

$$(12) A(0, 2, 0) \quad \angle(AD, AB) = \angle(AD, AC)$$

$$B(2, 3, 2)$$

$$C(2, 2, 4)$$

$$P \equiv \frac{x}{1} = \frac{y-3}{2} = \frac{z}{2}$$

$$D = ?$$

$$\cos \angle = \frac{\vec{AD} \cdot \vec{AB}}{|\vec{AD}| \cdot |\vec{AB}|}$$

$$\vec{AB} = 2\mathbf{i} + \mathbf{j} + 2\mathbf{k}$$

$$\vec{AC} = 2\mathbf{i} + 4\mathbf{k}$$

$$P \equiv \begin{cases} x = t \\ y = 2t + 3 \\ z = 2t \end{cases}$$

$$D(t, 2t+3, 2t)$$

$$\vec{AD} = t\mathbf{i} + (2t+3)\mathbf{j} + 2t\mathbf{k}$$

$$\frac{\vec{AD} \cdot \vec{AB}}{|\vec{AD}| \cdot |\vec{AB}|} = \frac{\vec{AD} \cdot \vec{AC}}{|\vec{AD}| \cdot |\vec{AC}|}$$

$$\frac{2t + 2t+4 + 2 \cdot 2t}{|\vec{AD}| \cdot \sqrt{4+1+4}} = \frac{2t+3 + 4(2t)}{|\vec{AD}| \cdot \sqrt{4+16}} \quad / \cdot |\vec{AD}|$$

$$\frac{8t+4}{3} = \frac{10t}{2\sqrt{5}}$$

$$30t = 2\sqrt{5} \cdot (8t+4)$$

$$30t = 16\sqrt{5}t + 2\sqrt{5}$$

$$30t - 16\sqrt{5}t = 2\sqrt{5}$$

$$t(30 - 16\sqrt{5}) = 2\sqrt{5}$$

$$t = \frac{2\sqrt{5}}{30 - 16\sqrt{5}}$$

$$t = \frac{2\sqrt{5}}{2(15 - 8\sqrt{5})}$$

$$t = \frac{\sqrt{5}}{15 - 8\sqrt{5}}$$

$$t = \frac{-\sqrt{5}}{8\sqrt{5} - 15}$$

$$D\left(\frac{-\sqrt{5}}{8\sqrt{5}-15}, \frac{-2\sqrt{5}}{8\sqrt{5}-15} + 3, \frac{-2\sqrt{5}}{8\sqrt{5}-15}\right)$$