Project 2: Grammar Analysis and Parsing

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1 Introduction

This report contains our implementation of a scanner and parser for context free grammars, a series of hygiene functions for sterilizing the grammar, and finally a parser *for* the grammar specified in the context free grammar.

It is divided up into several sections, roughly corresponding to the problems given in the specification, each a Haskell module. The work was split up evenly amongst the group members, and approximately 40 man hours went into the final preparation of this document, the source code, unit testing, and related work.

2 Context Free Grammar

In this section we provide the context free grammar data type.

At its heart, a grammar it consists of a list of productions, where each production consists of a constructor and two arguments; the first a paramaterized nonterminal, and the second a paramaterized right hand side.

An *RHS* is either empty, a terminal, which takes two arguments — the paramaterized object representing a terminal, and another *RHS*; or a non-terminal, which similarly takes two arguments.

```
{-# LANGUAGE FlexibleInstances, MultiParamTypeClasses #-} module ContextFreeGrammar (Grammar, Production (...), RHS (...), module Dropable, nonTerminals, terminals, Terminal (...)) where import <math>Dropable import Filterable import Filterable import Prelude\ hiding\ (drop\ filter) type Grammar\ nt\ t = [Production\ nt\ t]
```

```
data Terminal t = Epsilon \mid EOF \mid Terminal \ t \ deriving (Show, Eq. Ord)
instance (Eq \ nt) \Rightarrow Dropable \ nt \ (Grammar \ nt \ t) where
  drop \ x \ grammar = map \ (drop \ x) \ grammar
instance Filterable (nt \rightarrow Bool) (Grammar nt \ t) where
  filter\ pred\ grammar = map\ (filter\ pred)\ grammar
data Production nt \ t = Production \{ nonterminal :: nt, \}
  rhs :: RHS \ nt \ t \} \ deriving (Eq, Ord)
instance Show (Production String String) where
  show (Production \ nt \ rhs) = nt + " -> " + show \ rhs
instance Show (Production Char Char) where
  show (Production \ nt \ rhs) = show \ nt ++ " -> " ++ show \ rhs
instance (Eq\ nt) \Rightarrow Dropable\ nt\ (Production\ nt\ t) where
  drop \ x \ (Production \ nt \ rhs) = Production \ nt \ (drop \ x \ rhs)
instance Filterable (nt \rightarrow Bool) (Production nt \ t) where
  filter\ pred\ (Production\ nt\ rhs) = Production\ nt\ (filter\ pred\ rhs)
data RHS nt t = Empty
    Term\ t\ (RHS\ nt\ t)
   | NonT \ nt \ (RHS \ nt \ t) \ deriving \ (Eq, Ord)
instance Show (RHS String String) where
  show \ Empty = ""
  show (Term \ t \ rhs) = "" + t + (show \ rhs)
  show (NonT \ nt \ rhs) = " " + nt + (show \ rhs)
instance Show (RHS Char Char) where
  show \ Empty = ""
  show (Term \ t \ rhs) = show \ t + (show \ rhs)
  show (NonT \ nt \ rhs) = show \ nt + (show \ rhs)
instance (Eq\ nt) \Rightarrow Dropable\ nt\ (RHS\ nt\ t) where
  drop \ x \ (NonT \ nt \ rhs)
     | x \equiv nt = drop \ x \ rhs
     | otherwise = (NonT \ nt \ (drop \ x \ rhs))
  drop \ x \ (Term \ t \ rhs) = Term \ t \ (drop \ x \ rhs)
  drop \ \_Empty = Empty
instance Filterable (nt \rightarrow Bool) (RHS nt\ t) where
  filter \_Empty = Empty
  filter\ pred\ (Term\ t\ rhs) = (Term\ t\ (filter\ pred\ rhs))
  filter\ pred\ (NonT\ nt\ rhs) =
     if pred nt then (NonT nt (filter pred rhs)) else (filter pred rhs)
```

nonTerminals takes the RHS of a Production and returns a list of all Non Terminals

```
nonTerminals :: RHS \ nt \ t \rightarrow [nt]

nonTerminals \ (NonT \ nt \ rhs) = nt : nonTerminals \ rhs

nonTerminals \ (Term \ rhs) = nonTerminals \ rhs

nonTerminals \ Empty = []
```

