

PHASE TRANSFORMATIONS AND PHASE DIAGRAMS

ISSUES TO ADDRESS...

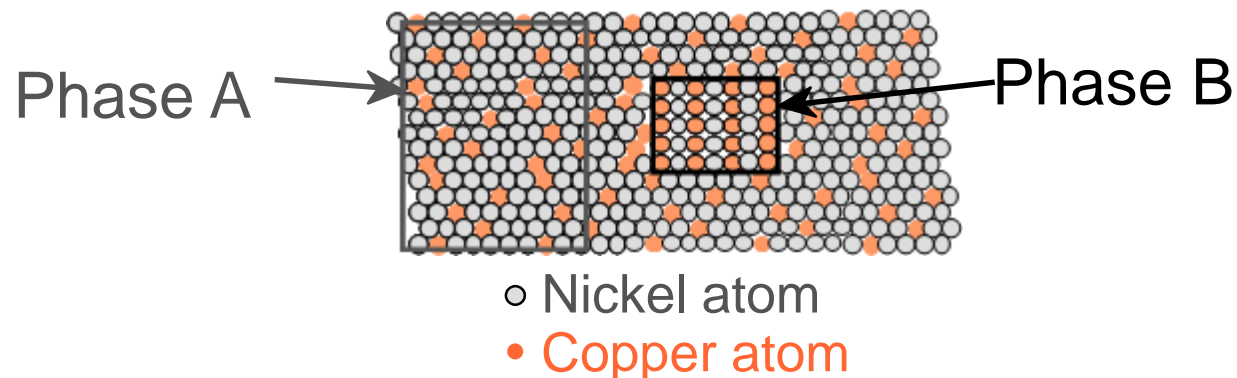
- When we combine two elements...
what is the resulting equilibrium state?
- In particular, if we specify...
 - the composition (e.g., wt% Cu - wt% Ni), and
 - the temperature (T)

then...

How many phases form?

What is the composition of each phase?

What is the amount of each phase?



Phase Equilibria: Solubility Limit

- **Solution** – solid, liquid, or gas solutions, single phase
- **Mixture** – more than one phase

- **Solubility Limit:**

Maximum concentration for which only a single phase solution exists.

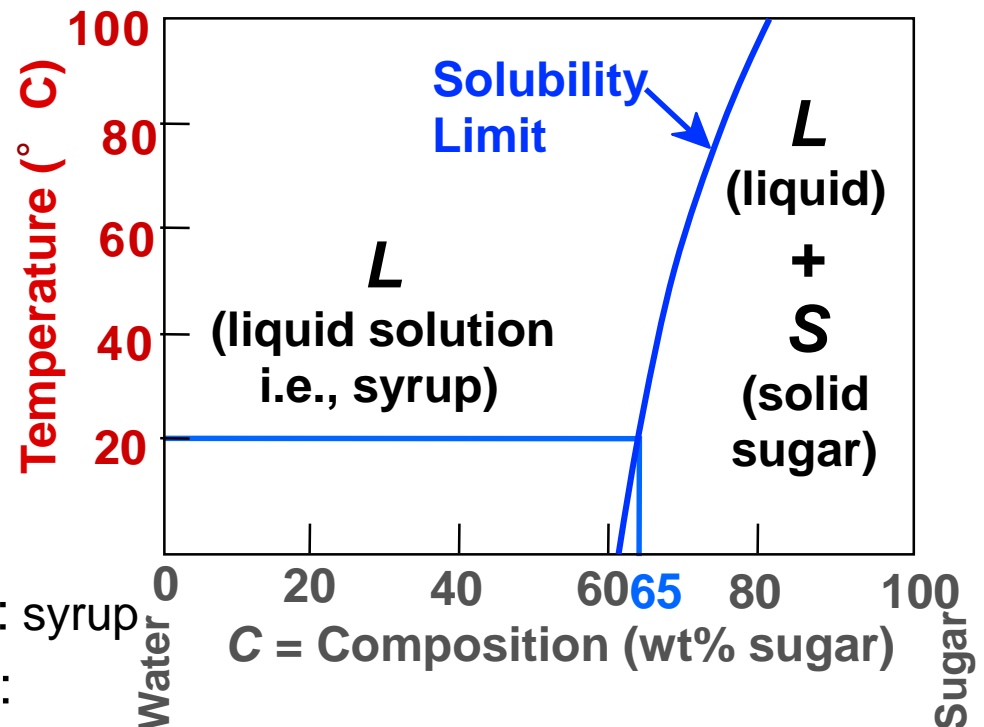
Question: What is the solubility limit for sugar in water at 20°C ?

Answer: **65 wt% sugar.**

At 20°C , if $C < 65$ wt% sugar: syrup

At 20°C , if $C > 65$ wt% sugar:
syrup + sugar

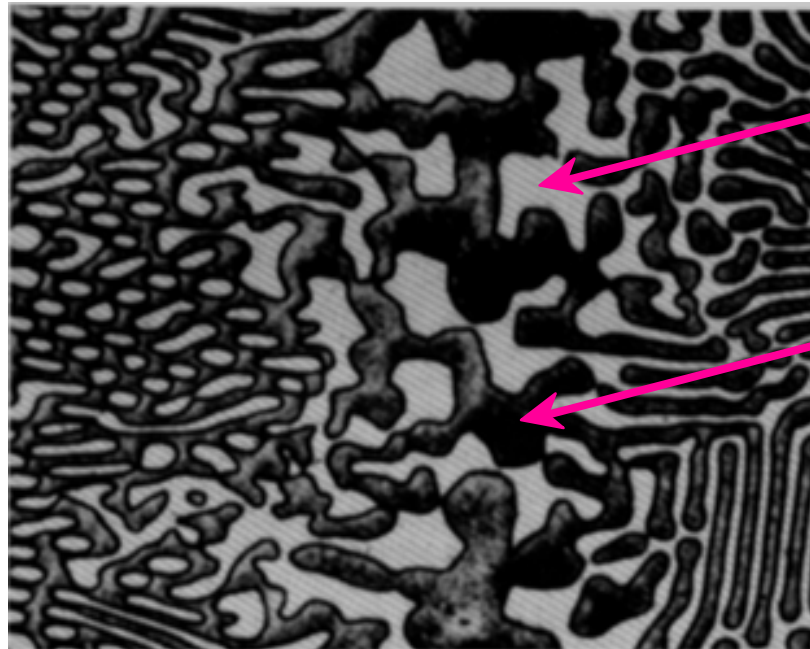
Sugar/Water Phase Diagram



Components and Phases

- **Components:**
The elements or compounds which are present in the alloy
(e.g., Al and Cu)
- **Phases:**
The physically and chemically distinct material regions
that form (e.g., α and β).

Aluminum-
Copper
Alloy

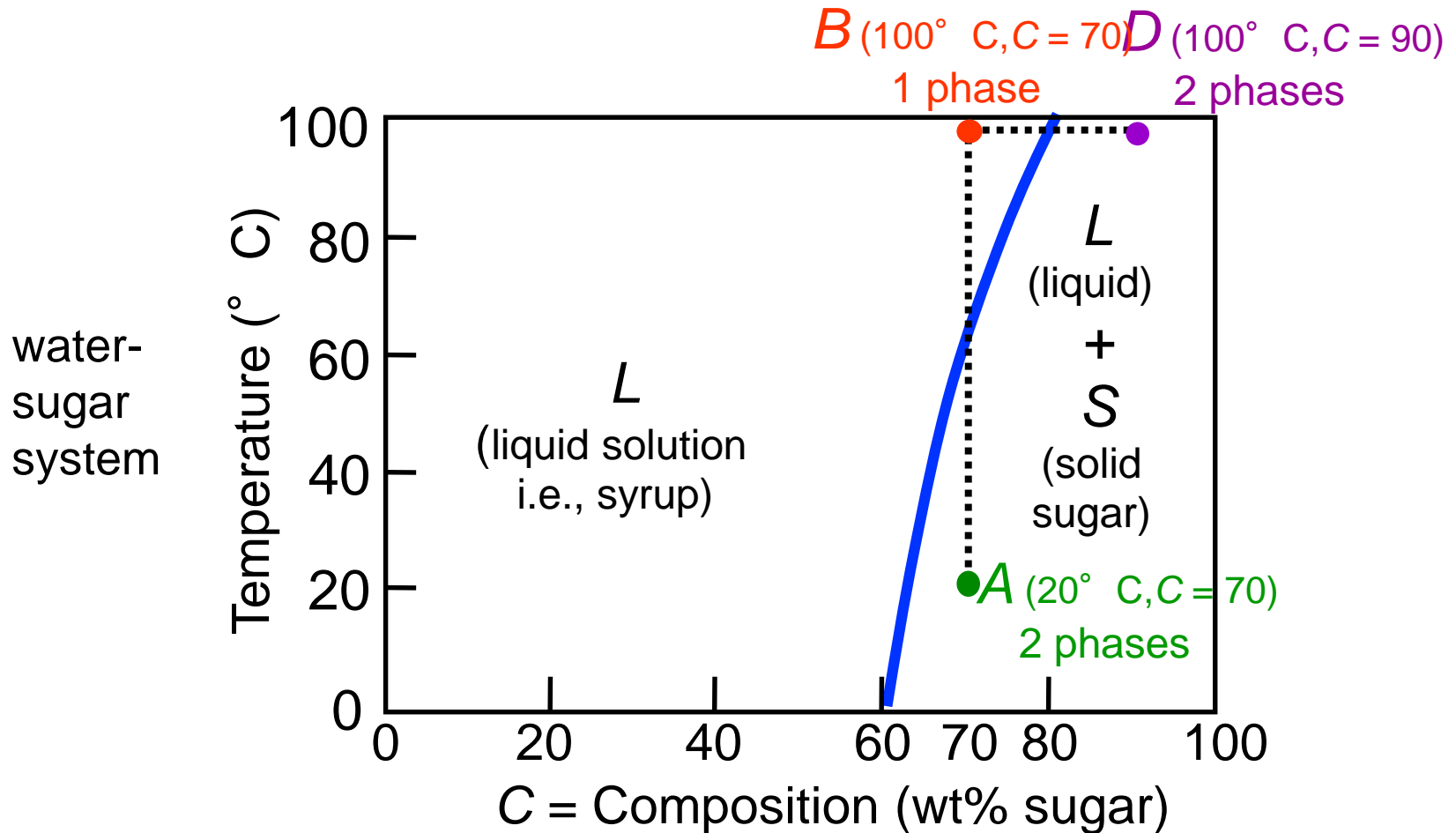


β (lighter
phase)

α (darker
phase)

Effect of Temperature & Composition

- Altering T can change # of phases: path A to B .
- Altering C can change # of phases: path B to D .



Criteria for Solid Solubility

Simple system (e.g., Ni-Cu solution)

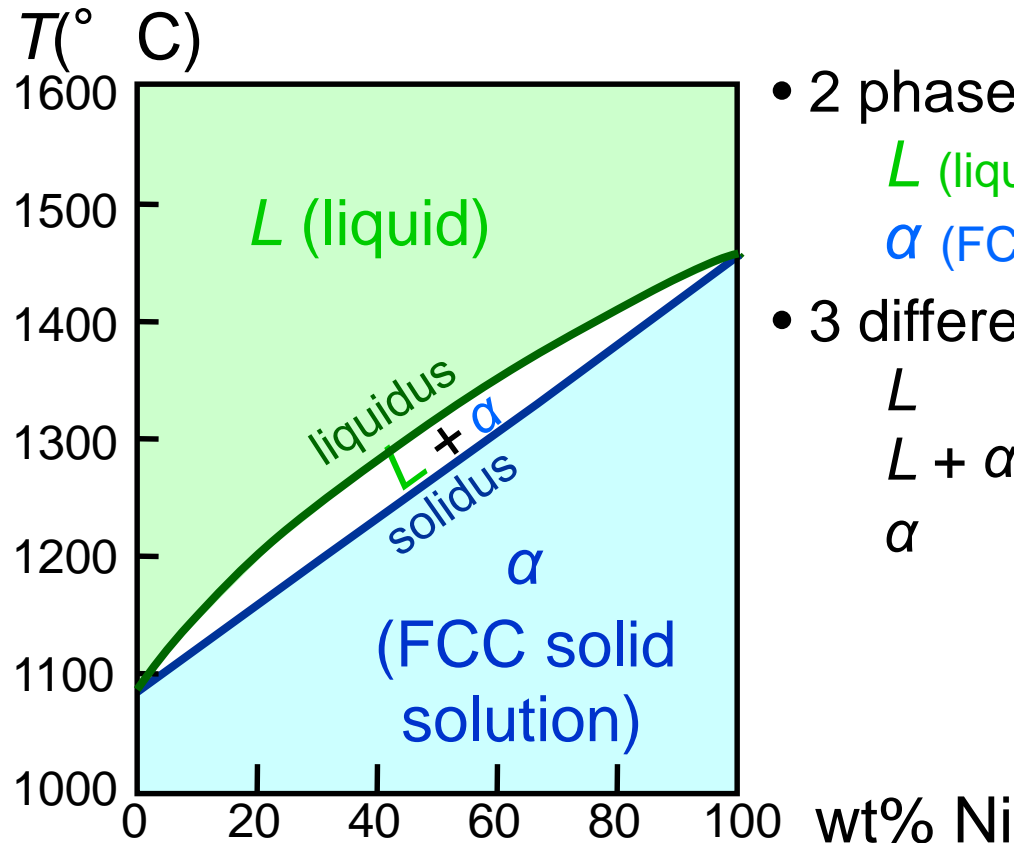
	Crystal Structure	electroneg	r (nm)
Ni	FCC	1.9	0.1246
Cu	FCC	1.8	0.1278

- Both have the same crystal structure (FCC) and have similar electronegativities and atomic radii (W. Hume – Rothery rules) suggesting high mutual solubility.
- Ni and Cu are totally soluble in one another for all proportions.

Phase Diagrams

- Indicate phases as a function of T , C , and P .
- For this course:
 - binary systems: just 2 components.
 - independent variables: T and C ($P = 1$ atm is almost always used).

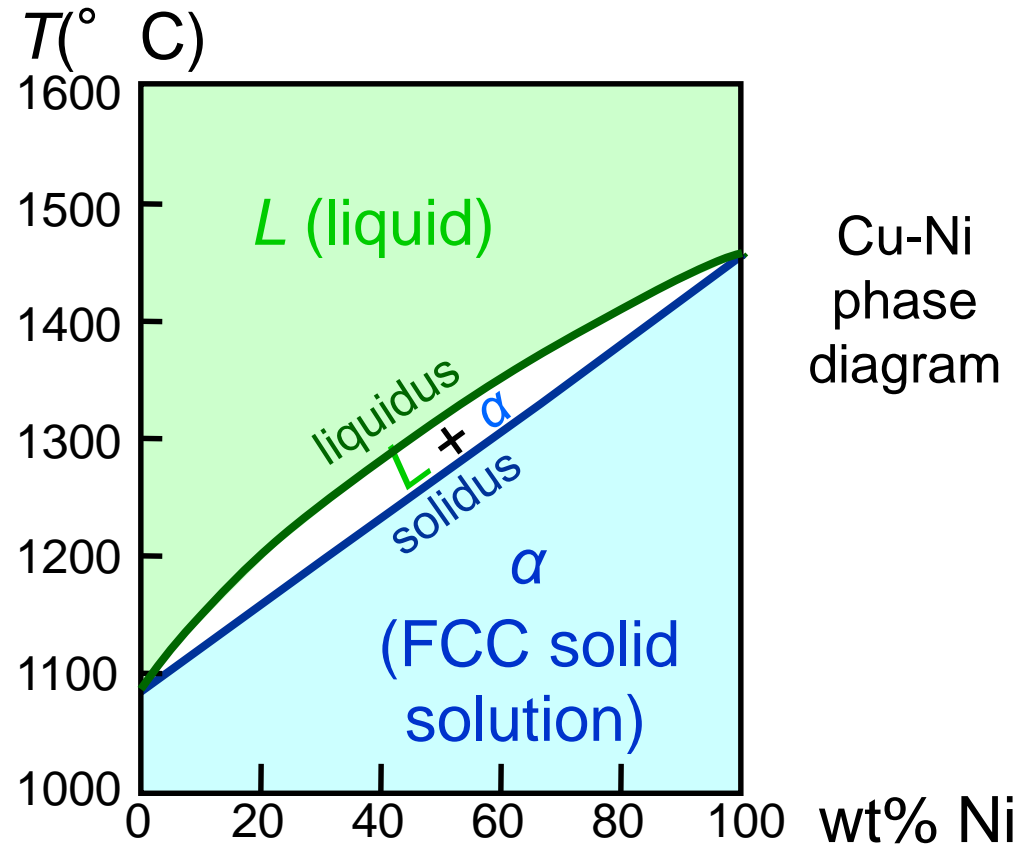
Phase
Diagram
for Cu-Ni
system



- 2 phases:
 - L (liquid)
 - α (FCC solid solution)
- 3 different phase fields:
 - L
 - $L + \alpha$
 - α

Isomorphous Binary Phase Diagram

- Phase diagram:
Cu-Ni system.
- System is:
 - **binary**
i.e., 2 components:
Cu and Ni.
 - **isomorphous**
i.e., complete
solubility of one
component in
another; α phase
field extends from
0 to 100 wt% Ni.



