

# State Estimation Lab

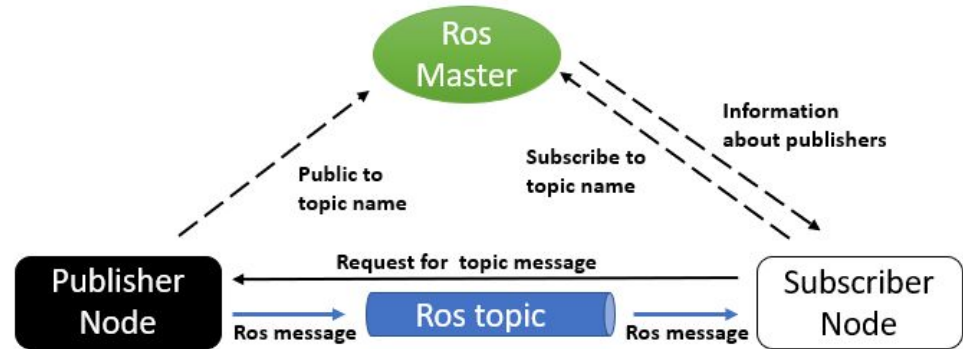
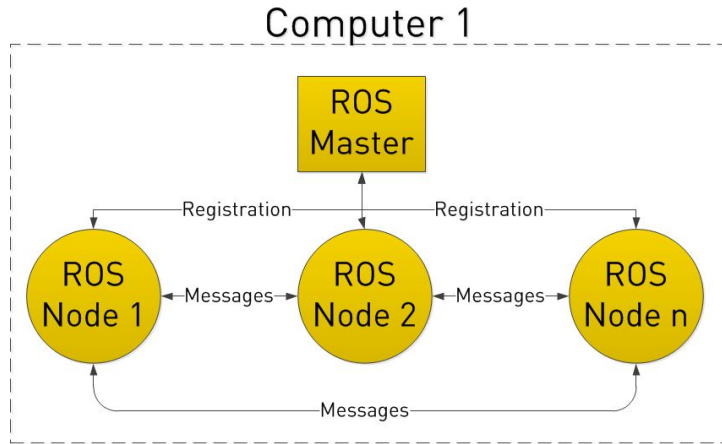
Lab 1

# Overview

- ROS Introduction
- Coordinate Systems (Extrinsic, Intrinsic Matrix)
- AprilTag, Calibration application
- Lab
  - Lab 1.1 Find camera intrinsic matrix
  - Lab 1.2 Pose estimation using single or multiple Apriltags

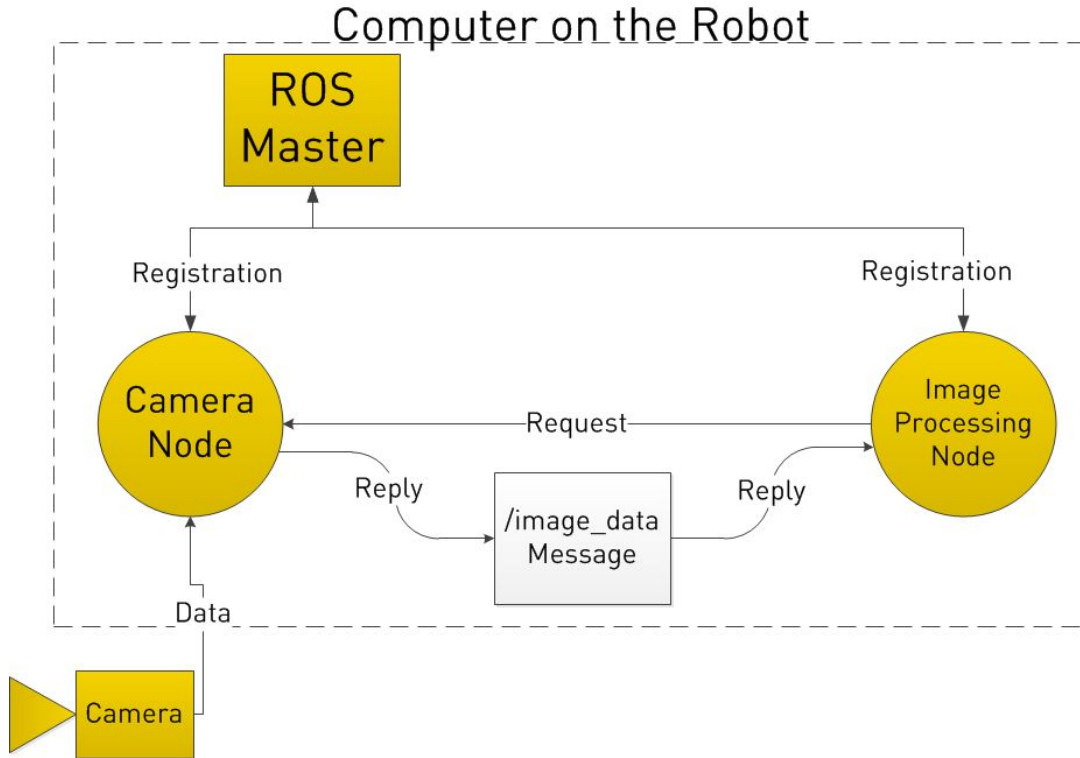
# ROS Introduction

- Comprised of a number of independent nodes.
- Each communicates with others by publishing and subscribing to topics.