terminals takes the RHS of a Production and returns a list of all Terminals

```
terminals :: RHS \ nt \ t \rightarrow [t] \\ terminals \ (Term \ t \ rhs) = t : terminals \ rhs \\ terminals \ (NonT \ \_rhs) = terminals \ rhs \\ terminals \ Empty = [] \\ simple Grammar :: Grammar \ String \ String \\ simple Grammar = [a, b, c, d] \ \mathbf{where} \\ a = Production \ "A" \ (Term \ "a" \ Empty) \\ b = Production \ "B" \ (NonT \ "B" \ Empty) \\ c = Production \ "C" \ (Term \ "a" \ (NonT \ "B" \ Empty)) \\ d = Production \ "D" \ (NonT \ "B" \ (Term \ "a" \ Empty))
```

3 Scanner and Parser for context-free grammars

In this section we provide code for a simple scanner and parser for a textual representation of a context free grammar.

The grammar for the concrete representation follows the suggestion in the assignment, with one minor difference:

```
Grammar -> Grammar Production
Grammar -> Production
Production -> UpperSymbol Arrow RHS
RHS -> RHS Symbol
RHS ->
Symbol -> UpperSymbol
Symbol -> AlphaNumSymbol
```

In other words, non-terminals are restricted to their first letter being upper case, terminals are sequences of alphanumeric characters where the first character cannot be upper-case, and right hand side terminals and non-terminals are delimited by spaces.

A couple helper functions are initially defined, in addition to the grammar token data structure, which is as follows:

```
module ScanAndParse (sparse) where

import ContextFreeGrammar

import Data.Char (isUpper, isSpace, isAlphaNum, isAlpha, isDigit)

data GrammarToken =

Symbol\ String\ |

ArrowToken\ |

NewLineToken\ deriving\ (Show, Eq)

alphanumeric = takeWhile\ isAlphaNum

drop'\ _[\ ] = [\ ]

drop'\ i\ (x:xs) =

if i\leqslant 0\ then\ (x:xs)

else

drop'\ (i-1)\ xs
```

The scanner is a simple function that checks for two special characters, the arrow, -> and the newline character, \n, scans symbols for nonterminals or terminals, and returns their appropriate tokens.

If a non alphanumeric character is found, the scanner returns an error.

```
scan :: String \rightarrow [GrammarToken]
scan [] = []
scan ('-':'>':cs) = ArrowToken : scan cs
scan ('\n':cs) = NewLineToken : scan cs
scan (c:cs) \mid isSpace \ c = scan \ cs
scan s@(c:cs) \mid isAlphaNum \ c =
let \ name = alphanumeric \ s
len = length \ name \ in
(Symbol \ name) : scan \ (drop' \ len \ s)
scan \ s@(c:cs) =
error ("lexical \ error; " + c:" \ is \ an \ unrecognized \ character.")
```

The parser generates a list of productions, i.e., a "grammar", from a list of grammar tokens. The helper function, *parseRHS*, will throw a syntax error if an arrow token is found on the right hand side.

The function *parse* will throw an error if multiple non-terminals occur on the left-hand side, or an arrow is missing.

```
parseRHS :: [GrammarToken] \rightarrow ((RHS String String), [GrammarToken])
parseRHS[] =
  (Empty, [])
parseRHS (NewLineToken: rhs) =
  (Empty, rhs)
parseRHS (ArrowToken: rhs) =
  error "syntax error; arrow token found on right hand side"
parseRHS ((Symbol (c:cs)):rhs) =
  let (term, rhs') = parseRHS rhs in
  if isUpper\ c then
    ((NonT (c:cs) term), rhs')
    ((Term\ (c:cs)\ term), rhs')
parse :: [GrammarToken] \rightarrow GrammarStringString
parse[] = []
parse\ (NewLineToken: p) = parse\ p
parse ((Symbol s) : ArrowToken : rhs) =
  let (production, rhs') = parseRHS rhs in
  (Production \ s \ (production)) : parse \ rhs'
parse ((Symbol \ s) : rhs) =
  error "Missing arrow or multiple non-terminals on left-hand side."
sparse = parse \circ scan
```