Phase Diagrams:

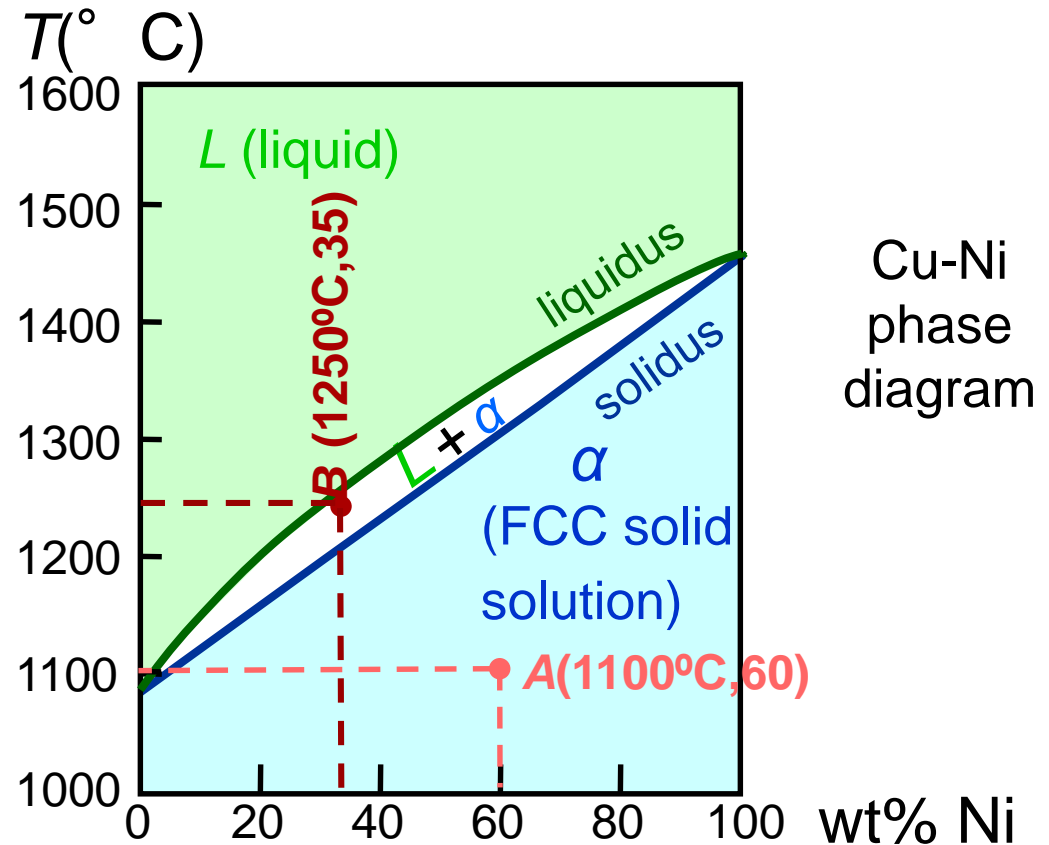
Determination of phase(s) present

- Rule 1: If we know T and C_0 , then we know:
 - which phase(s) is (are) present.

- Examples:

$A(1100^\circ \text{ C}, 60 \text{ wt\% Ni})$:
1 phase: α

$B(1250^\circ \text{ C}, 35 \text{ wt\% Ni})$:
2 phases: $L + \alpha$



Phase Diagrams:

Determination of phase compositions

- Rule 2: If we know T and C_0 , then we can determine:
 - the composition of each phase.

- Examples:

Consider $C_0 = 35 \text{ wt\% Ni}$

At $T_A = 1320^\circ \text{ C}$:

Only Liquid (L) present

$C_L = C_0$ ($= 35 \text{ wt\% Ni}$)

At $T_D = 1190^\circ \text{ C}$:

Only Solid (α) present

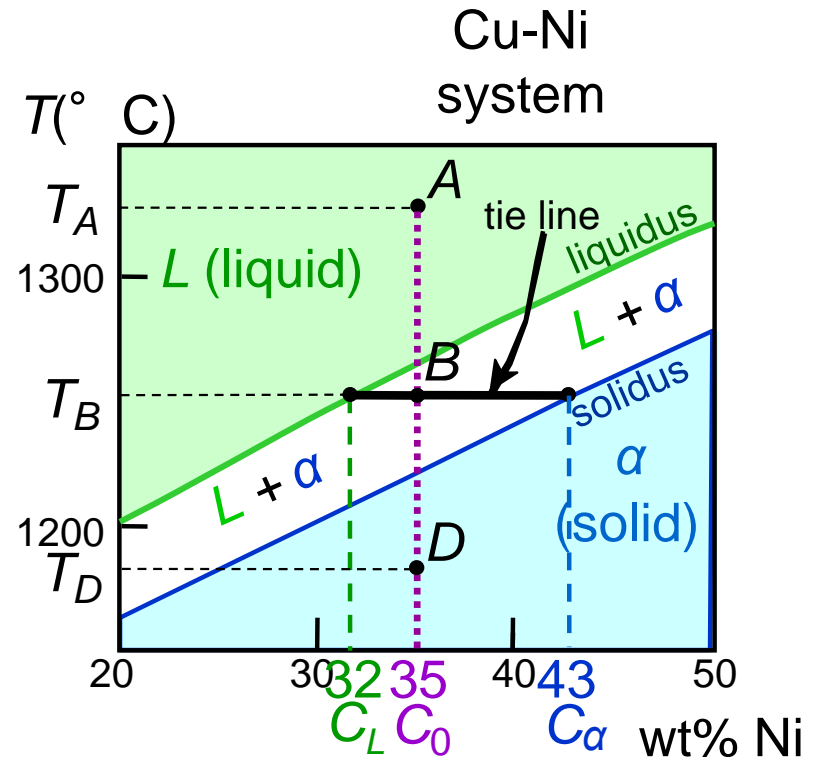
$C_\alpha = C_0$ ($= 35 \text{ wt\% Ni}$)

At $T_B = 1250^\circ \text{ C}$:

Both α and L present

$C_L = C_{\text{liquidus}}$ ($= 32 \text{ wt\% Ni}$)

$C_\alpha = C_{\text{solidus}}$ ($= 43 \text{ wt\% Ni}$)



Phase Diagrams:

Determination of phase weight fractions

- Rule 3: If we know T and C_0 , then can determine:
 - the weight fraction of each phase.

- Examples:

Consider $C_0 = 35 \text{ wt\% Ni}$

At T_A : Only Liquid (L) present

$$W_L = 1.00, W_\alpha = 0$$

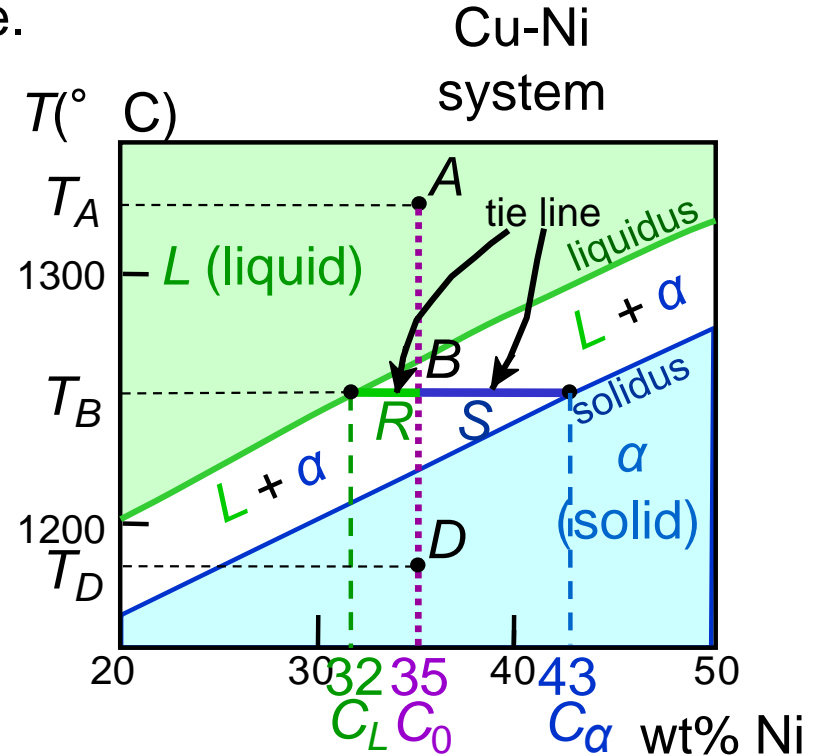
At T_D : Only Solid (α) present

$$W_L = 0, W_\alpha = 1.00$$

At T_B : Both α and L present

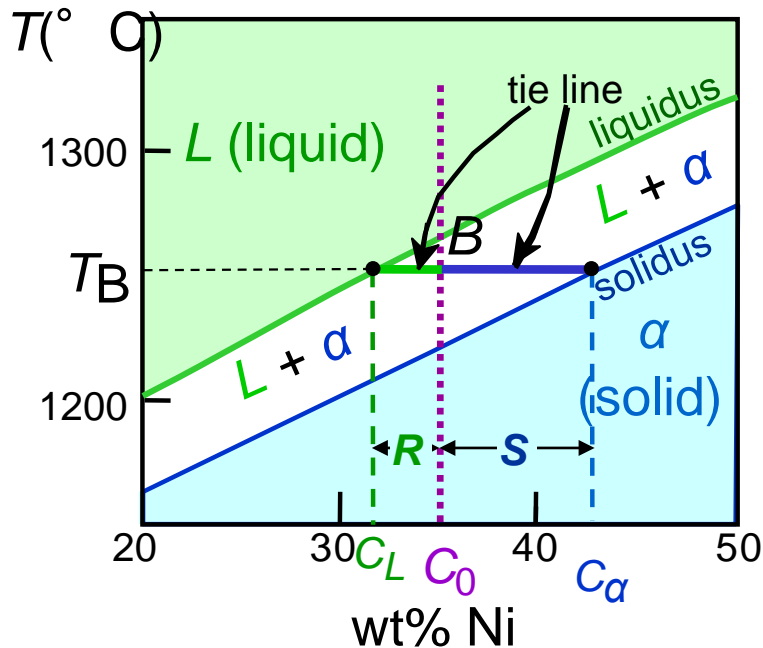
$$W_L = \frac{S}{R+S} = \frac{43-35}{43-32} = 0.73$$

$$W_\alpha = \frac{R}{R+S} = 0.27$$



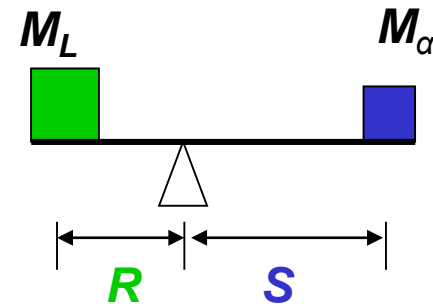
The Lever Rule

- Tie line – connects the phases in equilibrium with each other – also sometimes called an **isotherm**



What fraction of each phase?

Think of the tie line as a lever (teeter-totter)



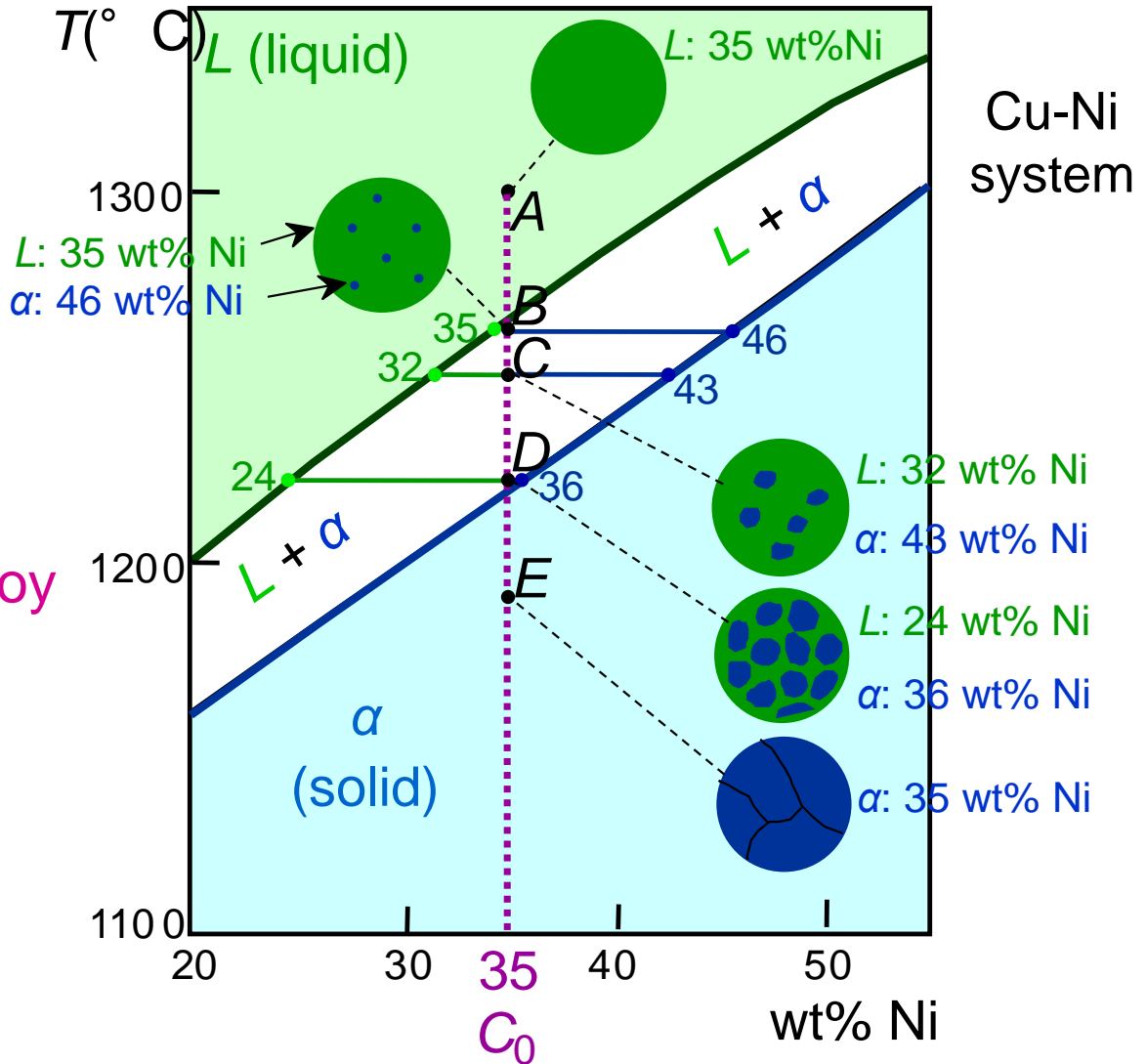
$$M_{\alpha} \times S = M_L \times R$$

$$W_L = \frac{M_L}{M_L + M_{\alpha}} = \frac{S}{R + S} = \frac{C_{\alpha} - C_0}{C_{\alpha} - C_L}$$

$$W_{\alpha} = \frac{R}{R + S} = \frac{C_0 - C_L}{C_{\alpha} - C_L}$$

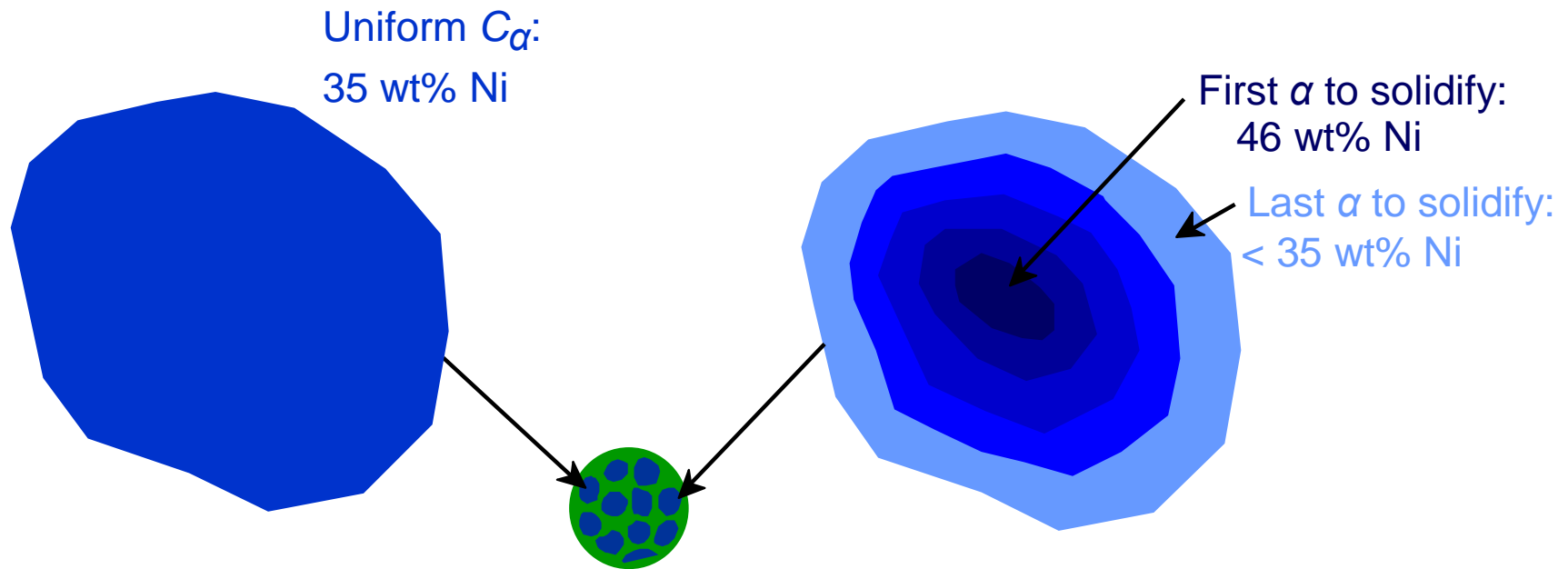
Ex: Cooling of a Cu-Ni Alloy

- Phase diagram: Cu-Ni system.
- Consider microstructural changes that accompany the cooling of a $C_0 = 35 \text{ wt\% Ni alloy}$