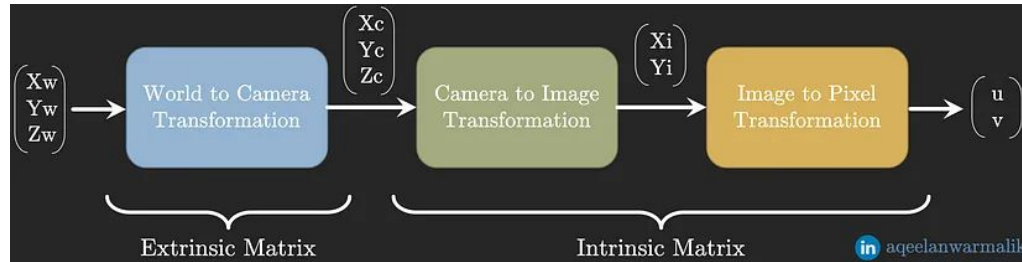
Please ensure that the ROS installation is completed in the [prelab](#).

# Example

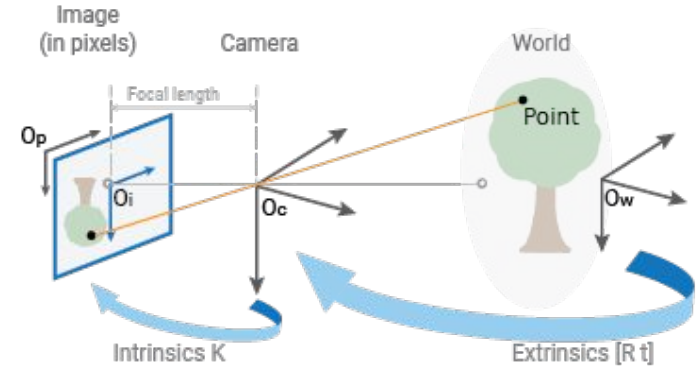


# Coordinate Systems

- Extrinsic: parameters of a camera depend on location and orientation (Pose)
  - World (3D)  $\rightarrow$  Camera coordinate system (3D)
- Intrinsic: parameters of a camera depend on how it captures the images, such as focal length, aperture, field-of-view, resolution
  - Camera (3D)  $\rightarrow$  Image (2D)  $\rightarrow$  Pixel coordinate system (2D)

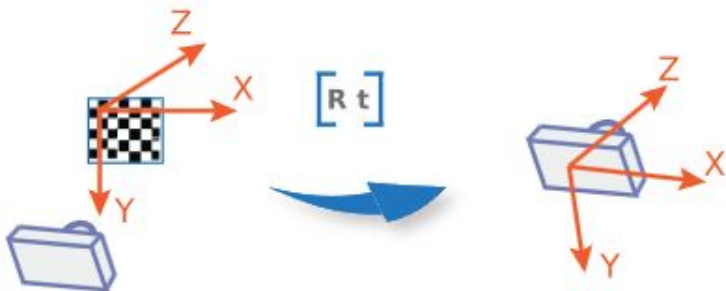
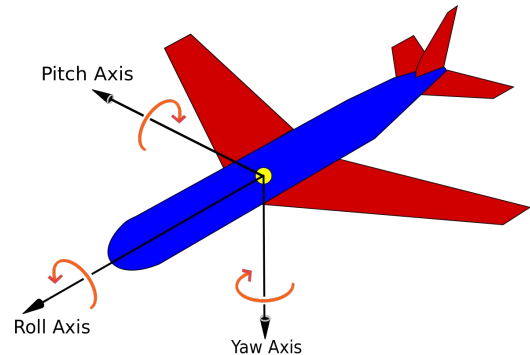


World (3D)  $\rightarrow$  Pixel coordinate system (2D)



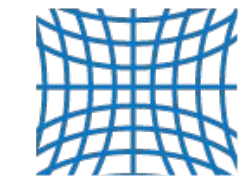
# Extrinsic Matrix

- World (3D)  $\rightarrow$  Camera coordinate system (3D)
- Consist of a rotation matrix  $\mathbf{R}$  and a translation matrix  $\mathbf{t}$ .
- Pose estimation

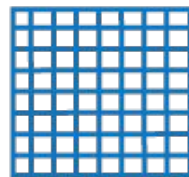


$$[R | t] = \begin{bmatrix} r_{1,1} & r_{1,2} & r_{1,3} & t_1 \\ r_{2,1} & r_{2,2} & r_{2,3} & t_2 \\ r_{3,1} & r_{3,2} & r_{3,3} & t_3 \end{bmatrix}$$

# Intrinsic Matrix



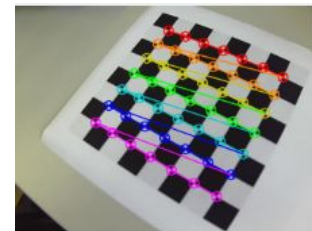
Pincushion distortion  
Positive radial displacement



