Compilers Project 1: Scanner Generator

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1 Introduction

This is the final report for project 1, CS454/CS554, on lexical analysis. It includes all of the source code for our Haskell implementation of a scanner generator. Our team consists of the authors listed above. In preparing this document, the work was split equally among the members of the group, in addition to the coding and testing duties. Approximately 40 man hours went into finishing the project.

Our first design decision was to use Haskell's literate mode to prepare all of our code. Secondly, we decided to use the distributed revision control software git for collaborative coding.

We decided to write each algorithm in the assignment as its own module, in addition to modules describing finite state automata (FSA), regular expressions, and similarly for the file input/output.

Lastly, we decided to write a scanner generator for our final output, instead of a scanner "interpeter". That is, we parse a lexical description, and return a Haskell source file to be compiled. Once suitably compiled, the binary will accept text files (return true) if and only if they are strings accepted by the language given in the lexical description.

2 Finite State Automaton

In this module we give our data structure for modelling a finite state automaton.

The formal definition of an FSA is a 5-tuple, where:

- 1. a finite set of states (Q)
- 2. a finite set of input symbols called the alphabet (Σ)
- 3. a transition function ($\delta : Q \times \Sigma \to Q$)
- 4. a start state $(q0 \in Q)$
- 5. a set of accept states ($F \subseteq Q$)

We tried to have our data structure mirror the mathematical definition of an FSA as closely as possible.

```
{-# LANGUAGE TypeFamilies, FlexibleContexts,FlexibleInstances #-}
module FiniteStateAutomata (
                              FSA(..),
                              NFA'(..),
                              NFAMap,
                              DFA'(..),
                              DFAMap,
                              epsilon, ppfsa) where
import qualified Data.Map as M
import qualified Data.Set as S
class (Ord (Alpha f),
  Show (Alpha f),
  Show f,
  Show (FSAVal f),
  Listable (FSAVal f)) \Rightarrow FSA f where
  type Alpha f
  type FSAVal f
  alphabet :: (Ord (Alpha f), Show (Alpha f)) \Rightarrow
             f \rightarrow S.Set (Alpha f)
  accepting :: f \rightarrow S.Set Int
  start
           :: f \rightarrow Int
  trans
           :: f \to M.Map Int (FSAVal f)
          :: f \rightarrow S.Set Int
  states\ fsa = S.unions\ [(S.fromList \circ M.keys \circ trans\ \$\ fsa),
     (accepting fsa),
     (S.fromList \circ
```

```
concatMap sndList ∘
     M.elems \circ trans \$ fsa)
data DFA' a = DFA' { alpha :: S.Set a,
                                :: DFAMap a,
  accept :: S.Set Int,
  st
                                :: Int } deriving (Show, Read)
data NFA' a = NFA' { nalpha :: S.Set a,
                                  :: NFAMap a,
  naccept :: S.Set Int,
                                  :: Int }
  nst
type DFAMap \ a = M.Map \ Int \ (M.Map \ a \ Int)
type NFAMap \ a = M.Map \ Int \ (S.Set \ (Maybe \ a, Int))
class (Show (Elem m)) \Rightarrow Listable m where
  type Elem m
  toList :: m \rightarrow [(Elem \ m, Int)]
instance (Show a) \Rightarrow Listable (M.Map a Int) where
  type Elem(M.Map\ a\ Int) = a
  toList = M.toList
instance (Show a) \Rightarrow Listable (S.Set (Maybe a, Int)) where
  type Elem (S.Set (Maybe\ a, Int)) = Maybe\ a
  toList = S.toList
sndList :: Listable \ m \Rightarrow m \rightarrow [Int]
sndList = map \ snd \circ toList
fsaShow :: (FSA f) \Rightarrow f \rightarrow String
fsaShow fsa = "{alphabet="
           ++ (show \circ S.toList \circ alphabet \$ fsa)
           #","#
           "states=" ++
           (show \circ S.toList \circ states \$ fsa) + ", " +
           "start=" ++ (show o start $ fsa) ++ ", " ++
           "accepting="
           ++ (show \circ S.toList \circ accepting \$ fsa)
           # ", " # "trans="
           ++ (show \circ map (filter (\not\equiv """)) \circ
             showTransitions $ fsa)
pettyPrinter :: (FSA f) \Rightarrow f \rightarrow IO ()
```

```
pettyPrinter fsa = (putStr $ "alphabet="
   ++ (show \circ S.toList \circ alphabet \$ fsa)
   # "\n" #
  "states="
   ++ (show \circ S.toList \circ states \$ fsa)
   # "\n" #
  "start=" ++ (show \circ start \$ fsa)
   # "\n" #
  "accepting="
   ++ (show \circ S.toList \circ accepting $ fsa)
   ++ "\n") ≫ trans
       where trans =
          mapM_{-}(putStrLn \circ filter (\not\equiv '"'))
             $ showTransitions fsa
ppfsa :: (FSA f) \Rightarrow f \rightarrow IO ()
ppfsa = pettyPrinter
showTransitions :: (FSA f) \Rightarrow f \rightarrow [String]
showTransitions\ fsa=map\ showTransition\ \circ
  M.toList \circ trans \$ fsa  where
  showTransition (from, ts) = (show from)
     #"::"
     ++ (show \circ map showTransition' \circ toList $ ts) where
       showTransition'(x, to) = (show x) + " -> " + (show to)
instance (Ord a, Show a) \Rightarrow FSA (DFA' a) where
  type Alpha (DFA' a) = a
  type FSAVal(DFA'a) = (M.Map\ a\ Int)
  alphabet = alpha
  accepting = accept
  start = st
  trans = ss
epsilon :: Maybe a
epsilon = Nothing
instance (Ord a, Show a) \Rightarrow FSA (NFA' a) where
  type Alpha (NFA'a) = a
  type FSAVal (NFA'a) = (S.Set (Maybe a, Int))
  alphabet = nalpha
  accepting = naccept
```

```
start = nst
  trans = nss
instance (Ord a, Show a) \Rightarrow Show (NFA' a) where
  show nfa = "NFA" + (fsaShow nfa)
simpleNFA :: NFA' Char
simpleNFA = NFA' alpha states accepting start where
  alpha = S.fromList['a','b']
  states = M.fromList
    [(0, S.fromList [(Just 'a', 1)]),
          (1, S.fromList [(Just 'b', 0), (epsilon, 2)])]
  start = 0
  accepting = S.fromList [2]
simpleDFA:: DFA' Char
simpleDFA = DFA' alpha states accepting start where
  alpha = S.fromList ['a','b','c']
  states = M.fromList
    [(0, M.fromList [('a',1)]),
          (1, M. from List [('b', 0), ('c', 2)])]
  start = 0
  accepting = S.fromList[2]
deadStateDFA:: DFA' Char
deadStateDFA = DFA' alpha states accepting start where
  alpha = S.fromList "ab"
  states =
    M.fromList [(0, trans0), (1, trans1), (2, trans2)] where
       trans0 = M.fromList[('a',1),('b',2)]
      trans1 = M.fromList[('b',3)]
       trans2 = M.fromList[('a',3)]
  accepting = S.fromList [1,2]
  start = 0
```

3 Regular Expressions

In this module we give the haskell data type for a regular expression; the encoding almost exactly mirrors the definition given in the assignment.