4 Hygiene Module

In this module, we perform basic hygiene checks on the grammar, remove unreachable non terminals, etc.

```
module BadHygiene (computeReachable, eliminateUnreachable, computeGenerating, eliminateNonGenerating, eliminateUseless, isEmptyGrammar) where import ContextFreeGrammar import qualified Data.Set as S import Filterable import ScanAndParse
```

{-BEGIN CLEANING FUNCTIONS -}

computeReachable finds the Set of all Non Terminals of a Grammar that can be reached from the start node.

```
compute Reachable :: Ord \ nt \Rightarrow Grammar \ nt \ t \rightarrow S.Set \ nt compute Reachable \ [] = S.empty compute Reachable \ ps = go \ (S.singleton \circ nonterminal \circ head \ ps) \ (concat \circ replicate \ (length \ go \ marked \ [] = marked go \ marked \ ((Production \ nt \ rhs) : prs) = \mathbf{if} \ S.member \ nt \ marked \mathbf{then} \ go \ marked' \ prs \mathbf{else} \ go \ marked \ prs \mathbf{vhere} \ marked' = S.union \ marked \circ S.fromList \circ nonTerminals \ rhs eliminate \ Unreachable \ removes \ all \ unreachable \ Non \ Terminals \ from \ a
```

eliminateUnreachable removes all unreachable Non Terminals from a Grammar.

```
eliminate Unreachable :: Ord nt \Rightarrow Grammar \ nt \ t \rightarrow Grammar \ nt \ t
eliminate Unreachable g = clean Grammar \ where
reachable = compute Reachable \$ g
-- unnecessary? By definition, the unreachable non-terminals cannot be in any
-- other production list.
-- clean Productions = Filterable. filter ('S. member' reachable) g
clean Grammar = Prelude. filter (\lambda(Production \ nt \ rhs) \rightarrow S. member \ nt \ reachable) g
```

compute Generating finds the Set of all Non Terminals of a Grammar that can produce a string of Terminals.

```
 \begin{array}{l} compute Generating :: (Ord \ nt, Ord \ t) \Rightarrow Grammar \ nt \ t \rightarrow S.Set \ nt \\ compute Generating \ [] = S.empty \\ compute Generating \ ps = go \ S.empty \ (concat \circ replicate \ (length \ ps) \ ps) \ \textbf{where} \\ all Terms = S.from List \circ concat Map \ (terminals \circ rhs) \ ps \\ go \ marked NT \ [] = marked NT \\ go \ marked NT \ ((Production \ nt \ rhs) : prs) = \textbf{if} \ (all \ (`S.member`all Terms) \circ terminals \ rhs) \\ (all \ (`S.member`marked NT) \circ non Terminals \ rhs) \\ \textbf{then} \ go \ (S.insert \ nt \ marked NT) \ prs \\ \textbf{else} \ go \ marked NT \ prs \end{array}
```

 $eliminate Non Generating \ {\bf removes \ all \ non \ Generating \ Non \ Terminals \ from \ a \ Grammar.}$

```
eliminateNonGenerating :: (Ord\ nt, Ord\ t) \Rightarrow Grammar\ nt\ t \rightarrow Grammar\ nt\ t
eliminateNonGenerating\ g = cleanGrammar\ \mathbf{where}
```

```
generating = computeGenerating g

cleanProductions = Filterable.filter ('S.member'generating) g

cleanGrammar = Prelude.filter (\lambda(Production nt rhs) \rightarrow S.member nt generating) cleanPr
```

eliminate Useless removes all non Generating and unreachable Non Terminals from a Grammar.

```
eliminateUseless :: (Ord\ nt, Ord\ t) \Rightarrow Grammar\ nt\ t \rightarrow Grammar\ nt\ t
eliminateUseless = eliminateUnreachable \circ eliminateNonGenerating
```

is Empty Grammar determines if a Grammar will produce any strings at all.

```
is Empty Grammar :: (Ord \ t, Ord \ nt) \Rightarrow Grammar \ nt \ t \rightarrow Bool is Empty Grammar \ [] = True is Empty Grammar \ g = \neg \circ elem \ nt \circ map \ nonterminal \ \$ \ g' \ \mathbf{where} g' = eliminate Non Generating \ g (Production \ nt \ \_) = head \ g \{-\text{END CLEANING FUNCTIONS -}\}
```

5 Nullable, First, and Follow

In this section, we provide several modules for computing the nullable, first and follow sets of a given context free grammar, respectively.