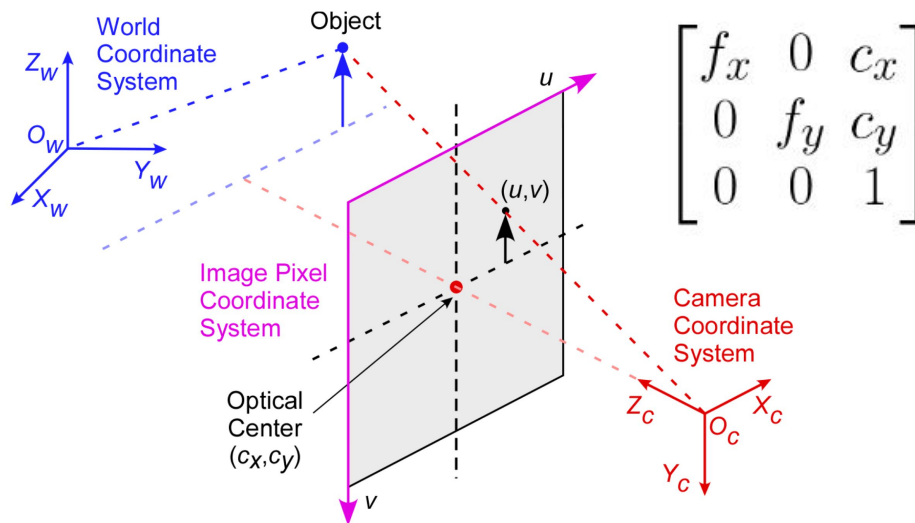
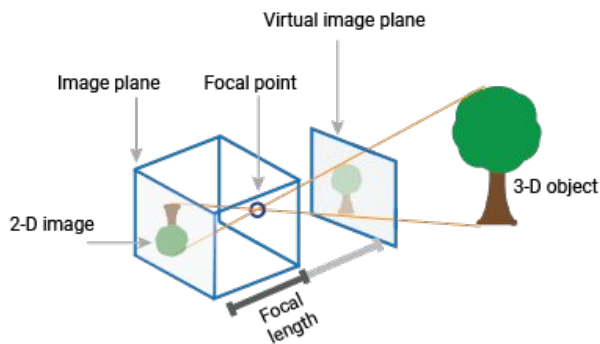
No distortion



Barrel distortion  
Negative radial displacement

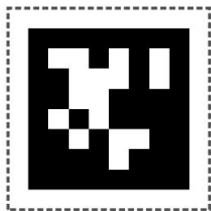


- Camera (3D)  $\rightarrow$  Image (2D)  $\rightarrow$  Pixel coordinate system (2D)
- Pinhole camera model
- Distortion

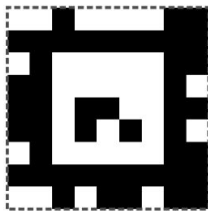


# AprilTag

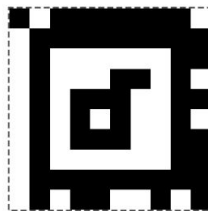
- Two-dimensional bar code, similar to QR Codes.
- Smaller data payloads, while still being detectable at longer distances.
- Can compute **3D pose** (position, orientation), and **tags ID** relative to camera.



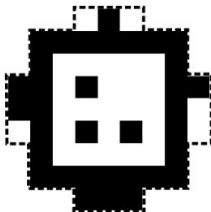
Tag36h11



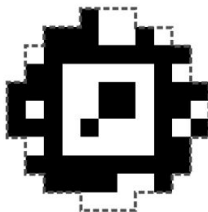
TagStandard41h12



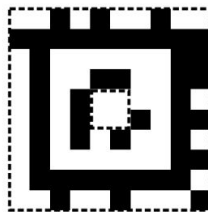
TagStandard52h13



TagCircle21h7



TagCircle49h12



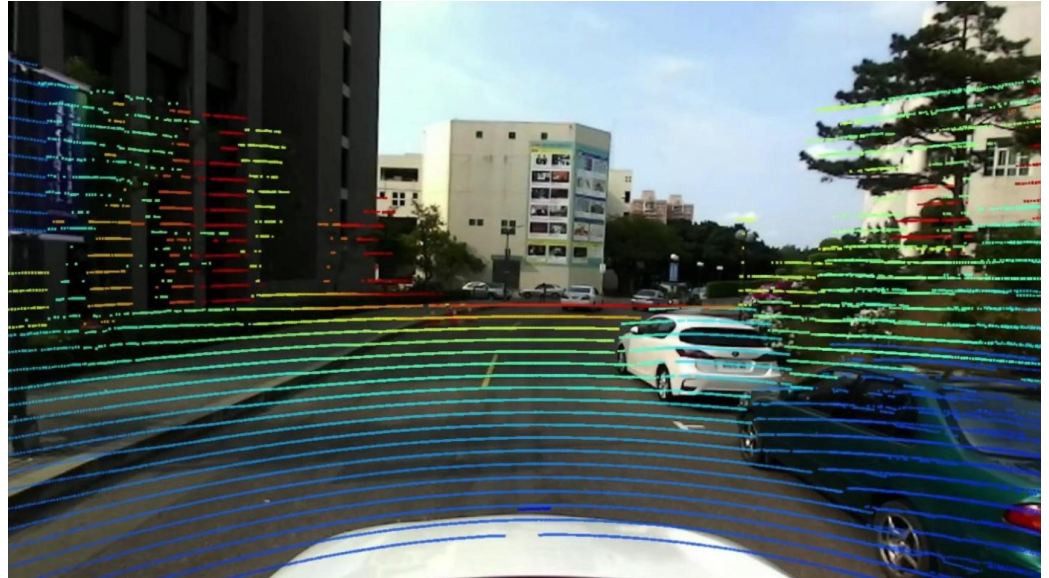
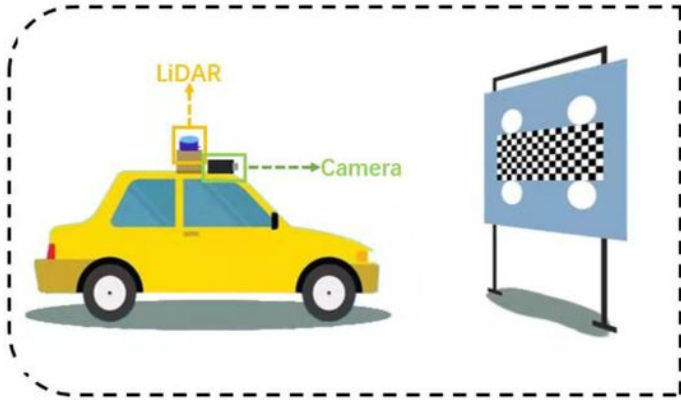
TagCustom48h12