{-# LANGUAGE TypeFamilies, FlexibleContexts,FlexibleInstances #-}

```
module Regex (Regex (..)) where

data Regex a = Alt (Regex a) (Regex a)

| Concat (Regex a) (Regex a)

| Kleene (Regex a)

| Term a

| Empty deriving Show
```

We wrote a pretty infix printer:

```
instance Show (Regex Char) where
show (Alt r1 r2 ) =
    "(" ++ (show r1) ++ "|" ++ (show r2) ++ ")"
show (Concat r1 r2) =
    "(" ++ (show r1) ++ "+" ++ (show r2) ++ ")"
show (Kleene r1) = "(" ++ (show r1) ++ "*" ++ ")"
show (Term c) = '\'':c:[]
show (Empty) = "\epsilon"
```

However, it was determined that writing a scanner generator would be easier if we used the default show for regular expressions.

4 Algorithms

Our solutions to the "in-memory" algorithms given in §1.2 have been modularized in the following way.

```
module Algorithms (module Thompson,
module SubsetConstruction,
module Hopcroft,
module Recognize
) where
import Thompson
import SubsetConstruction
import Hopcroft
import Recognize
```

In this way we encapsulated (and named) the solutions individually, as the assignment requested.

4.1 Thompson's Algorithm

In this module we provide our solution for converting a regular expression to an NFA.

```
module Thompson (thompson) where import Prelude hiding (concat) import qualified Data.Set as S import qualified Data.Map as M import FiniteStateAutomata (FSA (trans), NFA' (..), epsilon) import Regex
```

The function *thompson* returns the result of converting a regular expression to a non-deterministic finite state automaton. It uses Thompson's algorithm for doing so.

```
thompson :: (Ord\ a, Show\ a) \Rightarrow Regex\ a \rightarrow NFA'\ a

thompson = fst \circ thompson'\ 0

thompson' :: (Ord\ a, Show\ a) \Rightarrow

Int \rightarrow Regex\ a \rightarrow (NFA'\ a, Int)

thompson' lab\ (Alt\ r1\ r2) = union\ lab''\ fsa\ fsa'\ where

(fsa, lab') = thompson'\ lab\ r2

thompson' lab\ (Concat\ r1\ r2) = concat\ lab''\ fsa\ fsa'\ where

(fsa, lab'') = thompson'\ lab\ r1

(fsa', lab'') = thompson'\ lab\ r2

thompson' lab\ (Kleene\ r1) = mrKleene\ lab'\ fsa\ where

(fsa, lab') = thompson'\ lab\ r1

thompson' lab\ (Term\ x) = symbol\ lab\ x

thompson' lab\ (Term\ x) = symbol\ lab\ x
```

The following functions individually convert particular regular expressions to their NFA equivalents. For example, *concat* takes two regular expressions, say a and b, and returns an NFA where the NFA corresponding to a's accepting states are now transitions to the NFA corresponding to b's start state.

The other functions perform similar operations, according to the algorithm.

```
expression :: (Ord\ a, Show\ a) \Rightarrow Int \rightarrow (NFA'\ a, Int)
expression label = (fsa, label + 2) where
```

```
fsa = NFA' S.empty (M.fromList [n1])
     (S.singleton (label + 1)) label
  n1 = (label, S. singleton (epsilon, (label + 1)))
symbol :: (Ord \ a, Show \ a) \Rightarrow Int \rightarrow a \rightarrow (NFA' \ a, Int)
symbol\ label\ sym = (fsa, label + 2) where
  fsa = NFA' (S.singleton sym)
     (uncurry M.singleton n1) (S.singleton (label + 1)) label
  n1 = (label, S.singleton (Just sym, label + 1))
union :: (Ord a, Show a) \Rightarrow
  Int \rightarrow NFA' \ a \rightarrow NFA' \ a \rightarrow (NFA' \ a, Int)
union label nfa0 nfa1 = (fsa, label + 2) where
  (NFA' \ a0 \ m0 \ as0 \ st0) = updateAccepting [(label + 1)] \ nfa0
  (NFA' a1 m1 as1 st1) = updateAccepting [(label + 1)] nfa1
  fsa = NFA' alpha newMap (S.singleton (label + 1)) label
  alpha = S.union \ a0 \ a1
  newMap = M.unions [m0, m1, epsilonEdges]
  epsilonEdges =
     M.singleton label
        (S.fromList [(epsilon, st0), (epsilon, st1)])
concat :: (Ord \ a, Show \ a) \Rightarrow
  Int \rightarrow NFA' \ a \rightarrow NFA' \ a \rightarrow (NFA' \ a, Int)
concat label fsa0@(NFA' s0 m0 as0 st0) (NFA' s1 m1 as1 st1) =
  (fsa, label) where
  fsa = NFA' (S.union s0 s1) (M.union updated m1) as1 st0
  updated = trans $ updateAccepting [st1] fsa0
mrKleene :: (Ord\ a, Show\ a) \Rightarrow Int \rightarrow NFA'\ a \rightarrow (NFA'\ a, Int)
mrKleene\ label\ nfa@(NFA'\ a\ \_as\ st)=(fsa,label+2)\ \mathbf{where}
  (NFA' \_ m \_ \_) = updateAccepting [st, (label + 1)] nfa
  fsa = NFA' a m' (S.singleton (label + 1)) label
  m' = M.union m epsilons
  epsilons =
     M.singleton label
        (S.fromList [(epsilon, (label + 1)), (epsilon, st)])
  epsilons' = M.fromList \circ map func \circ S.toList \$ as
  func x = (x, S.singleton (epsilon, label + 1))
updateAccepting :: (Ord \ a) \Rightarrow [Int] \rightarrow NFA' \ a \rightarrow NFA' \ a
updateAccepting is nfa@(NFA' a ts as st) =
```

```
NFA' a newTrans (S.empty) st where

newTrans = M.union \ ts \ nts

nts = M.fromList \circ map \ func \circ S.toList \ as

func \ x =

(x, S.fromList \circ map \ (\lambda i \rightarrow (epsilon, i)) \ sis)
```