5.1 Nullable

Here we compute whether a production is nullable or not.

```
module Nullable (nullable) where
import ContextFreeGrammar
import qualified Data.Set as S
import Prelude hiding (drop)

type Set = S.Set

nullable :: (Ord nt) \Rightarrow Grammar nt t \rightarrow Set nt

nullable = nullable' S.empty

nullable' :: (Ord nt) \Rightarrow Set nt \rightarrow Grammar nt t \rightarrow Set nt

nullable' set grammar = set'' where

set'' = if nulls \equiv set then set else set'
```

```
set' = nullable' \ nulls \ (S.fold \ drop \ grammar \ nulls)
nulls = S.fromList \circ map \ nonterminal \circ filter \ isNull \ $\$ \ grammar \ isNull :: Production \ nt \ t \to Bool
isNull \ (Production \ \_Empty) = True
isNull \ \_= False
simple Grammar :: Grammar \ String \ String
simple Grammar = [a] \ \mathbf{where}
a = Production \ "A" \ (Term \ "ab" \ Empty)
simple Grammar 2 :: Grammar \ String \ String
simple Grammar 2 :: Grammar \ String \ String
simple Grammar 2 :: Grammar \ String \ String
simple Grammar 2 :: Grammar \ String \ String
simple Grammar 2 :: Grammar \ String \ String
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simpl
```

5.2 First

In this section, we compute the first set for a context-free grammar.

```
module First (first) where
import ContextFreeGrammar
import Control.Monad.State
import Data.Functor
import Data.List
import qualified Data.Map as M
import Data.Maybe
import Nullable
import ScanAndParse
import qualified Data.Set as S
import Test.HUnit hiding (State)
```

first is the interface function exported for general use. Given a Grammar, first computes the First Set for each Production, and returns the Sets in a Map from a Non-terminal to it's First Set.

```
first :: (Ord \ nt, Ord \ t)
\Rightarrow Grammar \ nt \ t
```

```
\rightarrow M.Map nt (S.Set (Terminal t))
first g = firsts \circ execState \ state \circ FS \ M.empty \circ nullable \$ g \ \mathbf{where}
state = mapM \ first' \circ concat \circ replicate \ (length \ g) \$ g
```

The FirstState Data Type stores the map of Sets of First Terminals that is modified and returned at the end of a call to first. It also stores the set of Non-terminals which are nullable.

```
data FirstState nt t = FS {
    firsts :: M.Map nt (S.Set (Terminal t)),
    nulls :: S.Set nt
}
type Environment nt t a = State (FirstState nt t) a
```

first' does the work for the first function. Given a production, first' will calculate the set of first terminals and store it in the implicit FirstState.

```
first':: (Ord nt, Ord t) \Rightarrow Production nt t \rightarrow Environment nt t ()
first' (Production nt rhs) = \mathbf{do}

fs \leftarrow get

let mp = firsts fs

case rhs of

Empty \rightarrow case M.lookup nt mp of

Nothing \rightarrow put fs {firsts = M.insert nt (S.singleton Epsilon) mp}

Just _{-} \rightarrow put fs {firsts = M.adjust (S.insert Epsilon) nt mp}

_{-} \rightarrow \mathbf{do}

sets \leftarrow firstRHS rhs

let s = fromMaybe S.empty (M.lookup nt mp)

put fs {firsts = M.insert nt (S.unions (s:sets)) mp}
```

firstRHS is a helper function which, given a RHS will return the first sets of every terminal and non-terminal until a non nullable terminal/nonterminal is found.

```
case S.member y nlls of

True \rightarrow do

set \leftarrow getFirsts y

sets \leftarrow firstRHS ys

return (set: sets)

False \rightarrow (:[]) < $ > getFirsts y
```