extrinsic



# Calibration application

Intrinsic, Extrinsic, Temporal



Lab

# Preparations before Lab

Download files from E3

Install packages:

```
pip install rospkg
```

```
pip install pupil-apriltags
```

```
pip install opencv-python
```

Install VSCode (Optional):

```
sudo apt update
```

```
sudo apt install snapd
```

```
sudo snap install code --classic
```

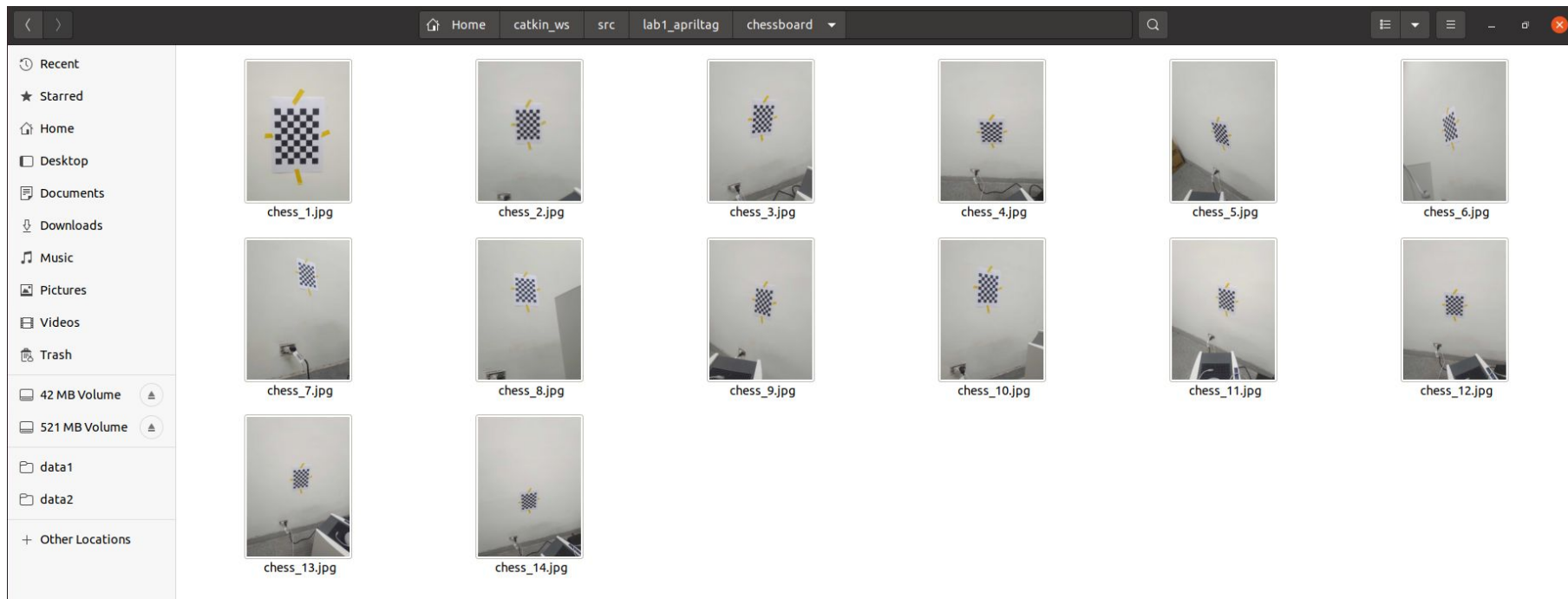
# Lab

1.1 Get camera's intrinsic matrix and distortion coefficient

1.2 Pose estimation using single or multiple AprilTags.

# Lab 1.1 - Find camera intrinsic matrix

Capture multiple images of a chessboard using the camera and save them in a folder.