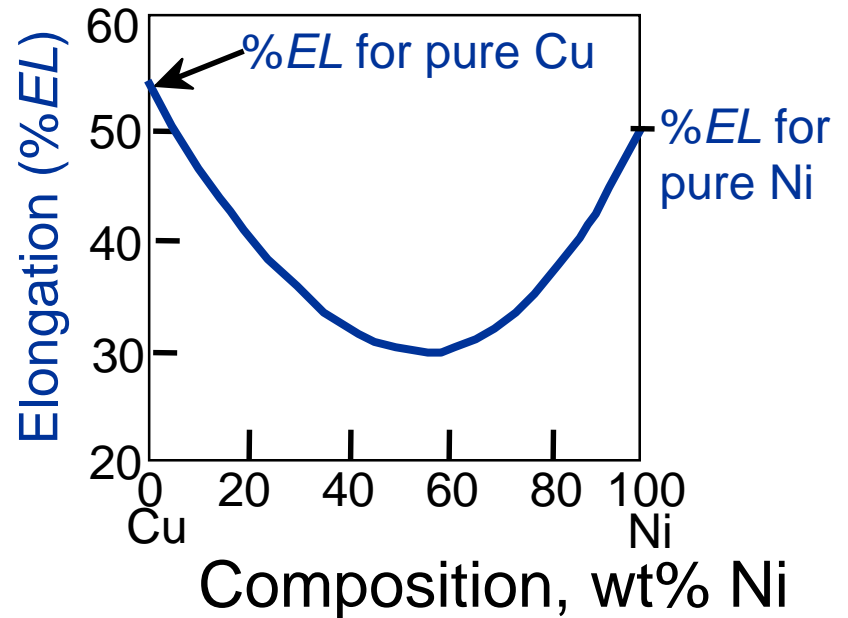
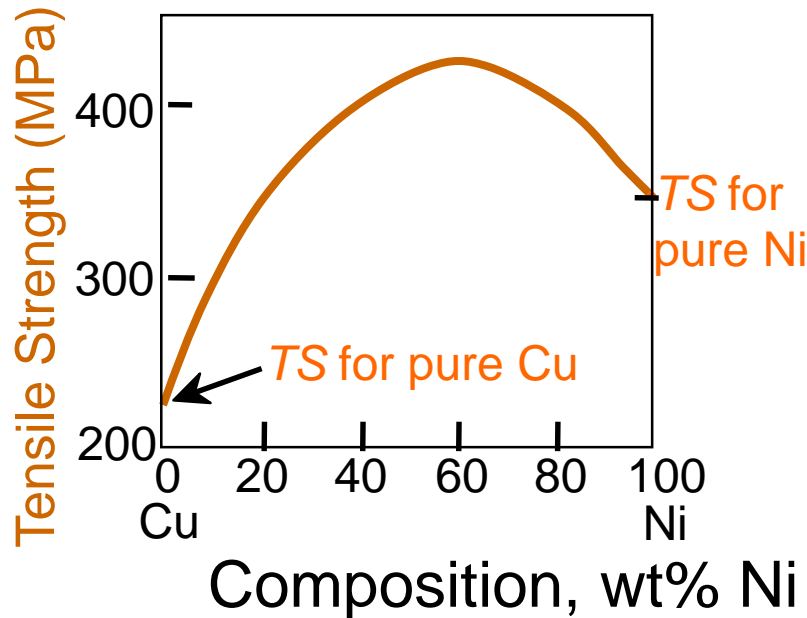
Cored vs Equilibrium Structures

- C_α changes as we solidify.
- Cu-Ni case: First α to solidify has $C_\alpha = 46$ wt% Ni.
Last α to solidify has $C_\alpha = 35$ wt% Ni.
- Slow rate of cooling:
Equilibrium structure
- Fast rate of cooling:
Cored structure



Mechanical Properties: Cu-Ni System

- Effect of solid solution strengthening on:
 - Tensile strength (*TS*)
 - Ductility (*%EL*)



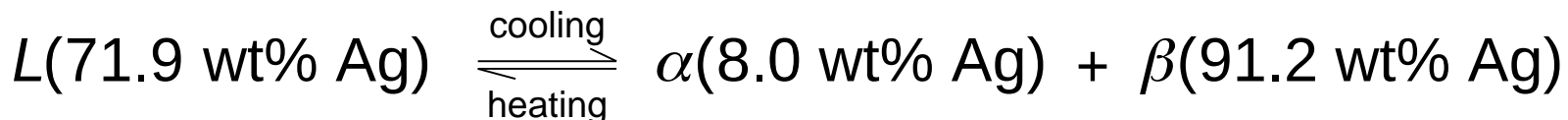
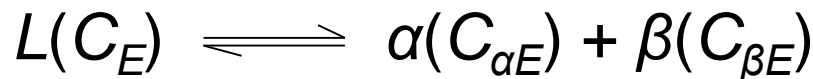
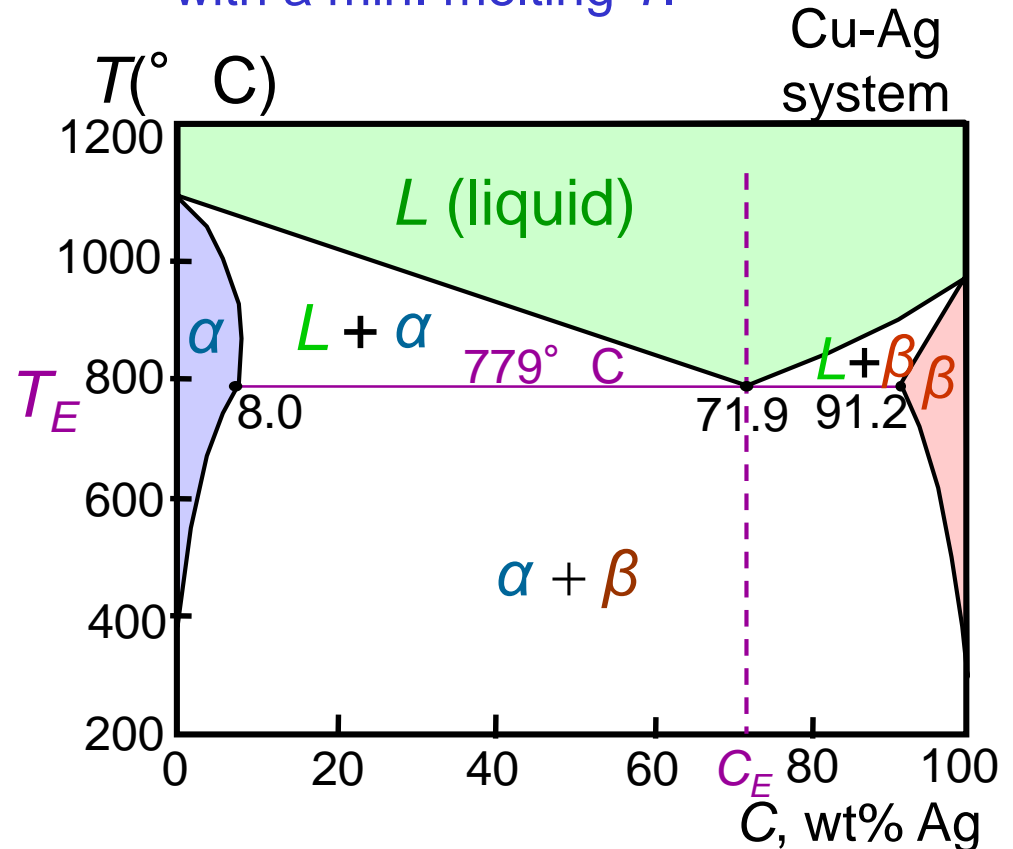
Binary-Eutectic Systems

2 components

has a special composition with a min. melting T .

Ex.: Cu-Ag system

- 3 single phase regions (L , α , β)
- Limited solubility:
 α : mostly Cu
 β : mostly Ag
- T_E : No liquid below T_E
- C_E : Composition at temperature T_E
- **Eutectic reaction**



EX 1: Pb-Sn Eutectic System

- For a 40 wt% Sn-60 wt% Pb alloy at 150° C, determine:
 - the phases present

Answer: $\alpha + \beta$

- the phase compositions

Answer: $C_\alpha = 11$ wt% Sn
 $C_\beta = 99$ wt% Sn

- the relative amount of each phase

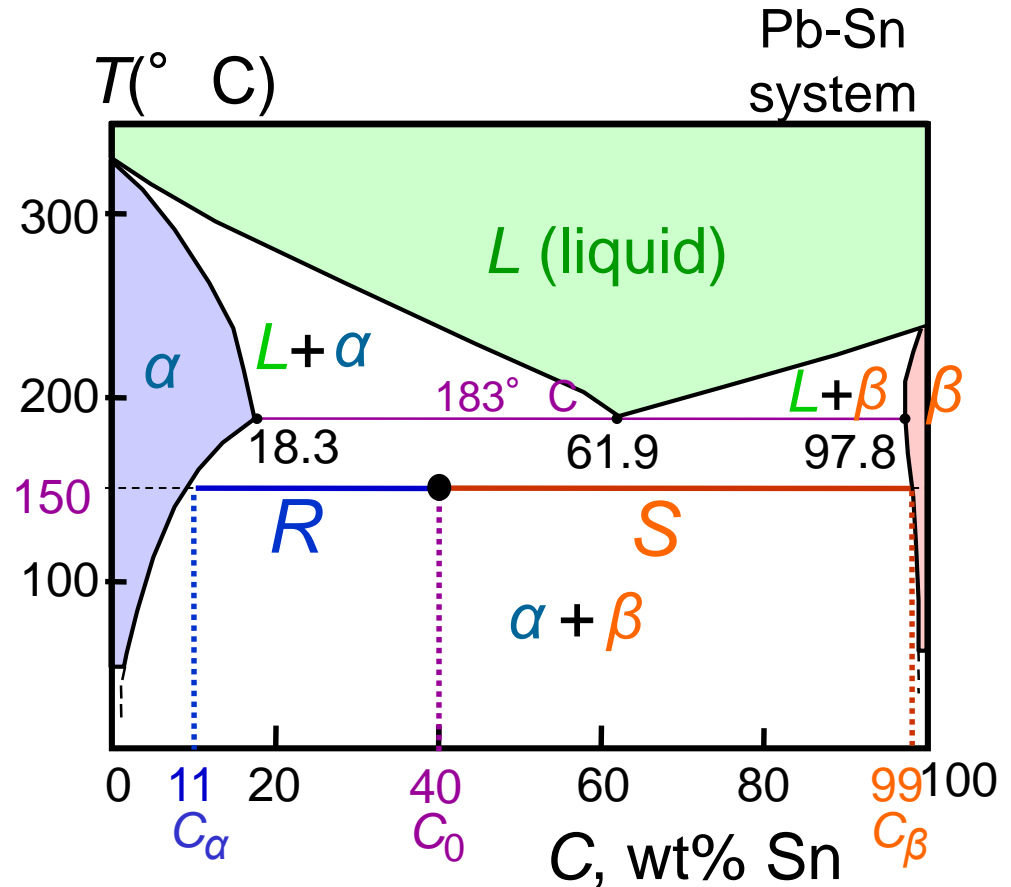
Answer:

$$W_\alpha = \frac{S}{R+S} = \frac{C_\beta - C_0}{C_\beta - C_\alpha}$$

$$= \frac{99 - 40}{99 - 11} = \frac{59}{88} = 0.67$$

$$W_\beta = \frac{R}{R+S} = \frac{C_0 - C_\alpha}{C_\beta - C_\alpha}$$

$$= \frac{40 - 11}{99 - 11} = \frac{29}{88} = 0.33$$



EX 2: Pb-Sn Eutectic System

- For a 40 wt% Sn-60 wt% Pb alloy at 220° C, determine:
 - the phases present:

Answer: $\alpha + L$

- the phase compositions

Answer: $C_\alpha = 17$ wt% Sn
 $C_L = 46$ wt% Sn

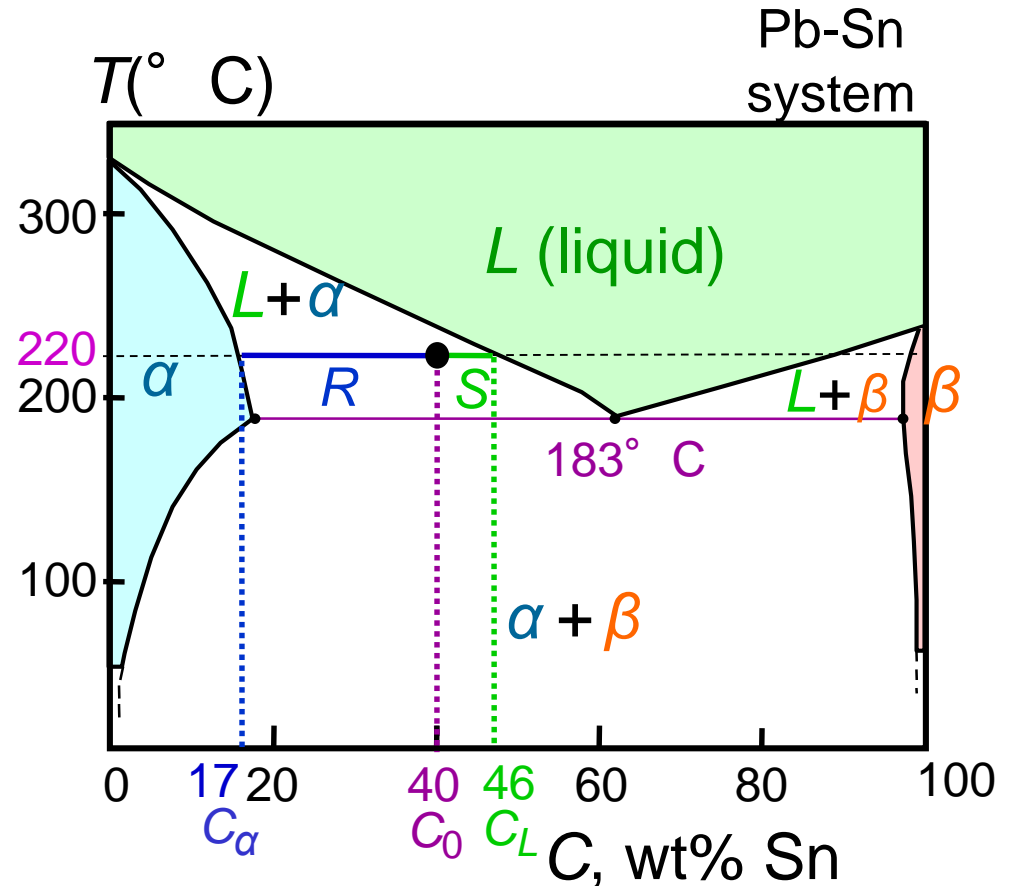
- the relative amount of each phase

Answer:

$$W_\alpha = \frac{C_L - C_0}{C_L - C_\alpha} = \frac{46 - 40}{46 - 17}$$

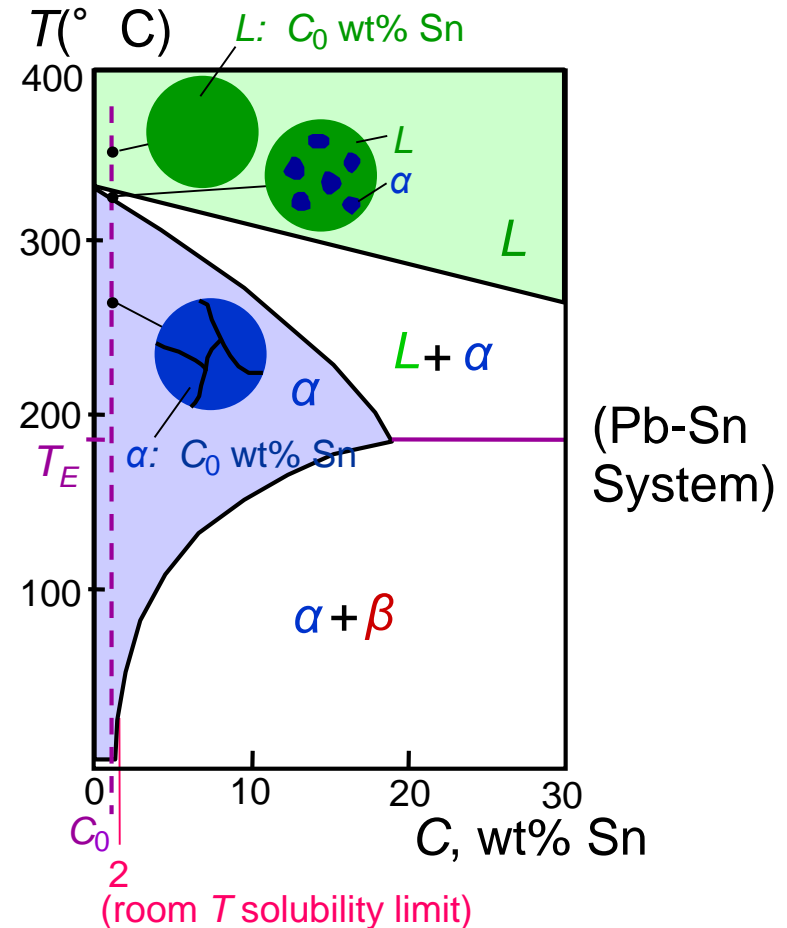
$$= \frac{6}{29} = 0.21$$

$$W_L = \frac{C_0 - C_\alpha}{C_L - C_\alpha} = \frac{23}{29} = 0.79$$



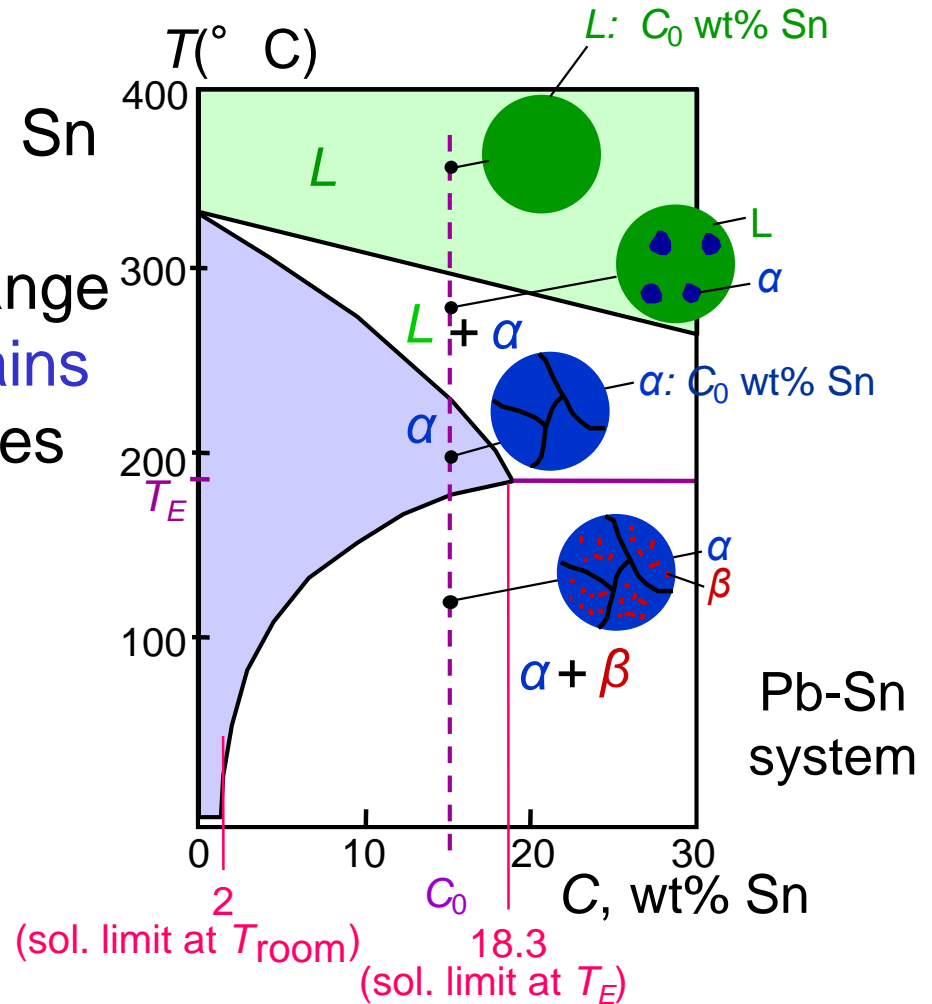
Microstructural Developments in Eutectic Systems I

- For alloys for which $C_0 < 2 \text{ wt\% Sn}$
- Result: at room temperature -- polycrystalline with grains of α phase having composition C_0



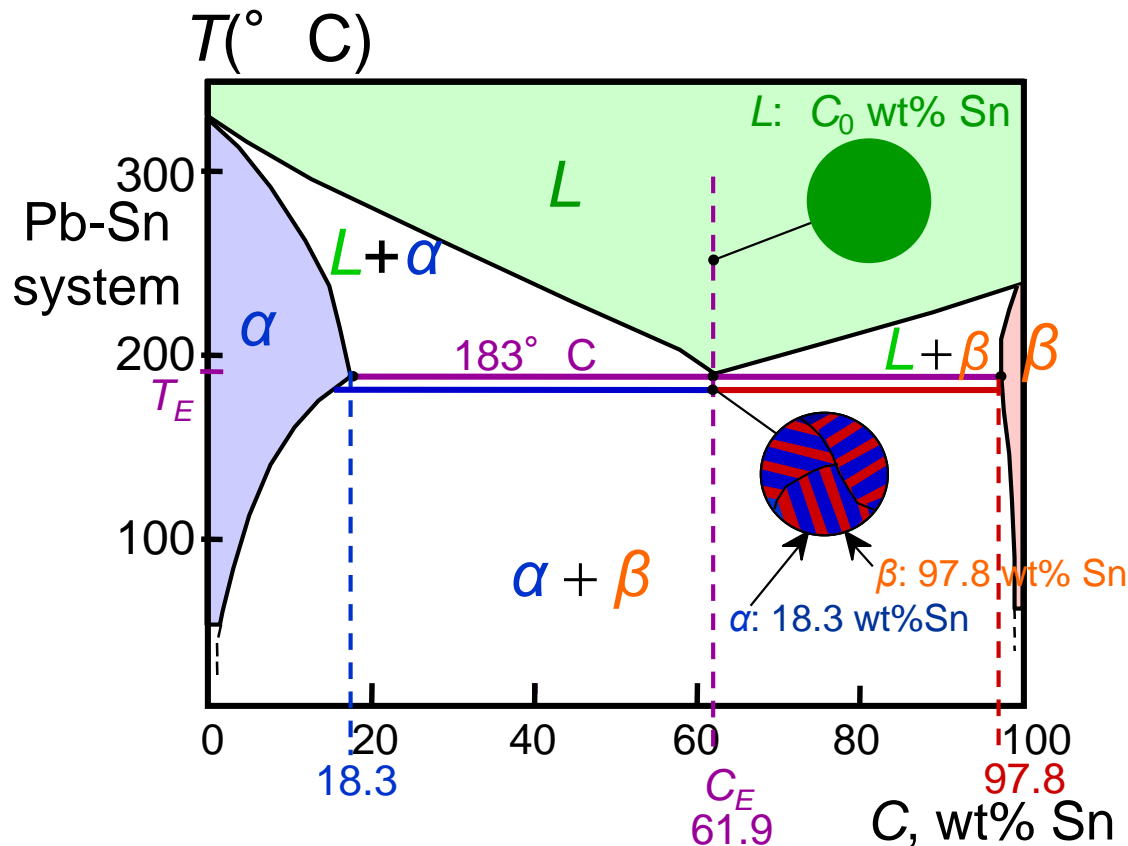
Microstructural Developments in Eutectic Systems II

- For alloys for which $2 \text{ wt\% Sn} < C_0 < 18.3 \text{ wt\% Sn}$
- Result:
at temperatures in $\alpha + \beta$ range
-- polycrystalline with α grains
and small β -phase particles



Microstructural Developments in Eutectic Systems III

- For alloy of composition $C_0 = C_E$
- Result: Eutectic microstructure (lamellar structure)
 - alternating layers (lamellae) of α and β phases.



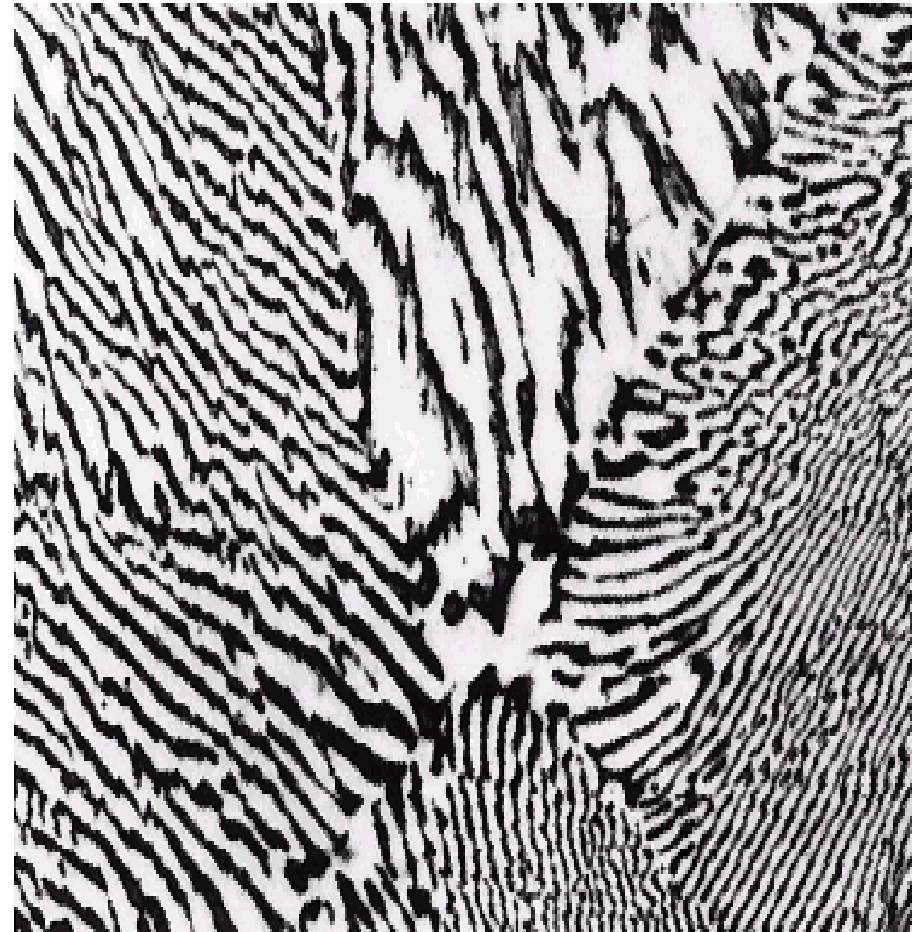
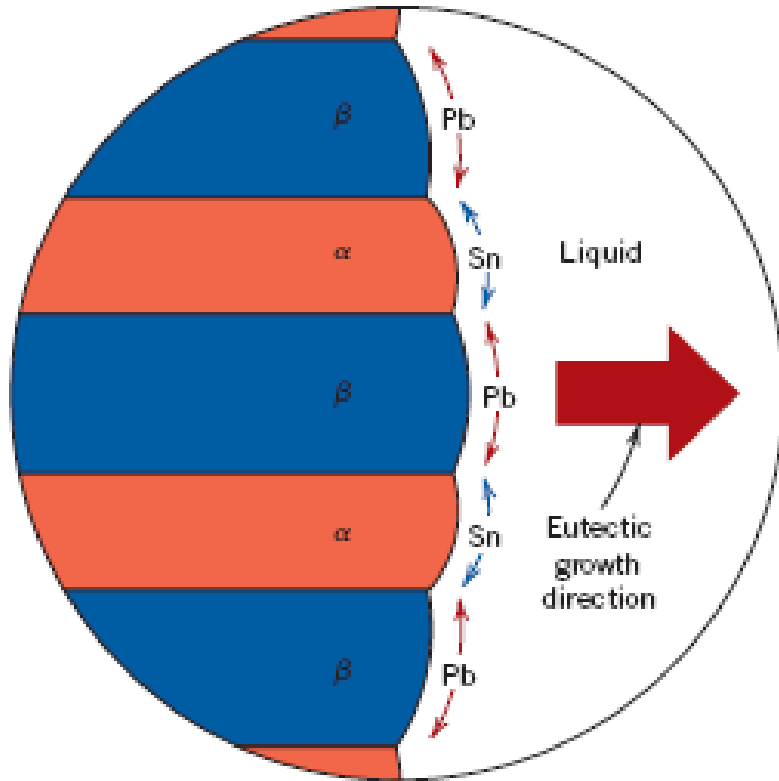
Micrograph of Pb-Sn eutectic microstructure



160 μm

Callister & Rethwisch 9e.
(From *Metals Handbook*, 9th edition, Vol. 9,
Metallography and Microstructures, 1985.
Reproduced by permission of ASM
International, Materials Park, OH.)

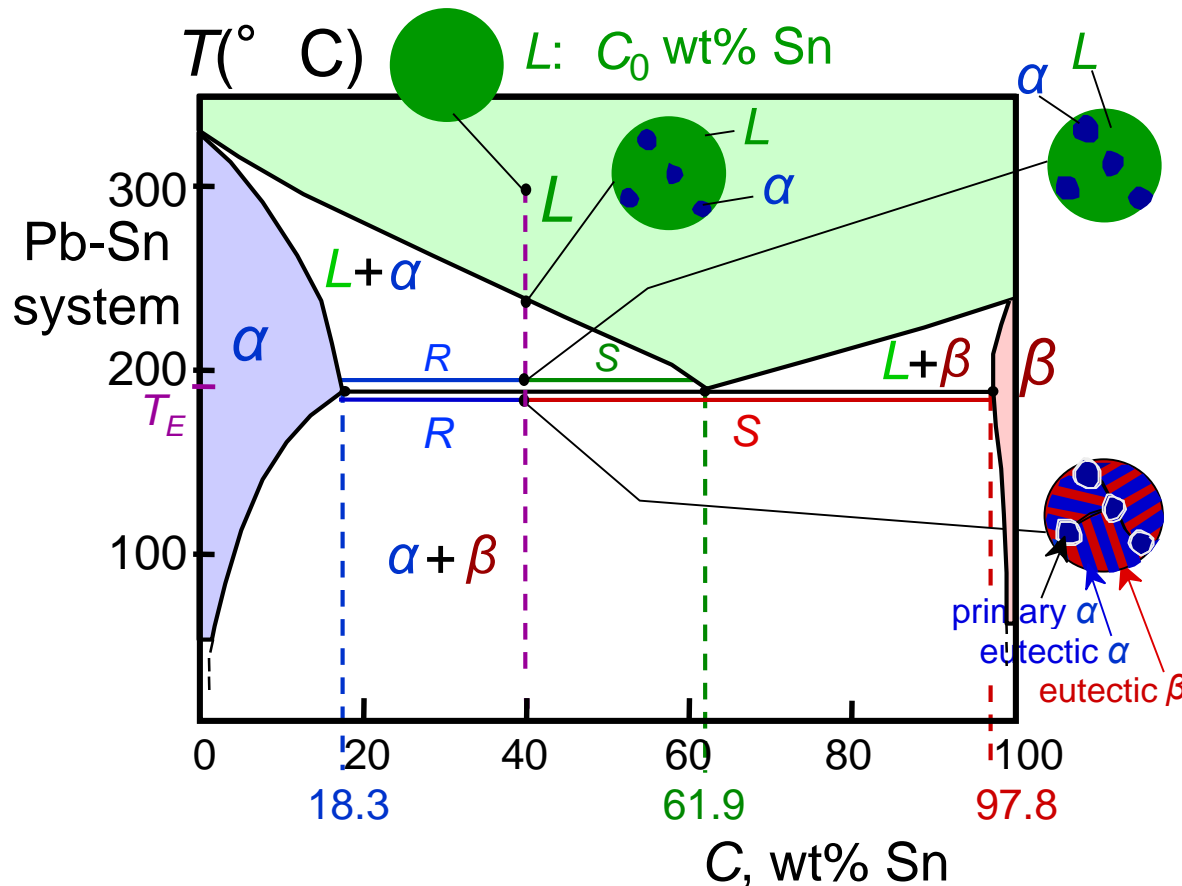
Lamellar Eutectic Structure



Callister & Rethwisch 9e. (Fig. 9.14 from *Metals Handbook*, 9th edition, Vol. 9, *Metallography and Microstructures*, 1985. Reproduced by permission of ASM International, Materials Park, OH.)