4.2 Subset Construction

In this module we provide our solution for converting a given non-deterministic finite state automaton to an equivalent deterministic finite state automaton.

```
{-# LANGUAGE FlexibleInstances #-}
module SubsetConstruction (subsetConstruction) where
import Data.Maybe
import FiniteStateAutomata
import qualified Data.Map as M
import qualified Data.Set as S
import Debug.Trace
type LabelMap = M.Map (S.Set Int) Int
subsetConstruction :: (Ord a, Show a) \Rightarrow NFA' a \rightarrow DFA' a
subsetConstruction nfa =
    DFA' (alphabet nfa) dfamap' accept start' where
         start' = labelsM.!startStateSet
         accept = findAccepting nfa labelmap
         (\_, labelmap, dfamap') =
           subsetConstruction' nfa next
              labels dfamap outSets
         startStateSet = closure nfa (start nfa)
         (labels, next) =
           labelSets 0 M.empty
            (S.fromList (startStateSet : outSets))
         edges = edgeMap labels edgeSet
         dfamap =
           M.singleton (labelsM.!startStateSet) edges
         outSets =
           map (closure' ∘ flip move' startStateSet)
```

```
alphabet'
           edgeSet = zip alphabet' outSets
           alphabet' = S.toList \circ alphabet \$ nfa
           closure' = closure nfa
           move' = move nfa
findAccepting :: (Ord a, Show a) \Rightarrow
                   NFA' a \rightarrow LabelMap \rightarrow S.Set Int
findAccepting nfa labels = S.fromList sets where
  sets = M.elems (M.filterWithKey isAccepting labels)
  isAccepting label _ =
        S.empty \not\equiv (S.intersection accept label)
  accept = accepting nfa
subsetConstruction' :: (Ord a, Show a) \Rightarrow
  NFA' \ a \rightarrow Int \rightarrow LabelMap \rightarrow
  DFAMap \ a \rightarrow [S.Set \ Int] \rightarrow
  (Int, LabelMap, DFAMap a)
subsetConstruction' \_ next \ labels \ dfamap \ [\ ] =
     (next, labels, dfamap)
subsetConstruction' nfa next labels dfamap (s:ss) =
     case (s \equiv S.empty) of
  True \rightarrow subsetConstruction' nfa next labels dfamap ss
  False \rightarrow if done then continue else recursion where
     done = M.lookup (labelsM.!s) dfamap \not\equiv Nothing
     continue = subsetConstruction' nfa next labels dfamap ss
     recursion =
           subsetConstruction' nfa next" labels" dfamap" ss
      (next'', labels'', dfamap'') =
           subsetConstruction' nfa next' labels' dfamap' outSets
      (labels', next') =
           labelSets next labels (S.fromList outSets)
     dfamap' = M.insert (labelsM.!s) edges dfamap
     edges = edgeMap labels' edgeSet
     edgeSet = zip alphabet' outSets
     outSets = map (closure' \circ flip move' s) alphabet'
     alphabet' = S.toList \circ alphabet \$ nfa
     move' = move nfa
     closure' = closure nfa
```

```
labelSets :: Int \rightarrow M.Map (S.Set Int) Int \rightarrow
                 S.Set (S.Set Int) \rightarrow
               (M.Map (S.Set Int) Int, Int)
labelSets next labels sets =
     labelSets' next labels (S.toList sets)
labelSets' :: Int \rightarrow LabelMap \rightarrow
   [S.Set\ Int] \rightarrow (LabelMap, Int)
labelSets' next labels [] = (labels, next)
labelSets' next labels (s:ss) =
  case (s \equiv S.empty) of
     True \rightarrow labelSets' next labels ss
     False \rightarrow
              if (M.member s labels) then
                  (labelSets' next labels ss)
              else
                 (labelSets' (next + 1)
                    (M.insert s next labels) ss)
edgeMap :: (Ord a, Show a) \Rightarrow
              M.Map (S.Set Int) Int \rightarrow
                 [(a, (S.Set\ Int))] \rightarrow M.Map\ a\ Int
edgeMap = edges' M.empty where
  edges' :: (Ord \ a, Show \ a) \Rightarrow
              M.Map \ a \ Int \rightarrow M.Map \ (S.Set \ Int) \ Int \rightarrow
              [(a, (S.Set\ Int))] \rightarrow M.Map\ a\ Int
  edges' acc _ [] = acc
  edges' acc labels ((alpha, set):ss) =
        case (set \equiv S.empty) of
      True \rightarrow edges' acc labels ss
     False \rightarrow edges' \ acc' \ labels \ ss \ where
        acc' = M.insert alpha (labelsM.!set) acc
class Constructable c where
  closure :: (Show a, Ord a) \Rightarrow NFA' a \rightarrow c \rightarrow S.Set Int
  move :: (Show a, Ord a) \Rightarrow NFA' a \rightarrow a \rightarrow c \rightarrow S.Set Int
instance Constructable Int where
  closure nfa state =
        fst ∘ closure' nfa (S.singleton state) M.empty $ state where
     closure' nfa acc memoize state =
```

```
case (M.lookup (acc, state) memoize) of
           Nothing \rightarrow
             if done then (acc', memoize') else (acc'', memoize'') where
                done = edges \equiv Nothing \lor eps \equiv S.singleton state
                edges = M.lookup state \circ trans \$ nfa
                eps = S.union (S.singleton state)
                   (S.map\ snd \circ S.filter\ isEpsilon \circ
                     fromJust $ edges)
                eps' = S.difference eps acc
                isEpsilon (label, \_) = label \equiv epsilon
                acc' = S.union acc (S.singleton state)
                acc'' = S.union \ acc' \circ S.unions \$ sets
                memoize' = M.insert (acc, state) acc' memoize
                (memoize''', sets) = memoMap memoize (closure' nfa acc') \circ S.toList \$ eps'
                memoize'' = M.insert (acc, state) acc'' memoize'''
           Just set \rightarrow (set, memoize)
  move nfa sym state =
     if (edges \equiv Nothing) then S.empty else eps where
     edges = M.lookup state \circ trans \$ nfa
     eps = S.map \ snd \circ S.filter \ isSym \circ fromJust \$ \ edges
     isSym (label, \_) =
           label \not\equiv Nothing \land sym \equiv from Just \ label
  -- func x = S.map (fst . (closure' memoize acc' nfa))
memoMap :: tbl \rightarrow (tbl \rightarrow a \rightarrow (b, tbl)) \rightarrow [a] \rightarrow ((tbl), [b])
memoMap = memoMap'[] where
  memoMap' acc m = [] = (m, acc)
  memoMap' acc m f (x:xs) = memoMap' (a:acc) m' f xs where
     (a, m') = f m x
instance Constructable (S.Set Int) where
  closure\ nfa\ states = concatMap'\ (closure\ nfa)\ states
  move nfa sym states = concatMap' (move nfa sym) states
concatMap' :: (Ord\ a, Ord\ b) \Rightarrow
   (a \rightarrow S.Set \ b) \rightarrow S.Set \ a \rightarrow S.Set \ b
concatMap' f = S.unions \circ S.toList \circ S.map f
simpleNFA:: NFA' Char
simpleNFA = NFA' alpha trans accept st where
```

```
alpha = S.empty
  accept = S.fromList[0]
        = 0
  trans = M.fromList [(0, trans0), (1, trans1)] where
    trans0 = S.fromList [(Nothing, 1)]
    trans1 = S.fromList [(Nothing, 0)]
testNFA :: NFA' Char
testNFA = NFA' alpha trans accept st where
  alpha = S.empty
  accept = S.fromList [0, 1]
        = 0
  trans = M.fromList[(0, trans0), (1, trans1), (2, trans2)] where
    trans0 = S.fromList [(Nothing, 1), (Nothing, 2)]
    trans1 = S.fromList [(Nothing, 2), (Nothing, 0)]
    trans2 = S.fromList [(Nothing, 0), (Nothing, 1)]
testNFA' :: NFA' Char
testNFA' = NFA' alpha trans accept st where
  alpha = S.fromList "a"
  accept = S.fromList [0, 1]
        = 0
  trans = M.fromList[(0, trans0), (1, trans1), (2, trans2)] where
    trans0 = S.fromList [(Nothing, 1), (Just 'a', 1), (Just 'a', 2)]
    trans1 = S.fromList [(Just'a', 2), (Just'a', 0)]
    trans2 = S.fromList [(Just 'a', 0), (Just 'a', 1)]
```