getFirsts is a helper function which given a Non-terminal will return its current first set.

```
getFirsts :: Ord \ nt \Rightarrow nt \rightarrow Environment \ nt \ t \ (S.Set \ (Terminal \ t))
qetFirsts \ nt = do
  set \leftarrow (M.lookup\ nt) < \$ > gets\ firsts
  \mathbf{case}\ set\ \mathbf{of}
     Nothing \rightarrow return \ S.empty
     Just\ set 
ightarrow return\ set
 {- BEGIN TESTS - -}
makeTestM :: (Eq \ a, Show \ a)
   \Rightarrow String
   \rightarrow FilePath
   \rightarrow String
   \rightarrow a
   \rightarrow (Grammar String String \rightarrow a)
   \rightarrow Test
makeTestM name file forF e f = TestLabel name \circ TestCase \$ do
  grammar \leftarrow fmap \ sparse \circ readFile \ file
  assertEqual\ for F\ e\ (f\ grammar)
testFirst = makeTestM "testFirst"
   "tests\\test1.txt"
  "for first with test1"
  expected
  first where
  expected = M.fromList [("A", S.singleton \circ Terminal \$ "a"),
     ("B", S.fromList [Terminal "b",
        Terminal "a",
        Epsilon]),
     ("C", S.fromList [Terminal "a",
        Terminal "b",
        Epsilon]),
        ("D", S.fromList [Terminal "a",
```

```
Terminal "b",
         Epsilon])]
testFirst2 = makeTestM "testFirst2"
  "tests\\39.txt"
  "for first with 39"
  expected
  first where
  expected = M.fromList [("T", S.fromList [Epsilon, Terminal "a", Terminal "b"]),
    ("R", S.fromList [Epsilon, Terminal "b"])]
tests = TestList [testFirst,
  testFirst2
runTests :: IO\ Counts
runTests = runTestTT tests
doTestsPass :: IO\ Bool
do TestsPass = \mathbf{do}
  counts \leftarrow runTests
  let \ errs = errors \ counts
    fails = failures \ counts
  return \$ (errs \equiv 0) \land (fails \equiv 0)
 {- END TESTS - -}
```

5.3 Follow

In this section, we implement a function *follow* which calculates the follow set for our data structure of production grammars.

```
module Follow (follow) where
import ContextFreeGrammar
import Control.Monad.State
import Data.Functor
import qualified Data.Map as M
import Data.Maybe
import qualified Data.Set as S
import First
import Nullable
import ScanAndParse
import Test.HUnit hiding (State)
```

A GrammarState holds data that the follow' function requires to work.

```
data GrammarState nt t = GS {
    grammar :: Grammar nt t,
    follows :: M.Map nt (S.Set (Terminal t)),
    firsts :: M.Map nt (S.Set (Terminal t))
}

type Environment nt t a = State (GrammarState nt t) a
```

follow is the interface function exported for general use. Given a Grammar, follow computes the Follow Set for each Production, and returns the Sets in a Map from a Non-terminal to it's Follow Set.

```
 follow :: (Ord \ nt, Ord \ t) \\ \Rightarrow Grammar \ nt \ t \\ \rightarrow M.Map \ nt \ (S.Set \ (Terminal \ t)) \\ follow \ [] = M.empty \\ follow \ g@((Production \ s \ rhs) : ps) = fs \ \mathbf{where} \\ state = mapM \ follow' \circ concat \circ replicate \ (length \ g) \ \$ \ g \\ fs = follows \circ execState \ state \circ GS \ g \ initial \circ first \ \$ \ g \\ initial = M.singleton \ s \ (S.singleton \ EOF)
```