Microstructural Developments in Eutectic Systems IV

- For alloys for which $18.3 \text{ wt\% Sn} < C_0 < 61.9 \text{ wt\% Sn}$
- Result: α phase particles and a eutectic microconstituent



- Just above T_E :

$$C_{\alpha} = 18.3 \text{ wt\% Sn}$$

$$C_L = 61.9 \text{ wt\% Sn}$$

$$W_{\alpha} = \frac{S}{R + S} = 0.50$$

$$W_L = (1 - W_{\alpha}) = 0.50$$

- Just below T_E :

$$C_{\alpha} = 18.3 \text{ wt\% Sn}$$

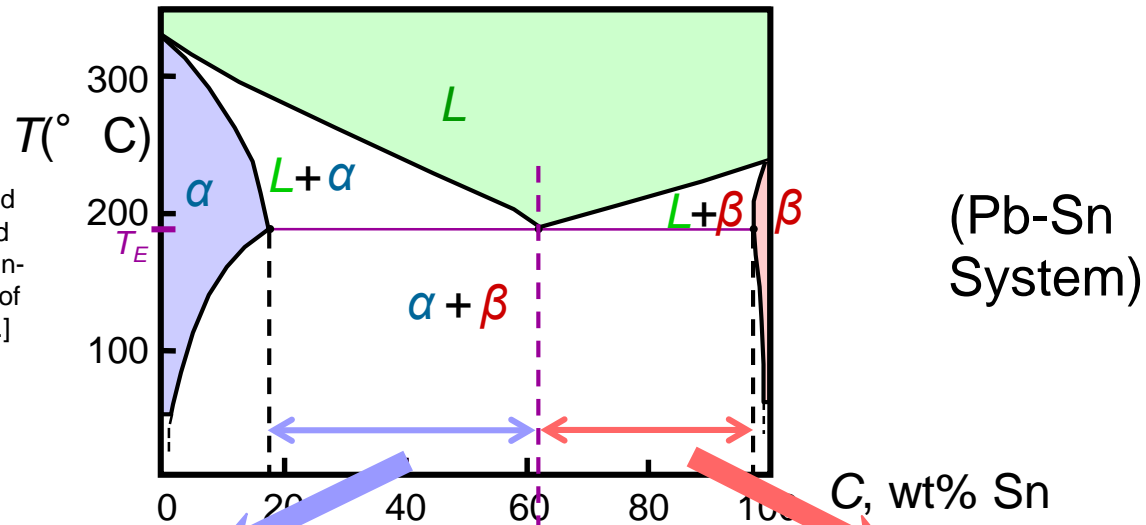
$$C_{\beta} = 97.8 \text{ wt\% Sn}$$

$$W_{\alpha} = \frac{S}{R + S} = 0.73$$

$$W_{\beta} = 0.27$$

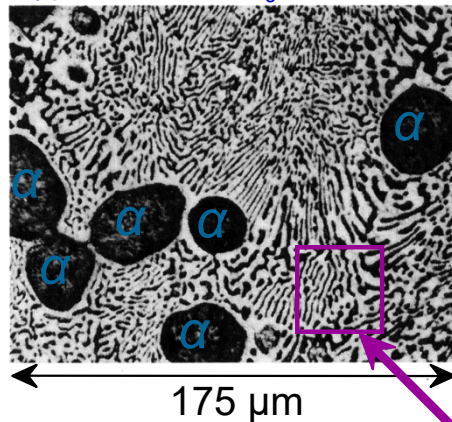
Hypoeutectic & Hypereutectic

Callister & Rethwisch 9e. [Adapted from *Binary Alloy Phase Diagrams*, 2nd edition, Vol. 3, T. B. Massalski (Editor-in-Chief), 1990. Reprinted by permission of ASM International, Materials Park, OH.]



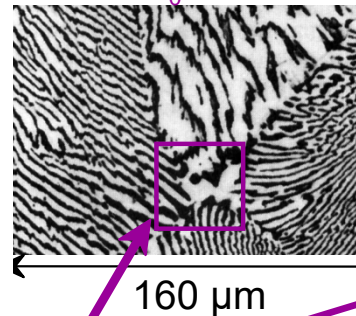
hypoeutectic: $C_0 = 50 \text{ wt\% Sn}$

(*Metals Handbook*, 9th ed., Vol. 9, *Metallography and Microstructures*, 1985. Reproduced by permission of ASM International, Materials Park, OH.)

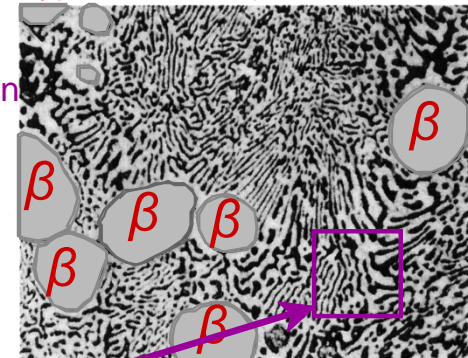


eutectic
61.9

eutectic: $C_0 = 61.9 \text{ wt\% Sn}$

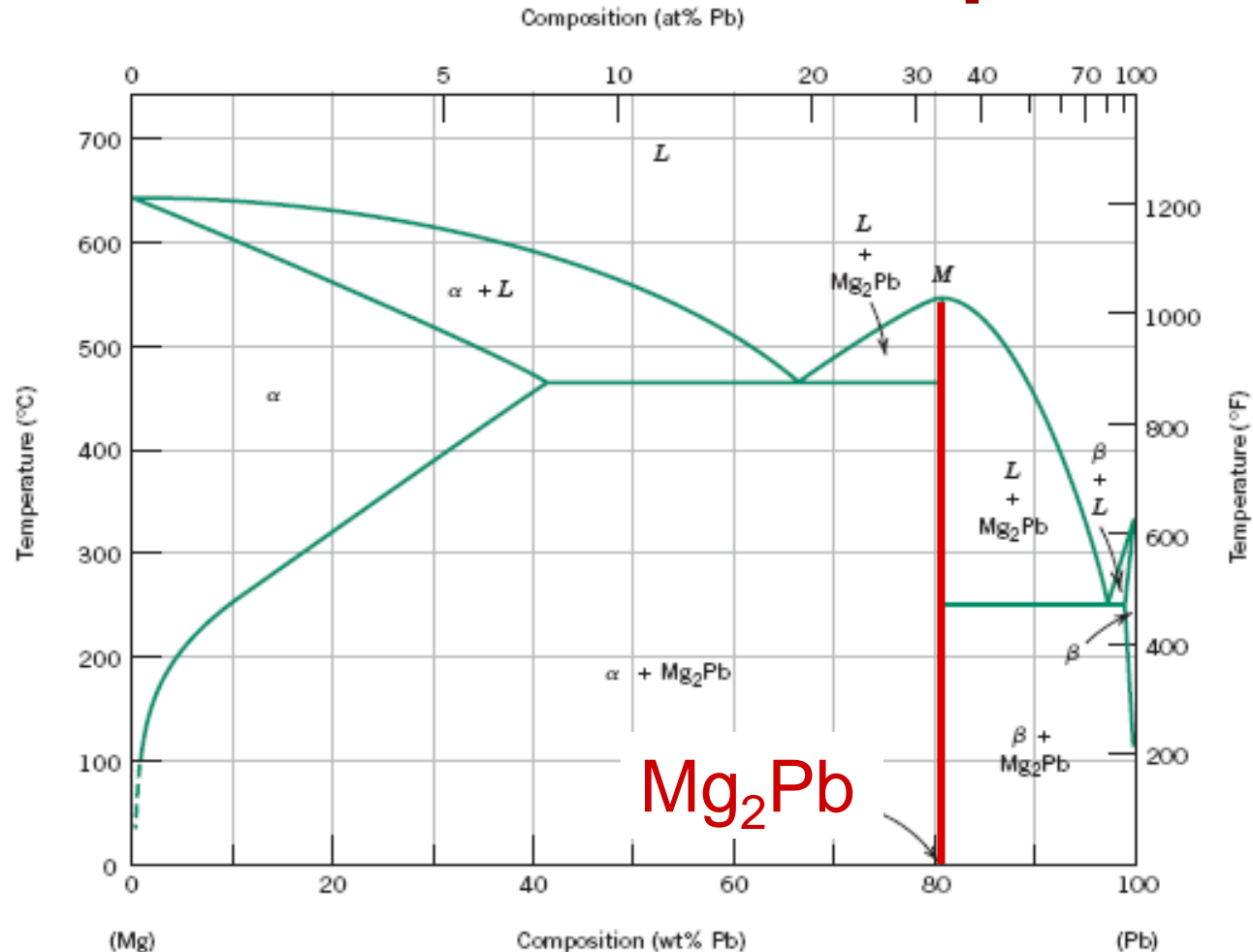


hypereutectic: (illustration only)



eutectic micro-constituent

Intermetallic Compounds

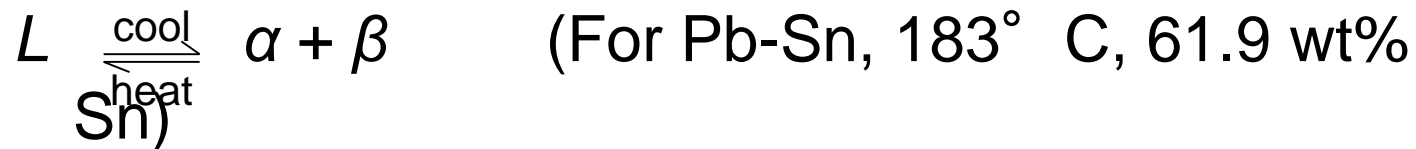


[Adapted from *Phase Diagrams of Binary Magnesium Alloys*, A. A. Nayeb-Hashemi and J. B. Clark (Editors), 1988. Reprinted by permission of ASM International, Materials Park, OH.]

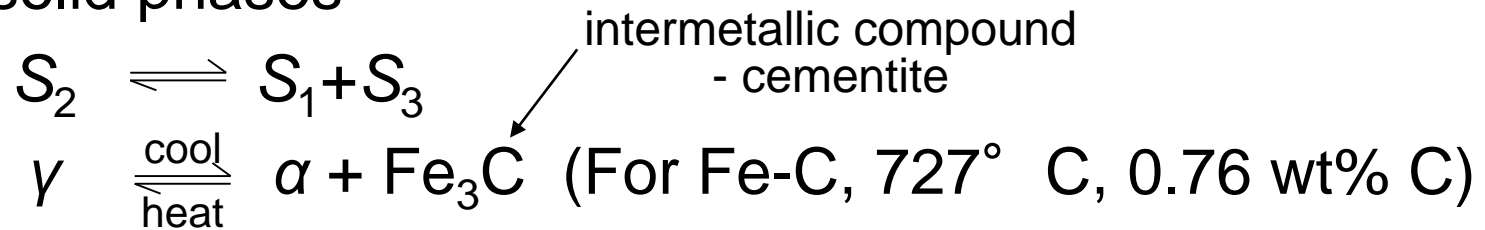
Note: intermetallic compound exists as a line on the diagram - not an area - because of stoichiometry (i.e. composition of a compound is a fixed value).

Eutectic, Eutectoid, & Peritectic

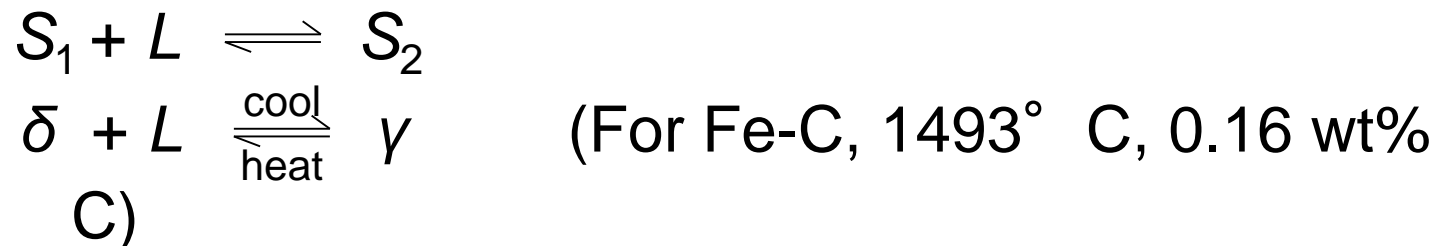
- **Eutectic** - liquid transforms to two solid phases



- **Eutectoid** – one solid phase transforms to two other solid phases



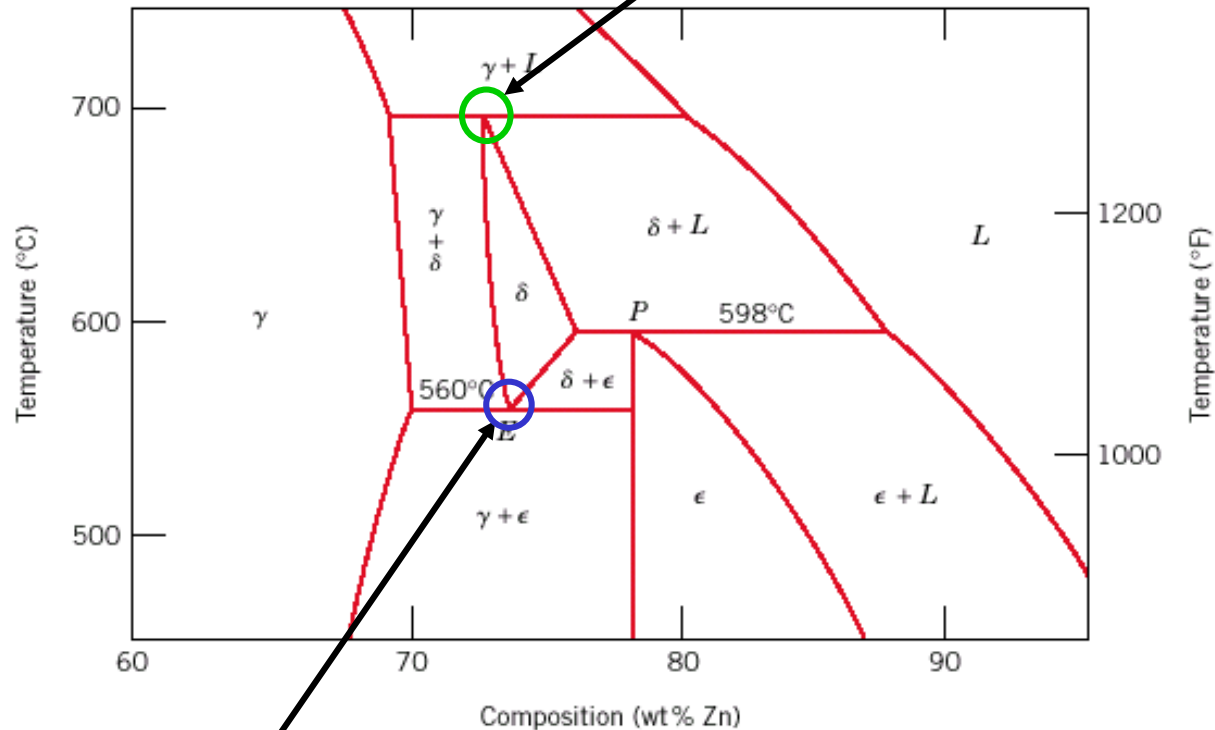
- **Peritectic** - liquid and one solid phase transform to a second solid phase



Eutectoid & Peritectic

Cu-Zn Phase diagram

Peritectic transformation $\gamma + L \rightleftharpoons \delta$



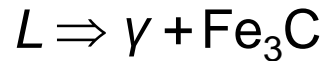
Eutectoid transformation $\delta \rightleftharpoons \gamma + \epsilon$

[Adapted from *Binary Alloy Phase Diagrams*, 2nd edition, Vol. 2, T. B. Massalski (Editor-in-Chief), 1990. Reprinted by permission of ASM International, Materials Park, OH.]