# Lab 1.1 - Find camera intrinsic matrix

Open camera\_calibration.py and modify the path to the folder containing the chessboard images.

```
19  # Load images
20  images_folder = ???
21  images_list = os.listdir(images_folder)
```

# Lab 1.1 - Find camera intrinsic matrix

Finished the code here, so it can show the value of  $f_x$ ,  $f_y$ ,  $c_x$ ,  $c_y$ .

```
53     # Print the camera matrix
54     print(f"Objective function value: {ret}\n")
55     print(f"Distortion coefficient: {dist}\n")
56     print("Camera Matrix:")
57     print(mtx)
58
59      $f_x$  = mtx[0, 0]
60      $f_y$  = mtx[1, 0]
61      $c_x$  = mtx[0, 1]
62      $c_y$  = mtx[1, 1]
63
64     print(f"\n $f_x$ : {fx},  $f_y$ : {fy},  $c_x$ : {cx},  $c_y$ : {cy}")
```

# Lab 1.1 - Find camera intrinsic matrix

Open the terminal and type "python camera\_calibration.py" Then the program will start executing and computing the intrinsic matrix and distortion coefficients.

```
~/catkin_ws/src/lab1_apriltag/src > python camera_calibration.py
Objective function value: 0.7488936896790611

Distortion coefficient: [[ 0.04884705  0.08326766  0.00990691 -0.00287781  0.51442997]]

Camera Matrix:
[[3.13524341e+03  0.00000000e+00  1.48682923e+03]
 [0.00000000e+00  3.13972523e+03  2.06891569e+03]
 [0.00000000e+00  0.00000000e+00  1.00000000e+00]]

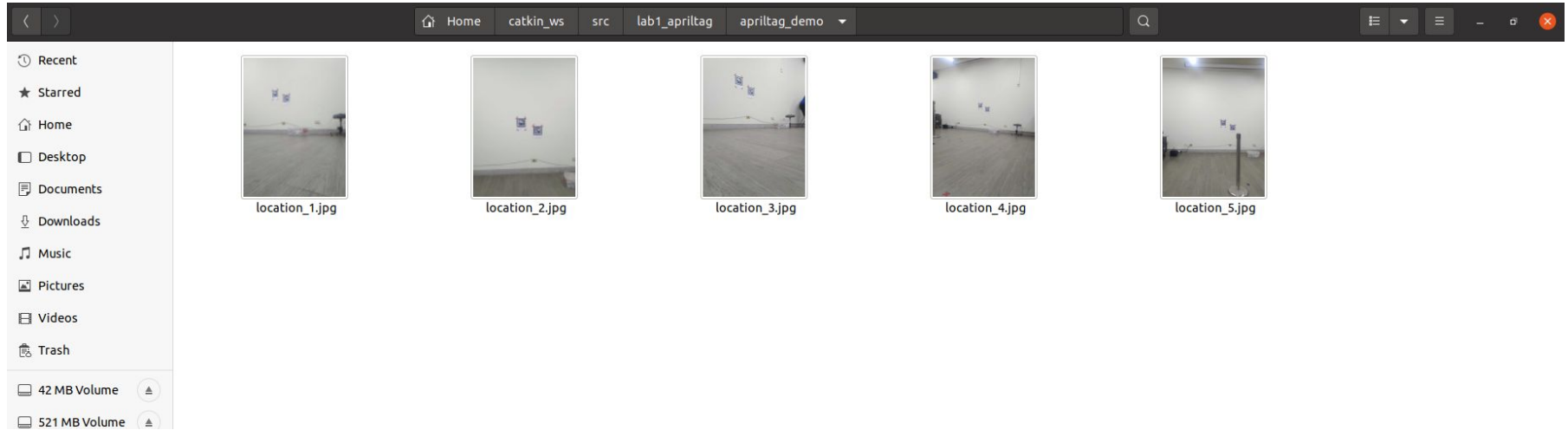
fx: 3135.243406828593, fy: 3139.7252280414996, cx: 1486.8292332587046, cy: 2068.915688921479
```

Record the values of fx, fy, cx, cy, and distortion coefficient. These values will be used in the next program.



# Lab 1.2 - Pose estimation using single or multiple Apriltags

Take pictures at the designated locations (5 places) and save them in a folder. Each image should include two Apriltags.



# Lab 1.2 - Pose estimation using single or multiple Apriltags

## 1. apriltag\_id\_3.csv

This file contains the world coordinates of the center of the AprilTag with ID = 3.

## 2. apriltag\_id\_4.csv

This file contains the world coordinates of the center of the AprilTag with ID = 4.

## 3. apriltag\_id\_3\_4.csv

This file contains the world coordinates of the center of the AprilTag with ID = 3 and ID = 4.

## 4. benchmark.csv

This file contains the benchmark pose information.

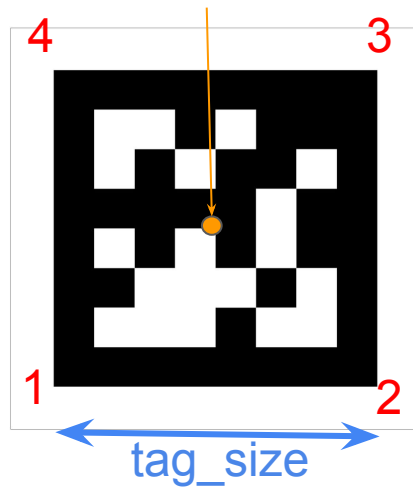
## Lab 1.2 - Pose estimation using single or multiple Apriltags

Please finish the function below. It takes the center of the AprilTag in the world coordinates and the size of the tag as input. The output of this function will be the corner points of the AprilTag in the world coordinates.