5 Hopcroft's Algorithm

In this module we provide our solution for minimizing a given deterministic finite state automaton.

We followed the algorithm given on page 30 of Basics of Compiler Design.

```
module Hopcroft (hopcroft) where
import FiniteStateAutomata (FSA (..), DFA' (..))
import Data.Maybe (fromJust, isJust, isNothing)
import qualified Data.Map as M
import qualified Data.Set as S
```

```
hopcroft :: (Ord a, Show a) \Rightarrow DFA' a \rightarrow DFA' a
hopcroft dfa = hopcroft' (dropUnreachable dfa)
                parts partMap where
  accept'
                = accepting dfa
  notAccept = S.difference (states dfa) accept'
  parts
                = S.fromList [accept', notAccept]
               = toPartitionMap parts
  partMap
hopcroft' :: (Ord \ a, Show \ a) \Rightarrow
         DFA' \ a \rightarrow S.Set \ (S.Set \ Int) \rightarrow
            M.Map\ Int\ Int \rightarrow DFA'\ a
hopcroft' dfa set eqMap =
         if done then dfa' else recurse where
  done
                     = consistent' \equiv S.empty
  consistent' = consistent dfa eqMap \circ S.toList $ set
                     = buildDFA dfa eqMap
  dfa′
                     = hopcroft' dfa set' eqMap' where
  recurse
        set' = S.union (S.delete consistent' set)
          (partition dfa eqMap consistent')
        eqMap' = toPartitionMap set'
consistent :: (Ord a, Show a) \Rightarrow
            DFA' \ a \rightarrow M.Map \ Int \ Int \rightarrow
            [S.Set\ Int] \rightarrow S.Set\ Int
consistent \_ \_ [] = S.empty
consistent dfa eqMap (s:ss') =
            if continue then recurse else s where
  continue = (isConsistent dfa eqMap (S.toList s))
  recurse = consistent dfa eqMap ss'
buildDFA :: (Ord a, Show a) \Rightarrow DFA' a \rightarrow
         M.Map\ Int\ Int \rightarrow DFA'\ a
buildDFA dfa eqMap = DFA' alphabet' ss' accept' st' where
  alphabet'
                    = alphabet dfa
  ss'
                    = M.fromList oldStates
                    = S.map lookup' (accepting dfa)
  accept'
  st'
                     = lookup' (start dfa)
  newStates
                     = S.toList \circ S.fromList \circ M.elems \$ eqMap
                     = zip newStates \circ
  oldStates
     map (updateState dfa eqMap) ∘ map check $ newStates
```

```
check ns
                     = M.keys \circ M.filter (\equiv ns) \$ eqMap
  lookup'
                        = (eqMapM.!)
updateState :: (Ord \ a, Show \ a) \Rightarrow
               DFA' \ a \rightarrow M.Map \ Int \ Int \rightarrow
                 [Int] \rightarrow M.Map \ a \ Int
updateState dfa eqMap oldStates = update where
  update = M.map (eqMapM.!) \circ
     M.unions ◦ map fromJust ◦
     filter is Just ∘ map lookup' $ oldStates
  lookup' = flip M.lookup (trans dfa)
  -- Builds a partition map for equivalence look up
toPartitionMap :: S.Set (S.Set Int) \rightarrow M.Map Int Int
toPartitionMap = toPartitionMap' 0 M.empty ∘ S.toList
  toPartitionMap' \_acc[] = acc
  toPartitionMap' next acc (s:ss') =
     toPartitionMap' (next + 1) acc' ss' where
        acc' = S.fold insert acc s
        insert = flip M.insert next
  -- Partitions a given equivalence group
partition :: (Ord \ a, Show \ a) \Rightarrow DFA' \ a \rightarrow
         M.Map\ Int\ Int \rightarrow S.Set\ Int \rightarrow S.Set\ (S.Set\ Int)
partition dfa parts toPart =
         partition' S.empty dfa parts (S.toList toPart)
         where
  partition' acc \_ [] = acc
  partition' acc dfa parts (s:ss) =
     partition' acc' dfa parts ss' where
               = S.insert set acc
        acc'
        sMap = eqMap s
        matches = filter ((sMap \equiv) \circ eqMap) ss
        set
               = S.fromList (s: matches)
        ss'
               = filter elems ss
        elems x = \neg (S.member x set)
        eqMap \ x = eqMap' \ \mathbf{where}
          map' = M.lookup x (trans dfa)
          eqMap' =
```

```
if isNothing map' then
                M.empty
             else
                equivalenceMap parts o fromJust $ map'
  -- Determines if a set of states all have the same edges
isConsistent :: (Ord\ a, Show\ a) \Rightarrow
                 DFA' \ a \rightarrow M.Map \ Int \ Int \rightarrow [Int] \rightarrow Bool
isConsistent \_ \_ [] = True
isConsistent\ dfa\ partitions\ (s:ss) =
                 isConsistent' dfa partitions eqMap ss where
  map = M.lookup s (trans dfa)
  eqMap =
     if isNothing map then
          M.empty
     else
          equivalenceMap partitions o fromJust $ map
equivalenceMap :: M.Map Int Int \rightarrow
  M.Map \ a \ Int \rightarrow M.Map \ a \ Int
equivalence Map partitions map' =
                      M.mapWithKey updateKey map' where
  updateKey v = partitionsM.!v
isConsistent' :: (Ord a, Show a) \Rightarrow
                    DFA' a \rightarrow M.Map Int Int \rightarrow
                    M.Map \ a \ Int \rightarrow \lceil Int \rceil \rightarrow Bool
isConsistent' \_ \_ \_ [] = True
isConsistent' dfa partitions eqMap (s:ss') =
                    if consistent' then
                       recurse
                    else
                         False where
  consistent' = map' \equiv eqMap
  mMap = M.lookup s (trans dfa)
  map' =
     if isNothing mMap then
        M.empty
     else equivalenceMap partitions ∘ fromJust $ mMap
  recurse = isConsistent' dfa partitions eqMap ss'
```

```
-- Removes all unreachable states in a DFA'
dropUnreachable :: (Ord\ a, Show\ a) \Rightarrow DFA'\ a \rightarrow DFA'\ a
dropUnreachable dfa = dropUnreachable' set set dfa where
  set = S.singleton \$ start dfa
dropUnreachable' :: (Ord\ a, Show\ a) \Rightarrow
  S.Set\ Int \rightarrow S.Set\ Int \rightarrow DFA'\ a \rightarrow DFA'\ a
dropUnreachable' reachable_states new_states dfa =
  if done then dfa' else recurse where
  reachable'
     S.unions \circ S.toList \circ S.map (reachable dfa) new_states
  new states' =
     S.difference reachable' reachable_states
  reachable_states' =
     S.union reachable_states new_states'
  recurse
     dropUnreachable' reachable_states' new_states' dfa
  dfa'
     updateDFA dfa reachable_states'
                = new\_states' \equiv S.empty
  done
updateDFA :: (Ord\ a, Show\ a) \Rightarrow
         DFA' \ a \rightarrow S.Set \ Int \rightarrow DFA' \ a
updateDFA dfa reachable_states =
         DFA' alphabet' trans' accept' start' where
  unreachable states =
     S.difference (states dfa) reachable_states
  accept'
     S.difference (accepting dfa) unreachable_states
  alphabet'
                   = alphabet dfa
  start'
                   = start dfa
  trans'
                   = M.filterWithKey removeKey (trans dfa)
  removeKey k = S.member k reachable\_states
reachable :: (Ord a, Show a) \Rightarrow DFA' a \rightarrow Int \rightarrow S.Set Int
reachable fsa state = S.fromList ns  where
  trans'
               = M.lookup state (trans fsa)
               = if isNothing trans' then [] else ns'
  ns
  ns'
               = M.elems \circ from Just \$ trans'
  -- A test DFA that has several unreachable states: [3,4,5,6]
```

```
testDFA :: DFA' Char
testDFA = DFA' alpha' ss' accept' st' where
  alpha' = S.fromList "ab"
  ss'
    M.fromList [(0, trans0),
                     (1, trans1),
                     (2, trans2),
                     (3, trans3)]
  trans0 = M.fromList[('a',1),('b',2)]
  trans1 = M.empty
  trans2 = M.empty
  trans3 = M.fromList[('a',4),('b',5)]
  accept' = S.fromList [1, 2, 3, 6]
  st'
         = 0
  -- Tests the removal of unreachable states
testDroppable :: Bool
testDroppable = alphabet' \land states'
                        \land start' \land accepting' where
                = (alphabet dfa) \equiv (S.fromList "ab")
  alphabet'
  states'
                = (states\ dfa) \equiv (S.fromList\ [0,1,2])
  start'
                = (start dfa) \equiv 0
  accepting' = (accepting dfa) \equiv (S.fromList [1,2])
                = dropUnreachable testDFA
  dfa
  -- A test DFA that can be reduced
  -- to a single node with two edges
  -- it recognizes strings of the language (a|b) *
testDFA' :: DFA' Char
testDFA' = DFA' alpha' ss' accept' st' where
  alpha' = S.fromList "ab"
  ss'
         = M.fromList
               [(0, trans'),
                  (1, trans'),
                  (2, trans')]
  trans' = M.fromList[('a',1),('b',2)]
  accept' = S.fromList [0,1,2]
  st'
         = 0
```