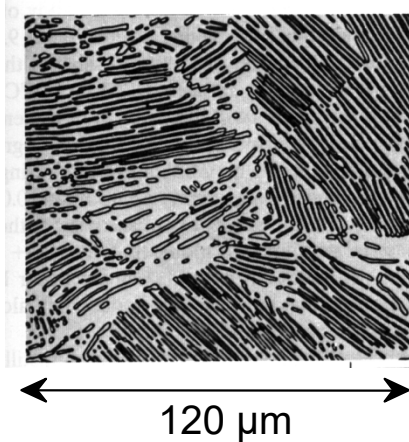
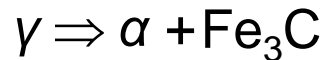
Iron-Carbon (Fe-C) Phase Diagram

- 2 important points

- Eutectic (A):



- Eutectoid (B):



Result: Pearlite = alternating layers of α and Fe_3C phases

Fig. 9.27, Callister & Rethwisch 9e.
(From *Metals Handbook*, Vol. 9, 9th ed.,
Metallography and Microstructures, 1985.
Reproduced by permission of ASM
International, Materials Park, OH.)

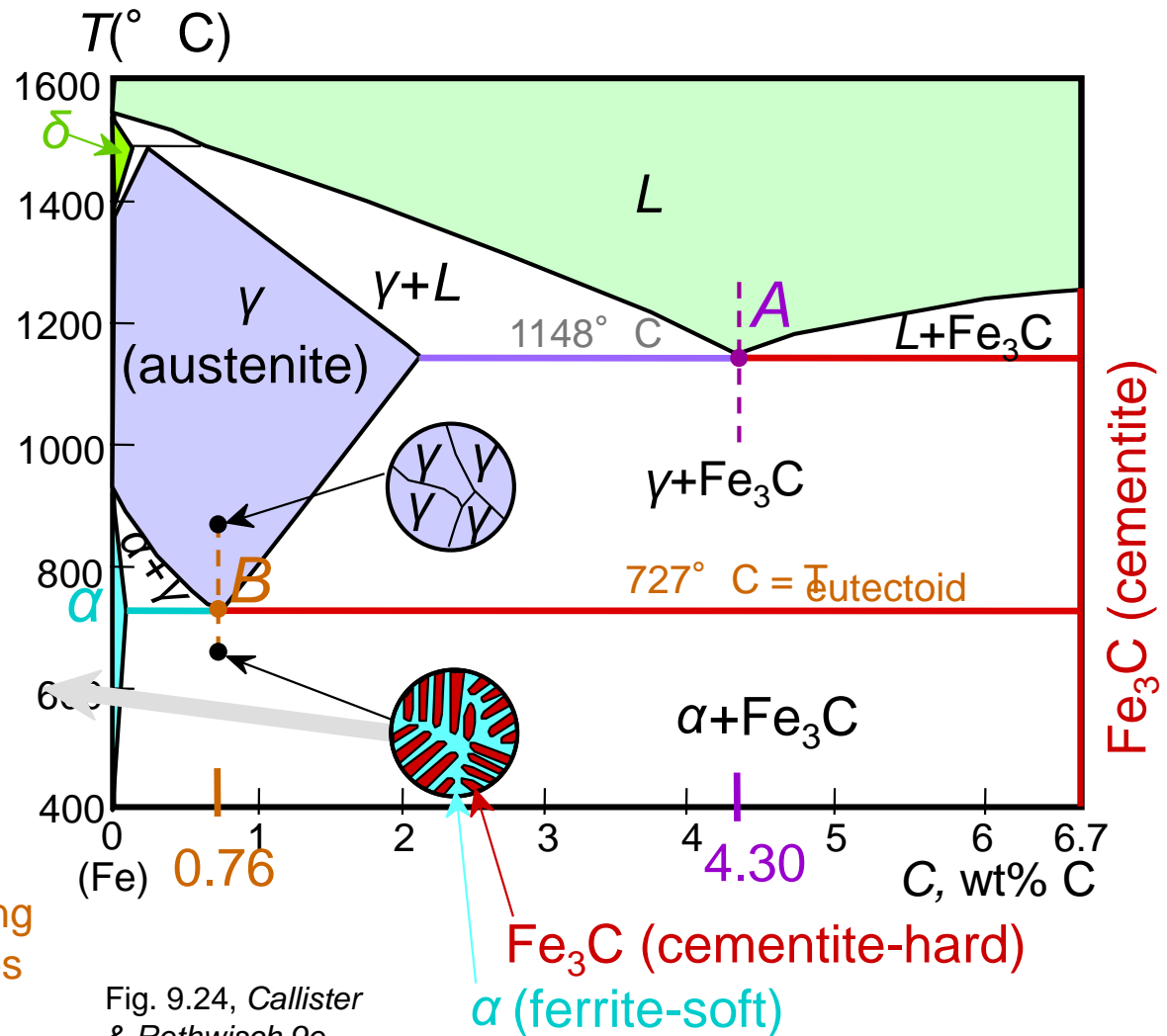
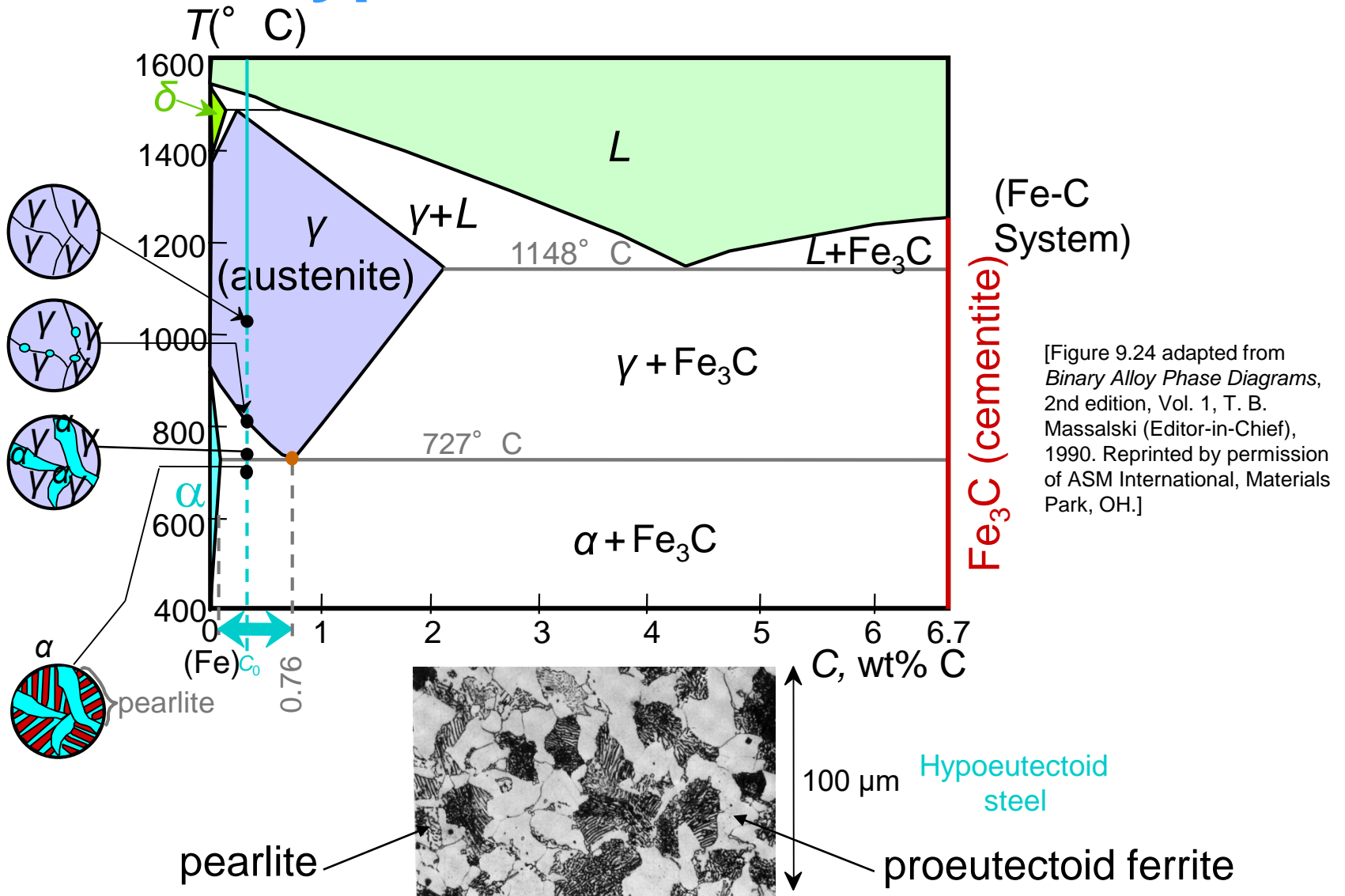


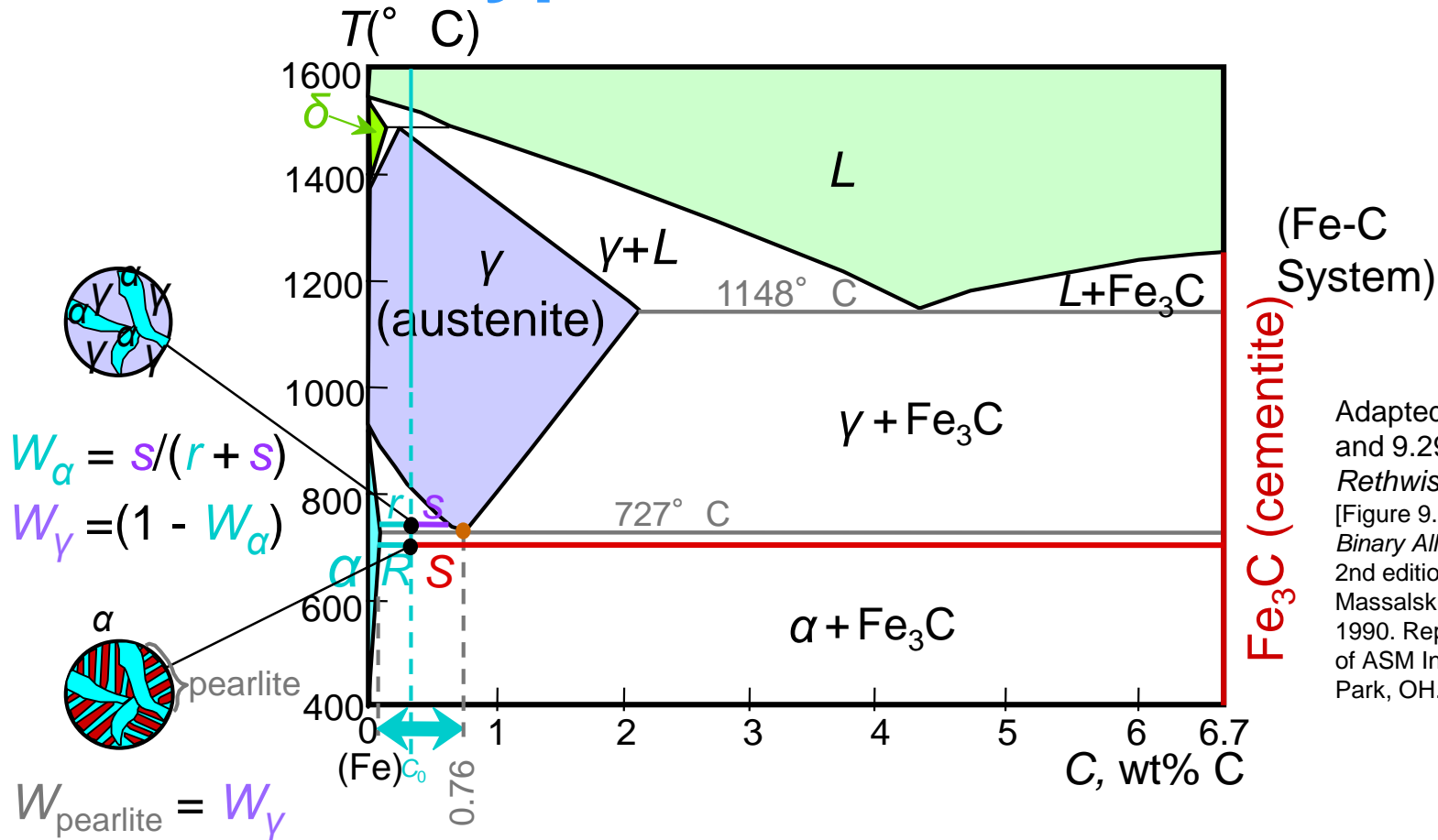
Fig. 9.24, Callister & Rethwisch 9e.

[Adapted from *Binary Alloy Phase Diagrams*, 2nd edition,
Vol. 1, T. B. Massalski (Editor-in-Chief), 1990. Reprinted
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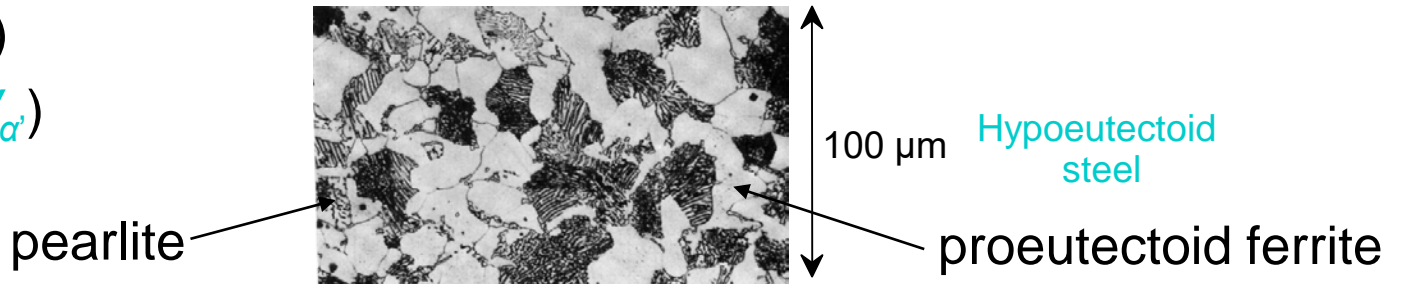
Hypo eutectoid Steel



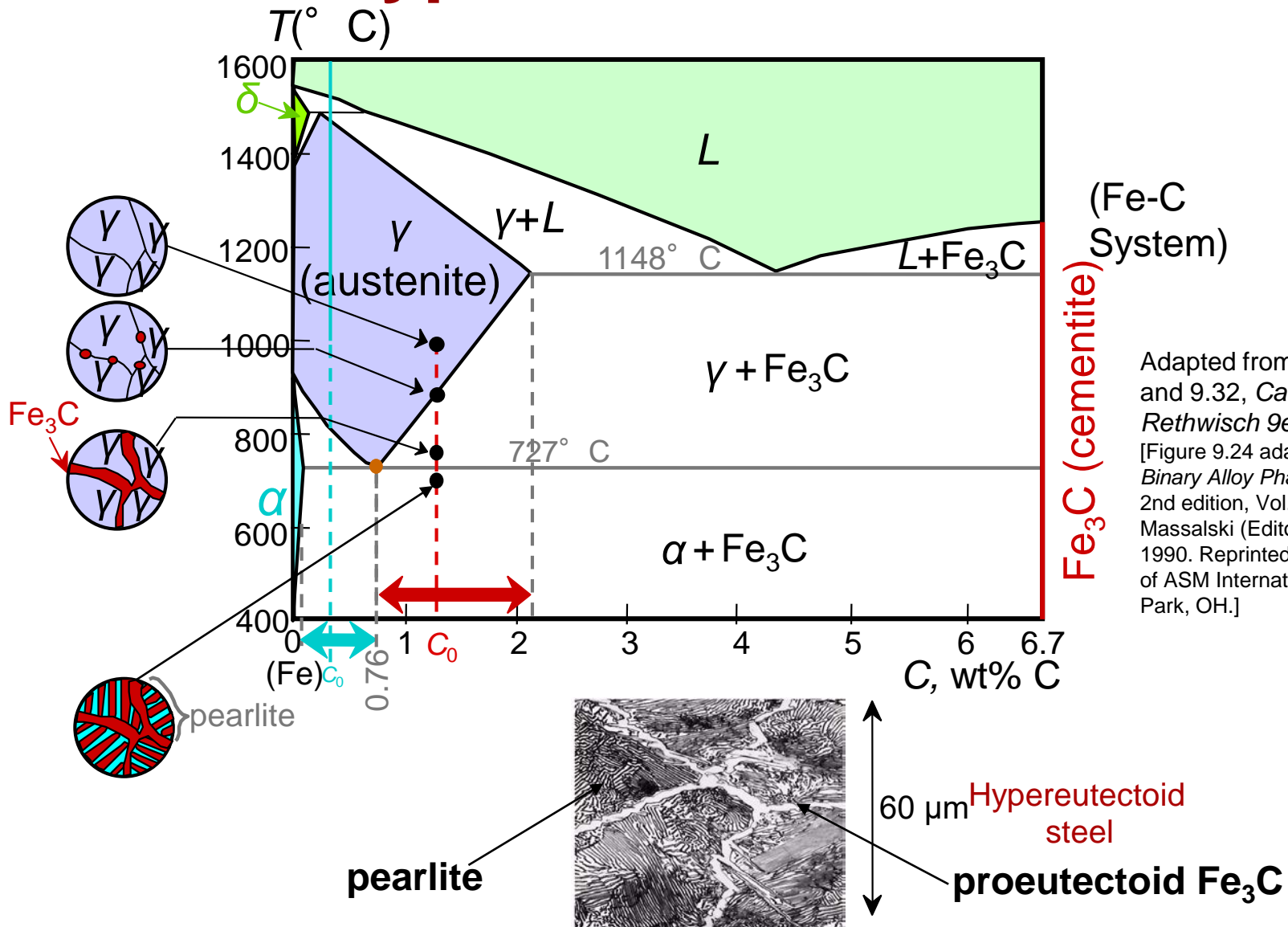
Hypoeutectoid Steel



Adapted from Figs. 9.24 and 9.29, *Callister & Rethwisch 9e*.
[Figure 9.24 adapted from *Binary Alloy Phase Diagrams*, 2nd edition, Vol. 1, T. B. Massalski (Editor-in-Chief), 1990. Reprinted by permission of ASM International, Materials Park, OH.]