Note: The order of the points is important! In the counter-clockwise order, the first point will be at the bottom left.

```
def get_apriltag_corners(world_x, world_y, world_z, tag_size):  
    return np.array([[??, ??, ??], # First point  
                    [??, ??, ??], # Second point  
                    [??, ??, ??], # Third point  
                    [??, ??, ??]], # Fourth point  
                    dtype = np.float32)
```

(world\_x, world\_y, world\_z)



# Lab 1.2 - Pose estimation using single or multiple Apriltags

Setting the following parameters

- `APRILTAG_SIZE` :  
width of the AprilTag, measured in meters.
- `APRILTAG_LOCATION_PATH`:  
path to `apriltag_id_3.csv` , `apriltag_id_4.csv` or `apriltag_id_3_4.csv`.

When the path is set to `apriltag_id_3.csv`, it means that we estimate the pose by only using the apriltag with `id = 3`. When the path is set to `apriltag_id_3_4.csv`, it means we estimate the pose by using two apriltags.

```
# Apriltag parameter
APRILTAG_SIZE = ???
APRILTAG_LOCATION_PATH = ???
```

# Lab 1.2 - Pose estimation using single or multiple Apriltags

- camera parameters :  
FX, FY, CX, CY, DIST\_COEFF.

```
# Camera parameters
FX = ???
FY = ???
CX = ???
CY = ???

DIST_COEFF = np.array([?, ?, ?, ?, ?])
```

- benchmark\_path:  
path to benchmark.csv

```
# Get Benchmark
bench_mark_path = ???
bench_mark_pose_list = read_csv(bench_mark_path)
```

# Lab 1.2 - Pose estimation using single or multiple Apriltags

- Image\_folder:

Path to the folder that contains the AprilTags image

```
# Get camera pose from image
Image_folder = ???
image_name_list = os.listdir(Image_folder)
```

- Output\_csv\_file

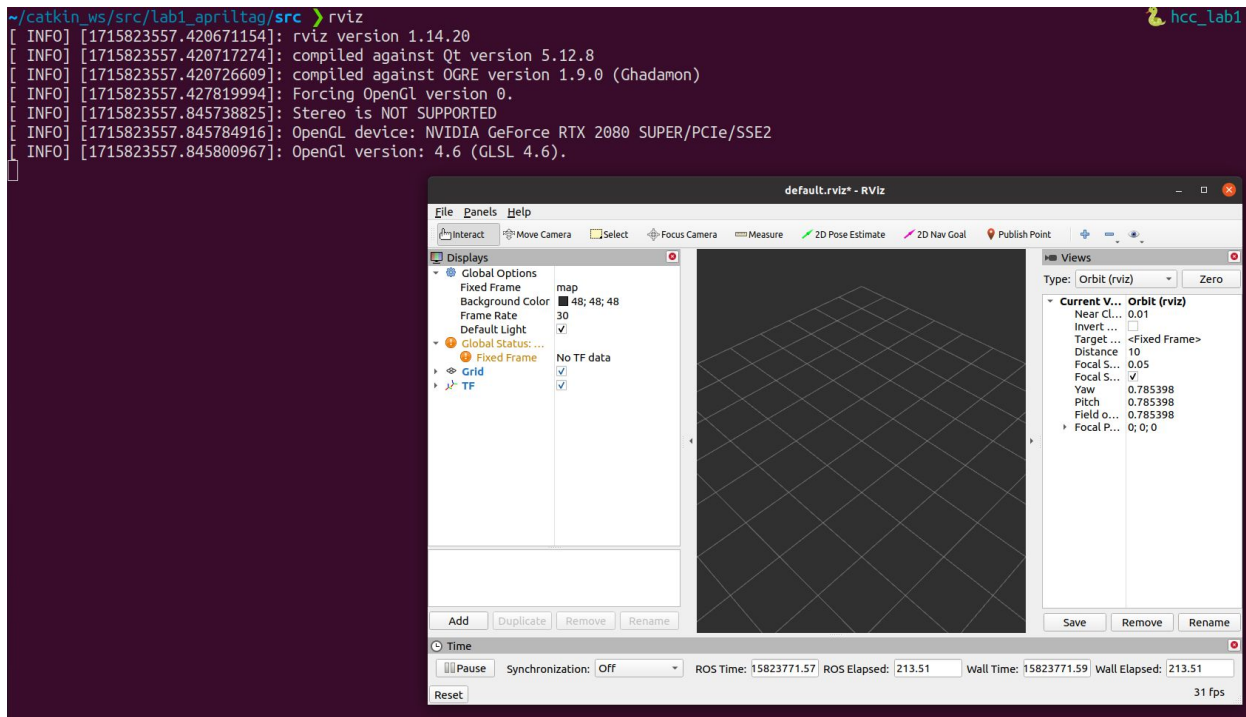
Path to the estimated output pose

```
## Write the result to csv
Output_csv_file = ???
header = ['x', 'y', 'z', 'roll', 'pitch', 'yaw']
with open(Output_csv_file, mode='w', newline='') as file:
    writer = csv.writer(file)
    writer.writerow(header)
    writer.writerows(content)
```