-- Tests that hopcroft reduces testDFA' to a minimal dfa

```
testHopcroft :: Bool
testHopcroft = alphabet' \land states'
                      \land accepting' \land trans' where
  alphabet'
                 = (alphabet dfa) \equiv (S.fromList "ab")
                 = (states dfa) \equiv (S.fromList [start'])
  states'
  start'
                 = (start dfa)
  accepting' = (accepting \ dfa) \equiv (S.fromList \ [start'])
  trans'
                 = (trans \ dfa) \equiv (M.fromList \ [(start', trans0)])
  trans0
                 = M.fromList [('a', start'), ('b', start')]
  dfa
                 = hopcroft testDFA'
testPartition :: Bool
testPartition = partition' \equiv correctPartition where
  partition' = partition dfa parts toPart
  correctPartition = S.fromList [s1, s2, s3]
            = S.fromList [1, 2, 5]
  s1
  s2
            = S.fromList [3]
  s3
            = S.fromList [4,7]
  parts
            = M.fromList
              [(0,0),(6,0),
                 (1,1),(2,1),
                 (3,1),(4,1),
                 (5,1),(7,1)
  toPart
            = S.fromList [1, 2, 3, 4, 5, 7]
            = nonMinimalDFA
  dfa
nonMinimalDFA :: DFA' Char
nonMinimalDFA = DFA' alpha' ss' accept' st' where
       alpha' = S.fromList "ab"
       ss'
              = M.fromList
                     [(0, trans0), (1, trans1), (2, trans2),
                       (3, trans3), (4, trans4), (5, trans5),
                       (6, trans6), (7, trans7)]
       trans0 = M.fromList[('a',1)]
       trans1 = M.fromList[('a',4),('b',2)]
       trans2 = M.fromList[('a',3),('b',5)]
       trans3 = M.fromList[('b',1)]
       trans4 = M.fromList[('a',6),('b',5)]
       trans5 = M.fromList[('a',7),('b',2)]
```

```
trans6 = M.fromList [('a',5)]

trans7 = M.fromList [('a',0),('b',5)]

accept' = S.fromList [0,6]

st' = 0
```

5.1 Recognize a string for a given DFA

In this module we test whether a "string" from an alphabet for a DFA is accepted by that DFA or not.

```
module Recognize (match) where import FiniteStateAutomata import qualified Data.Map as M import qualified Data.Set as S
```