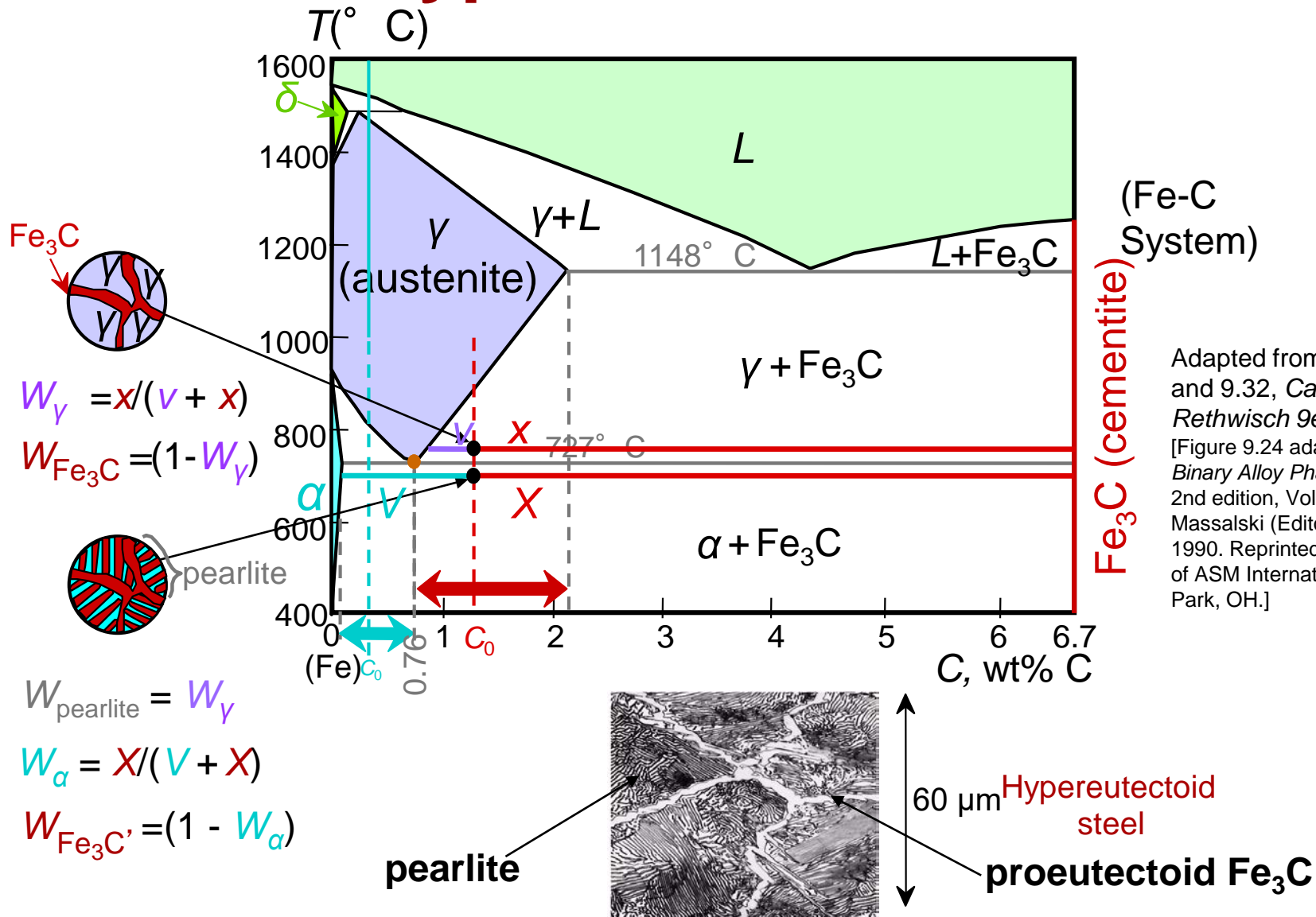


Hypereutectoid Steel



Adapted from Fig. 9.33, Callister & Rethwisch 9e.
 (Copyright 1971 by United States Steel Corporation.)

Hypereutectoid Steel



Adapted from Fig. 9.33, *Callister & Rethwisch 9e*.
 (Copyright 1971 by United States Steel Corporation.)

Example Problem

For a 99.6 wt% Fe-0.40 wt% C steel at a temperature just below the eutectoid, determine the following:

- a) The compositions of Fe_3C and ferrite (α).
- b) The amount of cementite (in grams) that forms in 100 g of steel.
- c) The amounts of pearlite and proeutectoid ferrite (α) in the 100 g.

Solution to Example Problem

a) Using the RS tie line just below the eutectoid

$$C_{\alpha} = 0.022 \text{ wt\% C}$$

$$C_{\text{Fe}_3\text{C}} = 6.70 \text{ wt\% C}$$

b) Using the lever rule with the tie line shown

$$W_{\text{Fe}_3\text{C}} = \frac{R}{R+S} = \frac{C_0 - C_{\alpha}}{C_{\text{Fe}_3\text{C}} - C_{\alpha}}$$

$$= \frac{0.40 - 0.022}{6.70 - 0.022} = 0.057$$

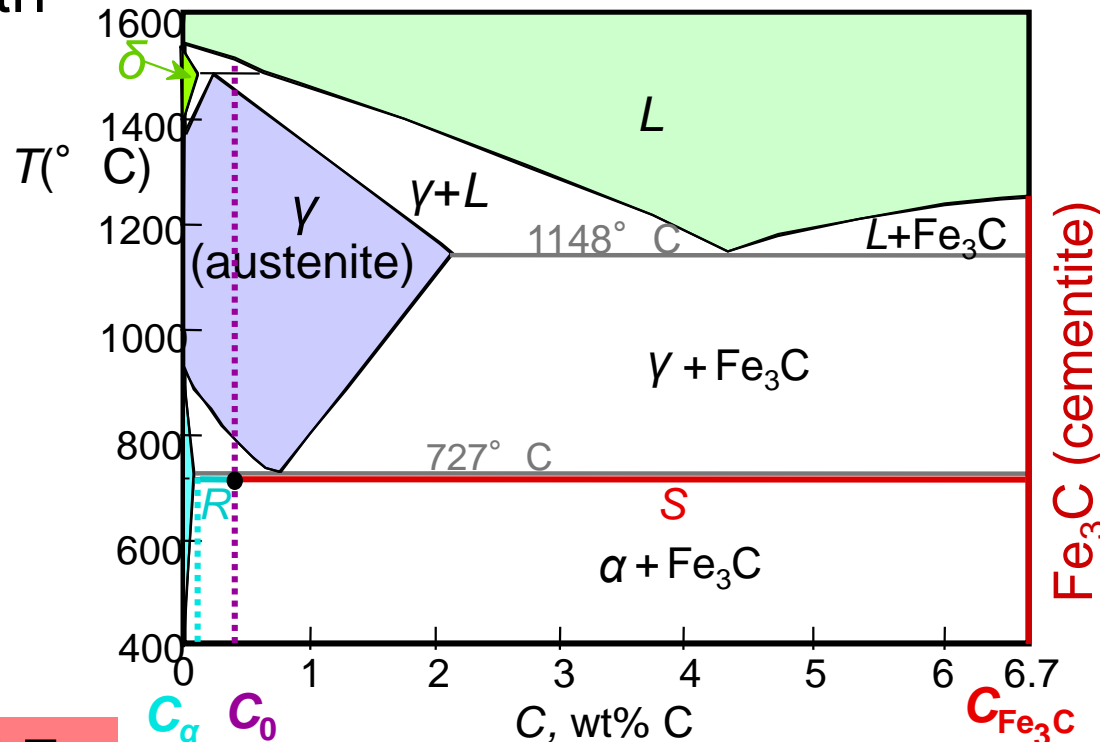
Amount of Fe_3C in 100 g

$$= (100 \text{ g}) W_{\text{Fe}_3\text{C}}$$

$$= (100 \text{ g})(0.057) = 5.7 \text{ g}$$

Fig. 9.24, Callister & Rethwisch 9e.

[From *Binary Alloy Phase Diagrams*, 2nd edition, Vol. 1, T. B. Massalski (Editor-in-Chief), 1990. Reprinted by permission of ASM International, Materials Park, OH.]



Solution to Example Problem (cont.)

- c) Using the VX tie line just above the eutectoid and realizing that

$$C_0 = 0.40 \text{ wt\% C}$$

$$C_\alpha = 0.022 \text{ wt\% C}$$

$$C_{\text{pearlite}} = C_\gamma = 0.76 \text{ wt\% C}$$

$$W_{\text{pearlite}} = \frac{V}{V + X} = \frac{C_0 - C_\alpha}{C_\gamma - C_\alpha}$$

$$= \frac{0.40 - 0.022}{0.76 - 0.022} = 0.512$$

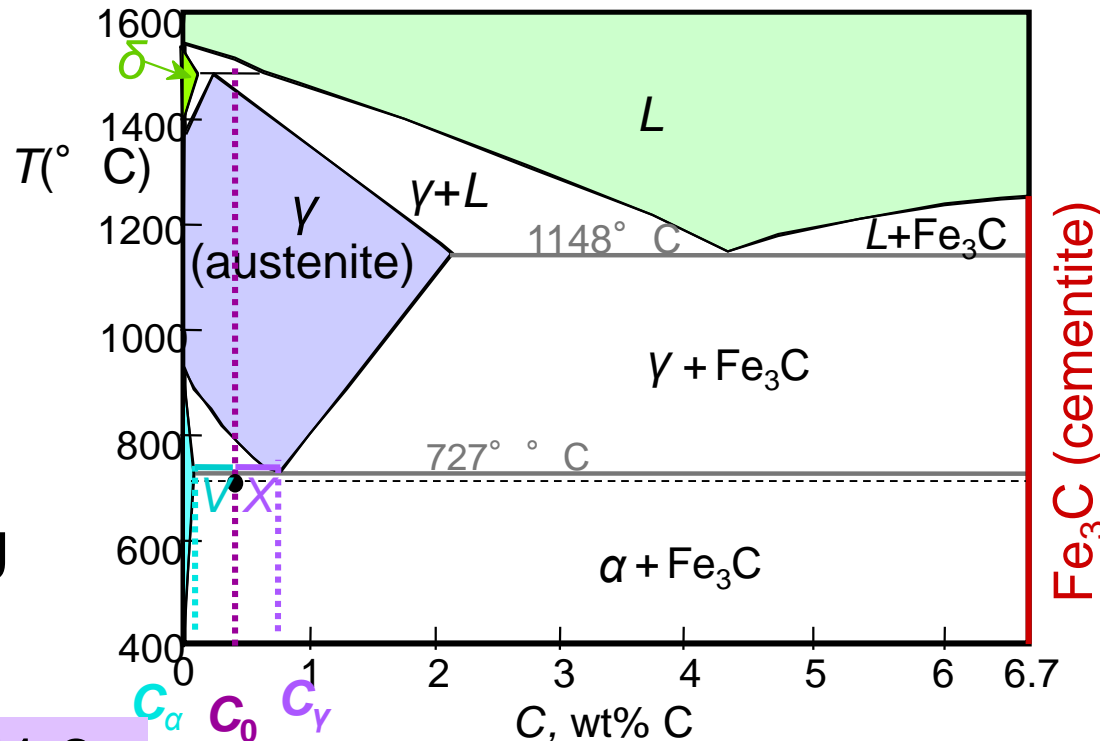
Amount of pearlite in 100 g

$$= (100 \text{ g}) W_{\text{pearlite}}$$

$$= (100 \text{ g})(0.512) = 51.2 \text{ g}$$

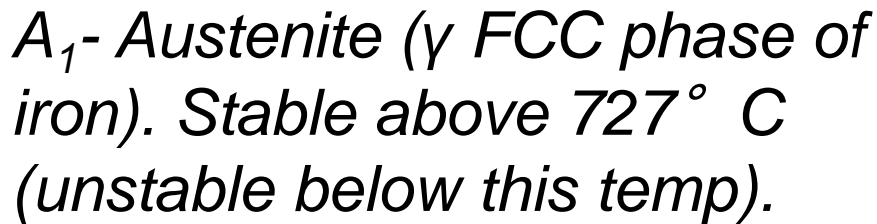
Fig. 9.24, Callister & Rethwisch 9e.

[From *Binary Alloy Phase Diagrams*, 2nd edition, Vol. 1, T. B. Massalski (Editor-in-Chief), 1990. Reprinted by permission of ASM International, Materials Park, OH.]

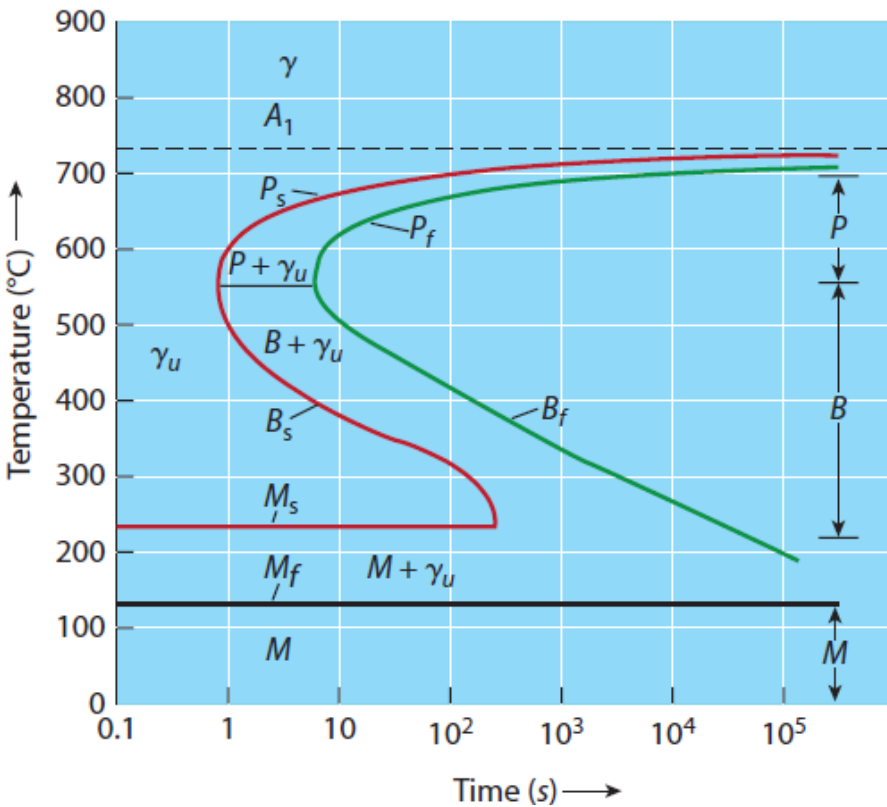


The Iron-Carbon Phase Diagram and Martensitic Phase Transformations: Time-Temperature-Transformation Diagrams for Plain-Carbon Steel

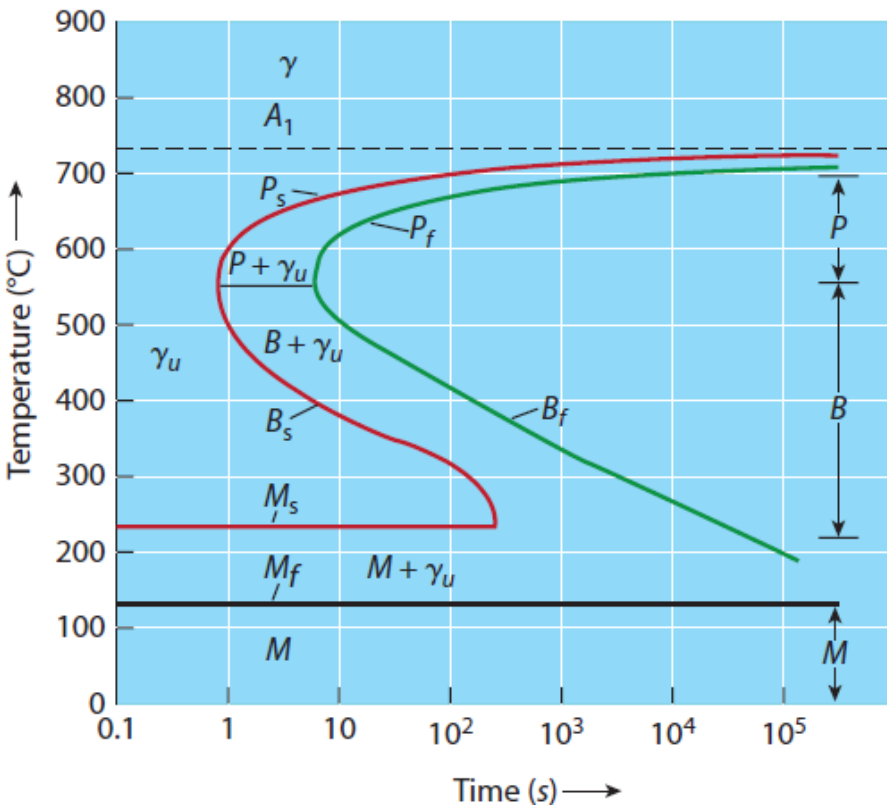
- The transformation of γ - to $\alpha + \text{Fe}_3\text{C}$ - phase can be understood using a Time-Temperature-Transformation (TTT) diagram.
- X-axis: Time and Y-axis: Temperature.
- For nucleation and growth phase transformations:
 - The TTT is obtained by keeping the material at an isothermal (constant temperature).
 - Then find the percent transformation as a function of time.