# Lab 1.2 - Pose estimation using single or multiple Apriltags

execute the code

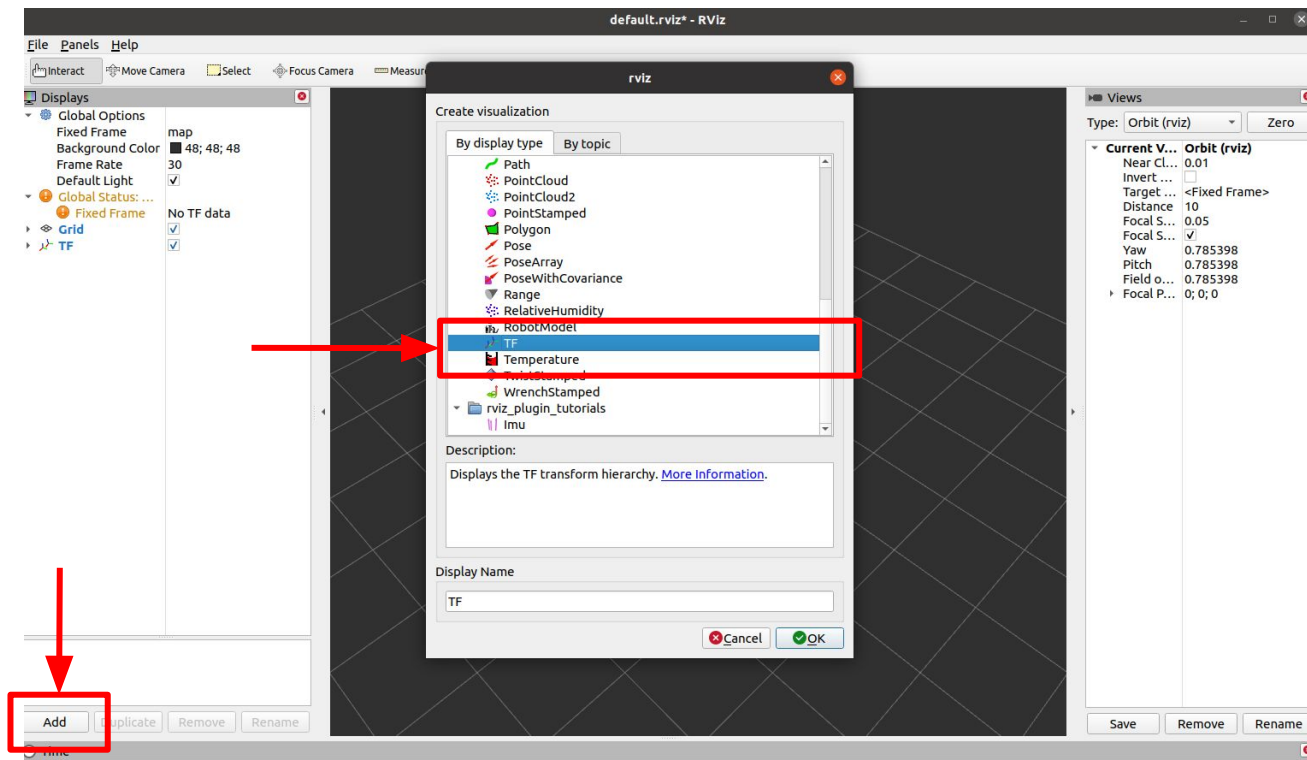
- open the terminal and type “rviz”