The function *match* takes an α DFA and list of α as input (a "string" in the language of that DFA), and returns true if the string is accepted by that DFA, and false otherwise. It is fairly straightforward.

```
match :: (Ord\ a, Show\ a) \Rightarrow DFA'\ a \rightarrow [a] \rightarrow Bool
match\ dfa = match'\ dfa\ (start\ dfa)\ \mathbf{where}
match'\ dfa\ curr\ [] = S.member\ curr\ (accepting\ dfa)
match'\ dfa\ curr\ (c:cs) =
\mathbf{let}\ labelMap = M.lookup\ curr\ (trans\ dfa)\ \mathbf{in}
\mathbf{case}\ labelMap\ \mathbf{of}
Nothing \rightarrow False
Just\ map \rightarrow \mathbf{let}\ labels = M.lookup\ c\ map\ \mathbf{in}
\mathbf{case}\ labels\ \mathbf{of}
Nothing \rightarrow False
Just\ next \rightarrow match'\ dfa\ next\ cs
```

6 Alphabet

This module provides functions for lexing and parsing alphabets found in input files, in addition to an alphabet token data structure.

```
module Alphabet (parseElement, parseAlphabet,
```

```
getAlphabet,
gotoGetAlphabet) where
import Data.List
import Parselib
import GHC.Unicode (isPrint)
import Data.Char (ord)
```

A formal description of an alphabet is:

The Haskell version of this might be written as follows:

```
data Alphabet =
  AlphabetToken |
  Symbol Char |
  EndToken deriving (Show, Eq)
```

The remaining functions find an alphabet in a file, tokenize, and generate a list of the symbols in the alphabet.

```
gotoAlphabet [] = []
gotoAlphabet cs | isPrefixOf "alphabet" cs = cs
gotoAlphabet (c:cs) = gotoAlphabet cs
-- old scanner
scanAlphabet [] = []
scanAlphabet ('a':'l':'p':'h':'a':'b':'e':'t':cs) =
AlphabetToken:scanAlphabet cs
scanAlphabet ('\":c:cs) =
Symbol c:scanAlphabet cs
scanAlphabet ('e':'n':'d':cs) =
```

```
[EndToken]
scanAlphabet (\_: cs) =
  scanAlphabet cs
  -- old parser
parseAlphabet'[] = []
parseAlphabet' (AlphabetToken: ts) =
  parseAlphabet' ts
parseAlphabet' (Symbol c:ts) =
  c: parseAlphabet' ts
parseAlphabet' (EndToken: ts) =
  getAlphabet' = parseAlphabet' \circ scanAlphabet \circ gotoAlphabet
  -- this was not a fun bug to track down
parseEscapedChar =
     do {string "\\n"; return '\n' }
   +++ do { string "\\t"; return '\t'}
   +++ do { string "\\v"; return '\v'}
   +++do { string "\\r"; return '\r' }
   +++ do { string "\\b"; return '\b' }
   +++do { string "\\a"; return '\a' }
   +++ do { string "\\f"; return '\f' }
   + + + do \{ string " \ "; return ' \ ' \}
printablePlus char =
  let ascii = ord char in
  (ascii \geqslant 7 \land ascii \leqslant 13)
   \lor (ascii \geqslant 32 \land ascii \leqslant 126)
parseElement :: Parser Char
parseElement = do
  space
  char'\"
  c \leftarrow
    parseEscapedChar + + +
    sat printablePlus
  return c
parseAlphabet :: Parser [Char]
parseAlphabet = do
```

```
space
string "alphabet"
alphabet ← many parseElement
space
string "end;" + + + string "end" -- need because test file
return alphabet

getAlphabet file =
    case (parse parseAlphabet) file of
    [] → error "Alphabet is empty (no alphabet provided)."
    regex → (fst o head) regex
-- to skip beginning contents and read alphabet
gotoGetAlphabet file =
    case (parse parseAlphabet) (gotoAlphabet file) of
    [] → error "Alphabet is empty (no alphabet provided)."
    regex → (fst o head) regex
```

7 Input

Similar to the Algorithms module, in this module we gather all of our solutions for problems 5-8, which deals with file input/output.

Module *ParseFSA* parses either DFAs or FSAs from text file descriptions; *ParseReg* parses regular expressions from text files (with an alphabet) and tests whether symbols occuring in the regular expression are elements of the alphabet provided in the file; and lastly *ParseLang* provides a data structure for lexical descriptions, reads in a complete lexical description from a text file, and transforms it into our internal representation, for use with the algorithms in the *Algorithms* module.

```
module Input (
module ParseFSA,
module ParseReg,
module ParseLang) where
import ParseFSA
import ParseReg
import ParseLang
```

7.1 Parse a Regular Expression

This module inputs, lexes, and parses a regular expression from a text file. It uses Hutton's Parselib library.

Parsing is divided into a function for each regular expression. It handles ascii spaces, newlines, tabs, etc. In other words, the printable subset of ascii, as required by the spec.

It uses the functions provided by the *Alphabet* module to lex elements from the alphabet properly (escapes, newlines, etc.), and additionally, correctly error checks whether a terminal symbol is an element of the alphabet provided in either a regular expression file or a lexical description.

```
module ParseReg (getRegex, parseRegex) where
import Alphabet
import Regex
import Parselib
type Alphabet = [Char]
parseAlt :: Alphabet \rightarrow Parser (Regex Char)
parseAlt \ alphabet = \mathbf{do}
  string " | "
  space
  regex \leftarrow parseRegex \ alphabet
  regex' \leftarrow parseRegex alphabet
  return (Alt regex regex')
parseConcat :: Alphabet \rightarrow Parser (Regex Char)
parseConcat \ alphabet = do
  string "+"
  space
  regex \leftarrow parseRegex alphabet
  space
  regex' \leftarrow parseRegex alphabet
  return (Concat regex regex')
parseKleene :: Alphabet \rightarrow Parser (Regex Char)
parseKleene alphabet = do
  string " * "
  space
```

```
regex \leftarrow parseRegex \ alphabet
  return (Kleene regex)
parseTerm :: Alphabet \rightarrow Parser (Regex Char)
parseTerm\ alphabet = do
  c \leftarrow parseElement
  if \neg (elem c alphabet) then
    let msg = "Regular expression contains terminal "
        ++ show c
        # " which is not an element of the"
        + " alphabet provided." in
       error msg
  else
     return (Term c)
parseRegex :: Alphabet \rightarrow Parser (Regex Char)
parseRegex alphabet = do
  space
  parseAlt\ alphabet + + +
    parseConcat alphabet + + +
    parseKleene alphabet + + +
    parseTerm alphabet
  -- takes an alphabet
getRegex :: String \rightarrow Alphabet \rightarrow Regex Char
getRegex file alphabet =
  case (parse (parseRegex alphabet)) file of
     ] \rightarrow error "Could not parse regular expression."
     regex \rightarrow (fst \circ head) regex
  -- example, should error
readRegex1 = do
  source ← readFile "regexp3.txt"
     -- get alphabet before, because alphabet is after
  let alphabet = gotoGetAlphabet source
  let regex = getRegex source alphabet
  putStrLn $ show regex
readRegex file = do
  source \leftarrow readFile file
  let alphabet = gotoGetAlphabet source
  let regex = getRegex source alphabet
```

7.2 Parse an FSA

In this module we parse a description of an DFA or an NFA and return the appropriate data structure.