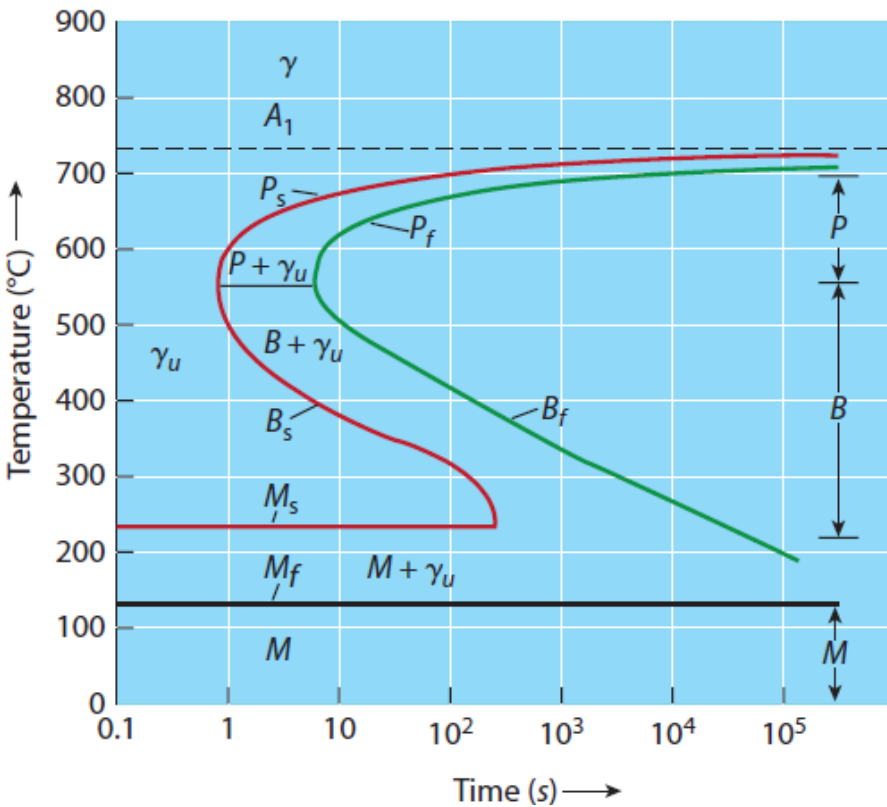
- 37



- If this alloy is cooled to room temperature, the structure of Pearlite remains.
 - Because it is comprised of the equilibrium phases of γ -iron and Fe_3C .
- Below 550°C (isothermal), Bainite (B) is formed than Pearlite.
 - Bainite has an α -matrix with thin narrow ribbons (laths) of Fe_3C .
 - The laths are smaller and closer spaced than in pearlite: At lower temperatures, diffusion of C-atoms is much slower.



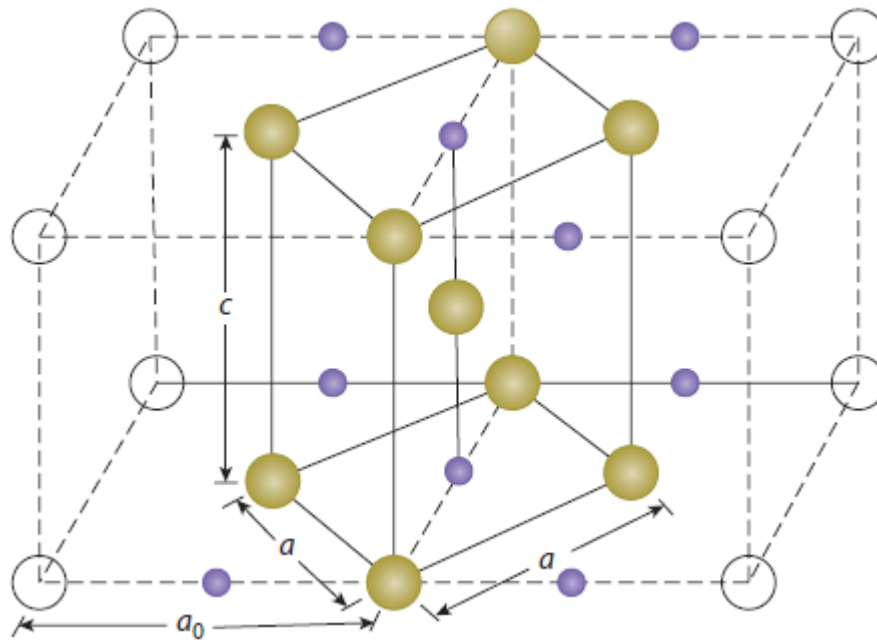
- At low temperatures:
 - Driving force for eutectoid reaction is large.
 - BUT, mobility of atoms is lowered.
 - Smaller diffusion distance favored hence finer Bainite than coarser Pearlite is formed.
- If the eutectoid alloy is quenched to 500° C and kept constant.
 - Bainite is first observed after 1-second.
 - After 10-seconds, unstable austenite phase is completely transformed to Bainite at B_f .
- When cooled to room temperature, the Bainite structure remains (equilibrium phases of α -iron and Fe_3C).



- If the temperature of Fe-0.77%C alloy is quenched from the eutectoid temperature to a low temperature (without crossing the P_s or B_s lines):
 - Not enough time for Pearlite or Bainite to form.
- In a Martensite transformation, the FCC γ -phase iron transforms to a Body-Centered Tetragonal Unit Cell.

M_s - Start of a Martensite transformation.

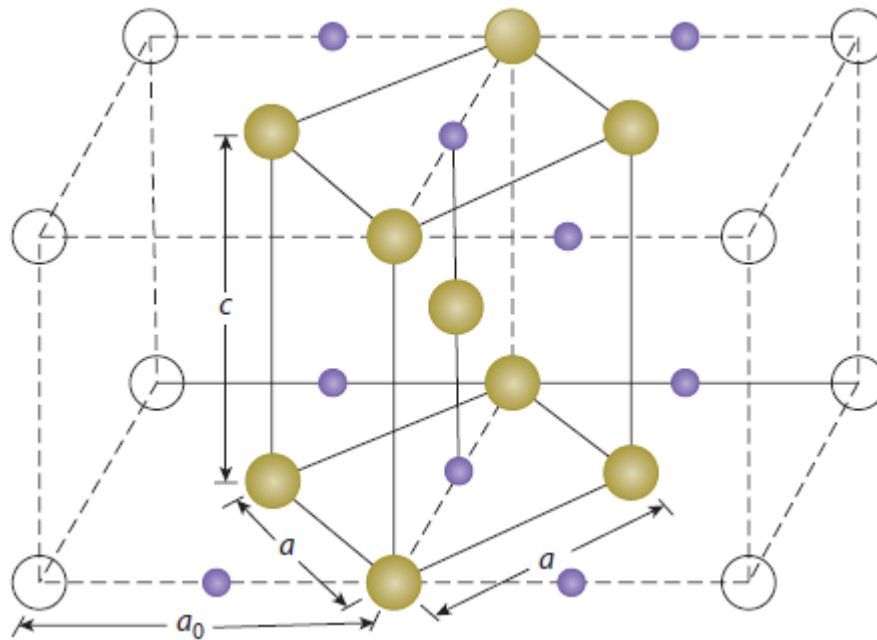
Unit Cells of an FCC Cubic Iron



Iron atoms are depicted by large circles.
Carbon atoms are the small solid circles.

- Lattice Parameters of a Tetragonal Unit Cell.
 - $a=b$ with $c \neq b$ and $c \neq a$.
 - All unit cell corner angles are 90° .
- The FCC unit cell can be indexed as a Body-Centered Tetragonal (BCT) unit cell.
 - However, when $a=c$, the BCT lattice is now BCC.
- Below 727° C , the equilibrium structure of iron-carbon alloys is BCC.
- If the alloy is rapidly cooled: No time for diffusion (nucleation/growth) to occur for FCC to transform to BCC.

Unit Cells of an FCC Cubic Iron

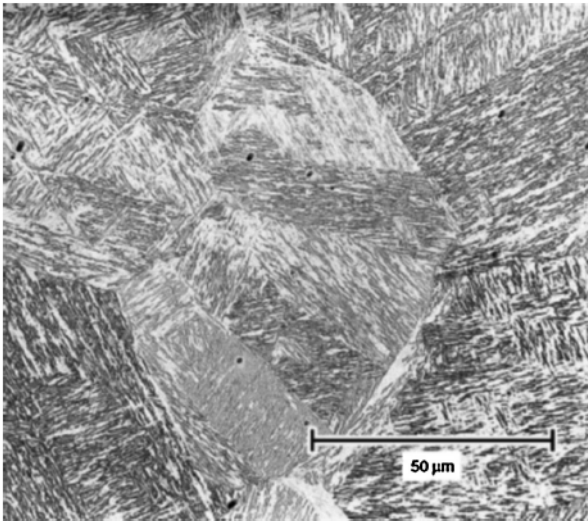


Iron atoms are depicted by large circles.

Carbon atoms are the small solid circles.

- The FCC structure instead transforms to BCT:
 - By diffusionless martensitic transformation.
- In a martensitic transformation, the lattice distorts into a new lattice with no long-range diffusion.
- If carbon atoms go preferentially into the position shown:
 - The a parameter expands, and the c parameter contracts: Lattice distorts.
 - Bain's Distortion where $a=b=0.285\text{nm}$ and $c=0.295\text{nm}$.
 - Body-Centered Tetragonal Unit Cell (close to BCC unit cell).

The Iron-Carbon Phase Diagram and Martensitic Phase Transformations: Time-Temperature-Transformation Diagrams for Plain-Carbon Steel



The microstructure of Martensite in low-carbon steel is acicular (needle-like as seen to the right).

The motion of the carbon atoms in Martensite transformation is more rapid than the long-range diffusion (required to form Pearlite or Bainite).

The Martensite transformation in plain carbon steel is athermal.

- **Athermal means the amount of transformation depends on the temperature but not time.**

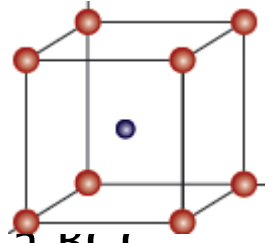
The Iron-Carbon Phase Diagram and Martensitic Phase Transformations: Time-Temperature-Transformation Diagrams for Plain-Carbon Steel

- Iron-carbon Martensite is hard and brittle.
 - Hence rarely used in engineering applications after quenching.
- Tempering:
 - Heating to an elevated temperature 600° C.
 - Martensite transforms to BCC α -phase iron and Fe_3C .
 - Quenching and tempering leads to the Fe_3C precipitate being nucleated throughout the alloy.
 - Tempering leads to iron-carbon alloys of high strength and good ductility.
 - E.g. Cutting tools, Crank shafts, Springs and Pistons.

Reversible Martensitic Phase Transformations

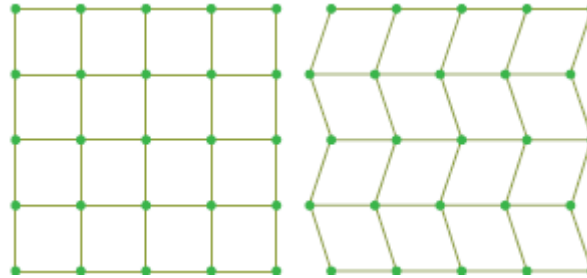
- Martensite phase transformation in iron-carbon alloys is irreversible.
 - Due to dislocation formation during Bain's Distortion.
 - Dislocations allow material to be continuous during Bain distortion in martensitic transformations..
- Formation of dislocations in a material is irreversible.
- A reversible martensitic transformation occurs in materials without dislocations during transformation.
 - Dislocation is accommodated by the reversible stretching and bending of atomic bonds.
 - Change in Gibbs Free energy is zero.
 - Negative change in GFE from change in structure= Positive change in GFE from bond stretching and bending.

Reversible Martensitic Phase Transformations



- Mostly seen in metal alloys especially TiNi.
- TiNi is a random mixture of Titanium and Nickel atoms in a BCC structure.
- The Martensite start temperature (M_s) for TiNi is around 70°C , and can be described as a shear distortion.
- The Martensite finish temperature (M_f) is one where TiNi is 100% Martensite, and is around $30^\circ - 40^\circ \text{C}$ below the start temperature.
- The reversible martensitic transformation in TiNi doesn't cause the overall shape of the specimen to change, even though the crystal lattice changes shape.

Reversible Martensitic Phase Transformations

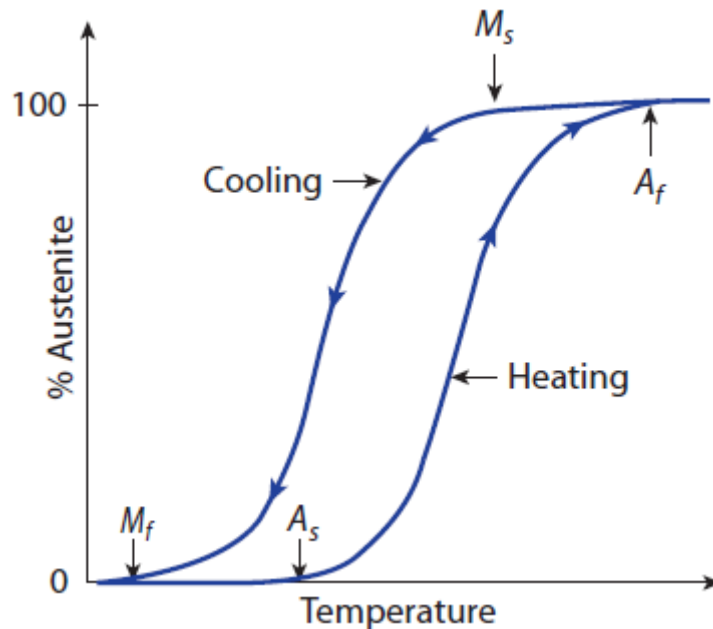


Left: 2D diagram of cubic austenite phase.

Right: Distorted Martensite lattice (reversible).

- The amount of Martensite in this transformation depends only on temperature (and not time).
- If the Martensite lattice (on the right) is heated, it will transform back into cubic austenite by reversing bond stretching and bending.

Reversible Martensitic Phase Transformations



- The Martensite to Austenite begins at the Austenite start temperature (A_s) and completes at the Austenite finish temperature (A_f).
- Where 100% of the Martensite has transformed to Austenite.
- In TiNi: Can go through cycles of cooling Austenite to form Martensite and heating Martensite to form Austenite.

Reversible Martensitic Phase Transformations: The Shape-Memory Effect and Training in Metal Alloys

- Shape-Memory effect is due to reversible Martensitic transformation in TiNi.
- Bend the wire into a desired shape, causes variations in distortion (that allow it to bend).
- When the wire is heated above A_f it returns to cubic structure and initial straight shape.
- If the wire is heated above A_f and bent to a different shape, it returns to that shape above A_f .
- The characteristic temperatures can be varied by changing the TiNi alloy composition.

Reversible Martensitic Phase Transformations: The Shape-Memory Effect and Training in Metal Alloys

- E.g. Coronary stents use shape-memory effect.
 - But need to reduce the temperature of martensitic transformation so that human body temperature is above A_f .

Summary

- Phase diagrams are useful tools to determine:
 - the number and types of phases present,
 - the composition of each phase,
 - and the weight fraction of each phasegiven the temperature and composition of the system.
- The microstructure of an alloy depends on
 - its composition, and
 - whether or not cooling rate allows for maintenance of equilibrium.
- Important phase diagram phase transformations include eutectic, eutectoid, and peritectic.