follow' is where the main work of the follow function is done. For a given production, follow' will add an entry into the GrammarState passed along. This function is meant to be mapM'd across the Grammar you want to compute the follow sets of.

```
follow' :: (Ord \ nt, Ord \ t)
    \Rightarrow Production \ nt \ t
    \rightarrow Environment \ nt \ t \ ()
follow' (Production \ a \ \_) = \mathbf{do}
   fllostate \leftarrow qet
  let g = grammar fllostate
         fllow = follows fllostate
         ps = filter (elem \ a \circ nonTerminals \circ rhs) \ g
   sets \leftarrow forM \ ps \ \lambda(Production \ x \ rhs) \rightarrow \mathbf{do}
      case after a rhs of
         Empty \rightarrow return \circ from Maybe \ S.empty \circ M.lookup \ x \ filow
          Term\ t \longrightarrow return \circ S.singleton \circ Terminal \ t
         NonT \ nt \ rest \rightarrow \mathbf{do}
             let frstb = (firsts \ filostate)M.! \ nt
                fllowx = \mathbf{case} \ S.member \ Epsilon \ frstb \ \mathbf{of}
                   False \rightarrow S.empty
```

```
True 
ightharpoonup from Maybe\ S.empty \circ M.lookup\ x\ \$\ fillow return\ \$\ S.union\ (S.delete\ Epsilon\ frstb)\ (fillowx) let s = from Maybe\ S.empty\ (M.lookup\ a\ fillow) newS = S.union\ s\ (S.unions\ sets) put\ fillostate\ \{follows = M.insert\ a\ newS\ fillow\}
```

after is a helper function which removes all Terminals and Non-terminals from a RHS until a specific Non-terminal is reached. Then the rest of the RHS is returned.

```
after :: (Eq \ nt) \Rightarrow nt \rightarrow RHS \ nt \ t \rightarrow RHS \ nt \ t
after \ nt \ Empty = Empty
after \ nt \ (Term \ t \ rhs) = after \ nt \ rhs
after nt (NonT \ nt2 \ rhs) = \mathbf{if} \ nt \equiv nt2
  then rhs else after nt rhs
 {- BEGIN TESTS - -}
makeTestM :: (Eq \ a, Show \ a)
   \Rightarrow String
   \rightarrow FilePath
   \rightarrow String
   \rightarrow a
   \rightarrow (Grammar String String \rightarrow a)
   \rightarrow Test
makeTestM name file forF e f = TestLabel name \circ TestCase \$ do
  grammar \leftarrow sparse < \$ > readFile file
  assertEqual\ forF\ e\ (f\ grammar)
testFollow = makeTestM "testFollow"
  "tests\\39.txt"
  "for first with 39"
  expected
  follow where
  expected = M.fromList [("R", S.fromList [EOF, Terminal "c"]),
     ("T", S.fromList [EOF, Terminal "c"])]
tests = TestList [testFollow]
runTests :: IO\ Counts
runTests = runTestTT tests
doTestsPass :: IO\ Bool
do TestsPass = \mathbf{do}
  counts \leftarrow runTests
```

```
let errs = errors \ counts

fails = failures \ counts

return \$ (errs \equiv 0) \land (fails \equiv 0)

{- END TESTS - -}
```