Since the formal definition of a lexical description of a language does not contain a description of an NFA or a DFA (only regular expressions), this module was simply used on the provided test cases, and for a basic sanity check on whether our implementation for NFAs and DFAs was correct.

It uses Haskell's Parsec library for parsing.

```
{-# LANGUAGE FlexibleContexts #-}
module ParseFSA (parseNFA, parseDFA) where
import Data.Functor
import qualified Data.Set as S
import qualified Data.Map as M
import FiniteStateAutomata
import Text.Parsec
data Transition = NFAT \{ fromState :: String, \}
    symbols :: [Char],
    toState :: String }
   | DFAT { fromState :: String,
    symbol :: Char,
    toState :: String }
instance Show Transition where
  show (NFAT f ss t) = "NFAT " + f + + " " + (show ss) + + " -> " + t
  show (DFAT f s t) = "DFAT " + f + + " " + (show s) + + " -> " + t
data Description = Description { states' :: [String],
  startState :: String,
  acceptStates :: [String],
  trans' :: [Transition] } deriving Show
parseNFA :: [Char] \rightarrow String \rightarrow NFA' Char
parseNFA = parseFSA "nfa" (NFA') (toNFAMap)
parseDFA :: [Char] \rightarrow String \rightarrow DFA' Char
parseDFA = parseFSA "dfa" (DFA') (toDFAMap)
```

```
parseFSA typ constr toMap alpha s =
  case parse (description typ isNFA) "Syntax Error" s of
     Left er \rightarrow error \circ show \$ er
     Right desc \rightarrow convertToFSA alpha desc constr toMap
  where isNFA = if typ \equiv "nfa" then True else False
convertToFSA :: FSA f \Rightarrow [Alpha f] \rightarrow Description \rightarrow
   (S.Set\ (Alpha\ f) \rightarrow M.Map\ Int\ (FSAVal\ f) \rightarrow S.Set\ Int \rightarrow Int \rightarrow f) \rightarrow
   (M.Map\ String\ Int \rightarrow [Transition] \rightarrow M.Map\ Int\ (FSAVal\ f)) \rightarrow
  f
convertToFSA alpha desc const toMap = const alphabet nfaMap accepting start where
  normal = M.fromList \$ zip (states' desc) [0..]
  alphabet = S.fromList alpha
  nfaMap = (toMap normal) \circ trans' \$ desc
  accpting = S.fromList \circ map (normalM.!) \circ acceptStates \$ desc
  start = normalM.!(startState desc)
toNFAMap :: M.Map \ String \ Int \rightarrow [Transition] \rightarrow NFAMap \ Char
toNFAMap \ m \ ts = M.fromList \circ map \ convert \circ M.toList \circ go \ ts \$ M.empty \ \mathbf{where}
  convert (s, es) = (mM.!s, S.fromList \circ map (\lambda(c, s2) \rightarrow (c, mM.!s2)) \$es)
  toM "" = [Nothing]
  toM s = map \ Just s
  go[]acc = acc
  go ((NFAT f syms t) : ts) acc = case M.lookup f acc of
     Nothing \rightarrow go ts $ M.insert f (zip (toM syms) (repeat t)) acc
     Just es \rightarrow go ts $ M.insert f ((zip (toM syms) (repeat t)) ++ es) acc
toDFAMap :: M.Map \ String \ Int \rightarrow [Transition] \rightarrow DFAMap \ Char
toDFAMap \ m \ ts = M.fromList \circ map \ convert \circ M.toList \circ go \ ts \$ M.empty \ \mathbf{where}
  convert (s, es) = (mM.!s, M.fromList \circ map (\lambda(c, s2) \rightarrow (c, mM.!s2)) \$es)
  go[]acc = acc
  go ((DFAT f symb t) : ts) acc = case M.lookup f acc of
     Nothing \rightarrow go ts $ M.insert f [(symb, t)] acc
     Just es \rightarrow go ts $ M.insert f ((symb, t) : es) acc
description :: Stream s m Char \Rightarrow
           String \rightarrow
           Bool \rightarrow
           ParsecT s u m Description
description keyword is NFA = \mathbf{do}
  spaces \gg string \ keyword \gg spaces
```

```
stats ← statelist "states" "end; " identifier
  initState ← initialState "initial"
  acceptStates ← statelist "accept" "end; "identifier
  trans \leftarrow statelist "transitions" "end; " (transition isNFA)
  return $ Description stats initState acceptStates trans
transition :: Stream s m Char \Rightarrow
  Bool \rightarrow
  ParsecT s u m Transition
transition isNFA = do
  from \leftarrow identifier
  syms \leftarrow option [] symbolList
  string "->" ≫ spaces
  to \leftarrow identifier
  return $ case isNFA of
     True \rightarrow NFAT from syms to
     False \rightarrow DFAT from (head syms) to
initialState :: Stream \ s \ m \ Char \Rightarrow String \rightarrow ParsecT \ s \ u \ m \ String
initialState\ keyword = string\ keyword \gg spaces \gg identifier
parseStringOrTerm :: Stream s m Char \Rightarrow String \rightarrow
  ParsecT s u m a \rightarrow
  ParsecT s u m (Either String a)
parseStringOrTerm\ term\ s = \mathbf{do}
  ter \leftarrow try \$ optionMaybe \$ string term
  case ter of
     Just t \rightarrow return \$ Left t
     Nothing \rightarrow Right < $ > s
statelist :: Stream s m Char \Rightarrow
  String \rightarrow
  String \rightarrow
  ParsecT s u m a \rightarrow
  ParsecT s u m [a]
statelist startTok endTok elem = do
  string\ startTok \gg spaces
  reverse < $ > parseSets' [] where
     parseSets' acc = do
        sOrT \leftarrow parseStringOrTerm\ endTok\ elem
        spaces
```

```
case sOrT of
            Left \_ \rightarrow return acc
            Right \ str \rightarrow parseSets' \ str : acc
identifier :: Stream s m Char \Rightarrow ParsecT s u m String
identifier = do
   i \leftarrow many1 \ alphaNum
   spaces
   return i
sym :: Stream \ s \ m \ Char \Rightarrow ParsecT \ s \ u \ m \ Char
sym = do
   char'\"
   c \leftarrow anyChar
   case c of
      ' \setminus \setminus ' \rightarrow do
         c2 \leftarrow anyChar
         return \$ read \$ "' \setminus " + [c2] + "'"
      _{-} \rightarrow return c
symbolList :: Stream \ s \ m \ Char \Rightarrow ParsecT \ s \ u \ m \ [Char]
symbolList = sym 'sepEndBy1' (spaces)
```

