case c of
      ' \setminus \setminus ' \to do
         c2 \leftarrow anyChar
         return \$ read \$ "' \ + [c2] + "'"
      _{-} \rightarrow return c
symbolList :: Stream \ s \ m \ Char \Rightarrow ParsecT \ s \ u \ m \ [Char]
symbolList = sym 'sepEndBy1' (spaces)
```

7.3 Parse a Lexical Description of a Programming Language

In this module we parse a lexical description of a language, and prepare it for parsing with respect to our previous data structures and algorithms.

It also uses Hutton's Parselib.

```
{-# LANGUAGE TypeFamilies, FlexibleContexts,FlexibleInstances #-}
module ParseLang where
import Parselib
import Regex
import ParseReg
import FiniteStateAutomata
import Alphabet
import Data.Char (isSpace)
import Data.List (intersperse)
```

We use a data structure *Desc* to internally represent a lexical description. *Desc* is a basic record type, with three functions, *language*, *symbols*, and *classes* which return the name of the language as a string, the alphabet, and a list of classes given by the lexical description, respectively.

The data structure *Class* is another record type with three functions, *name*, *regex*, and *relevance*, which return the name of the class, the regular expression which describes it, and its semantic relevance, respectively.

Thus to obtain an NFA equivalent of the regular expression for the first class given in a parsed lexical description l, we write: $(thompson \circ regex \circ head \circ classes) l$.

```
type Identifier = String
data Relevance = Relevant | Irrelevant | Discard
instance Show Relevance where
  show (Relevant) = "relevant"
  show (Irrelevant) = "irrelevant"
  show (Discard) = "discard"
data Class = Class  {
  name:: Identifier,
  regex :: Regex Char,
  relevance :: Relevance }
instance Show Class where
  show c = "class" + name c + + "" + +
    show (regex c) ++ " " ++
    show (relevance c) ++
    " end;"
data \ Desc = Desc \ \{
```

```
language:: String,
  symbols:: [Char],
  classes:: [Class]
}
showAlphabet a = "'" ++ (intersperse '\'' a)
instance Show Desc where
  show desc =
    "language: " ++ language desc ++ "\n" ++
    "alphabet: " ++
    showAlphabet (symbols desc) ++
    " end;" ++ "\n" ++
    "classes: " ++ "\n" ++
    unlines (map show (classes desc)) ++
    " end;"
```

The remaining functions parse a text file of a lexical description, and deposit that description (if it is well-formed), into our data structure.

```
parseLangIdentifier :: Parser String
parseLangIdentifier = do
  ident \leftarrow many \$ sat (\neg \circ isSpace)
  return ident
parseRelevance :: Parser Relevance
parseRelevance =
     do {string "relevant"; return Relevant } + + +
     do {string "irrelevant"; return Irrelevant} + + +
     do {string "discard" ;return Discard}
parseClass :: [Char] \rightarrow Parser Class
parseClass\ alphabet = do
  space
  string "class"
  space
  name \leftarrow parseLangIdentifier
  space
  string "is"
  regex \leftarrow parseRegex \ alphabet
  space
  relevance \leftarrow parseRelevance
```

```
space
  string "end;"
  return $ Class name regex relevance
parseLang :: Parser Desc
parseLang = do
  space
  string "language"
  space
  language \leftarrow parseLangIdentifier
  alphabet \leftarrow parseAlphabet
  classes ← many $ parseClass alphabet
  space
  string "end;"
  return (Desc language alphabet classes)
getLang :: String \rightarrow Desc
getLang\ desc = \mathbf{do}
  case (parse parseLang) desc of
     [] 
ightarrow error "Could not parse lexical description."
     regex \rightarrow (fst \circ head) regex
  -- example
readLang1 = do
  source ← readFile "tests/lexdesc3.txt"
  let x = (parse \ parseLang) source
  putStrLn $ show x
readLang file = do
  source \leftarrow readFile file
  let x = (parse parseLang) source
  putStrLn $ show x
```

7.4 Scanner Generator

This module performs the work necessary to output a scanner, thus making our implementation a scanner generator.

```
module ScannerGenerator (scannerGenerator) where import Regex import Algorithms
```

import Input

```
alternate :: [Class] \rightarrow Regex Char
alternate [] = Empty
alternate(c:[]) = regex c
alternate (c:cs) =
  Alt (regex c) (alternate cs)
scannerGenerator :: String \rightarrow String
scannerGenerator desc = program where
  regex = Kleene \circ alternate \circ classes \circ getLang \$ desc
  dfa = hopcroft \circ subsetConstruction \circ thompson \$ regex
  program = "module Main where\n" ++
     "import FiniteStateAutomata(DFA'())\n" ++
     "import Recognize(match)\n" ++
     "dfa :: DFA' Char\n" ++
     "dfa = read \"" ++
     (replace '"' "\\\"") (show dfa) ++ "\"\n" ++
     "main = do { contents <- getContents;" ++</pre>
     " putStrLn $ (show (match dfa contents)) }"
replace :: (Eq \ a) \Rightarrow a \rightarrow [a] \rightarrow [a] \rightarrow [a]
replace \ a \ b = concatMap \ replace' \ \mathbf{where}
  replace' x = if \ a \equiv x then \ b else [x]
```

8 Module: Main.lhs

The final module, *Main*, puts everything together, by simply calling the function *scannerGenerator* on a lexical description.

```
module Main where
```

```
import ScannerGenerator (scannerGenerator)
main = do
    contents ← getContents
    putStr $ scannerGenerator contents

Example for interpreted scanner.

testfile <- readFile "tests/testfile3.txt"
desc <- getLang "tests/lexdesc3.txt"</pre>
```

```
let regex = Kleene (alternate (classes desc))
let test = ((match . hopcroft . subsetConstruction . thompson) regex) testfile
putStrLn $ show test
putStrLn $ show desc
```