# Lab 1.2 - Pose estimation using single or multiple Apriltags

execute the code

- add the TF topic





# Lab 1.2 - Pose estimation using single or multiple Apriltags

execute the code

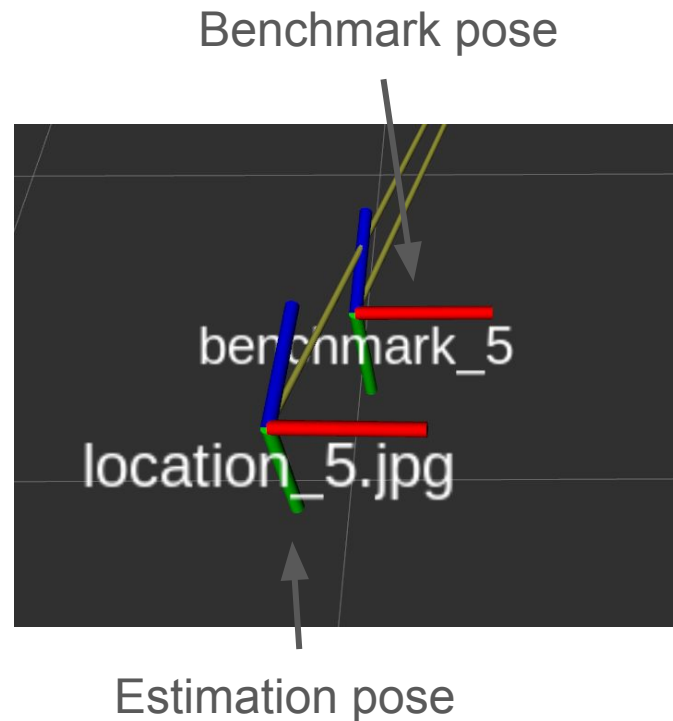
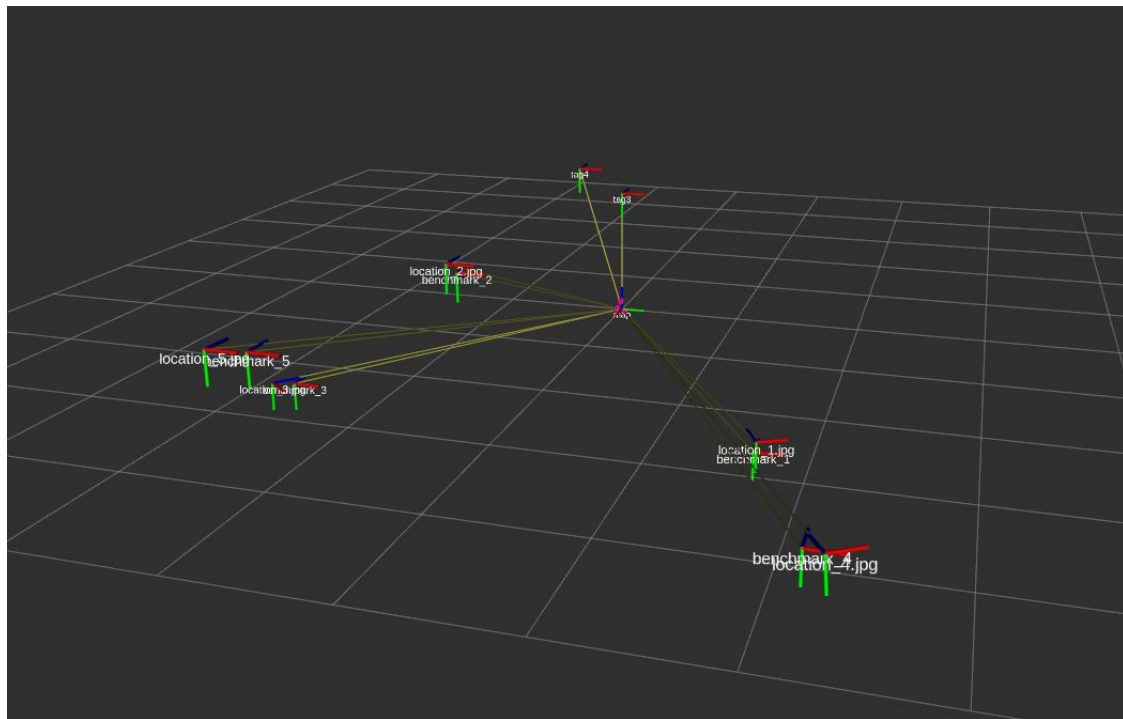
- open the terminal and type “python lab1\_apriltag.py”

```
~/catkin_ws/src/lab1_apriltag/src > python lab1_apriltag.py
[INFO] [1715824058.396524]: Publish tag3 coordinate
[INFO] [1715824059.399218]: Publish tag4 coordinate
[INFO] [1715824060.404208]: Publish benchmark_1
[INFO] [1715824061.409240]: Publish benchmark_2
[INFO] [1715824062.414610]: Publish benchmark_3
[INFO] [1715824063.419648]: Publish benchmark_4
[INFO] [1715824064.424326]: Publish benchmark_5
[INFO] [1715824065.734655]: Publish location_3.jpg
[INFO] [1715824066.975111]: Publish location_2.jpg
[INFO] [1715824068.262690]: Publish location_4.jpg
[INFO] [1715824069.543793]: Publish location_5.jpg
[INFO] [1715824070.807137]: Publish location_1.jpg
[INFO] [1715824071.810216]: CSV file saved to /home/ee904/catkin_ws/src/lab1_apriltag/result/camera_pose.csv
```

# Lab 1.2 - Pose estimation using single or multiple Apriltags

execute the code

- In the rviz window



# Lab 1.2 - Pose estimation using single or multiple Apriltags

After the code stops executing, please change the `APRILTAG_LOCATION_PATH` parameter so that we can observe the difference by using a different number of tags to calculate the pose.

You will receive 3 CSV results by using different parameters of `APRILTAG_LOCATION_PATH`.

# Lab 1.2 - Pose estimation using single or multiple Apriltags

Evaluate the pose using a benchmark.

Open the evaluate.py, and modify the following parameters.

- BENCHMARK\_PATH: Path to benchmark.csv
- PRED\_PATH: The output csv file from lab1\_apriltag.py

```
BENCHMARK_PATH = ???  
PRED_PATH = ???
```

Open the terminal and type “python evaluate.py”,

The result shows the average distance error along x-axis, y-axis and z-axis.

```
~/catkin_ws/src/lab1_apriltag/src > python evaluate.py  
Average error:  
x: 0.184683980000000014 m  
y: 0.065328357999999995 m  
z: 0.098115924 m
```

# Lab 1.2 - Pose estimation using single or multiple Apriltags

Answer the following question.

1. Which result is better: using one Apriltag or using two Apriltags for pose estimation?
2. If there were no benchmark provided today, what result would you prefer to use as the result for pose estimation, and why?

# Reference

[Intro to ROS — ROS Tutorials 0.5.2 documentation \(clearpathrobotics.com\)](http://clearpathrobotics.com/ROS-Tutorials-0.5.2-documentation)

[AprilTag Introduction — FIRST Tech Challenge Docs 0.2 documentation \(firstinspires.org\)](http://firstinspires.org/FIRST-Tech-Challenge-Docs-0.2-documentation)

[What Is Camera Calibration? - MATLAB & Simulink \(mathworks.com\)](http://mathworks.com/What-Is-Camera-Calibration?)