7.3 Parse a Lexical Description of a Programming Language

In this module we parse a lexical description of a language, and prepare it for parsing with respect to our previous data structures and algorithms. It also uses Hutton's Parselib.

```
{-# LANGUAGE TypeFamilies, FlexibleContexts,FlexibleInstances #-}
module ParseLang where
import Parselib
import Regex
import ParseReg
import FiniteStateAutomata
import Alphabet
import Data.Char (isSpace)
import Data.List (intersperse)
```

We use a data structure *Desc* to internally represent a lexical description. *Desc* is a basic record type, with three functions, *language*, *symbols*,

and *classes* which return the name of the language as a string, the alphabet, and a list of classes given by the lexical description, respectively.

The data structure *Class* is another record type with three functions, *name*, *regex*, and *relevance*, which return the name of the class, the regular expression which describes it, and its semantic relevance, respectively.

Thus to obtain obtain an NFA equivalent of the regular expression for the first class given in a parsed lexical description l, we write: ($thompson \circ regex \circ head \circ classes$) l.

```
type Identifier = String
data Relevance = Relevant | Irrelevant | Discard
instance Show Relevance where
  show (Relevant) = "relevant"
  show (Irrelevant) = "irrelevant"
  show (Discard) = "discard"
data Class = Class  {
  name::Identifier,
  regex :: Regex Char,
  relevance :: Relevance }
instance Show Class where
  show (regex c) ++ " " ++
    show (relevance c) ++
    " end; "
data Desc = Desc  {
  language :: String,
  symbols :: [Char],
  classes :: [Class]
showAlphabet a = "'" ++ (intersperse ' \setminus "a)
instance Show Desc where
  show desc =
    "language: " ++ language desc ++ "\n" ++
    "alphabet: " ++
    showAlphabet (symbols desc) ++
    " end; " ++ " \n" ++
    "classes: " # " \n" #
```

```
unlines (map show (classes desc)) ++
" end;"
```

The remaining functions parse a text file of a lexical description, and deposit that description (if it is well-formed) into our data structure.

```
parseLangIdentifier :: Parser String
parseLangIdentifier = do
  ident \leftarrow many \$ sat (\neg \circ isSpace)
  return ident
parseRelevance :: Parser Relevance
parseRelevance =
     do {string "relevant"; return Relevant} + + +
     do {string "irrelevant"; return Irrelevant } + + +
     do {string "discard" ;return Discard}
parseClass :: [Char] \rightarrow Parser Class
parseClass\ alphabet = do
  space
  string "class"
  space
  name \leftarrow parseLangIdentifier
  space
  string "is"
  regex \leftarrow parseRegex alphabet
  relevance \leftarrow parseRelevance
  space
  string "end; "
  return $ Class name regex relevance
parseLang :: Parser Desc
parseLang = do
  space
  string "language"
  space
  language \leftarrow parseLangIdentifier
  alphabet \leftarrow parseAlphabet
  classes ← many $ parseClass alphabet
  space
```

```
string "end; "
  return (Desc language alphabet classes)
getLang :: String \rightarrow Desc
getLang\ desc = do
  case (parse parseLang) desc of
     ] \rightarrow error "Could not parse lexical description."
     regex \rightarrow (fst \circ head) regex
  -- example
readLang1 = do
  source ← readFile "tests/lexdesc3.txt"
  let x = (parse \ parseLang) source
  putStrLn $ show x
readLang file = do
  source \leftarrow readFile file
  let x = (parse \ parseLang) source
  putStrLn $ show x
```

7.4 Scanner Generator

This module performs the work necessary to output a scanner, thus making our implementation a scanner *generator*.

From a given lexical description, we first alternate all of the regular expressions found in the classes, then kleene star the entire expression; we then apply Thompson's algorithm, generate a dfa from the nfa (subset construction), and finally apply Hopcroft's minimization algorithm.

We then construct (and output to stdout) a Haskell program, which when compiled, will accept only those strings given by the language description that we were originally given. I.e., the scanner takes a file, <file>, as a command line argument, and returns the result of the function *match* (our implementation of algorithm 4) applied to the generated DFA and the strings in <file>.

```
module ScannerGenerator (scannerGenerator) where
import Regex
import Algorithms
import Input
import System.Environment (getArgs)
```

```
alternate :: [Class] \rightarrow Regex Char
alternate [] = Empty
alternate (c:[]) = regex c
alternate(c:cs) =
  Alt (regex c) (alternate cs)
scannerGenerator :: String \rightarrow String
scannerGenerator desc = program where
  regex = Kleene \circ alternate \circ classes \circ getLang \$ desc
  dfa = hopcroft \circ subsetConstruction \circ thompson \$ regex
  program = "module Main where\n" ++
     "import FiniteStateAutomata(DFA'())\n" ++
     "import Recognize (match) \n" ++
     "import System.Environment(getArgs)\n" ++
     "dfa :: DFA' Char\n" ++
     "dfa = read \"" +
     (replace''''') (show dfa) ++ "\n" ++
     "main = do \n \t args <- getArgs\n" ++</pre>
     "\t let [contents] = args\n" ++
     "\t string <- readFile contents\n" ++
     "\t putStrLn $ (show (match dfa string))\n"
replace :: (Eq a) \Rightarrow a \rightarrow [a] \rightarrow [a] \rightarrow [a]
replace \ a \ b = concatMap \ replace' \ \mathbf{where}
  replace' x = \mathbf{if} \ a \equiv x \ \mathbf{then} \ b \ \mathbf{else} \ [x]
```

8 Module: Main.lhs

The final module, *Main*, puts everything together, by simply calling the function *scannerGenerator* on a lexical description to output a scanner to stdout.

```
module Main where

import System.Environment

import ScannerGenerator (scannerGenerator)

main = do

args \leftarrow getArgs

let [contents] = args
```

file ← readFile contents
putStrLn \$ scannerGenerator file

Thus, given a lexical description for a language \mathcal{L} in a file <code>desc.txt></code>, a string in file <code>string.txt></code> (which may or may not be a string in the language \mathcal{L}), and the binary <code>desc.txt></code> compiled from our Haskell source code, the following sequence of commands in a GNU/Linux environment will produce a scanner for \mathcal{L} and will test whether <code>desc.txt></code> is a string in \mathcal{L} :

```
./gen desc.txt > scanner.hs
ghc --make scanner.hs -o scanner
./scanner string.txt
```