6 Generating a Parse Table

In this section we generate a parse table for a given grammar, assuming it has been properly scanned, parsed, and thoroughly cleansed.

```
module Table where
import ContextFreeGrammar
import Filterable
import Nullable
import First
import Follow
import System. Environment
import Data.List
import qualified Data. Map as M
import qualified Data. Set as S
import ScanAndParse
import BadHygiene
type Table nt \ t = M.Map \ nt \ (M.Map \ t \ (Production \ nt \ t))
foo1 :: Grammar String String
foo1 = [a, b, c, d] where
  a = Production "A" (Term "a" Empty)
  b = Production "B" (NonT "B" Empty)
  c = Production "C" (Term "a" (NonT "B" Empty))
  d = Production "D" (NonT "B" (Term "a" Empty))
getFeature\ feature\ productions = loop\ productions
    loop [] acc = sort \circ nub \circ concat \$ acc
    loop\ ((Production\ s\ rhs): xs)\ acc = loop\ xs\ ((feature\ rhs): acc)
  -- need to generate S' \rightarrow S$
qetNewStart[] = error "getNewStart run on empty grammar --- a new low point"
getNewStart (Production nt rhs : ps) =
    Production (nt + ",") (NonT nt (Term "\$" Empty))
```

```
isRHSNullable :: Ord \ a \Rightarrow S.Set \ a \rightarrow RHS \ a \ t \rightarrow Bool
      isRHSNullable \_Empty = True
      isRHSNullable \_ (Term \ t \_) = False
      isRHSNullable \ m \ (NonT \ nt \ rhs) =
        if S.member nt m then
           isRHSNullable m rhs
         else False
      firstRHS \_ Empty = S.empty
      firstRHS \ i \ (Term \ t \ rhs) = S.insert \ (Terminal \ t) \ (firstRHS \ i \ rhs)
      firstRHS \ i \ (NonT \ nt \ rhs) =
        if (S.member nt (nulls i)) then
           S.union firstsnt (firstRHS i rhs)
         else
           firstsnt
         where firstsnt = ((firsts\ i)M.!\ nt)
      data GrammarInfo\ nt\ t=GI\ \{
         firsts :: M.Map \ nt \ (S.Set \ (Terminal \ t)),
        follows :: M.Map \ nt \ (S.Set \ (Terminal \ t)),
         nulls :: S.Set nt
      } deriving Show
    A production N \to \alpha is in the table (N,a) iff a is in first (\alpha) \lor (\text{nullable}(\alpha))
\wedge a is in follow(\alpha)). This condition is readily translateable into our code:
      validEntry\ (Production \ \_ \ \alpha)\ term\ nterm\ gi = firstalpha \lor (nullablea \land follown)
         where
           firstalpha = S.member (term) (firstRHS gi \alpha)
           nullablea = isRHSNullable (nulls gi) \alpha
           follown = S.member\ (term)\ ((follows\ gi)M.!\ nterm)
      to Terminal [] = []
      to Terminal ("\$" : ss) = EOF : to Terminal ss
      to Terminal (s:ss) = Terminal s: to Terminal ss
      from Terminal' Epsilon = ""
      from Terminal' EOF
      from Terminal' (Terminal t) = t
      from Terminal Set \ ts = map \ from Terminal' \ S.to List \ ts
      columns \ p \ t \ [] \ gi = []
      columns \ p \ t \ (nt:nts) \ qi =
         if validEntry p t nt qi then
```

```
(t, p) : (columns \ p \ t \ (nts) \ qi)
  else
    columns p t nts gi
rows p[] nts gi = []
rows p(t:ts) nts qi = (columns p t nts qi) : (rows p ts nts qi)
buildTable'[] terms nterms gi = []
buildTable'(p:ps) terms aterms gi = (concat (rows p terms nterms gi)) : buildTable' ps terms
buildTable\ grammar =
  let grammar' = (getNewStart\ grammar) : grammar\ in
  let terms = toTerminal \circ qetFeature terminals \$ grammar' in
  let nterms = getFeature nonTerminals grammar' in
  let gi = GI (first grammar') (follow grammar') (nullable grammar') in
  let table = buildTable' grammar' terms nterms gi in
  table
man = do
contents \leftarrow readFile "tests/39.txt"
let q = sparse contents
let g' = eliminateUseless \circ sparse \$ contents
\mathbf{let}\ gnull = nullable \circ sparse \ \$\ contents
let gfollow = follow \circ sparse \$ contents
let gfirst = first \circ sparse \$ contents
let qi = GI qfirst qfollow qnull
putStrLn \$ show (getFeature terminals g')
putStrLn \$ show (getFeature nonTerminals g')
putStrLn \$ show gi
putStrLn ""
putStrLn \circ show \circ buildTable \$ g
```

7 Main module

The main module puts everything together, takes a textual representation of a context-free grammar as input, scans, parses, and performs the rest of the duties that are required.

```
module Main where
import ContextFreeGrammar
import ScanAndParse
import BadHygiene
```

```
import Table
import System.Environment

main = do
   -- [file] j- getArgs
   -- contents j- readFile file
   contents \leftarrow readFile "tests/39.txt"
   -- contents j- readFile "tests/ir.txt"

let g = sparse \ contents
let g' = eliminateUseless \circ sparse \$ \ contents
   putStrLn \$ show g
   putStrLn \$ show g'
```